Spatial Correlations in Physical Unclonable Functions

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Abstract—Physical Unclonable Functions (PUFs) are circuits which extract a device dependent secret from inherently available manufacturing variations. This work focuses on evaluating the quality of such circuits regarding intra-die correlations, because canonical quality metrics for PUFs do not sufficiently cover them. Correlations reduce the effort for an attacker to guess the secret with the same severity as biases, yet canonical tests focus only on the latter. Three tests which are used to consider topological properties along with the secret are introduced and adapted to quality evaluation of PUFs. To show the efficiency and effectiveness but also the limitations of the tests, we apply them to three real-world measurement datasets from ring-oscillator PUFs on FPGAs, standard SRAM and Two-Stage PUFs on ASICs. The results show that the presented statistical tests are ideal candidates to complement state-of-the-art metrics for PUF quality.

I. EXTENDED ABSTRACT

Silicon-based Physical Unclonable Functions (PUFs) are security primitives which are used to extract a secret from intrinsic manufacturing variations of an electronic device. A bit is extracted in a PUF cell by measuring and quantizing analog properties of common digital circuits. The goal in designing a PUF is to make the bits hard to predict for an attacker, but reliable over the lifetime of the device. The former can be achieved if random local manufacturing variations dominate the behavior of the PUF, such that the response of individual PUF cells is statistically independent. If global variations — e.g. a speed gradient over the die — dominate, this allows for the prediction of the behaviour of other PUF cells on the die and thus impairs security [1].

Current quality measures for PUFs mainly focus on measuring biases [2]. Correlations are only considered via Joint Entropy [3] and rarely via Pearson’s correlation coefficient. But Joint Entropy can only be bounded, e.g. by compression algorithms, and Pearson’s correlation coefficient is limited to analyzing pairs of locations on the die separately. Neither of them is suited to find spatial correlations, especially in datasets with few devices.

This work advances the state of the art in the field of evaluation of PUF quality by adapting and analyzing methods to find spatial correlations. Moran’s I [4], Geary’s c [5], and Join Count Statistic [6] are introduced as tests to find weaknesses which can hardly or not at all be found with state-of-the-art tests for PUFs. These statistical tests are well known in other scientific fields, e.g., in geographical analysis, and have shown their efficiency there. This work adapts them for PUF analysis.

Modern textbooks on statistics provide generalized versions of Moran’s I, Geary’s c, and Joint Count Statistic. These can be applied to evaluate dependencies of data points within neighbourhoods instead of only the dependencies of direct neighbours like in the original methods. For this purpose, the generalized methods introduce a two-dimensional weighting matrix, which reflects how close the data points are in some chosen distance metric. The size of the considered neighbourhood can be used to trade insight vs. computational effort and is carefully selected in this work.

Even though an elaborate investigation of the proposed methods will be presented in future work, their application on the following three datasets — all measured on real-world devices — already gives a good overview of their capabilities:

1) Response bits of an array of 4096 Two-Stage ID PUFs [7] on 243 ASICs in a 90nm technology.
2) Frequencies of an array of 512 ring-oscillators (ROs) implemented on 193 Xilinx Spartan 3 FPGAs, measured at uncontrolled room temperature [2]. This data is well explored and can be seen as a reference to show that important design flaws can be identified.
3) Start-up values of 160 KiB of SRAM cells on 144 Infineon XMC4500 microcontrollers, sampled at uncontrolled room temperature.

Figures 1 to 4 exemplify the results for the different tests using Moran’s I. For the visualization and hypothesis testing, the Moran’s I values are transformed into z-scores, which can be compared to the overlaid standard normal distribution.

The results for the first experiment (Two-Stage ID PUF) are given in Figure 1. The figure shows that the kernel density estimate resembles the standard normal distribution (continuous) closely, i.e. no spatial correlations have been found in this data set. Since previous laborious analysis also came to the result that the PUF structure does not contain any spatial correlations, the result shows the behavior of the tests for uncorrelated binary PUF responses.

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Also, it shows that there is room to improve the tests. Therefore, it is important to know the limitations of the tests, as there are cases where other state-of-the-art tests are more fitting.

The analyses of the discussed PUFs show that the new methods can be used to identify spatial correlations in typical PUF scenarios efficiently, even if only a few PUF devices can be measured. This is the main advantage of the proposed tests. All presented tests are based on the knowledge of the exact asymptotic distribution, such that a sound statistical test for the rejection of the null hypothesis of spatial independence can be set up. These tests can be seen as a complement to existing methods for PUF evaluation.

**REFERENCES**


