

1 Article

2 Onset frequency of fatigue effects in pure aluminum 3 and 7075 (AlZnMg) and 2024 (AlCuMg) alloys

4 Jose I. Rojas ^{1,*} and Daniel Crespo ²

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7 ¹ Department of Physics - Section of Aerospace Engineering of Escola d'Enginyeria de Telecomunicació i
8 Aeroespacial de Castelldefels, Universitat Politècnica de Catalunya; c/ Esteve Terradas 7, 08860,
9 Castelldefels (Spain); Correspondence: josep.ignasi.rojas@upc.edu

10 ² Department of Physics, Universitat Politècnica de Catalunya; c/ Esteve Terradas 7, 08860, Castelldefels
11 (Spain); daniel.crespo@upc.edu

12 * Correspondence: josep.ignasi.rojas@upc.edu; Tel.: +34-93-413-4130

13 **Abstract:** The viscoelastic response of pure Al and 7075 (AlZnMg) and 2024 (AlCuMg) alloys,
14 obtained with a dynamic-mechanical analyzer (DMA), is studied. The purpose is to identify
15 relationships between viscoelasticity and fatigue response of these materials, of great interest for
16 structural applications, in view of their mutual dependence on intrinsic microstructural effects
17 associated to internal friction. The objective is to investigate the influence of dynamic loading
18 frequency and temperature on fatigue, based on their effect on the viscoelastic behavior. This
19 research suggests that the decrease of yield and fatigue behavior reported for Al alloys as
20 temperature increases may be associated to the increase of internal friction. Also, materials
21 subjected to dynamic loading below a given threshold frequency exhibit a static-like response, such
22 that creep mechanisms dominate and fatigue effects are negligible. In this work, an alternative
23 procedure to the time-consuming fatigue tests is proposed to estimate this threshold frequency,
24 based on the frequency dependence of the initial decrease of storage modulus with temperature,
25 obtained from the relatively short DMA tests. This allows for a fast estimation of the threshold
26 frequency. The frequencies obtained for pure Al and 2024 and 7075 alloys are 0.001–0.005, 0.006 and
27 0.075–0.350 Hz, respectively.

28 **Keywords:** aluminum alloys; AlZnMg; AlCuMg; viscoelasticity; dynamic-mechanical analysis;
29 internal friction; loading frequency; fatigue
30

31 1. Introduction

32 Fatigue is a form of failure which may occur in structures subjected to dynamic loading, even at
33 stress levels significantly lower than the ultimate tensile strength under static loading [1]. Failure
34 results from a gradual process of damage accumulation and local strength reduction, which is
35 manifested by crack initiation and propagation, after relatively long periods of dynamic loading. It is
36 particularly dangerous in structural applications because of its brittle, catastrophic nature, and
37 because it occurs suddenly and without warning, since very little plastic deformation is observed in
38 the material prior to failure [1,2]. The fatigue fracture behavior of materials is dominated by the
39 microstructure [3]. When a material is subjected to dynamic loading, energy is dissipated due to
40 internal friction phenomena. Most of this energy manifests as heat and causes temperature increases
41 in the material, a process termed hysteresis heating. It has been suggested that all metals, when
42 subjected to hysteresis heating, are prone to fatigue [4].

43 In previous investigations, the viscoelastic response (including the internal friction behavior) of
44 Al alloys (AA) 7075 and 2024 was measured with a dynamic-mechanical analyzer (DMA) [5,6]. In
45 this work, experimental results on the viscoelastic response of pure Al are presented, first. Second,

1 these results for pure Al and the aforementioned alloys are analyzed with the purpose of identifying
2 relationships between the viscoelastic response and the fatigue behavior of these materials, in view
3 of their mutual dependence on intrinsic microstructural effects associated to internal friction [7].
4 Particularly, the objective is to investigate the influence of the dynamic loading frequency and
5 temperature on fatigue, based on the effect of these variables on the viscoelastic behavior. The
6 results seem to support the work by Amiri and Khonsari [4], as per the correlation between the
7 fatigue life and the initial hysteresis heating during dynamic loading. Namely, it is likely that the
8 decrease of yield and fatigue response observed in some metals as temperature increases is
9 associated to the increase of internal friction with temperature. Moreover, following previous
10 investigations by other researchers, suggesting the existence of a threshold frequency marking the
11 transition from a static-like response of the material to the advent of fatigue effects, in this work an
12 alternative procedure is proposed to estimate this threshold frequency based on experimental data
13 obtained with the relatively short DMA tests. These findings are of remarkable importance,
14 especially for the alloys, in view of their widespread use in structural applications under dynamic
15 loading. Particularly, AA 7075 and 2024 are key representatives of the AlZnMg and AlCuMg alloy
16 families (or 7xxx and 2xxx series, respectively), belonging to the group of age-hardenable alloys.
17 These alloys feature excellent mechanical properties and are highly suitable to a number of
18 industrial applications, especially in the aerospace sector and transport industry [8].

19 *1.1. Influence of the loading frequency on the fatigue response of metals*

20 Fatigue may be sensitive, for instance, to the strength, the manufacturing conditions and the
21 surface treatment of the material, but also to the loading frequency and loading environment, the
22 displacement rates and the stress amplitude [1,9–11]. In this work, we address the effects of the
23 dynamic loading frequency and temperature, in conjunction with the microstructure.

24 Much research has been devoted to ascertain whether accelerated laboratory tests (i.e., with
25 loading frequencies higher than those in service conditions) affect the fatigue response and how, but
26 this is yet a controversial issue. This is particularly true for the study of high cycle fatigue (HCF) and
27 very high cycle fatigue (VHCF) behavior by means of very high frequency tests. Tests in VHCF and
28 very low crack growth rates are time consuming with conventional fatigue testing techniques, like
29 rotating bending, with a maximum frequency of 100 Hz. Hence, accelerated laboratory tests are very
30 interesting because a significant reduction of testing time is possible using high-speed
31 servo-hydraulic machines [12], which may work at frequencies of 600 Hz, or specially using
32 ultrasonic equipment, which may reach frequencies of 20 kHz [13].

33 Zhu et al. [14] state that environmental effects need to be considered, and Mayer et al. [15]
34 explain that this is so because the time-dependent interaction with the environment may cause an
35 extrinsic frequency influence on fatigue properties, on top of the intrinsic strain rate effects. Furuya
36 et al. [12] state that frequency generally affects high frequency fatigue tests because: 1) fatigue limits
37 and lives decrease due to the temperature increase caused by plastic deformation [16]; 2)
38 dislocations may not match the applied frequency because dislocation movement is slow compared
39 to sonic velocity [17]; 3) provided that embrittlement by hydrogen diffusion had an effect [18],
40 fatigue lives would depend on both the number of loading cycles and time. However, Mayer [19]
41 reported also that the HCF behavior of metallic alloys is relatively insensitive to the test frequency,
42 provided that the ultrasonic testing procedure is appropriate (e.g., adequate cooling) and that
43 fatigue-creep interaction and the time-dependent interaction with the environment are negligible.
44 The reasons suggested are, on the one hand, that cyclic plastic straining is limited near the fatigue
45 limit or the threshold of fatigue crack growth (FCG), and thus plastic strain rates are low even at
46 high frequencies; and, on the other hand, the fact that shear stress has little sensitivity to strain rate
47 [20]. Mayer et al. [15] also commented that the influence of frequency becomes significantly smaller
48 if the dynamic stress amplitude is lower, maybe because cyclic loading is almost perfectly elastic.

49 For body-centered cubic (bcc) metals and metallic alloys, the HCF behavior is reported to be
50 more sensitive to frequency than for face-centered cubic (fcc) metals [13]. However, Furuya et al. [12]
51 observed that fatigue behavior of high-strength steels is independent of frequency. The argued cause

1 was their extremely high-strength, and thus reduced plasticity and dislocation mobility. The
2 hysteresis energy is low in low plasticity materials, and thus the frequency effects on fatigue
3 associated to the temperature increase are minimized. Likewise, Yan et al. [21] observed very little
4 variation of the fatigue strength of high-strength steel when testing at a conventional frequency (52.5
5 Hz) and at an ultrasonic frequency (20 kHz).

6 For an Al alloy similar to AA 7075 tested in the HCF regime at room temperature (RT), samples
7 tested at 100 Hz were reported to fail earlier than those tested at 20 kHz. However, the effect of
8 frequency on fatigue behavior was not statistically significant [15]. On the contrary, for E319 cast Al
9 alloy at 293, 423 and 523 K, fatigue life at 20 kHz was 5 to 10 times longer than that at 75 Hz [14], but
10 this author states that fatigue crack initiation is not influenced either by temperature or frequency.
11 Rather, the observed difference in fatigue life is attributed to environmental effects on FCG rate. The
12 fact that the moisture of ambient air deteriorates the fatigue life of high-strength Al alloys by
13 increasing the FCG rate has also been suggested by other authors [15,22]. Namely, Menan and
14 Henaff [23] suggest for AA 2024-T351 that fatigue and corrosion may interact such that FCG rates are
15 enhanced. These synergistic effects are more notorious at low frequencies, for a given number of
16 cycles at RT. Finally, Benson and Hancock [24] observed strain rate effects on cyclic plastic
17 deformation of AA 7075-T6, provided that cyclic stresses were close to the yield stress.

18 As per low frequency loading, on one hand, Nikbin and Radon [25] proposed a method to
19 predict the frequency region of interaction between creep and FCG using static data (obtained at 423
20 K for Al alloy RR58) and RT high frequency fatigue data, and assuming a linear cumulative damage
21 law. The results showed that the interaction region is 0.1 to 1 Hz for the Al alloy (see Figure 4 in [25]).
22 In the intermediate (steady state) stage of cracking for static and low frequency tests, crack growth is
23 sensitive to frequency and the fracture mode is time-dependent inter-granular in nature, suggesting
24 that creep dominates. Conversely, for high frequency tests, crack growth is insensitive to frequency
25 and the fracture mode is trans-granular, suggesting that pure fatigue mechanisms dominate. The
26 results indicated also little interaction between these processes.

27 On the other hand, Henaff et al. [26] analyzed creep crack growth (CCG) rates, FCG rates and
28 creep-fatigue crack growth (CFCG) rates of AA 2650-T6 at 293, 403 and 448 K, for frequencies of 0.05
29 and 20 Hz. The objective was to enable prediction of crack growth resistance of that alloy under very
30 low frequency loading at elevated temperatures. It was concluded that, in the studied frequency
31 range, frequency has only a slight effect on FCG rates at 448 K. In particular, under low frequency
32 loading it was observed a high increase in fracture surface fraction of inter-granular type, similar to
33 that corresponding to CCG. This shows that creep damage might occur during loading at low
34 frequency, in accordance with findings in [25]. Henaff et al. [26] reported also that, for a given
35 temperature, CF CG is unaffected by frequency above a critical value of the loading frequency (see
36 Figure 12(b) in [26]). Below, CF CG is inversely proportional to excitation frequency, i.e., a
37 time-dependent crack growth processes take place. This researcher suggested the existence of
38 creep-fatigue-environment interaction, as CF CG is affected by the environment at low frequency
39 loading, and proposed an alternative method to predict CF CG rates at very low frequencies, using a
40 superposition model and results obtained at higher frequencies.

41 1.2. Influence of temperature on the fatigue response of Al alloys

42 For E319 cast Al alloy tested at 293, 423 and 523 K, Zhu et al. [14] observed that the fatigue
43 strength decreases with temperature, and that the temperature dependence of the fatigue resistance
44 at 108 cycles follows closely the temperature dependence of the yield and tensile strength for this
45 alloy. Furthermore, by integration of a universal version of a modified superposition model, the
46 effects of temperature, frequency and the environment on the S-N curve of this alloy can be
47 predicted, and it is possible also to extrapolate ultrasonic data to conventional fatigue behavior [14].
48 Henaff et al. [26] concluded that the temperature has almost no influence on FCG rates for AA
49 2650-T6, after conducting tests at 293, 403 and 448 K and frequencies of 0.05 and 20 Hz. Amiri and
50 Khonsari [4] state that the initial slope of the temperature rise due to hysteresis heating observed at
51 the beginning of fatigue tests is a characteristic of metals. Capitalizing on this, they developed an

1 empirical model that predicts fatigue life based on that slope, thus preserving testing time. Indeed,
2 correlation of the temperature evolution with fatigue has been used successfully in many ways,
3 aside from for predicting fatigue life, as in the previous example. Namely, it has been used for
4 providing information on FCG [27] and the endurance limit of materials [28], or for quantification of
5 the cumulative damage in fatigue [16]. Also, the heat dissipated during ultrasonic cycling can be
6 used to calculate the cyclic plastic strain amplitude [15].

7 1.3. Influence of the microstructure on the fatigue response of Al alloys

8 There is abundant research in the literature on the effect of the microstructure on the fatigue
9 response of materials. For example, it is proposed that the mechanisms responsible for the fatigue
10 fracture behavior are associated to competing and synergistic influences of intrinsic microstructural
11 effects and interactions between dislocations and the microstructure [3]. Indeed, researchers claim
12 that prediction of fatigue life should be possible based on the knowledge of the microstructure prior
13 to beginning of service, without the need for expensive, time consuming fatigue experiments [29].
14 This would enable optimization of the material properties by controlling the microstructure.
15 Accordingly, a model based on dislocation stress was proposed to predict S-N curves using
16 microstructure/material sensitive parameters instead of constitutive equation parameters [29]. The
17 model is successful for low cycle fatigue life prediction.

18 2. Materials and Methods

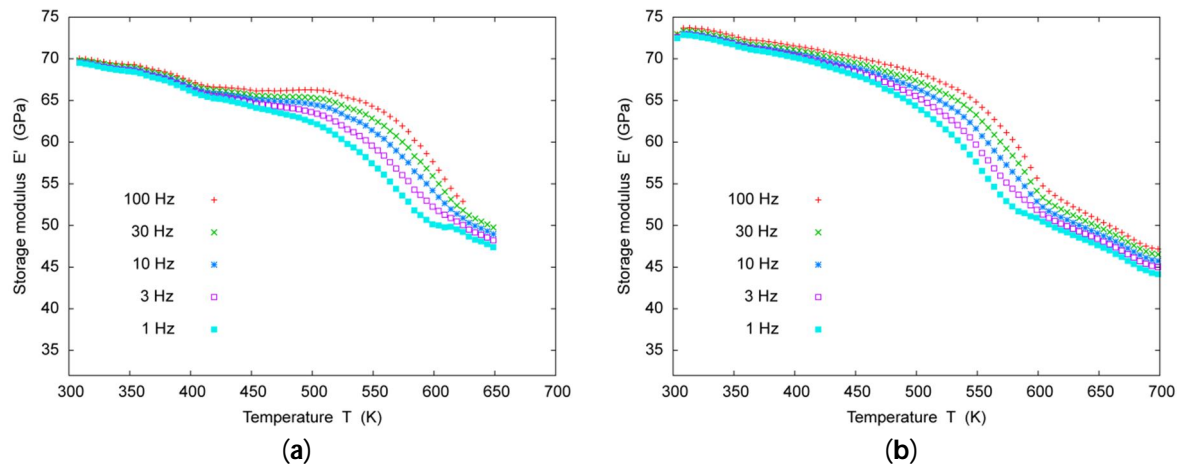
19 The tested specimens were machine cut from sheet of as-received pure Al (99.5 wt.% purity
20 according to the supplier, Alu-Stock, S.A.) in the H24 temper. The H24 temper consists in
21 cold-working (i.e., strain hardening) beyond desired hardness, followed by a softening treatment
22 consisting in annealing up to halfway of peak hardness. The specimens were rectangular plates 60
23 mm long, 8–12 mm wide and 2 mm thick. Half of these plates were annealed at 750 K for 30 min, and
24 immediately quenched in water to RT, to remove the strain hardening. A TA Instruments Q800
25 DMA was used to measure the viscoelastic response of the samples in N₂ atmosphere. Namely, the
26 DMA measured the storage modulus E' (i.e., the elastic –real– component of the dynamic tensile
27 modulus, accounting for the deformation energy stored by the material), the loss modulus E'' (i.e.,
28 the viscous –imaginary– component of the dynamic tensile modulus, accounting for the energy
29 dissipation due to internal friction during relaxation processes) and the loss tangent (also termed
30 mechanical damping or $\tan \delta$) [7]. The 3-point bending clamp was used, and the DMA was set to
31 sequentially apply dynamic loading with frequencies ranging from 1 to 100 Hz, at temperatures
32 from RT to 723 K in step increments of 5 K. More details on the procedure, as well as the viscoelastic
33 data of AA 7075-T6 and 2024-T3 used in this work, can be found in [5,6].

34 3. Results and Discussion

35 3.1. Storage modulus

36 Figure 1(a) shows E' for pure Al in the H24 temper, from RT to 648 K, while Figure 1(b) shows
37 E' for pure Al, from RT to 723 K, in both cases as obtained from DMA tests at frequencies ranging
38 from 1 to 100 Hz. The behavior of E' for pure Al is similar in some aspects to that observed for AA
39 7075-T6 and 2024-T3 [5,6] and AA 6082 [30] (an excel file including the values of E' , E'' , and loss
40 tangent measured for pure Al in the H24 temper, pure Al, AA 7075-T6 and AA 2024-T3 is provided
41 as supplementary material). For example, E' also decreases initially. The slope at low temperatures
42 (below the beginning of the dissolution of Guinier-Preston (GP) and Guinier-Preston-Bagariastkij
43 (GPB) zones, for the alloys) is what is most interesting in this study, as explained in Section 4.3. Also,
44 a significant decrease in E' is observed, with the beginning of this drop shifted to higher
45 temperatures (from around 423 to 523 K) as the loading frequency increases. Thus, at a given
46 temperature, the alloys show a stiffer response (i.e., E' is larger) at higher frequencies, as expected.
47 Also, E' depends more significantly on frequency at high temperatures (above 423 K). The fact that

1 the viscoelastic behavior becomes more prominent with temperature has already been observed in
 2 amorphous alloys [31], aside from AA 7075-T6 and 2024-T3 [5,6] and AA 6082 [30].



3 **Figure 1.** Storage modulus E' vs. temperature T from dynamic-mechanical analyzer tests at
 4 frequencies ranging from 1 to 100 Hz: (a) for pure Al in the H24 temper, from room temperature (RT)
 5 to 648 K; (b) for pure Al, from RT to 723 K.

6 3.2. Loss modulus

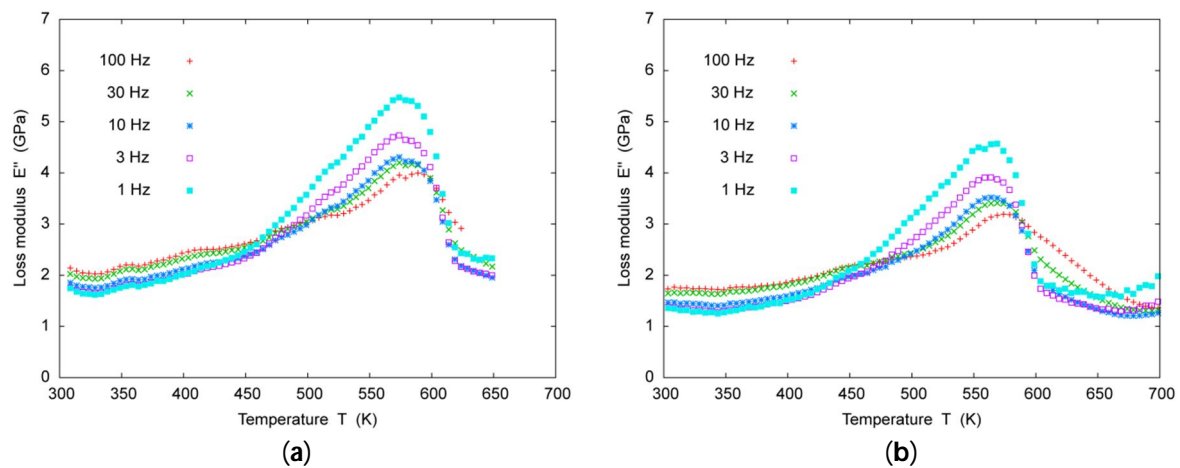
7 Figure 2(a) shows E'' for pure Al in the H24 temper, from RT to 648 K, while Figure 2(b) shows
 8 E'' for pure Al, from RT to 723 K, in both cases as obtained from DMA tests at frequencies ranging
 9 from 1 to 100 Hz. In this case, the behavior of E'' for pure Al shows noticeable differences to that
 10 observed for AA 7075-T6 and 2024-T3 [5,6] and AA 6082 [30]. At low temperatures, the slopes of E''
 11 are similar for all the studied frequencies and not very steep (all show almost a plateau). At 393–533
 12 K the slopes increase sharply. This variation in the slope is shifted towards higher temperatures with
 13 increasing loading frequency. The observed behavior may be due to the viscous loss at higher
 14 frequencies competing with shorter relaxation times. Since the relaxation time decreases with
 15 temperature due to the Arrhenius-type behavior of the relaxation rate [7], this means that the
 16 temperature above which the viscous effect exceeds the relaxation is higher for higher frequency. In
 17 other words, higher frequency viscous loss curves rise at a higher temperature than lower frequency
 18 curves.

19 For AA 7075-T6, 2024-T3 and 6082, the sharp growth in E'' with temperature reaches very high
 20 values without showing a peak, which is usually explained by presence of coupled relaxations [7].
 21 On the contrary, for pure Al, E'' clearly exhibits a peak, which is achieved virtually at the same
 22 temperature for all the frequencies (around 573 K). The peak is larger (both in width and height) as
 23 the loading frequency decreases. Previous works suggest that AlZnMg alloys, AlCuMg alloys and
 24 pure Al exhibit mechanical relaxation peaks associated to dislocations and to grain boundaries
 25 [32,33]. For example, dislocation motions explain some internal friction peaks associated to
 26 semi-coherent precipitates for the alloys [34], and also the Bordoni peak, which has been extensively
 27 studied in cold-worked pure Al [7]. In this case, the observed peak corresponds to a typical internal
 28 friction peak in polycrystalline Al, related to grain boundaries [7]. In particular, the mechanism
 29 governing this relaxation is based on sliding at boundaries between adjacent grains. Upon
 30 application of stress, this process starts with the sliding of a grain over the adjacent one, caused by
 31 the shear stress acting initially across their mutual boundary. As a consequence, the shear stress is
 32 reduced gradually and opposing stresses build up at the end of the boundary and into other adjacent
 33 grains. The process terminates when the shear stress has vanished across most of the boundary, and
 34 most of the total shearing force is sustained by the grain corners.

35 In addition, in Figure 2, a transition is observed around 473–513 K between the low temperature
 36 region where E'' is smaller for lower loading frequencies, and the high temperature region where

1 E'' is smaller for higher frequencies (a stiffer response in this case is expected). Finally, after the
 2 aforementioned peak, E'' seems to increase again in Figure 2(b), particularly for the lower
 3 frequencies.

4 As usual, the loss tangent obtained from the DMA tests exhibits qualitatively the same behavior
 5 as E'' (the plots of loss tangent vs. temperature are included as supplementary material). The only
 6 remarkable comment is that there are no appreciable differences between the mechanical damping
 7 behavior for pure Al in the H24 temper and for pure Al, like for the E'' behavior (differences in the
 8 measured absolute values fall virtually within the instrument accuracy).



9 **Figure 2.** Loss modulus E'' vs. temperature T from dynamic-mechanical analyzer tests at frequencies
 10 ranging from 1 to 100 Hz: (a) for pure Al in the H24 temper, from room temperature (RT) to 648 K; (b)
 11 for pure Al, from RT to 723 K.

12

13 3.3. Temperature dependence of the storage modulus

14 In absence of microstructural transformations, e.g., for pure Al and the alloys in the range RT–
 15 373 K, E' decreases linearly with temperature. The reasons supporting this assumption are
 16 explained herein. There is abundant literature reporting a decrease with temperature of the elastic
 17 stiffness constants of metals, e.g., the static elastic modulus of pure Al and Al alloys [35–38]. This
 18 decrease can be assumed linear in a wide temperature range. Significant deviations from linearity
 19 are only observed close to 0 K and well above the temperature range of most interest for this
 20 research, i.e., well above RT–373 K, as explained in Section 4.3. Wolfenden and Wolla [39] observed
 21 also a highly quasi-linear decrease of the dynamic elastic modulus with temperature, measured at
 22 high frequency (80 kHz) from RT to 748 K, for pure Al and for AA 6061 reinforced with alumina.

23 Figure 3 in [6] shows a comparison of static and high frequency dynamic elastic modulus data
 24 available in the literature with data obtained with the DMA for AA 2024-T3 and for pure Al at 1 Hz.
 25 As expected, our DMA results for pure Al in the range RT–373 K fall between the static and high
 26 frequency dynamic values of elastic modulus in the literature, but they show a pronounced decrease
 27 of dynamic elastic modulus starting around 423–523 K. This is coincident with the observed E''
 28 peak, as shown in Figure 2. Wolfenden and Wolla [39] assumed a linear behavior from RT to 748 K
 29 and explained this in terms of the Granato–Lücke theory for dislocation damping [40], but their data
 30 are too scattered to be explained with a single mechanism in the considered temperature range, as
 31 shown by our DMA results. Moreover, the low frequency dynamic elastic modulus of pure Al
 32 should also be sensitive to micrometric mechanisms such as boundary migration during
 33 recrystallization and grain growth, as shown by Zhang et al. [41]. This mechanism is likely to be
 34 much more relevant in fatigue processes. However, the microstructural evolution and mechanical
 35 properties of AA 7075-T6 and 2024-T3 are controlled by the successive redissolution and

1 precipitation of minority phases, and that is why it is likely that boundary migration is not the single
2 most significant mechanism governing the behavior of their dynamic elastic moduli.

3 Consequently, it can be assumed that, in absence of microstructural transformations, E'
4 decreases linearly with temperature. Accordingly, Table 1 shows the slope of the decrease of E'
5 with temperature for pure Al in the H24 temper and for pure Al, as obtained from linear regression
6 of the DMA experimental results. In the following, to refer properly to this parameter on the basis of
7 its physical meaning, it is termed "temperature softening coefficient", E'_0 . Finally, it is important to
8 note that the larger decrease of E' for low frequencies is typically explained by the Arrhenius-type
9 behavior of the relaxation rate. That is, the mechanical relaxation time decreases with temperature
10 [7] so that, at low frequencies, the shorter relaxation times lead to responses with larger values of E''
11 and smaller values of E' .

12 **Table 1.** Temperature softening coefficient E'_0 , for pure Al in the H24 temper and for pure Al, as
13 obtained from linear regression of dynamic-mechanical analyzer test data.

loading frequency [Hz]	E'_0 (pure Al in H24 temper) [MPa·K ⁻¹]	E'_0 (pure Al) [MPa·K ⁻¹]
100	-23.1	-26.4
30	-25.24	-27.7
10	-26.4	-29.1
3	-27.9	-31.0
1	-29.7	-32.2

14 3.4. Effect of internal friction on fatigue strength

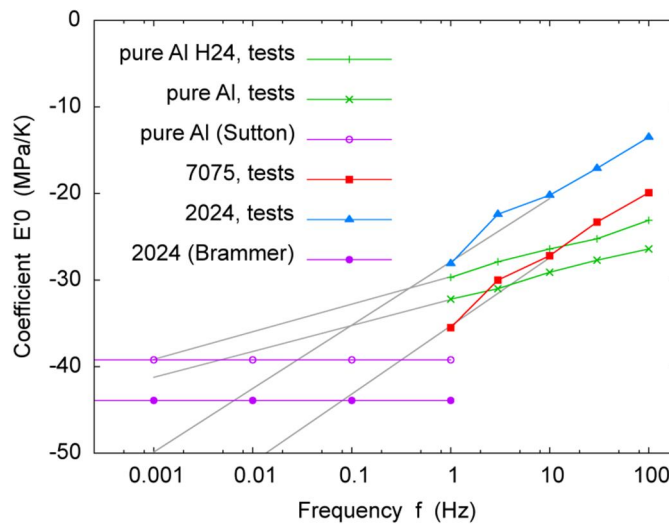
15 Considering that viscoelasticity is linked to the fatigue and yield stress behavior [7], it is likely
16 that the decrease of fatigue and yield stress behavior observed in metals as temperature increases is
17 associated to the increase of internal friction. The reasons supporting this assumption are explained
18 herein. Namely, Zhu et al. [14] observed that the fatigue strength of an Al alloy decreases with
19 temperature, with a behavior that follows closely the temperature dependence of the yield and
20 tensile strength. Also, Liaw et al. [16] suggested that the fatigue limits and fatigue lives of steels
21 decrease due to the temperature increase caused by plastic deformation. Finally, from the work by
22 Amiri and Khonsari [4], it appears that the more intense the hysteresis heating of a metal during
23 dynamic loading, the lower its fatigue resistance. Extrapolating the assumption stated above to AA
24 7075-T6, 2024-T3 and AA 6082, their yield and fatigue strength would decrease with temperature
25 according to the observed increase in internal friction in the tested temperature range, as shown in
26 [5,6] and [30], respectively. For pure Al, the yield and fatigue strength would decrease up to the E''
27 peak.

28 Furthermore, if considering the influence of loading frequency on internal friction, our results
29 suggest that below 423 K the yield and fatigue strength would decrease with increasing frequency,
30 while at high temperatures these properties would increase. These presumptions agree with some of
31 the research reported in the literature, but still there is controversy about the effect of frequency on
32 the fatigue response, as shown in Section 1.1. For example, our findings agree with results from low
33 frequency investigations for Al alloy RR58 at 423 K [25] and for AA 2650-T6 at 175°C [26], pointing
34 that fatigue life is sensitive to frequency and that it increases with loading frequency. There is
35 agreement also with results for E319 cast Al alloy at 423 and 523 K, pointing that fatigue life at 20
36 kHz was longer than at 75 Hz [14]. However, this behavior is attributed to environmental effects on
37 FCG rate, rather than intrinsic temperature or frequency effects.

38 3.5. Onset frequency of fatigue effects

1 It is reasonable to accept that, at sufficiently low loading frequency, fatigue effects become
 2 negligible. Indeed, in a series of dynamic loading tests with loading frequency decreasing to very
 3 low values, the test time scale will eventually become much larger than the largest mechanical
 4 relaxation time for any of the possible relaxation processes for the tested material. That is, the
 5 reduction in the loading frequency is equivalent to an increase in the reaction time and, therefore,
 6 there is a threshold frequency below which the reaction time is longer than the relaxation time.
 7 Consequently, the viscous effect as the loss mechanism is negligible as compared with the relaxation.
 8 This means that eventually E'' will decrease to a level that there will be no appreciable frictional
 9 energy loss due to relaxation effects. Recalling the statement by Amiri and Khonsari [4] that some
 10 degree of hysteresis heating (which is caused by the energy dissipated due to internal friction) is
 11 necessary for metals to experience fatigue, the conclusion is that, eventually, fatigue effects vanish.
 12 This hypothesis is in line with research by Henaff et al. [26] and Nikbin and Radon [25], suggesting
 13 the existence of a critical value of loading frequency below which, for a given temperature, the
 14 material exhibits a static-like response (relaxed case), crack growth is sensitive to frequency and
 15 static creep dominates instead of pure fatigue mechanisms.

16 Next, a procedure to estimate this threshold frequency is proposed based on the frequency
 17 dependence of the temperature softening coefficient E'_0 . The procedure is illustrated in Figure 3,
 18 which shows E'_0 as a function of the loading frequency for pure Al in the H24 temper and pure Al,
 19 as obtained from linear regression of DMA data, and for AA 7075-T6 and 2024-T3, as obtained in
 20 [5,6]. These values of E'_0 are compared to average values of the rate of loss of static elastic modulus
 21 with temperature, as obtained by linear regression of data in the literature for pure Al [36] and AA
 22 2024 [35]. To calculate these averages, data from Kamm and Alers [37] and from Varshni [38] were
 23 disregarded as they correspond to temperatures below RT. Data from Wolfenden and Wolla [39]
 24 were also disregarded since these data are too scattered in a broad temperature range, and thus the
 25 computable slope is probably not be representative.



26 **Figure 3.** Temperature softening coefficient E'_0 vs. frequency f for pure Al in the H24 temper, pure
 27 Al, Al alloy (AA) 7075-T6 and AA 2024-T3, as obtained from linear regression of test data from the
 28 dynamic-mechanical analyzer. Logarithmic tendency lines fitted to the data to extrapolate it to lower
 29 frequencies are also shown, as well as the rates of loss of static elastic modulus with temperature, as
 30 obtained by linear regression of data in the literature for pure Al [36] and AA 2024 [35].

31 Assuming that, at the threshold frequency, E'_0 should become equal to the rate of loss of elastic
 32 modulus with temperature under static loading conditions, this threshold frequency may be
 33 estimated by intersection of the latter rate with a tendency line extrapolating the behavior of E'_0
 34 measured experimentally to lower frequencies. In the example shown in Figure 3, the intersection of

1 a logarithmic tendency line with the rate of loss of static elastic modulus for pure Al in the H24
2 temper and pure Al gives a threshold frequency of around 0.001 and 0.005 Hz, respectively. For AA
3 2024-T3, the threshold frequency obtained with the same procedure would be about 0.006 Hz. For
4 AA 7075-T6, no data on the variation of the elastic stiffness constants with temperature was found in
5 the literature, but using the data available for AA 2024 and pure Al, a threshold frequency of 0.075
6 and 0.350 Hz would be obtained, respectively. These results are similar to those in the literature:
7 Henaff et al. [26] reported a critical frequency of 0.020 Hz for AA 2650-T6, and Nikbin and Radon
8 [25] reported that the transition region is 0.100 to 1 Hz for cast Al alloy RR58 at 423 K. However, to
9 better assess the performance of the proposed procedure, further comparison with experimental
10 data on fatigue response at very low frequencies is necessary. Unfortunately, there is a lack of this
11 type of test data [26], due to the extremely long testing time. It is interesting to note that, on one side,
12 according to our results, fatigue effects would seem to appear at lower loading frequencies for pure
13 Al, compared to the alloys. Thus, apparently the precipitation structure in the alloys would cause
14 not only hardening but would also enable for the alloys to be loaded at a wider range of low
15 frequencies without experiencing fatigue. On the other side, fatigue would appear already at lower
16 frequencies for pure Al in the H24 temper compared to pure Al. In this case, the reason may be the
17 lower ductility (and thus lower resistance to FCG) associated to the H24 temper.

18 The proposed procedure for the determination of the threshold frequency is a major result of
19 this work. Low frequency fatigue experiments are, by definition, very long. Furthermore, there is
20 still controversy about the effects of the exposure to the environment on the experimental results, as
21 it is not feasible to perform longstanding experiments in constant environment conditions. Besides,
22 the environment during service life is likely to be different than that during the experiments, and
23 thus estimations of the threshold frequency based on conventional, time-consuming fatigue
24 experiments are likely to be inaccurate. The determination of the threshold frequency from the data
25 obtained with the relatively short DMA tests (less than 3h) reflects intrinsic properties of the material
26 only. This offers also a standardized method, which allows precise comparison between different
27 alloys. Furthermore, it is quite insensitive to the specific instrumental range available for the tests,
28 provided the range is large enough to allow a consistent regression fit.

29 4. Conclusions

30 It was suggested that some degree of hysteresis heating is necessary for metals to experience
31 fatigue when subjected to dynamic loading. Hysteresis heating is caused by energy dissipated due to
32 internal friction, and thus an increase in the latter should have an effect on the fatigue response. In
33 particular, the results of this research suggest that the decrease of yield and fatigue behavior
34 reported for Al alloys as temperature increases may be associated to the increase of internal friction
35 with temperature. Due to the Arrhenius-type behavior of relaxation processes, the relaxation time
36 decreases with temperature. The reduction in the loading frequency is equivalent to an increase in
37 the reaction time and, therefore, there is a threshold frequency below which the reaction time is
38 longer than the relaxation time. Consequently, the viscous effect as the loss mechanism is negligible
39 as compared with the relaxation. In other words, with the dynamic loading frequency decreasing to
40 very low values, eventually there will be no appreciable frictional energy dissipation, and thus no
41 hysteresis heating, due to mechanical relaxation phenomena. Thus, below the threshold frequency
42 the material will exhibit a static-like response (relaxed case), such that creep mechanisms dominate
43 and fatigue effects are negligible. In this work, an alternative procedure to the time-consuming
44 conventional fatigue tests is proposed to estimate this threshold frequency, based on the frequency
45 dependence of the slope of the initial decrease of E' with temperature, which in this work is termed
46 temperature softening coefficient. The interesting point of our approach comes from the fact that this
47 coefficient is easily obtained from the relatively short DMA tests, hence allowing for a fast estimation
48 of the threshold frequency. For pure Al, AA 2024-T3 and AA 7075-T6, the threshold frequencies
49 obtained with this procedure are 0.001–0.005, 0.006 and 0.075–0.350 Hz, respectively. This suggests
50 that fatigue effects start to appear at lower loading frequencies for pure Al, while the alloys may be
51 loaded at a wider range of low frequencies without experiencing fatigue, probably due to effects

1 related to presence of precipitates. However, to better assess the performance of the proposed
2 procedure, further comparison with experimental data on fatigue response at very low frequencies
3 is necessary.

4 **Supplementary Materials:** The following supplementary material is available online at www.mdpi.com/link: 1)
5 Spreadsheet S1 - DMA test data (MS Excel file), which includes the measured values of storage modulus E' , loss
6 modulus E'' , and loss tangent (also termed mechanical damping or $\tan \delta$) for pure Al in the H24 temper, pure
7 Al, AA 7075-T6 and AA 2024-T3; 2) Figure S2a - mechanical damping of pure Al in the H24 temper and Figure
8 S2b - mechanical damping of pure Al.

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16 the decision to publish the results.

17

1 Abbreviations

2 The following abbreviations are used in this manuscript:

- 3 AA: Aluminum alloy(s)
- 4 bcc: Body-centered cubic
- 5 CFCG: Creep-fatigue crack growth
- 6 CCG: Creep crack growth
- 7 DMA: Dynamic-mechanical analyzer
- 8 fcc: Face-centered cubic
- 9 FCG: Fatigue crack growth
- 10 GPBZ: Guinier-Preston-Bagariastkij zones
- 11 GPZ: Guinier-Preston zones
- 12 HCF: High cycle fatigue
- 13 RT: Room temperature
- 14 VHCF: Very high cycle fatigue

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