

Parameter Identification of Large-Scale Magnetorheological Dampers in a Benchmark Building Platform

Arash Bahar, Francesc Pozo, Leonardo Acho, José Rodellar and Alex Barbat

Abstract—Magnetorheological (MR) dampers are devices that can be used for vibration reduction in structures. However, to use these devices in an effective way, a precise modeling is required. In this sense, in this paper we consider a modified parameter identification method of large-scale magnetorheological dampers which are represented using the normalized Bouc-Wen model. The main benefit of the proposed identification algorithm is the accuracy of the parameter estimation. The validation of the parameter identification method has been carried out using a black box model of an MR damper in a smart base-isolated benchmark building. Magnetorheological dampers are used in this numerical platform both as isolation bearings as well as semiactive control devices.

I. INTRODUCTION

Magnetorheological (MR) dampers are devices that change their mechanical properties when they are exposed to a magnetic field. The magnetorheological fluid of these actuators is characterized by a great ability to vary, in a reversible way, from a free-flowing linear viscous liquid to a semi-solid one within milliseconds [1]. Moreover, MR dampers have a low cost, low power requirements, large force capacity, robustness and can be controlled with a low voltage at the coils [1]. All these features make MR dampers very attractive and promising as actuators controlled by the voltage that can be used in different engineering fields, such as dampers and shock absorbers (pressure driven flow mode devices), as well as clutches, brakes, chucking, and locking devices (direct-shear mode devices) [9]. From a structural control point of view, MR dampers are usually employed as actuators operated by low voltages. In this respect, semi-active control systems seem to combine the best compromise between *passive* and *active* control: they offer the reliability of passive devices together with the versatility and adaptability of active

systems [3], [5], [19]. However, the first step in the design of a semi-active control strategy is the development of an accurate model of the MR device. It is worth noting that the system-identification issue plays a key role in this control problem [18]. High-accuracy models can be designed using two different model families: semi-physical models [15], [19], and black box models [10], [22]. Some of the most known semi-physical models to describe the hysteretic behaviour of MR dampers are the Bingham model and its extended versions, the Bouc-Wen model, the Dahl model, the modified LuGre model and some other non-parametric models [16]. It is important to remark that these models are not linear-in-parameters and, therefore, classical parameter identification methods, such as the gradient or the mean square algorithms, cannot be applied.

Using a normalized version of the Bouc-Wen model, Ikhoulane et al. [7] present an identification algorithm which is directly used for MR dampers in shear-mode [16]. However, this methodology can produce large parameter identification errors if the viscous friction is much smaller than the dry friction [16]. To cope with this drawback, a modified step was proposed by Rodríguez et al. [16] and tested in a small-scale MR damper. When the identification is applied to a large-scale MR damper, the parameter identification errors increase [17]. The aim of this paper is to improve the accuracy of the identification algorithm. This is based on augmenting the normalized Bouc-Wen model with an additional term. The validation of this modified parameter identification method has been carried out using a black box model of an MR damper in a smart base-isolated benchmark building [13]. This model is unknown for the user of this benchmark and for the designer of control systems. The benchmark platform is then considered as a virtual laboratory experiment. The numerical results show that the proposed modified method is able to improve significantly the accuracy of the parameter identification.

The paper is organized as follows. In Section II, the magnetorheological damper model is presented. In Section III, the key points of the modified identification method are discussed. In Section III, the application of the proposed identification method to a large-scale MR damper in a benchmark building is considered. Finally, some concluding remarks are stated in Section IV.

II. THE MAGNETORHEOLOGICAL DAMPER MODEL

The normalized version of the Bouc-Wen model [7] is an equivalent representation of the original Bouc-Wen model

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[22]. For MR dampers in shear mode it takes the form:

$$\Phi_n(\dot{x}, w)(t) = \kappa_{\dot{x}}(v)\dot{x}(t) + \kappa_w(v)w(t), \quad (1)$$

$$\dot{w}(t) = \rho(\dot{x}(t) - \sigma|\dot{x}(t)||w(t)|^{n-1}w(t) + (\sigma - 1)\dot{x}(t)|w(t)|^n), \quad (2)$$

where $\Phi_n(\dot{x}, w)$ is the output force of the MR damper, $\dot{x}(t)$ and v are the velocity and voltage inputs, respectively. The voltage input v is the applied voltage at the coil of the MR damper. The system parameters, which are voltage-dependent, are $\kappa_{\dot{x}}(v) > 0$, $\kappa_w(v) > 0$, $\rho > 0$, $\sigma > 1/2$, and $n \geq 1$. These parameters control the shape of the hysteresis loop and their meaning can be found in [6]. The state variable $w(t)$ has not a physical meaning so that it is not accessible to measurements.

Since the normalized Bouc-Wen representation described in equations (1)-(2) is not a linear-in-parameter model, classical parameter identification methods cannot be applied. In this regard, a new parameter identification algorithm has been proposed in [7, p. 38], which is based on a physical understanding of the device along with a black box description. Rodríguez et al. [17] used this methodology for a large-scale MR damper. The method is based on applying a periodic input velocity $\dot{x}(t)$ at a constant voltage coil v and observing the periodic steady-state force response of the MR damper. Nonetheless, large relative errors in the identification process can be observed when the MR damper has a viscous friction ($\kappa_{\dot{x}}(v)\dot{x}(t)$) small enough with respect to the dry friction ($\kappa_w(v)w(t)$). To cope with this drawback, when the displacement is large enough, an alternative method based on the plastic region of the force-velocity diagram of the MR damper has been proposed in [16]. However, the model in equations (1)-(2) may not give an accurate representation of large-scale MR dampers which do not belong to the shear-type category. For instance, consider the black box model of an MR damper in the smart base-isolated benchmark building [13]. Figure 1 contains the force-displacement and force-velocity diagrams when this MR damper is excited by a sinusoidal displacement and velocity. In order to test the goodness of the Bouc-Wen model, this figure also contains the response of the dynamic model in equations (1)-(2) with some appropriate parameters. It can be observed that the resulting plastic branch in the force-velocity diagram is wider than the corresponding branch of the Bouc-Wen model. In the literature, the same type of cycles have been experimentally reported, for instance, in [4, Figure 4(b)], [11, Figure 9] and [12, Figure 7]. Therefore, it can be derived that this kind of hysteretic loops are unable to be reproduced with the original Bouc-Wen model. To improve the accuracy of the model representation and, consequently, the accuracy of the parameter identification, we use the following extended Bouc-Wen model:

$$\Phi_e(x, \dot{x}, w)(t) = \kappa_x(v)x(t) + \kappa_{\dot{x}}(v)\dot{x}(t) + \kappa_w(v)w(t), \quad (3)$$

$$\dot{w}(t) = \rho(\dot{x}(t) - \sigma|\dot{x}(t)||w(t)|^{n-1}w(t) + (\sigma - 1)\dot{x}(t)|w(t)|^n), \quad (4)$$

where the term $\kappa_x(v)x(t)$, which represents a linear elastic force, has been added. We consider that the coefficient κ_x is voltage-dependent, as the other parameters. The effect of this term can be observed not only in the force-velocity diagram, but also in the force-displacement: the resulting plot is inclined. This feature has also been experimentally reported in, for instance, [2, Figure 8], [11, Figure 9] and [12, Figure 7].

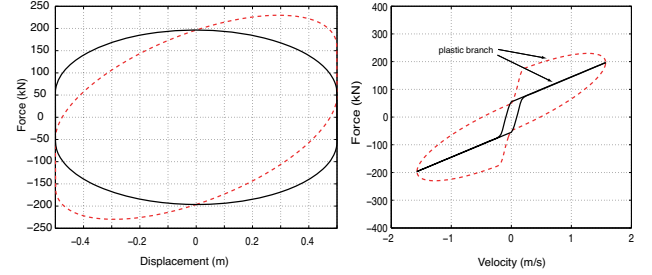


Fig. 1. Force-displacement (left) and force-velocity (right) diagrams of the black box model of the MR damper when it is excited by a sinusoidal displacement and velocity (dashed). The response of the dynamic Bouc-Wen model in equations (1)-(2) under the same excitation is represented by a solid line.

III. MODEL PARAMETER IDENTIFICATION

This section is concerned with the computation of the parameters of the extended model in equations (3)-(4). The proposed algorithm will be divided in two steps: (a) the estimation of the value of κ_x and (b) the estimation of the rest of the parameters based on the identification algorithm in [17].

At constant voltage, the computation of the parameter $\kappa_x(v)$ can be performed graphically by considering the force-displacement diagram of the MR damper. When this device is excited by a sinusoidal displacement with a large enough amplitude, the average inclination of the resulting plot gives an estimation of this parameter. As an example, consider the black box model of an MR damper in the smart base-isolated benchmark building. When this MR damper is driven with zero coil command voltage, we obtain the force-displacement diagram in Figure 2 (left). The estimated value of κ_x is then computed as $\kappa_x = \frac{82.8}{0.4} = 207$ kN.

To estimate the rest of the parameters, we use the knowledge of the parameter κ_x and the fact that

$$\Phi_n(\dot{x}, w)(t) = \Phi_e(x, \dot{x}, w)(t) - \kappa_x(v)x(t).$$

Figure 2 (right) depicts (in solid line) the force-velocity diagram for the resulting output force Φ_e of the MR damper minus the linear elastic force $\kappa_x(v)x(t)$, when this device is excited by a sinusoidal displacement and velocity. It can be recognized from this figure that this *new* cycle has the same shape as the force-velocity cycle of the model in equations (1)-(2), which is plotted in Figure 1 right. As a result, for the identification of the rest of the parameters, that is, the

parameters of the model

$$\begin{aligned}\Phi_n(\dot{x}, w)(t) &= \kappa_{\dot{x}}(v)\dot{x}(t) + \kappa_w(v)w(t), \\ \dot{w}(t) &= \rho(\dot{x}(t) - \sigma|\dot{x}(t)||w(t)|^{n-1}w(t) \\ &\quad + (\sigma - 1)\dot{x}(t)|w(t)|^n),\end{aligned}$$

we can follow basically the same idea as in [17]. The details of this method are omitted here but can be found in the Appendix.

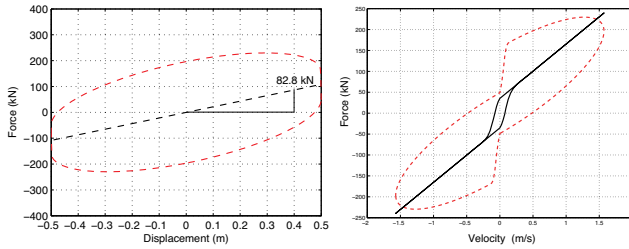


Fig. 2. The average inclination of the force-displacement diagram, when the MR damper is excited by a sinusoidal displacement, gives an estimation of the parameter κ_x (left). Force-velocity diagram for the resulting output force Φ_e of the MR damper (dashed) and the force $\Phi_n = \Phi_e - \kappa_x(v)x(t)$ (solid) (right).

This section is concerned with the application of the proposed method on a virtual MR damper. More precisely, the proposed identification algorithm is tested using a black box model of an MR damper, which is a part of a smart base-isolated benchmark building problem [13]. Consequently, we use this numerical platform as a virtual laboratory test. To validate the results, the output forces of the virtual device and the identified one will be compared using seven predefined earthquake records of the benchmark problem with their corresponding fluctuating voltage during full simulations. The MR damper is used in this context as a semi-active device to reduce the structural response of the building.

A. Smart base-isolated benchmark building

The smart base-isolated benchmark building [13] is employed as an interesting and more realistic example to further investigate the effectiveness of the proposed design approach. This benchmark problem is recognized by the American Society of Civil Engineers (ASCE) Structural Control Committee as a state-of-the-art model developed to provide a computational platform for numerical experiments of seismic control attenuation [14], [20].

The benchmark structure is an eight-storey frame building with steel-braces, 82.4 m long and 54.3 m wide, similar to existing buildings in Los Angeles, California. Stories one to six have an L-shaped plan while the higher floors have a rectangular plan. The superstructure rests on a rigid concrete base, which is isolated from the ground by an isolator layer, and consists of linear beam, column and bracing elements and rigid slabs. Below the base, the isolation layer consists of a variety of 92 isolation bearings. The isolators are connected between the drop panels and the footings below.

B. Identification results

In order to implement the identification procedure in Section II it is necessary to apply a periodic excitation displacement and observe the corresponding MR damper force. Figure 3 illustrates these two signals for a zero voltage. A set of experiments have been performed for different voltages in the range $[0, 1]$ volts.

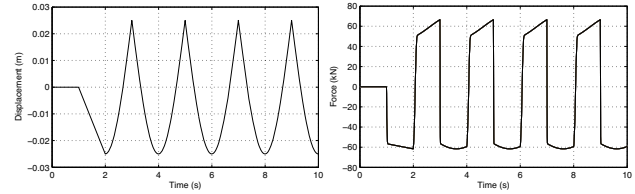


Fig. 3. Response of the MR damper model in the benchmark building platform.

The resulting values of the parameters of the model in equations (3)-(4) are listed in Table I. Figure 5 plots these parameters as a function of the voltage. To find an accurate voltage-dependent relation of these parameters, and according with the functional dependence in Figure 5, we consider that $\kappa_x(v)$ is constant, $\kappa_{\dot{x}}(v)$ is linear and $n(v)$, $\rho(v)$ and $\sigma(v)$ are exponential:

$$\kappa_x(v) = \kappa_x \quad (5)$$

$$\kappa_{\dot{x}}(v) = \kappa_{\dot{x},a} + \kappa_{\dot{x},b}v \quad (6)$$

$$n(v) = n_a + n_b \exp(-13v) \quad (7)$$

$$\rho(v) = \rho_a + \rho_b \exp(-14v) \quad (8)$$

$$\sigma(v) = \sigma_a + \sigma_b \exp(-14v) \quad (9)$$

Because of the importance of the parameter κ_w due to its great influence in the resulted force (the range of its magnitude is, approximately, from 50 kN to 1000 kN, as can be seen in Table I), its voltage dependence function has been estimated in three different regions based on the variation of the resulted values (Figure 4).

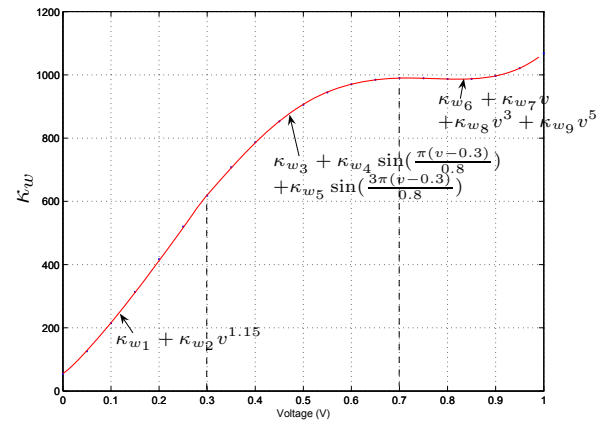


Fig. 4. Results of the parameter identification algorithm.

The coefficients $\kappa_{\dot{x},a}$, $\kappa_{\dot{x},b}$, $\kappa_{w1}, \dots, \kappa_{w9}$, n_a , n_b , ρ_a , ρ_b , σ_a and σ_b , which are listed in Table II, can be computed using

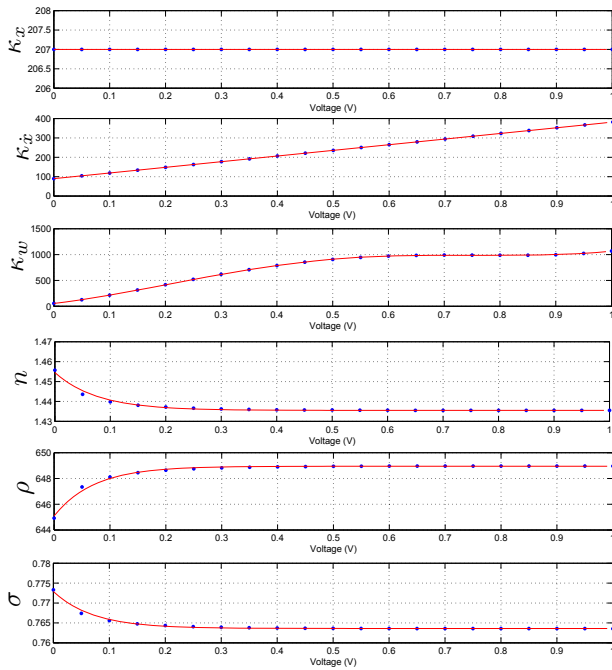


Fig. 5. Results of the parameter identification algorithm.

MATLAB. The voltage-dependent functions are plotted in Figure 5.

 TABLE I
IDENTIFICATION RESULTS

v	κ_x	$\kappa_{\dot{x}}$	κ_w	ρ	n	σ
0.00	207	89.643	54.652	644.92	1.4557	0.7733
0.05	207	104.24	125.97	647.34	1.4436	0.7674
0.10	207	118.84	214.49	648.11	1.4398	0.7656
0.15	207	133.44	313.47	648.45	1.4381	0.7648
0.20	207	148.04	416.96	648.64	1.4372	0.7643
0.25	207	162.64	519.87	648.75	1.4366	0.7641
0.30	207	177.24	617.94	648.82	1.4362	0.7639
0.35	207	191.84	707.73	648.87	1.4360	0.7638
0.40	207	206.44	786.63	648.90	1.4358	0.7637
0.45	207	221.04	852.86	648.92	1.4357	0.7636
0.50	207	235.64	905.48	648.94	1.4357	0.7636
0.55	207	205.25	944.37	648.95	1.4356	0.7636
0.60	207	264.84	970.24	648.96	1.4356	0.7636
0.65	207	279.44	984.64	648.96	1.4355	0.7636
0.70	207	294.04	989.94	648.96	1.4355	0.7636
0.75	207	308.64	989.34	648.96	1.4355	0.7636
0.80	207	323.24	986.89	648.96	1.4355	0.7636
0.85	207	337.84	987.43	648.96	1.4355	0.7636
0.90	207	352.44	996.67	648.96	1.4355	0.7638
0.95	207	367.04	1021.1	648.96	1.4355	0.7636
1.00	207	381.64	1068.2	648.98	1.4355	0.7635

C. Model validation

The identification models presented in the literature usually have good accuracy when they consider a constant voltage. However, because of the role of MR dampers as a semi-active devices in structural control systems, the final identified model has to be checked under a simulated con-

 TABLE II
IDENTIFICATION RESULTS

parameter	value
κ_x	207
$\kappa_{\dot{x}}$	$\kappa_{\dot{x},a}$ 89.64
	$\kappa_{\dot{x},b}$ 292
ρ	ρ_a 648.95
	ρ_b -3.86
n	n_a 1.44
	n_b 0.02
σ	σ_a 0.76
	σ_b 0.009
κ_w	κ_{w1} 55.38
	κ_{w2} 2270.0
	κ_{w3} 619.85
	κ_{w4} 387.34
	κ_{w5} 18.42
	κ_{w6} -87.52
	κ_{w7} 2665.0
	κ_{w8} -3054.7
	κ_{w9} 1545.5

dition using, for instance, an earthquake record and the corresponding fluctuating command voltage as a consequence of the control process. To do this, our identified model is compared with the corresponding black box model of the MR damper in the benchmark building platform under exactly the same situation. To measure the discrepancy between the two models, the 1-norm error (ε) is used:

$$\varepsilon = \frac{\|F_{BM} - F_{id}\|_1}{\|F_{BM}\|_1}, \quad (10)$$

$$\|f\|_1 = \int_0^{T_r} |f(t)| dt, \quad (11)$$

where F_{BM} is the output force of the black box model (benchmark building platform) and F_{id} is the resulting force of the identified MR damper based on the model in equations (3)-(4). The length in time of each earthquake is denoted by T_r . The 1-norm is a measure that reflects the average size of a signal and thus it is a good tool for computing the discrepancy between these two models. Based on this 1-norm, if the computed value of the damping force is far from the reference value, the value of ε will be large. On the contrary, if it is small, the identified model can produce forces which are very close to *real* ones. Table III presents the model errors for several earthquakes (FP- x and FP- y are the estimation errors in the x -force and y -force directions). A sample earthquake record and the corresponding command voltage during the control process are presented in Figure 6. In this application, the MR damper is used as a semi-active device in which the voltage is varying by a feedback control loop [8].

D. Comparison of results

It is interesting to compare the resulting model errors in Table III with the resulting model errors when the parameter identification is performed with the model in equations (1)-(2). Table IV shows the values of the errors for this case.

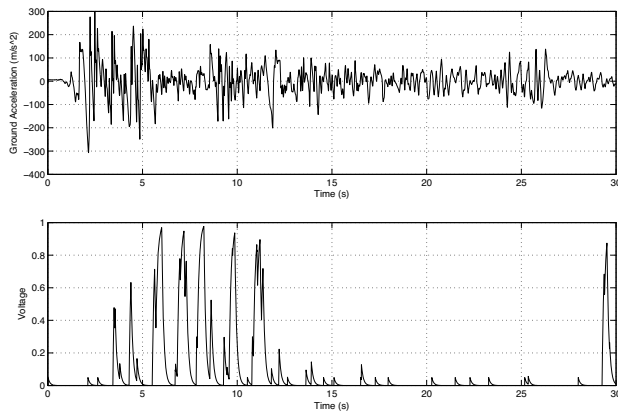


Fig. 6. El Centro, ground acceleration (top) and corresponding command voltage (bottom).

TABLE III
ERROR NORM (ε) FOR THE PROPOSED PARAMETER IDENTIFICATION

	Newhall	Sylmar	El Centro	Rinaldi
FP- x	6.47%	5.67%	7.78%	7.12%
FP- y	3.84%	8.44%	7.90%	5.67%
	Kobe	Jiji	Erzinkan	
FP- x	6.52%	3.61%	4.88%	
FP- y	7.85%	4.02%	5.35%	

TABLE IV
ERROR NORM (ε) FOR THE METHOD IN [16]

	Newhall	Sylmar	El Centro	Rinaldi
FP- x	16.15%	18.06%	22.89%	17.55%
FP- y	15.83%	24.14%	19.68%	18.48%
	Kobe	Jiji	Erzinkan	
FP- x	18.22%	14.16%	14.91%	
FP- y	24.72%	20.09%	18.80%	

By comparing these two tables, the proposed parameter identification algorithm is clearly more accurate than the method presented in [16].

Figure 7 shows the comparison between the output force of the black box MR damper during the simulation of the benchmark building under Kobe earthquake, with the two identified models, the proposed one and the model in [16]. Since the two plots in Figure 7 (top) are very close, Figure 8 shows the corresponding errors in both cases.

IV. CONCLUSION

This paper has proposed an extension of a parameter identification method for MR dampers. This extension allows to identify a larger class of MR dampers more accurately. The validation of the parameter identification method has been carried out using a black box model of an MR damper in a smart base-isolated benchmark building. The versatility

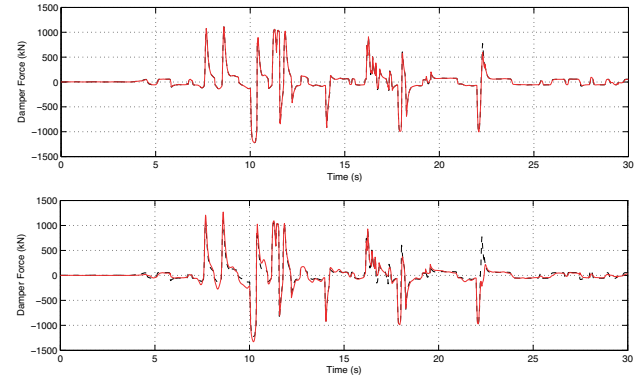


Fig. 7. Comparison of the MR damper force for the proposed model (top/solid) and for the model in [16] (bottom/solid), both with the response of the original black box model (dashed), under Kobe ground motion (FP- y).

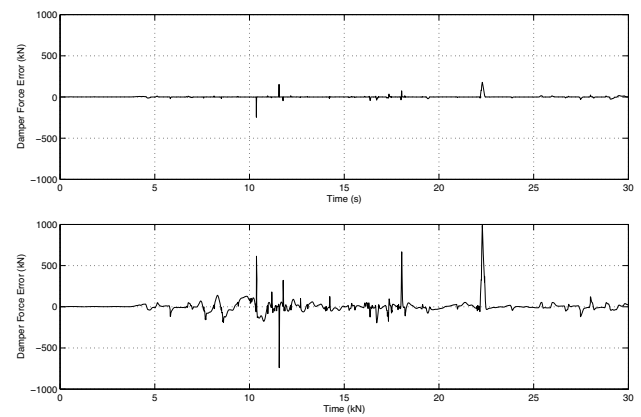


Fig. 8. Generated damper force errors for proposed model (above), and original method [16] (below), under Kobe ground motion (FP- y).

of the parameter identification method has been tested using the MR damper as a semi-active device under time-varying voltage and earthquake excitation.

APPENDIX

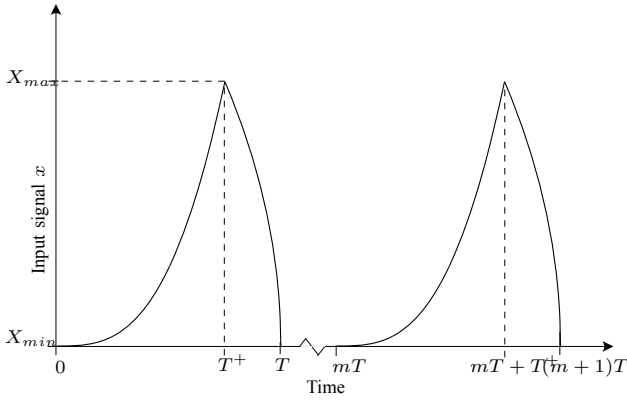
The parameter identification in [17] departs from the next shear-mode model:

$$\Phi_n(\dot{x})(t) = \kappa_{\dot{x}}(v)\dot{x}(t) + \kappa_w(v)w(t) \quad (12)$$

$$\begin{aligned} \dot{w}(t) = & \rho(\dot{x}(t) - \sigma|\dot{x}(t)||w(t)|^{n-1}w(t) \\ & + (\sigma - 1)\dot{x}(t)|w(t)|^n) \end{aligned} \quad (13)$$

where $\kappa_x > 0$, $\kappa_w > 0$, $\rho > 0$, $\sigma > 1/2$, and $n \geq 1$. For parameter identification, a T -periodic input $\dot{x}(t)$ (see Figure 9) is applied to the Bouc-Wen system under constant voltage v . It has been proved [7] that the output force of the Bouc-Wen model goes asymptotically to a periodic steady-state so that a limit cycle is obtained. The identification method assumes the knowledge of the relation $\bar{w}(x)$ that describes this cycle. The whole identification process can be summarized as follows.

The parameter $\kappa_{\dot{x}}$ is first determined using the plastic region ($\bar{w} \approx 1$) of the hysteresis loop by a linear regression


 Fig. 9. A sample T -wave periodic signal

for each constant voltage:

$$\bar{F}(\tau) = \kappa_x(v)\dot{x}(\tau) + \kappa_w(v).$$

To continue with parametric estimation, a function θ is computed as:

$$\theta(x(\tau)) = \bar{F}(x(\tau)) - \kappa_x \frac{dx(\tau)}{d\tau}, \quad \tau \in [0, T^+], \quad (14)$$

which has a unique zero, i.e., there exists a time instant $\tau_* \in [0, T^+]$, and a corresponding value $x_* = x(\tau_*) \in [X_{\min}, X_{\max}]$, such that the function θ is zero. Because θ is known, then \dot{x}_* is also known. Define the quantity

$$a = \left(\frac{d\theta(x)}{dx} \right)_{x=x_*}. \quad (15)$$

Then, the parameter n is determined as:

$$n = \frac{\log \left[\frac{\left(\frac{d\theta(x)}{dx} \right)_{x=x_{*2}} - a}{\left(\frac{d\theta(x)}{dx} \right)_{x=x_{*1}} - a} \right]}{\log \left(\frac{\theta_{x=x_{*2}}}{\theta_{x=x_{*1}}} \right)} \quad (16)$$

where $x_{*2} > x_{*1} > x_*$ are design parameters. Define

$$b = \frac{a - \left(\frac{d\theta(x)}{dx} \right)_{x=x_{*2}}}{\theta(x_{*2})^n}. \quad (17)$$

Then, the parameters κ_w and ρ are computed as follows:

$$\kappa_w = \sqrt[n]{\frac{a}{b}}, \quad (18)$$

$$\rho = \frac{a}{\kappa_w}. \quad (19)$$

The function $\bar{w}(x)$ can be computed as:

$$\bar{w}(x) = \frac{\theta(x)}{\kappa_w}. \quad (20)$$

Finally, the remaining parameter σ is determined as:

$$\sigma = \frac{1}{2} \left(\frac{\left(\frac{d\bar{w}(x)}{dx} \right)_{x=x_{*3}} - 1}{\frac{\rho}{(-\bar{w}(x_{*3})^n)} + 1} \right) \quad (21)$$

where x_{*3} is a design parameter such that $x_{*3} < x_*$.

REFERENCES

- [1] G. Bossis, P. Khuzir, S. Laci, and O. Volkova, Yield behavior of magnetorheological suspensions, *Journal of Magnetism and Magnetic Materials*, **258-259**:456-458, 2003.
- [2] W.W. Chooi, S.O. Oyadiji, Design, modelling and testing of magnetorheological (MR) dampers using analytical flow solutions, *Computers & Structures*, **86**(3-5):473-482, 2008.
- [3] A. Dominguez, R. Sedaghati, and I. Stiharu, Modeling and application of MR dampers in semi-adaptive structures, *Computers & Structures*, **86**(3-5):407-415, 2008.
- [4] S.J. Dyke, B.F. Spencer Jr., M.K. Sain, and J. D. Carlson, An experimental study of MR dampers for seismic protection, *Smart Materials and Structures*, **7**(5):693-703, 1998.
- [5] Z.Q. Gu, and S.O. Oyadiji, Application of MR damper in structural control using ANFIS method, *Computers & Structures*, **86**(3-5):427-436, 2008.
- [6] F. Ikhouane, J.E. Hurtado, and J. Rodellar, Variation of the hysteresis loop with the Bouc-Wen model parameters, *Nonlinear Dynamics*, **48**(4):361-380, 2007.
- [7] F. Ikhouane, and J. Rodellar, *Systems with Hysteresis: Analysis, Identification and Control Using the Bouc-Wen Model*, John Wiley & Sons, Inc., 2007.
- [8] L.M. Jansen, and S.J. Dyke, Semiactive control strategies for MR dampers: comparative study, *Journal of Engineering Mechanics*, **126**(8):795-803, 2000.
- [9] M. R. Jolly, J. W. Bender, and J. D. Carlson, Properties and applications of commercial magnetorheological fluids, *Journal of Intelligent Material Systems and Structures*, **10**(1):5-13, 1999.
- [10] J. Gang, M. K. Sain, K. D. Pham, B. F. Spencer Jr., and J. C. Ramallo, Modeling MR dampers: A nonlinear black box approach, *Proceedings of the American Control Conference*: 429-434, 2001.
- [11] H. Gavin, J. Hoagg, and M. Dobossy, Optimal design of MR dampers, *Proceedings of the US-Japan Workshop on Smart Structures for Improved Seismic Performance in Urban Regions*, Seattle WA, 225-236, 2001.
- [12] G. Jin, M. K. Sain, and B. F. Spencer Jr., Nonlinear blackbox modeling of MR-damper for civil structural control, *IEEE Transactions on Control Systems Technology*, **13**(3):345-355, 2005.
- [13] S. Narasimhan, S. Nagarajaiah, E. A. Johnson, and H. P. Gavin, Smart base-isolated benchmark building. Part I: Problem definition, *Structural Control and Health Monitoring*, **13**(2-3):573-588, 2006.
- [14] Y. Ohtori, R.E. Christenson, B.F. Spencer and S.J. Dyke, Benchmark problems in seismically excited nonlinear buildings. *Journal of Engineering Mechanics*, **130**(4):366-385, 2004.
- [15] F. Pozo, L. Acho, A. Rodriguez, and G. Pujol, Nonlinear modeling of hysteretic systems with double hysteretic loops using position and acceleration information, *Nonlinear Dynamics*, doi: 10.1007/s11071-008-9414-7.
- [16] A. Rodriguez, F. Ikhouane, J. Rodellar, and N. Luo, Modeling and identification of a small-scale magnetorheological damper, *Journal of Intelligent Material Systems and Structures*, doi: 10.1177/1045389X08098440.
- [17] A. Rodriguez, N. Iwata, F. Ikhouane, and J. Rodellar, Model identification of a large-scale magnetorheological fluid damper, *Smart Materials and Structures*, **18**(1), doi: 10.1088/0964-1726/18/1/015010, 2009.
- [18] S. M. Savaresi, S. Bittanti, and M. Montiglio, Identification of semi-physical and black box nonlinear models: The case of MR dampers for vehicles control, *Automatica*, **41**(1):113-127, 2005.
- [19] B. F. Spencer Jr., S. J. Dyke, M. K. Sain, and J. D. Carlson, Phenomenological model of a magnetorheological damper, *Journal of Engineering Mechanics*, **123**(3): 230-238, 1997.
- [20] B.F. Spencer, and S. Nagarajaiah, State of the art of structural control. *Journal of Structural Engineering*, **129**(7):845-856, 2003.
- [21] D. H. Wang, and W. H. Liao, Neural network modeling and controllers for magnetorheological fluid dampers, *Proceedings of the 10th IEEE International Conference on Fuzzy Systems*, **3**: 1323-1326, 2001.
- [22] Y. K. Wen, Method for random vibration of hysteretic systems, *Journal of Engineering Mechanics*, **102**(2):249-263, 1976.
- [23] P.Q. Xia, An inverse model of MR damper using optimal neural network and system identification, *Journal of Sound and Vibration*, **266**(5):1009-1023, 2003.