Study of space condition effects and analyzing digital techniques for improving RF power amplifier's linearity and efficiency for small satellites

Kamran Haleem

SUPERVISED BY

Pere L. Gilabert Pinal
Gabriel Montoro Lopez

Universitat Politècnica de Catalunya
Master in Aerospace Science & Technology
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Abstract:

Objective of modern small satellite communication is to provide the end users with higher data rate downlink capability, in addition to, reliability and system efficiency. A significant device, with respect to power consumption and influence on system linearity, use in the transmission chain of small satellites, is power amplifier. The power amplifier tends to add distortion and non-linearity in the transmitted signal, when operating close to saturation point. For avoiding the non-linearity addition by the PA, it should be operated in linear region which causes the degradation in power efficiency. Therefore, for having the maximum power efficiency and improving linearity, the predistortion should be performed before inputting the signal to power amplifier. For compensating non-linear distortion, linearization scheme based on digital predistortion is used, which requires a feedback path for adaptation and extraction of new coefficients for DPD. Hence for making the DPD adaptive, ADC is required to add in the system. As a consequence of performing digital predistortion, the spectral regrowth occurs which causes the increase in bandwidth up to five times of original signal. Due to this reason, digital to analog converter has to sample the signal at five times of nyquist frequency which increases the cost and power consumption of DAC.

This master thesis presents the methodology implementation for compensating the non-linear distortion in PAs, applicable for small satellite communication, with a cooperative technique of digital and analog predistortion. This thesis provides with the solution for the increased sampling rate of signal at analog to digital converter with a use of combination of digital and analog predistortion. The predistortion (digital and analog) is design to focus on maximizing the linearity and minimizing the distortion and spectral regrowth. While the adaptive scheme of combined digital predistortion and analog predistortion (simulated) is designed, with an ideal low-pass filter between them, for implementation ease of the digital-to-analog converter and decrease in signal sampling rate.

The results provided in the thesis have shown that same linearity and efficiency can be achieved at amplifier’s output by implementing the above mentioned solution with a benefit of reducing the signal sampling frequency at DAC. A comparative analysis of power amplifier behavior in various configuration is presented in the dissertation.
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Glossary

ADC  Analog-to-Digital Converter
AM  Amplitude Modulation
APD  Analog Predistorter
ACEPR  Adjacent Channel Error Power Ratio
ACLR  Adjacent Channel Leakage Ratio
ACPR  Adjacent Channel Power Ratio
DPD  Digital Predistortion
DAC  Digital-to-Analog Converter
DDR  Dynamic Deviation Reduction
HEMT  High Electron Mobility Transistor
I/Q  In-phase/Quadrature
LS  Least-Squares
LMS  Least Mean Squares
NMSE  Normalized Mean Square Error
PA  Power Amplifier
PAE  Power Added Efficiency
PSD  Power Spectral Density
QAM  Quadrature Amplitude Modulation
RLS  Recursive Least Square
SNR  Signal-to-Noise Ratio
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Chapter 01

1.1. Introduction:

This Master Thesis addresses the study and implementation of cooperative digital and analog predistortion technique for improving power amplifier’s linearity. It also caters the solution for decrease in sampling frequency rate of digital to analog converter, that occurred due to the bandwidth expansion around five times of original signal, caused due to predistortion. The technique is implemented through simulating the model of power amplifier in Matlab Software and then perform the analysis of result achieved through feeding it to the predesigned real-time hardware test bed. The idea of this master thesis involves the designing of adaptive predistortion system for that purpose the accurate modelling of power amplifier is the initial and foremost step. Keeping in view of countering memory effects and better modelling of power amplifier the Dynamic Deviation Reduction Volterra Series is selected.

1.2. Background and Motivation:

In this era of communication, every communication technique has its significance and effects on daily life of people. Satellite communication is currently a vast field of research and improvement, whereas, substantial progress has been made in this regard recently. With the advancement in this area, commercial large satellites are now being replaced with the small (micro, nano and pico) satellites. These are largely using for the purpose of communication, building constellations of satellites for certain objectives and in-orbit inspection. Having certain advantages for this development, there are also few problems in their implementation which needs to be countered. Due to the decrease in size, the on-board power generation and storing capabilities have reduced by large factor. Therefore, the power consumption of each instrument becomes comparatively more significant.

Power amplifier is one of high power consuming devices in the transmission chain of a satellite. It not only consumes more power but also tends to add non-linearities which effect the efficiency of system.

With the increase in demand of enhanced spectral efficiency and less distortion, consequently affecting the power consumption, the multi-level modulation schemes were introduced in past such as QAM (Quadrature Amplitude Modulation). These modulation schemes are more sensitive to the non-linearity introduce by the power amplifier,
therefore, this matter has to be dealt with for making the transmission system more efficient.

One of the trivial solution for this problem is the use of power amplifier in its linear region. In this region of operation the average output power would be much less than the amplifier’s saturation region output power. The drawback for this solution is that it will make the transmission system costly and inefficient because of the fact that more power will consumed while integrating more number of amplifier stages to achieve the required gain and the power consumption is a major issue when the topic under consideration is satellite communication (especially small satellites).

The other solution which is more complicated in terms of implementation but, on the other hand, provides more linearity in PA behavior and reduce distortion. It comprises of predistortion of the input signal so that it can counter the effects of non-linearities introduce by power amplifier.

The predistortion technique is the development of inverse model of power amplifier behavior. The inverse behavior of PA is introduced in the original signal before inputting it to the power amplifier in a way that the output becomes linear. This methodology has an effect on the bandwidth expansion of the signal, consequently, the digital to analog converter has to be designed at the sampling frequency of up to five times of original signal.

This master thesis represents the implementation of predistortion scheme for linearizing the power amplifier’s behavior. It also provides the solution for decreasing the sampling frequency of digital to analog converter up to, approximately, the same bandwidth as original signal.

1.3. Thesis Outline

This master thesis is composed of three phases. First phase includes the literature review and the study of few aspects which are quite important while designing a communication system. Some of these parameters are the power budget (especially for the small satellites), type and class of power amplifier and modulation scheme. A comparison is provided regarding the selection of these parameters based on the research performed in past. Another important issue in the communication is Doppler Effect which needs to be countered. A brief explanation is compiled in one of the sections of this phase.

Second phase of this thesis majorly contributes towards the behavioral modelling of RF power amplifier. Literature review has been provided regarding the selected model of PA i.e. Volterra series. The implementation/simulation of the model has been done in Matlab. With the use of modeled power amplifier, a static predistortion system has designed and simulated. This phase of report also shows the results achieved on every step of implementation and analysis/commenting is done with respect to the change in important
parameters. Furthermore, it consists of the concluding results of adaptive digital predistortion with the use of hardware implemented power real-time power amplifier. For this purpose, Web Lab is utilized to observe the behavior of designed system.

In the third phase of this master thesis, a simulated APD (Analog predistorter) which is essentially equivalent to a memoryless DPD is used in cascade with adaptive DPD system designed previously by applying a low-pass filter between them for countering the in-band distortions. The objective of this combination scheme is to reduce the bandwidth expansion (caused by DPD) so that the sampling frequency of digital to analog converter can be reduced for the ease of implementation. The analysis is provided on the factors of normalized mean square error (NMSE), adjacent channel leakage ratio (ACLR) and output power for proving the mentioned concept.

Finally, the conclusion and future work extension is projected at the end of the presented report.
Chapter 02

2.1. Satellite communication – Transmitter

The communication subsystem of a small satellite requires comparatively more power (watts) to perform its desirable operation which depends on the size and mass of the satellite. The communication subsystem may consist of several sections including antennas and transmission/receiver chain of components. The downlink assembly of the transmitter is of utmost importance with respect to data rate, bandwidth utilization and power requirement.

Currently, the most research and application oriented region is the small satellites in lower earth orbit, developed for the purpose of earth observation and monitoring such as remote sensing and disaster monitoring and management satellites. However, besides great advantages of small satellites, there also exist few drawbacks such as the availability of less on-board power and requirement of higher data rate due to the limitation of short visibility pass.

The downlink chain for a small satellite (shown in Fig.1 [2]) is majorly consisted of constellation mapping, pulse shaping, digital to analog converter, modulation, RF amplification and eventually passes the signal to the antenna. A digital technique is applied in this project for improving the linearity and efficiency (output to input power ratio) of the RF power amplifier which is called as digital predistortion.

![Figure 1: Transmitter chain assembly](image)

As when operating close to the peak efficiency or to the maximum rated output, the RF power amplifiers tends to show non-linear behavior. Furthermore, the modulation
schemes used in the transmission system are sensitive to the non-linear behavior of RF power amplifier. Therefore, the PA has to operate in linearity region which needs more power consumption and higher cost. Predistortion technique is a cost-effective and power efficient technique. It basically models the inverse circuit of amplifier’s characteristics such as gain and phase which is when added to the amplifier’s input provides a linear behavior for overall system and causes reduction in the distortion of amplifier.

The predistortion technique can be applied in both analog and digital domains which will be discussed later in the report.

2.2. Power Budget:

Power required to operate for a device is an important factor of its selection for a space mission.

The small satellites can be classified into four sub-categories depending on the mass namely mini-satellites, micro-satellites, nano-satellites and pico-satellites.

Mini-satellites are commonly refer to those having mass between 100 to 500 kg.

Micro-satellite are known to have wet-mass (fuel included) from 10 to 100 kg. According to the specification of project, this report will be focused on such type of satellites.

Nano-satellites are consisted of mass between 1 to 10 kg. Most of the Cubesat projects lies under this category.

Pico-satellites are those who have total mass between 0.1 to 1 kg.

An approximate power budget is shown in the table below which is collected from the previous successful satellite missions ([2] and [3]). The table also shows the power allocated to the communication subsystem and transmitter.

<table>
<thead>
<tr>
<th>Satellite Mass (Kg)</th>
<th>Total Power (Watts)</th>
<th>Communication Subsystem Available power (Watts)</th>
</tr>
</thead>
<tbody>
<tr>
<td>50</td>
<td>100</td>
<td>20</td>
</tr>
<tr>
<td>10</td>
<td>20</td>
<td>6-7</td>
</tr>
<tr>
<td>2-3</td>
<td>5</td>
<td>1-1.5</td>
</tr>
</tbody>
</table>

*Table 1: Satellite Mass and Power*
2.3. Power Amplifiers – Description and Comparison:

Based on the specifications and requirements of the project there are several RF power amplifiers used in the previous mission of similar capacity. Each one of them has pros and cons and with advancement in technology, the most recent RF power amplifiers having High electron mobility transistors are better in terms of power consumption and efficiency.

The RF PA most commonly used in the history of small satellites is classified into three main types. Firstly, the gallium arsenide (GaAs) field-effect transistors used in amplifier circuits. This type of amplifier is known because of its carrier mobility, sensitivity and less internal noise. These type of amplifiers have maximum power-added efficiencies (PAE) ranging from 20% to 50% and the power level range varies from 24 dBm to 32 dBm depending upon the type of GaAs FET used [2].

However, these RF power amplifiers are more suitable for the communication in C-band and X-band because of their operating frequency capability which ranges from 7.7 to 8.5 GHz.

Efficiency and output power vs frequency curves are shown in the figure below [5] for two types GaAs FET amplifiers which can be used.

Gallium Nitride (GaN) High Mobility Transistors (HEMT) is the other type of transistor used in RF amplifiers. This technology is more recently developed and entail better characteristics/properties in terms of drift velocity of electrons and thermal conductivity as compared to the previously discussed type. Besides, Gallium Nitride HEMT also provides wider range of bandwidth operability and higher power density.
The GaN amplifiers discussed here belong to RF amplifier’s class AB and class F.

![Figure 4: Comparison in terms of Output power, input power and PAE [2]](image)

![Figure 5: Input power vs phase shift [2]](image)

<table>
<thead>
<tr>
<th>Amplifier Type</th>
<th>GA As AB class</th>
<th>GaN AB class</th>
<th>GaN F class</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum Power ( dBm)</td>
<td>38</td>
<td>37</td>
<td>36</td>
</tr>
<tr>
<td>Maximum PAE (%)</td>
<td>37</td>
<td>46</td>
<td>60</td>
</tr>
<tr>
<td>Maximum Gain ( dB)</td>
<td>10</td>
<td>11</td>
<td>12</td>
</tr>
<tr>
<td>Maximum Phase Shift (Degrees)</td>
<td>10</td>
<td>-2</td>
<td>-34</td>
</tr>
</tbody>
</table>

Table 2: Properties comparison of different types of Amplifiers
As for comparison, class F GaN amplifiers have the maximum power-added efficiency (PAE) among the three types discussed but if the concern parameter is the change in phase then it exhibits a maximum of 34° phase shift [2]. The phase shifting, in this context, is the change in phase at a certain level of input power of amplifier. This can be a deciding factor for the selection of GaN class F amplifier because it exhibits a large amount of change in phase at high values of input power. This change in phase of the signal is large enough, when the modulation scheme to be used is amplitude-phase modulation. On the contrary, GaN class AB amplifiers have less output power and power-added efficiency as compared to class F, but it exhibits a phase shift of 2°.

2.4. Modulation Scheme Comparison:

Modulation is a process of altering the properties of high frequency signal commonly known as carrier signal, with a signal containing the information needs to be transmitted. The main goal of modulation is to transmit maximum amount of data in available bandwidth.

While selecting the modulation scheme for a small satellite downlink, there exist several key factor that needs to address. Some of them are stated as Bit error rate (BER), Power consumption, circuit complexity and bandwidth. However, for a small satellite, the available power is one of the major issues, therefore power efficiency (energy required in each bit to transmit data at specific bit error rate) and spectral efficiency (ratio of the data rate and bandwidth of modulated signal) are the two most important parameters for selecting a modulation scheme.

The modulation scheme is sensitive to the non-linear behavior of the power amplifier used which is also an important factor. For understanding, Fig. [7] Shows the effect of power amplifier non-linear behavior on a 64-QAM constellation.

![Figure 7: Transmitted constellation before amplification](image1)

![Figure 6: Transmitted constellation at PA output](image2)
In table 3, a comparison of several modulation schemes is provided [2], widely used in previous missions, in terms of spectral efficiencies, probability of error and power consumption.

<table>
<thead>
<tr>
<th>Type of Modulation</th>
<th>Spectral efficiency (Bits/s/Hz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>FSK</td>
<td>&lt;1 (depends on modulation index)</td>
</tr>
<tr>
<td>BPSK</td>
<td>1</td>
</tr>
<tr>
<td>ASK</td>
<td>1</td>
</tr>
<tr>
<td>GMSK</td>
<td>1.35</td>
</tr>
<tr>
<td>QPSK or 4PSK</td>
<td>2</td>
</tr>
<tr>
<td>8PSK</td>
<td>3</td>
</tr>
<tr>
<td>16QAM</td>
<td>4</td>
</tr>
<tr>
<td>64QAM</td>
<td>6</td>
</tr>
<tr>
<td>OFDM</td>
<td>&gt;10 (depends on modulation index)</td>
</tr>
</tbody>
</table>

Figure 8: Modulation schemes in terms of power consumption vs data rate

Table 3: Spectral efficiency for modulation methods
From the figure [9], it can be clearly observed that data predistorter can mitigate the amplifier’s non-linear behavior effects. Predistorter can considerably reduce the amplitude compression and phase rotation which is caused by the power amplifier.

However, from the above analysis it is resulted out that in view of the project requirements and specifications, the 16 QAM modulation scheme is a better option to adopt with respect to its power consumption and nominal spectral efficiency. Although there is new and more recently developed modulation scheme known as adaptive modulation technique can also be considered for the small satellite downlink communication. This method has the tendency to adopt the modulation scheme (M-QAM of interest depending on the current conditions of channel such as amplifier back-off, SNR levels and fading characteristics. Eventually, by the use of this technique improvement can be made in power and spectral efficiencies as well as non-linear distortion and inter-symbol interference can also be reduced.

Fig.10 shows [7] the channel capacity when the adaptive modulation technique is applied with combination of predistortion method.
2.5. Doppler Effect for LEO satellites:

Doppler shift is a phenomenon of a change in frequency which is observed when an object moves towards or away from the observer. In case of satellite communication, the object is satellite and observer is the ground station/terminal.

During satellite communications, the radio waves are affected by the Doppler phenomenon. Although it is small for the communications using lower frequency i.e. few Hz for a VHF mobile receiver. But it becomes significant while the use of SSB (Single Side Band) operations. Doppler shift is directly proportional to the operating frequency which means it is more significant (needs to be compensated) on UHF. Furthermore, its effect on communication depends on the type of modulation scheme, multiplexing techniques and satellite access methods.

The Doppler Effect becomes more substantial during the case of lower earth orbit satellites. Because the LEO satellites are moving at a velocity near to 7.5 Km/s relative to earth’s surface. For the users on the ground, the Doppler shift frequency changes when the satellites passes overhead. In most cases, it depends on the orbital geometry on the satellite and the latitude and longitude of the ground terminal. The pass of the satellite is divided into two section depending on the elevation angle and viewing point of the ground observer. If the satellite is ascending part of the orbit, then ground observer can notice the maximum frequency shift when the satellite appears at south horizon and it goes on decreasing to minimum value until the satellite reaches north horizon. Similarly if the satellite is in descending part of the orbit, the frequency shift maximizes at the north horizon with respect to the ground terminal/observer.
In the figure [11], the change in Doppler frequency shift for a satellite (typical iridium satellite) overhead pass with respect to the ground station is shown. The pass starts as the satellite appears to be rising above the horizon until it disappears.

![Doppler Frequency Shift Curve](image)

**Figure 11: Doppler Frequency Shift Curve**

To calculate the Doppler rate, we can take the derivative of above curve with respect to time and the resultant is shown in the Fig.12 [9].

![Doppler Rate Curve](image)

**Figure 12: Doppler Rate Curve**
The Doppler shift for a circular orbit with relation to the height of the satellites' orbit can be given by

$$\Delta f_D = f_0 \frac{v_d}{c}$$

Where $v_d$ can be given as:

$$v_d = \left[ \frac{\mu r_e^2}{(r_e + h)^3} \cos \gamma \sin \varphi - \frac{2\pi}{86164} r_e \cos l_t \cos \gamma \cos \varphi \right]$$

In the above equation, $l_t$ is defined as the latitude of the ground terminal whereas $\varphi$ is the angle between latitudinal tangent at sub satellite point and terminal projection line onto the tangential plane at sub satellite point, $r_e$ represents the radius of earth, $\mu$ is defined to the gravitational constant and $h$ is the height of satellite’s orbit.

There are several methods developed for the compensation of Doppler frequency shift such as:

- Closed-terminal satellite frequency control loop
- On-board satellite Doppler correction
- Pre-correction on the receiver side of the link
- Pre-correction on the transmitter side of the link
Chapter 03

3.1. Power Amplifier linearization techniques

As discussed in the previous chapters, the working and output behavior of power amplifier is affected when the power amplifier approaches to its saturation point. The non-linear behavior of and saturation point relation of power amplifier varies with the type/class and operating conditions of power amplifier. The most significant signal distortion affects are harmonic distortion, spectral regrowth and inter-modulation distortions. The distortion not only affects the clarity of the signal but also creates inter-frequency interference.

However, the main idea is to decrease the non-linearity in PA’s output as much as possible so that the unwanted intermodulation terms and signal distortion can be reduced to a minimum level. There are certain parameters for the evaluation of performance and efficiency of power amplifier, such as, NMSE, ACLR and power spectrum mask. These factors evaluate the working of power amplifier, for example, normalized mean square error defines the estimated deviation of output signal with respect to the input signal. It should be kept to a level of -35 dB to -40 dB to represent the comparison of input and output signal of power amplifier. It shows that how much in-band distortion is adding by the power amplifier and the quantity of change in output signal as compared to input. Similarly, ACLR (adjacent channel leakage ratio) is defined to be the ratio between transmitted power and adjacent channel power. The level of this factor is kept to be between -45 dB to -50 dB for achieving desired results of amplification, linearity of power amplifier. Power spectral density (PSD) is also a measure of defining the behavior of power amplifier. With the help of power spectrum mask, the amplification occurred in out-of-band signal and in-band can be noticed. This master thesis will be focusing on these parameters for determining the behavior of power amplifier as well as the designed predistortion system.

For the said purposes, a signal must be well operated and gone through several procedures before inputting it to the power amplifier so that the desirable level of linearity can be achieved. These schemes and procedures varies with the requirement of projects in which power amplifier needs to be used. The deriving parameters can be efficiency, channel interference, wider bandwidth, and complexity and modulation methods. In the field of digital signal processing, extensive research has been made in past to formulate different methodologies for countering the non-linear effect of power amplifier. Resulting in various PA linearization schemes, where each of them has its own advantages and flaws.

However, there is not a single methodology which can work in different set of circumstances. Some of these schemes are elaborated in this report which are applicable in several situations. Ending with one of the mostly researched and stable method
(predistortion) which is also applied in this particular Master thesis to achieve the desired results.

3.2. Methods to compensate Non-linearity in PA behavior

Few commonly known/researched Power amplifier linearizer methods are enlisted below with a comprehensive description of each.

- **Feedback**
- **Feed Forward**
- **Predistortion**

3.2.1. Feed Back system:

The feedback system technique is the most commonly used method to make the PA behavior linear to a certain level. This technique can have various shapes depending on the various types of feedback systems used. Some extensively used categories of this methodology are local feedback system, global feedback system, baseband feedback system, Cartesian feedback system and polar feedback system.

The local feedback system can certainly be used when the operating frequency of power amplifier should be too high so that the voltage gain of PA can be high enough [12]. This condition has foremost importance to make this procedure practical and work correctly. The following diagram shows a simple mechanism of feedback system for power amplifiers.

![Figure 13: Local Feedback System](image)

However, the global feedback system is a better option when the voltage gain of a single stage amplifier is not high enough. In this type of conditions, various power amplifiers are cascaded to make a system of amplifiers having higher gain. This method is practically more viable when it comes to low frequencies, but on the other hand when higher frequencies are under discussion then to achieve a higher gain, a number of stages of PA are to be implemented to make this method practical [12].
The implementation of baseband feedback system is shown in the Fig.15. The idea in this method is to feedback the baseband signal to the input instead of RF signal. As the bandwidth of baseband signal is much lower than RF signal, therefore, the bandwidth requirement in the feedback loop can be reduced by performing it [12]. This method is more applicable in the conditions of higher frequency bands or larger bandwidths. On the other hand, this method is more complex.

3.2.2. Feed forward System:

The feed forward system is also a commonly used linearization method under a set of certain circumstances. Mainly this method uses the two loops of distortion cancellation mechanism as can be seen in the following diagram.

The main course of action in this system is to achieve only the distortion at the output of first loop of cancelling mechanism by minimizing the gain and tweaking the phase of input signal. As the distortion is known then the original signal can be subtracted from it to obtain an amplified and non-distorted output signal.
The feed forward system is suitable choice for in band amplitude and phase distortion correction. One of the benefits of this system is its inherited stability. However, this can be a viable approximation method when the bandwidth of modulated carrier is small as compared to the frequency of carrier [12].

3.2.3. Predistortion:

The predistortion is a most commonly and widely used/researched method for linearizing the behavior of non-linear RF power amplifier. The RF or baseband signal can be treated before inputting to the RF power amplifier by a cost-effective and efficient method known as digital predistortion. However, there can more than one ways to implement the predistortion technique. Either the amplitude/ phase of RF signal can be predistorted before it passes to the RF amplifier or the predistortion of baseband input signal can be performed to directly nullify the power amplifier's distorted performance [15].
Furthermore, the predistortion method can be applied in various forms depending on the requirement/specification of the project. These forms can be open loop predistortion, closed loop, iterative/adaptive feedback and memoryless/with memory effect. Although with the enhancement in the efficiency of a system the method becomes more complex in terms of model estimation and hardware implementation yet manageable.

![Figure 19: Closed Loop Predistortion](image)

Basically, the digital Predistortion method deals with the modelling of RF PA behavioral characteristics but inverse in nature. This method changes the signal before amplification, counter the effects the of distortion produce by PA, eventually obtaining a clear and distortion-less signal at the output of PA. From the implementation point of view, an estimated prediction of power amplifier behavior is modelled by using the polynomial expressions. Then inverse replica of the modelled data is generated to perform the inverse operation on the baseband or RF signal before inputting it to the power amplifier (as can be seen in Fig. 20).

![Figure 20: Predistortion System](image)

The predistortion scheme can be developed and implemented in both analog and digital domain. Predistortion in both domain have their own advantages as well as disadvantages. There are transceivers with capability to perform digital to RF conversion on a single chip which can reduce the cost and save the space as well as power consumption. With the advantage of using digital predistortion for the linearity of power amplifier, there also exists a drawback. The predistortion causes the increase in the bandwidth to at least five times of its original bandwidth. This phenomenon is termed as
bandwidth expansion. Due to exhibition of this phenomenon, the digital to analog converter, implemented at the output of predistortion, has to be designed at a sampling frequency of five times greater than the original bandwidth of the signal. This causes the complexity in the design of DAC and also hardware implementation becomes challenging.

This master thesis involves in design of such cooperative scheme of digital and analog predistortion that can counter the aforementioned problem.

3.2.3.1 Predistortion System Configurations:

Accurate modelling of PA is the foremost step in designing of predistortion system. The better the model of PA is the better designing of PD (Predistortion) system can be done. As far as modelling is concerned, there exists several mathematical model to simulate the behavior of power amplifier. These models are different in nature regarding hardware implementation complexity, memory effects execution and polynomial orders. The selection of model is mostly dependent on the requirements of the assignment and available resources.

This Master Thesis deals with a combination of Digital and Analog (Simulated) predistortion system. The PA model selected for designing this system is based on the Dynamic Deviation Reduction (DDR) Volterra series which is a reduced and truncated form of original Volterra series. The Volterra series provides a general input output relationship of power amplifier behavior with the involvement of memory effect. But due the high level of implementation complexities (because of exponential increase in the number of parameters with the increase in memory length and non-linearity degree) [19], the general form of Volterra series is truncated and reduced to DDR Volterra series for making it practically feasible for hardware implementation. The details related to Volterra series and parameters involved is provided in the upcoming chapters.

While referring to the predistortion system designing, certain parameters/processes in both domains (digital and analog) are introduced for making the whole system response more linear and efficient. These parameters consists of implementing the PA model with memory effects or without memory effect. The static or adaptive are the two process involves in designing the predistortion system. The memory effects and static/adaptive schemes are elaborated below in detail.

3.2.3.2 Memory/Memoryless Effect:

This term is used in reference to power amplifier response when the output of PA is no more dependent on the instantaneous input but also caters the effect of previous inputs applied to it. This effect is quite important to consider while modelling of PA. Although it does not directly affect the linear behavior of amplifier yet it influences the complexity and
linearity of the transmission system causing an effect on the predistortion linearization [20].

Most commonly used way to analyze the behavior of PA is the static AM-AM curves and AM-PM curves. For the case of memoryless system, these static curves and the predistorter coefficients/gain values can be stored and utilized again to achieve the desired linear response from non-linear PA. But with the conversion/upgradation of wireless system to wider bandwidths, higher frequencies and higher data rates it is almost impossible to model static AM-AM and AM-PM curves for a non-linear power amplifier. Static modeling can be applied to the narrow bandwidth scenarios but it is no longer applicable to the wider modulation bandwidths and the memory effect is no longer negligible in this particular case. From the experimentation in past, it has been seen that the PA show the memory effects when the bandwidth becomes wider than 20 MHz.

![Figure 21: Memoryless Vs Memory polynomial Analysis Diagram](image)

Fig.21 from the previous research [21] elaborates the on the spectra of output signal when using a memory polynomial based PA model, memoryless model and without Digital Predistortion system. In Fig.21, it can be seen that the curve (a) gives the most appropriate and with least out of band distortion amplification as compared to (b) and (c) curves which represents the memoryless polynomial predistorter and without predistortion system respectively. As it was commented before, Fig.21 proves that, after a certain wideness of bandwidth it is necessary to counter the effect of memory issue for achieving better results in amplification.

Generally, PA behavioral modelling can be classified into three categories based on the memory effects in the system. Firstly there comes the nonlinear memoryless system
which is represented with the AM-AM curves of narrow band signal. Secondly, there is quasi-memoryless non-linear system which is dependent on the order of period of RF carrier having memory time constants. Lastly, with memory non-linear system having a long term memory effect depending on the order of period of envelope signal [22]. In this thesis, the focus of work is on the third category of the PA behavioral modelling (non-linear systems with memory effect) by applying the DDR Volterra series model.

There exists a number of causes for the occurrence of memory effect in the behavior of power amplifier depending whether the memory effect is rather linear or non-linear. The linear memory effect can be caused due to the time delays among the various instruments of the system or it can be produced because of phase shifts between the devices used or matching networks. On the other hand, the non-linear memory effects occurred due to the temperature influenced by the input power, network biasing and trapping effect [19] (associated to both surface and layer, gate lagging is incorporated in surface trapping whereas the drain current collapsing is demonstrated as layer trapping effect).

3.2.3.3 Static/Adaptive Predistortion System:

The predistortion system can be designed on the concept of two approaches namely static design and adaptive design. The earlier design is easy in terms of implementation and complexity as compared to the later one.

Static predistortion system is time independent and it involves the modelling of PA behavior at a certain time instant. After finding the parameters for the predistorter, it is multiplied with the original signal to incorporate the inverse properties of PA into the signal. The parameters of PD remains same for every signal assuming that the behavior of PA is constant over a certain period of time. Linearization in the output signal can be achieved up to some extent with the help of this design. But with the passage of time and the changes occur in the behavior of PA like heating or ageing of amplifier and introduction of memory effect due to time delays, this method becomes more vulnerable to distortion and turn out to be less efficient.

The static PD can be designed by making inverse model of PA and using it with the original signal or can be designed with the implementation of look-up tables in which PD parameters are stored already. The Fig.22, Fig.23 shows the implementation of both methods on the block level.
Adaptive predistortion system, on the other hand, is more complex and requires more processing than the static but it is more prevailing and immune to the out-of-band distortions. This method can be implemented with several iterative algorithms such as least square (LS), least mean square (LMS) and recursive least square (RLS). These algorithms can be selected on the basis of parameters like calculation of quadratic error, amplitude and phase error and ACPR (Adjacent channel power ratio).

The adaptive system is a more apposite preference because it is time dependent (doesn’t depend on the instantaneous input but also on the past inputs/outputs) and counters the effect of ageing, heating and similar parameter of PA. With this system the predistorter parameters alter in every iteration making the whole system more linearized. Below mentioned block diagram shows a process of complete scenario for linearizing PA output with the involvement of adaptation algorithm in the feedback loop.

The basic concept of designing an adaptation algorithm is to calculate the error among the input and output of the system and after processing, update the DPD parameters.
accordingly. The DPD updater takes the error, output and input signal to find out the updated coefficients of DPD and feed it to the DPD function in every iteration. This process takes place until the desired output is achieved and the system converges. Following diagrams illustrates the least mean square method for adaptation and the complete system level design respectively.

*Figure 25: Adaptive predistortion algorithm block diagram*
Chapter 04

4.1. Implementation of Adaptive DPD Algorithm

This chapter of Master thesis comprises of the modelling of power amplifier behavior by the use of DDR Volterra series, designing of digital predistortion (system function and parameters calculation) and constructing an adaptive algorithms for the feedback system. As discussed in the previous chapters, the use of DPD is to linearize the output of PA by introducing the inverse properties of PA to the signal, the similar approach is considered to design the DPD. The results are shown with descriptive analysis on the basis of AM-AM and AM-PM curves where required.

4.2. Design and Implementation Procedure:

The purpose is to design a Digital predistortion system that can accurately simulate the inverses behavior of power amplifier.
The modelling of PA is the first and foremost step in the complete procedure.

All the simulation and the results have been compiled in the Matlab Software. The other steps of the design and implementation phase are presented in the above mentioned flow chart diagram and explained step by step in the upcoming section of the chapter.

4.3. PA Behavioral Modelling:

An essential and foremost step in designing the complete linearization system mentioned above is the modelling of power amplifier behavior. The PA modelling, generally, means to replicate the properties and the effects that a power amplifier can have on a signal when passes through it. In the case of power amplifier, the mostly observed property is the non-linearity introduced in the original signal at the output PA. Concluding, it can be said that the behavioral modelling of PA is the accurate simulation for the non-linearity of power amplifier. These models are based on software simulations including efficient computational algorithms so that the relation between input and output of PA can be described (in terms non-linearity) without the use of a physical instrument.

For designing the model of a power amplifier, the basic principle is to observe and measure the PA non-linear behavior and based of the already defined model architectures take the parameter for the new model. These model are represented mathematically in the shape of set of equations and applied in designing of communication systems.

While discussing the PA behavioral modelling it is important to mention that, in communication system and signal processing research literature, the PA can be modeled as memoryless as well as with memory effects. The memoryless PA behavioral modelling, as described in detail in previous chapters, is based on AM-AM and AM-PM functions/curves which are static in terms of input state (having only instantaneous input). But with the thermal effect over a long period of time and the dc-biasing circuits time constants, the memory effects arises in the behavior of power amplifier [25].

Various studies/research had been made, on this issue of non-linear memory effects, in the literature. Some of the studies shows the reasons of this matter, like in [15] it is explained that the asymmetric effects is a result of distortion in amplitude of the signal, in addition, it also produces when they react/interact with AM-AM and AM-PM functions. Similarly, in [26] the authors categorizes the memory effects into thermal and electrical classes and explained that the intermodulation asymmetry is the effect of thermal memory issue.

However, with the study of various reason, it is necessary to formulate such a PA model which involves the memory issues. For this purpose and for achieving the better efficiency and linearity in communication system a non-linear memory PA model is used. This thesis also consist of study and implementation of the digital and analog predistortion system by
the use of non-linear memory model of power amplifier. This model is an extraction and truncation of the original Volterra series.

Volterra series can be defined as a combination of nonlinear power terms and the linear convolution terms formulate together to describe the relation between input and output of RF power amplifier including the memory effects. While commenting on the general Volterra series, its high computational complexity is a major concern for its implementation for some applications. This computational complexity comes due to the increase in number of parameters for this series is exponential with the increase in degree of non-linearity and memory length. Therefore for making the Volterra series more applicable and feasible for hardware implementation with ease of computation, it is truncated to a certain level with which the PA behavior model is not affected much due to neglecting the higher order term. This report involves the implementation of such technique called as Dynamic Deviation Reduction Volterra Series.

The basic concept of reduction applied here is by assuming that the memory duration of device as compared to signal period is short enough so that the original Volterra series can be truncated into single integral term that can provide the modelling of weak as well as strong non-linearities in the amplifier behavior [27] the general form of Volterra series can be mathematically represented in discrete form as follows.

\[ y(n) = \sum_{p=1}^{P} \sum_{i1=0}^{M} \ldots \sum_{ip=0}^{M} h_p(i_1 \ldots \ldots i_p) \prod_{j=1}^{p} x(n - i_j) \]

Here \( x(n) \) is the input signal whereas \( y(n) \) is the output. The Volterra kernel are represented in the equation by \( h_p(i_1 \ldots \ldots i_p) \) and the order kernel order is ‘p’. \( P \) is denoting the order of non-linearity and \( M \) shows the memory length for a given system in which the mathematical model is applied.

In several applications, the memory length can be truncated to a finite number. With applying the truncation and combining the deviation reduction function the Volterra series can take the form as following.

The deviation reduction function can be represented as

\[ e(n, i) = x(n - i) - x(n) \]

Which is representing the deviation of delayed signal \( x(n-i) \) with respect to \( x(n) \) [27]. As the output signal has two elements (static and dynamic), therefore
\[ y(n) = y_s(n) + y_d(n) \]

And consequently,

\[ y(n) = \sum_{p=1}^{P} a_p(n) x^p(n) + \sum_{p=1}^{P} x^{p-1}(n) \sum_{i=0}^{N-1} g_{p_1}(i) e(n, i) \]

The memory effect has a tendency to decrease with the passage of time which concludes that the longer the time-delayed input signal is the less effect it has on the output of amplifier with respect to memory [27]. Therefore, by apply the deviation reduction and truncation to the second order, the Volterra model can be represented as

\[
\sum_{p=1}^{P} a_p(n) x^p(n) + \sum_{p=1}^{P} x^{p-1}(n) \sum_{i=1}^{N-1} h_{p_1}(i)x(n - i) \\
+ \sum_{p=2}^{P} x^{p-2}(n) \sum_{i_1=1}^{N-1} \sum_{i_2=i_1}^{N-1} h_{p_2}(i_1,i_2)x(n - i_1)x(n - i_2)
\]

The final form of DDR Volterra series is implemented in Matlab and the results are obtained for the model of power amplifier. The results shows the promising behavior modeling of the non-linearity introduce by the PA in original input signal which is then further used for the designing of digital predistortion system.

The behavior of power amplifier is shown with the respect of AM/AM graphs and the frequency spectrum in the following diagrams for memoryless model and model including memory effects. The Volterra series model shows quite promising value of normalized mean square error (NMSE) between the predicted output and the output achieved from the modelled PA.
Fig. 27: PA input and output power spectrum without linearization technique

Fig. 29 represents the frequency spectrum of the input and output signal of power amplifier’s behavioral model based on DDR Volterra series. The amplification in the desired band of the signal can be seen, but the amplification in out of band signal is quite high. This is the purpose that we use the predistortion so that the amplification of out of band distortions can be kept as minimum as possible. However, this diagram is only to elaborate the behavior and output amplification result for the power amplifier but the analysis can be done in the upcoming sections of the report when predistorter will be applied to the system.

Fig. 28: AM/AM curve for memoryless model of PA (Polynomial degree P=9)
The graphs in Fig. 29 shows a comparison between the behavioral output of power amplifier model designed and the actual output provided for testing. The green curve represents the model output whereas the curve in blue shows the actual provided output. The purpose of these AM/AM curves are to elaborate the fact that how close is the model approximation to the actual output. As the resemblance can be seen in the diagrams pictorially as well as in the Table.4 with respect to mean square error (NMSE) values.

The point to ponder in the Fig. 29 is that with the inclusion of memory effect in the PA model the NMSE has increased considerably with the increase in the output signal width to matchup with the width of actual output. This fact reveals that if memory effect is not considered in the behavioral modelling of PA then a better and efficient system cannot be designed.

<table>
<thead>
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<th>Polynomial Degree</th>
<th>Memory Length</th>
<th>NMSE (dB)</th>
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<td>10</td>
<td>-</td>
<td>-31.4</td>
</tr>
<tr>
<td>9</td>
<td>7</td>
<td>-34.5</td>
</tr>
<tr>
<td>9</td>
<td>15</td>
<td>-38.95</td>
</tr>
<tr>
<td>12</td>
<td>7</td>
<td>-35.9</td>
</tr>
</tbody>
</table>

Table 4: NMSE comparison

4.4. Predistortion:

As discussed in the previous chapter, the predistortion system is designed to reverse the effects implicated by power amplifier on the input signal. The methodology derive here to
design the predistortion involves the working of power amplifier in reverse order. Practically, it is not impossible but as the implementation is done in simulations, therefore, the reverse working of PA could be executed. The concept used here is to provide the output signal as input to already designed PA model function and conclude the output.

![Diagram of PA Modelling](image)

*Figure 30: Implementation of PA Modelling*

The AM/AM curve in Fig.31 and Fig.32 represents the inverse behavior of PA which will be used as the predistortion applied to input signal. PD curves are derived for the various scenarios such as memoryless predistorter, with short length memory effect and long length of memory taps.

![AM-AM Curve](image)

*Figure 31: AM/AM curve, Memoryless DPD with polynomial degree P=9*
4.5. Static DPD Assembly:

Static assembly of predistortion implies the working of PD and PA in cascade but with time independence which means that the input and output relation is instantaneous. This is the simplest way to implement a predistortion system to decrease the distortion especially in the out-of-band distortion and reduction of spectral regrowth.

After deriving the DPD coefficients, as mentioned in the above sub section, the original and inverse PA functions executed in series to form a static assembly. This concept is sketched in the Fig.34.

The frequency spectrum and AM/AM function curves below shows the input output relation of static DPD system.
The frequency spectrum in Fig.34 shows the difference in out-of-band distortion and spectral regrowth reduction between input and output signal with the use of DPD as well as without DPD. By implementing designed DPD in series with the PA the channel leakage ratio decreases about 20 dB. Further, in the upcoming sections of the report, the results with adaptive DPD feedback will be illustrated.
Chapter 05

5.1. Web Lab setup for PA Predistortion implementation

The remote setup including power amplifier and analyzing instruments are used for implementing and testing the predistortion system designed in previously. The adaptive predistortion system is designed in addition to the previously build setup for reducing the spectral regrowth and distortion among output of PA.

This remote setup is known as Web Lab which was structured by University of Chalmers (Sweden) and National Instruments. This web Lab is provided to the students for testing the linearizing algorithms on hardware by accessing it remotely online. This setup is consisted of a signal generator, Non-linear GaN power amplifier and signal analyzer.

Figure 36: Web Lab Instruments [28]

The use of Web lab platform can be performed in two separate ways. One method is to upload the data to the server of Web Lab and it will process the data and compile the results in some time and the analysis can be done on these results afterwards. The other methodology to access the web Lab is the dedicated m.file (Matlab file) on to the personal computer and use it for compiling the results. There is no restriction for any user for the use of these instruments but few parameters are needed to be kept in mind before uploading the data to access the Web Lab. These parameters includes PAPR and RMS power levels of the signal. The test signal used for the obtaining results in various experimentation scenarios is an OFDM-like signal with a bandwidth of 40 MHz.
5.2. Adaptive Predistortion Implementation through Web Lab

As discussed in the previous chapters, the adaptive predistortion is a setup in which iteration procedure is applied to calculate the error signal at the output of power amplifier and utilize it to calculate new coefficients for predistorter in each iteration to make it better and efficient in terms of linearity. Therefore, the adaptive system is developed with the use of Least Square approach. The concept of the system is sketched in the below diagram on a block level.

![Adaptive DPD Block Diagram](image)

**Figure 37: Adaptive DPD Block Diagram**

In Fig.37, U represents the input signal given to the digital predistorter designed previously. The least square method for the adaptive predistortion system can be expressed mathematically as follows.

In Fig.37, X shows the output of digital predistortion that can be represented mathematically as

\[
x(n) = u(n) - d(n) \]

\[
d(n) = \Phi_n w_n \]

\[
w_n = (\alpha_{00} \ldots \alpha_{0P} \ldots \alpha_{N0} \ldots \alpha_{NP}) \]

\(u(n)\) is the original input signal and \(d(n)\) is the data matrix obtained after inputting the signal to the DPD function \(\Phi_n\) and multiplying with the coefficient of DPD i.e. \(w_n\). \(w_n\) is dependent on the polynomial degree \(P\) and number of memory taps \(N\). After deriving \(x(n)\), it is inputted to amplifier and an output \(y\) is obtained. The error signal is obtained by using
the following expression which leads to the calculation of new coefficients of DPD for the next iteration.

\[ e(n) = y(n)/G_0 - u(n) \]

Where \( e(n) \) represents the error signal, \( y(n) \) and \( u(n) \) is the output and input respectively and \( G_0 \) is the gain. Once the error signal is obtained, new coefficients for DPD are calculated through following equations. The well-known least-squares solution for feedback system and obtaining the new coefficients in every iteration is mathematically expressed as

\[
\begin{align*}
  w_{n+1} &= w_n + \lambda \Delta w_n \\
  \Delta w_n &= (\Phi^H \Phi)^{-1} \Phi^H e
\end{align*}
\]

In the first iteration the DPD will consider the coefficients as zeros and provide and input \( X \) to the power amplifier. After amplification, the preprocessor will up sample and align the signal for the use in next iteration. The DPD updater block will calculate the error signal by comparing the input and output and further use it to calculate the new DPD coefficients. These coefficients will be used in digital predistorter for the next iteration. The same procedure will keep on continuing until the desired ACLR or NMSE values are achieved.

The AM/AM curves and frequency spectrum is calculated by using this procedure and shown in Fig. 38. These graphs are derived on different degrees of polynomial and memory length for analyzing the effect of these parameters on the linearity and efficiency of power amplifier output.
Figure 38: AM/AM curves, Memoryless Adaptive DPD (Polynomial degree P=9)

Figure 39: Memoryless DPD (input and output) power spectrum
Figure 40: PA (input and output) power spectrum for memoryless adaptive DPD assembly

The graphs shown in Fig.38 depict the AM/AM function curves for DPD, PA and Adaptive system response in terms of input and output signal. Fig.42 shows the power spectrum between the input and output of DPD. Here the point to ponder is the spectral regrowth that occurs at the output of digital predistortion. Fig.41 presents the input and output spectrum for the PA with adaptive DPD configuration. Here it is noticeable that by applying the adaptive DPD algorithm, spectral regrowth is reduced. For analysis of output at PA, Table 5 shows the NMSE and ACLR values for several configuration/combinations of non-linearity degree and memory length parameters.
**Figure 41**: AM/AM curves, Memory DPD configuration (Polynomial Degree $P=9$, Memory length $M=6$)

**Figure 42**: Input and output power spectrum of memory DPD configuration (Polynomial degree $P=9$, Memory length $M=6$)
Figure 43: PA input and output power spectrum with and without DPD

Figure 44: Memory DPD (P=9, M=6) input and output power spectral density estimate
Figure 45: PA input and output power spectral density estimate with and without DPD

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Table 5: Memory length effects on important parameters

Figure 46: AM/AM curve for Memory DPD and PA behavioral model with Polynomial degree $P=9$, Memory length $M=15$
Concluding, this chapter demonstrates the fact that output of power amplifier becomes more linear and spectral regrowth is reduced by the use of adaptive digital predistortion (as compared to static DPD configuration).
Chapter 06

6.1. Cascaded PD Implementation

This chapter represents the concept addressing the problem of bandwidth expansion, resulting due to the predistortion linearization. As discussed earlier, the digital predistortion, on one side, removes the non-linearity from power amplifier behavior and thus making the system response linear. On the other hand, it also introduce the expansion in the bandwidth of original signal. According to rule of thumb, this expansion can be up to five times of original signal bandwidth. Due to this problem the digital to analog converter has to design at a greater sampling frequency which increases the cost and power consumption of DAC. For example, the bandwidth of the baseband signal is 20 MHz, the bandpass signal’s bandwidth would be equal to 40 MHz. According to nyquist theorem, the sampling rate will be greater than twice of baseband bandwidth (means greater than 40 MHz). In the case of spectral regrowth introduced by DPD, the bandwidth expanded to at least five times, then at input of DAC, the signal bandwidth becomes 100 MHz. Consequently, the DAC has to set the sampling rate of signal at greater the 200 MHz which causes an increase in power consumption of system.

This section of report presents a cooperative scheme of digital and analog predistortion system with a use of low-pass filter. The resultant of this scheme is that the system response will be as linear as the use of memory DPD whereas the DAC has to only sample the signal at the original signal bandwidth instead of five times. This scheme comprises of a digital with memory predistortion, the output of which is filtered with a use of digital ideal low-pass filter and cascaded with an analog predistortion. The analog predistortion, in this case, is essentially a memoryless DPD for countering the effects of in-band distortion. The analysis of this technique is made on the factors of NMSE, ACLR, output power of amplifier and the power spectrum mask of output at each stage. Comparison is performed and presented in terms of aforementioned parameters at each stage of system.

6.2. Emulated APD design:

Simulation of analog predistortion is designed in Matlab for using it alongside the cooperative scheme mentioned above. The emulated APD is designed on the principle of a digital predistortion without the effects of memory. Therefore a static memoryless DPD is designed with different polynomial degree configuration for obtaining the maximum level of NMSE, ACLR and output power. The results in Table 6 shows that by changing the polynomial degree in the DPD design the three parameters has shown some
variations. The configuration of APD used in the experimentation is with polynomial degree P=9.

<table>
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<td>12</td>
<td>-34.6085</td>
<td>-47.9349</td>
<td>27.3770</td>
</tr>
</tbody>
</table>

Table 6: Polynomial degree effects on various parameters

6.3. Low-pass Filter Designing:

An ideal low-pass filter is simulated in Matlab for filtering out the expanded bandwidth as a result of digital predistortion. The low-pass filter is designed by making a spectrum mask of 1’s (in magnitude) for the desired passband frequencies and 0’s for the stopband frequencies. Then after computing the FFT of DPD output signal, apply the mask to it. After multiplying the ideal filter mask with the DPD output signal, perform the IFFT of output and feed it to the APD.

The results of low-pass filter is shown in Fig.49 and Fig.50 shows the signals before and after the application of ideal low-pass filter in logarithmic and linear scale.

![Filter (Input and output) frequency spectrum](image)

*Figure 49: Input and output spectrum (after fft) of ideal low-pass filter in logarithmic scale*
6.4 Adaptive DPD and APD Model:

A cooperative scheme of digital predistortion and analog predistortion is designed and implemented. The results are obtained by implementing the system with the GaN power amplifier by accessing the web lab.

A schematic block diagram in Fig. shows the complete adaptive loop and the working mechanism of the aforementioned DPD+APD approach.
This methodology provides the solution for the problem of bandwidth expansion caused due to the digital predistortion. The results on every stage of the schematic is obtained. It has been observed that by adopting this mechanism, the signal at DAC input has the same bandwidth as of the original signal, therefore, the DAC has to sample the signal at nyquist frequency. After the up conversion, APD will counter the effects of out of-band distortion while, on other hand, the DPD will find the system (APD+ PA) as linear and will only compensate the effects of memory. The digital filter is applied to ensure that the bandwidth expansion introduced by DPD couldn’t possibly affect the sampling rate of signal at DAC. The NMSE, ACLR and pout remains the same (improved in some configuration) as in only DPD application scenario. Comparative analysis and stage by stage output is presented ahead in the report.

Figure 52: DPD input and output (after fft) spectrum in logarithmic scale

Figure 53: Low-pass filter input and output (after fft) spectrum in logarithmic scale
Figures from Fig.52 to Fig.55 shows the signals in frequency domain (after fft) in logarithmic scale for the illustration of spectral regrowth at every stage of the designed system. The advantage of using this scheme is that the DAC can now be designed on the sampling frequency equivalent to original bandwidth. All the provided graphs were taken with the 9th order polynomial and 7 memory length of the DPD.

In this cooperative scenario, the APD is countering the effects of spectral regrowth, therefore DPD is not trying to compensate for it and focusing on in-band distortion. This is the reason that filtering is not done for a lot of out-of-band signal. As shown in Fig.57 if we use the configuration having only DPD, it can be observed that the spectral regrowth
is introduced by the DPD. Whereas by using a combination of DPD and APD (shown in Fig. 56), it is witnessed that there is no spectral regrowth at the output of memory DPD.

Figure 56: DPD input and output PSD spectra in DPD+APD configuration

Figure 57: DPD input and output power spectral density comparison without APD
**Figure 58:** PA input and output power comparison with and without linearization technique application.

**Figure 59:** PA output PSD comparison with and without linearization technique application.
Figure 60: PA output spectrum (without DPD, with APD and With DPD+APD)

PA output power spectral density spectrum
<table>
<thead>
<tr>
<th>Configuration</th>
<th>Bandwidth at DAC</th>
<th>Polynomial Degree</th>
<th>Memory</th>
<th>NMSE (dB)</th>
<th>ACLR (dB)</th>
<th>Pout (dB)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Memoryless DPD</td>
<td>200 MHz</td>
<td>9</td>
<td>0</td>
<td>-34.608</td>
<td>-47.861</td>
<td>27.375</td>
</tr>
<tr>
<td>Memory DPD</td>
<td>200 MHz</td>
<td>9</td>
<td>6</td>
<td>-38.523</td>
<td>-47.723</td>
<td>27.371</td>
</tr>
<tr>
<td>Memory DPD</td>
<td>200 MHz</td>
<td>9</td>
<td>15</td>
<td>-40.12</td>
<td>-47.785</td>
<td>27.378</td>
</tr>
<tr>
<td>Memory DPD + APD</td>
<td>40 MHz</td>
<td>9</td>
<td>6</td>
<td>-39.6793</td>
<td>-47.8002</td>
<td>27.4091</td>
</tr>
<tr>
<td>Memory DPD + APD</td>
<td>40 MHz</td>
<td>9</td>
<td>11</td>
<td>-40.0225</td>
<td>-47.9664</td>
<td>27.3303</td>
</tr>
<tr>
<td>Memory DPD + APD</td>
<td>40 MHz</td>
<td>9</td>
<td>15</td>
<td>-40.2012</td>
<td>-47.9887</td>
<td>27.4320</td>
</tr>
</tbody>
</table>

Table 7: Final Results for various configurations

Table 7 presents the final results for the cooperative configuration of DPD and APD. The results have shown that the by using only adaptive DPD, the NMSE reaches up to maximum of -40 dB while ACLR has the peak value of -47.785 dB. The same results is observed for the combined configuration of DPD and APD with a low-pass filter between them. By adopting this methodology, maximum NMSE obtained is noted to be -40.2 dB which is greater than the only DPD scenario. Further, the ACLR remain approximately on the same level. The advantage of using this cascaded technique is the bandwidth of signal at the input of DAC. With the use of only DPD, the bandwidth is at least five times, therefore, the DAC has to sample the signal at five times of nyquist frequency. But with the use of cascaded technique, the DAC has to be designed with a sampling rate of nyquist rate, which is twice of signal bandwidth. These results have shown the promising behavior of the proposed scheme and can be adopted for improving the system linearity as well as reduce the signal bandwidth at the input of designed DAC.
Chapter 07

7.1. Conclusion

Initially, the theoretical analysis has been provided on the basis of few parameters that need to be considered while designing a small satellite transmission system. In the first part of report, brief introduction for several parameters, such as, modulation scheme, power budget and types of power amplifiers are discussed and the constraints for their selection in a specific mission are elaborated. Doppler frequency shift effects on the small satellites in lower earth orbit are considered and the state of art methods to counter these effect, in the literature, are presented.

Later part of the thesis implements the concept of reducing the non-linearities in power amplifier behavior with the use of digital predistortion. Further, a solution for the issue of bandwidth expansion due to digital predistortion is presented. As a result of digital predistortion, spectral regrowth occurs and the original signal under goes the phenomenon of bandwidth expansion for up to five times of original. Consequently, while designing the digital to analog converter, sampling frequency of signal should be kept at least five times of nyquist frequency. This thesis provides the cooperative scheme for reducing the signal bandwidth at the output of DPD, while countering the non-linear behavior of power amplifier. This baseband signal at the input of DAC is then sampled at nyquist rate and passed through APD before inputting to the power amplifier.

For the aforementioned purpose, modelling of power amplifier was performed by the use of dynamic deviation reduction based Volterra series. The performance of model is observed in terms of AM/AM curves and NMSE which shows the promising value of -37.5 dB. Further, static and adaptive digital predistortion system is designed countering the effects of memory. Various configuration of polynomial degree and memory length is implemented to observe the behavior of complete system. The adaptive digital predistortion with GaN power amplifier provides the results showing better performance of the system, in terms of NMSE, ACLR and output power. The maximum values of these parameters obtained in several configurations are -40.72 dB, -48.2 dB and 27.3269 dBm respectively.

Moreover, the cooperative scheme consisting of digital and analog predistortion in cascade with a low-pass filter between them is implemented. The frequency spectrum is shown at every stage of the designed scheme which illustrates that the system linearity and power efficiency at amplifier’s output can be achieved without suffering from designing DAC at high sampling rate due to bandwidth expansion phenomenon.

From this master thesis, it is concluded that the problem of bandwidth expansion caused by the digital predistortion can be solved by the cooperative technique used. The concept applied is to avoid the bandwidth expansion caused by DPD with the use of cascaded DPD+APD strategy. The purpose of APD in this scheme is to compensate the out-of-
band distortion from the RF signal, while DPD is responsible of compensating the in-band distortions. For the case, when APD is working properly, the DPD will find the system of APD+PA as linear and only compensate the memory effects introduced by the amplifier. Then there will be no need to put a filter between DPD and APD, but to make sure that the bandwidth expansion doesn’t affect the sampling rate of signal at DAC, the low-pass filter is applied. The results provided in this report has shown that the NMSE, ACLR and output power of the amplifier remain same or improves (in some configurations) by the use of this scheme. While the DAC has to operate at sampling rate of original signal bandwidth rate i.e. if the bandpass is of 40 MHz, then the DAC sampling frequency would be > 40 MHz.
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Bibliography


