# A CONTRIBUTION TO STUDENTS' ASSESSMENT ADJUSTS OF MULTIPLE CHOICE QUESTIONNAIRES WITH FUZZY LOGIC 

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#### Abstract

In University environment, it is common to use multiple-choice objective tests with three or four possible answers, of which only one is correct and the rest are erroneous. In this type of tests, usually the wrong answers are penalized in order to avoid the effect of the random answers. However, there are questions that hardly students answer since their difficulty is high. On the other hand, there are also questions that answer virtually all students since their difficulty is simple. While sometimes the course professor chooses to suppress these questions, it is also common to leave them as part of the calculation of the overall score. This communication proposes a way of, without suppressing any question, making a readjustment of the grades based on fuzzy logic techniques. To do this, it is considered, on the one hand, the initial grade obtained by each student and, on the other, the total difficulty index of the test. With these two variables, an approximation can be made to a system of linguistic variables that allows correcting the final grades of each student based on the objective difficulty of the test and a set of rules established by the professor. This will revert to greater "justice" in students' mark system, since it will be a function of the difficulty of the test.


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## 1 INTRODUCTION

### 1.1 Assessment system

Student assessment is the process that allows knowing what is the level achieved by these students in certain formative objectives. A fair and transparent evaluation assessment system is the one that guarantees that the student body receives a grade that does not limit their future opportunities. Notice that to approve or fair unfairly is vital and the qualification must be, first of all, fair for each student, and as close as possible to the reality of the knowledge achieved for him/her, since each person is unique and, therefore, the assessment should take into account this diversity.
In order to assess the students' performance, in terms of knowledge acquired, one of the most widely used tests is the multiple choice questionnaire (MCQ), consisting of a question and three or four possible answers. Only one of them is valid and the others, called distractors, are false. These formats are known, in a short form, as MCQ-3 and MCQ-4, respectively.

Research of [1], [2] and [3] suggest the model with three answers (MCQ-3) since it saves response time to the student and does not oblige the professor, especially junior, to use improbable and/or defective distractors. On the other hand, the fouranswer model is more suitable if there is a reasonable time available for the test or if the professor is already a senior.
On the other hand, since Zadeh [4] established the principles of fuzzy logic, this has been used to solve problems in very different fields, calling attention also in the academic field as it helps to obtain fairer grades in students and with greater transparency. For instance, in a course/subject rated over 100 points, in which at least 50 points are needed to pass it, the case of a student with a grade of 49 would be considered as a "questionable" mark since it could be considered approved or not, taking into account factors such as the time taken to answer the test, its difficulty, the importance of each question, the complexity in determining the correct answer, etc. Therefore, these factors should be considered in some way when course professor defined the mark obtained by his/her student. In addition, the teacher may have different types of students in his classroom with different learning rhythms or particular educational needs, which means that not all of them, perhaps, should be evaluated in the same way, since the classroom is a very diverse human space. With fuzzy adjusts it's possible be a more accurate assessment. With diffuse adjustments, it is possible that the evaluation is more precise and even fairer by being able to attend to particular cases.

### 1.2 Literature Review Concerning Recalculation of Students' Assessment Using Fuzzy Logic

Following [5], fuzzy logic is a generalization of crisp set theory and traditional dualvalued logic. In fact, in fuzzy set theory the range of the membership function characterizing a set is extended from only two values, 0 or 1 , to any value between 0 and 1.

Most of publications related to student assessment with fuzzy logic techniques refer
to seminal articles of Zadeh and Biswas [6]. The article by Chen and Lee [7], also related to students' assessment through fuzzy logic, is also cited profusely in the literature. Since then, fuzzy logic has been used in very different academic fields, being a current of interest the adjustment of the grades obtained by students taking different adjustment parameters and mixing fuzzy logic with other techniques traditionally associated with artificial intelligence (AI) as the case of data mining. One interesting example is in [8], [9] and [10].
They are in the literature many different approachs using fuzzy logic, as can see in [11] and [12], and also in [13] to [18]; in many approaches with multiple input variables, it seems reasonable to use a fuzzy inference model by successive steps, since it allows establishing the rule bases by pairs of variables, giving rise to small and simple base rules simply deductible by the experience.
Studies carried out related to the different fuzzy inference techniques should also be pointed out, and defuzzification methods like those of related in [19], [20] and [21]. In addition, many authors use Matlab ${ }^{\circledR}$ to implement their contributions.

Regarding the geometry of the fuzzy sets used, almost all the publications consulted refer to triangular or trapezoidal sets due to the simplicity of calculation since the differences that would be obtained with other joint geometries (sigmoidal -used by [12]-; Gaussian -used by Hameed and Sorensen [17]-, hyperbolic tangents, etc.) are not relevant to the outcome. Also, the use of other geometries that are not trapezoidal or rectangular are used only when the use of Matlab ${ }^{\circledR}$ software is available.
We propose in the following section a very simple method of calculation using the inference of Mamdani [22], and taking into consideration only the difficulty of the test and the qualification obtained. Some authors such [19] have used the difficulty of a certain competence based on students' marks who studied the subject before and with a difficulty level specified by the professor. In any case, the use of the difficulty index of an objective test has not been located in the bibliography consulted by authors.

## 2 METHODOLOGY

In an MCQ, the calculation of the difficulty index $(D I)$ of each of the questions is the one expressed in (1):

$$
\begin{equation*}
D I=\frac{\# \text { Correct answers }}{\# \text { Questions }} \tag{1}
\end{equation*}
$$

It is considered a classic classification of the difficulty scale, taken from [23], which is the one that can be seen in Table 1. The scale and difficulty may vary, but authors consider that that listed in Table 1 is very convenient for academic purposes.
The overall difficulty index of an entire test, $D I_{\text {tотац }}$, may be established by taking the average of all difficulty indexes for all questions, according to (2). Therefore, it is simple, by means of a simple table with a spreadsheet that contains in the rows to the students and in the columns the questions, to have in each cell the qualification obtained by each student in each question. Applying (1) to each column, you can determine the parameter DI and identify the difficulty of each question. In addition,
applying (2) the difficulty of the test, as a whole, can be obtained.
Table 1. Classic interpretation of the difficulty index (DI).

| Value | Interpretation | Suggested Action for the question |
| :--- | :--- | :--- |
| $D I>0.75$ | Very Easy | Dismiss definitively |
| $0.56<D I<=0.75$ | Easy | Candidate to be discarded |
| $0.46<D I<=0.55$ | Regular | Review |
| $0.26<D I<=0.45$ | Difficult | Candidate to be discarded |
| $D I<=0.25$ | Very Difficult | Dismiss definitively |

For MCQ-3, the optimal total difficulty would be 0.67 [24]. However, it is considered average difficulty, in general, between 0.50 and 0.60 [25]. If possible, experts suggest that items should have indices of difficulty no less than 0.20 and no greater than 0.80 . It is desirable to have most items in the 0.30 to 0.50 range of difficulty. Very difficult and very easy items contribute little to the discriminating power of a test [26].

$$
\begin{equation*}
D I_{\text {TOTAL }}=\frac{\text { Mean of Difficulty Indexes }}{\text { Number of Indexes }} \tag{2}
\end{equation*}
$$

When differentiating one category of difficulty from the next using crisp values, it is difficult to consider that a question with $D I=0.55$ is "regular" and that one with $D I=$ 0.56 is "easy" so that it seems natural to consider this variable as a fuzzy set taking as many subsets as difficulty categories. Likewise, when considering the $D I_{\text {TOTAL }}$, the overall difficulty of the test can be established diffusely, considering that a test with $D I_{\text {TOTAL }}=0.55$ is "regular" and one with $D I_{\text {TOTAL }}=0.56$ is "easy". For this reason, and taking as reference the crisp values of this indicator, a categorization based in fuzzy subsets is established such as the proposed in Figure 1. In this article, we use triangular membership functions because this shape has been proven popular in fuzzy logic and being used extensively in student academic performance assessment [26].
In Figure 1 it can be observed, respecting the spirit of the differentiation of difficulty index, that values below 0.25 and above 0.75 as well as those between 0.45 and 0.55 , will only belong to one fuzzy subset, while that the rest of values will belong to two fuzzy subsets.
Taking as reference the crisp values of this indicator, a categorization based in fuzzy subsets is established such as the proposed in Figure 1. We use triangular membership functions [27], but other shapes are possible (that not has a significative difference respect to results).
Let us take as an example, a test with 5 questions in format type MCQ-3 (three answers per question, an answer right and two answers acting as distractors), in which five students participated. In order to discard the random factor and, in some way, discourage the student to try his luck in case he does not clearly know the answer. The amount of penalty would be established, in this case, by the expression (3) taken from [28] which, in turn, [29] cites and also is studied by [30] and [31]. The unanswered questions will have zero value and the wrong answers, will have the corresponding

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penalty according to their weight.

$$
\begin{equation*}
\text { Penalty }=\frac{1}{\text { \#Possible answers }-1}=\frac{1}{3-1}=0,5 \tag{3}
\end{equation*}
$$



Figure 1. Fuzzy sets for difficulty index total, DItotal.
This means that, in case all the questions are MCQ-3 type, the penalty will be half the value of the right answered. If the number of possible answers is different in some questions, the local penalty for each different question would apply. Table 2 shows a hypothetical result of the presented example.

Table 2. Difficulty Index per question and global grade per student.

| Question $\boldsymbol{\rightarrow}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Weight (\%) $\boldsymbol{\rightarrow}$ | $\mathbf{1 5}$ | $\mathbf{2 0}$ | $\mathbf{1 5}$ | $\mathbf{3 0}$ | $\mathbf{2 0}$ |  |
| Student $\downarrow$ |  |  |  |  |  | Grade over $\mathbf{1 0 0}$ points $\downarrow$ |
| $1 \rightarrow$ | -7.5 | 0 | 15 | 30 | 20 | $\mathbf{5 7 . 5}$ |
| $2 \rightarrow$ | -7.5 | 20 | 0 | 0 | 0 | $\mathbf{1 2 . 5}$ |
| $3 \rightarrow$ | -7.5 | 20 | 0 | 30 | -10 | $\mathbf{3 2 . 5}$ |
| $4 \rightarrow$ | 0 | 0 | 15 | 0 | 20 | $\mathbf{3 5}$ |
| $5 \rightarrow$ | 15 | 0 | -7.5 | 0 | 20 | $\mathbf{2 7 . 5}$ |
| $D I$ | 0.2 | 0.4 | 0.4 | 0.4 | 0.6 |  |

In example shown in Table 2, $D I_{T O T A L}=0.4$. Thus, we can calculate the fuzzy difficulty index ( $F I_{\text {total }}$ ) with fuzzy sets shown in Figure 1. We want to highlight the use of Excel ${ }^{\circledR}$ for all calculations in this paper. After fuzzification, Table 3 shows the values of membership subsets.

Table 3. Fuzzy total difficulty index (FDITOTAL) of the questionnaire.

| Fuzzy sets | Very Poor | Poor | Regular | Difficult | Very Difficult |
| :--- | :---: | :---: | :---: | :---: | :---: |
| FDI $_{\text {TOTAL }}$ | 0 | 0.5 | 0.5 | 0 | 0 |

In order to place the student grade in one of, for example, five categories, it is important to place his initial grade in a fuzzy environment like shown in Figure 2.
Some authors cited in [21] make a different proposal for the distribution of these subsets in order to categorize students' grades placing any grade between 0-0.2 points only in the category of 'poor' and between 0.85 and 1.0 only in the 'good' category. However, most of authors establish the limit of 'poor' between 0 and 0.1 and 'good' between 0.9 and 1.0. Continuing with the previous example, for calculate the
membership to each fuzzy set, we need to obtain the equations of every subset segment, for example, for interval 0.1-0.3 (Below Average), the equation used is $y=5 x+1,5$. Fuzzy grades for each student of the example are shown in table 4.


Figure 2. Fuzzy sets for grades.


Figure 3. Output fuzzy subsets for student \#4.

Table 4. Fuzzy membership grades for every student.

| Student | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Crisp Grade Normalized to 1 | 0.575 | 0.125 | 0.325 | 0.35 | 0.275 |
| Poor | 0 | 0.875 | 0 | 0 | 0.125 |
| Below Average | 0 | 0.125 | 0.875 | 0.75 | 0.875 |
| Average | 0.625 | 0 | 0.125 | 0.25 | 0 |
| Above Average | 0.375 | 0 | 0 | 0 | 0 |
| Good | 0 | 0 | 0 | 0 | 0 |

With this information, it is possible to make the rule base in terms of 'IF-THEN' sentences. Consulted literature refers to different techniques for establish the rules; in this example (see Table 5), each category of output is present in five cells (it is possible to make small changes to this rule base for special cases).

Table 5. Rule base for fuzzy grades and difficulty index.

|  |  | Difficulty Index |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Very Poor | Poor | Regular | Difficult | Very Difficult |
| $\begin{aligned} & \mathscr{y} \\ & \stackrel{0}{0} \\ & \text { U } \end{aligned}$ | Poor | Poor | Poor | B. Average | B. Average | Average |
|  | Below Average | Poor | Poor | B. Average | Average | A. Average |
|  | Average | Poor | B. Average | Average | A. Average | Good |
|  | Above Average | B. Average | Average | A. Average | Good | Good |
|  | Good | Average | A. Average | A. Average | Good | Good |

Considering Mamdani inference, results of the example is listed in Table 6.
Table 6. Result of applying the base rules to each student.

|  | Student | \#1 | \#2 | \#3 | \#4 | \#5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Crisp Grade | 0.575 | 0.125 | 0.325 | 0.35 | 0.275 |
|  | Poor | 0 | 0 | 0 | 0 | 0 |
|  | Below Average | 0 | 0.5 | 0.5 | 0.5 | 0.5 |
|  | Average | 0.5 | 0.125 | 0.5 | 0.5 | 0.5 |
|  | Above Average | 0.5 | 0 | 0.125 | 0.25 | 0 |
|  | Good | 0.375 | 0 | 0 | 0 | 0 |

If we take, for example, the student number \#4, his score would be the result of calculating the center of the area resulting from the fuzzy subsets trimmed to each output value, as we can see in Figure 3.
Finally, it is necessary to return these assessment values to crisp quantities by means of one of the different defuzzification techniques that allow obtaining a unique numerical value that represents them properly in [32]. The technique of singletons [33] is the more easy and concrete way for accurate calculation. Applying singletons, the scores that the calculation would return values showed in Table 7.

Table 7. Results of defuzzified grades vs. initial obtained grades.

| Student | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Initial Grade Normalized to 1 | 0.575 | 0.125 | 0.325 | 0.35 | 0.275 |
| Deffuzified Grade Normalized to 1 | 0.712 | 0.353 | 0.455 | 0.473 | 0.413 |

## 3 DISCUSSION

Some authors such as [21] rightly point out that the choice of defuzzification method depends on each context or on each specific problem, reaching the possibility of using different techniques depending on the fuzzy output subsets for each student, depending on what categories include and not use the same technique for students with grades that are poor, below average, average, since the same technique for all grading intervals can harm some students. This is completely true since a student with an initial score of 100 in a very easy test, could lose a grade and that would not be fair because he has guessed all the answers and should not be penalized, while a student with a poor grade in a high difficulty test, possibly know more than what the test has allowed him to manifest.
Likewise, other authors also indicate that not only is there no universal defuzzification operator but that their choice depends on factors such as the speed at which this operation should be done. For example, in the case of industrial controls in real time where computational efficiency is a very important factor or in the case of information support systems where the calculation time is not as important, as is the case of adjusting student grades. The method of extended intervals in order to defuzzify outputs is correct for the qualification in students, but considering that it will be necessary to take some correction elements to differentiate the cases in which the student may be affected by the calculation.
On the other hand, any fuzzy calculus technique is very variable since it depends on:

1) The number and geometry of linguistic subsets of each variable.
2) The number of input variables, since more variables can be used in addition to the rating and the $D I_{\text {Total, }}$, as seen in the literature review.
3) Geometry and position of input and output fuzzy subsets.
4) Rules contained in the rules base. As it is said in [34], the rules have to be determined by expert experience and it is difficult to make a determination of a
system designed according to the fuzzy logic; that is, it cannot be estimated how the system reacts beforehand.
5) The way to make the inference, which is this case has been taken mamdani inference, but there are many other ways to do it (see, for example, [35]).
6) Defuzzification method used. They are multiple different defuzzification methods.
7) Etc.

Each change in the above factors will cause a different adjustment of results. However, at least, it is an adjustment that does not imply suppression of questions that all or no one answered correctly (with no or maximum difficulties), and should not harm anyone. In addition, it involves the concept of "justice" that each professor should establish and that, undoubtedly, it varies from professor to professor, since it is based on his personal way of understanding teaching, the fair assessment, and the corrective actions of results that are frequently doubtful.
Thus, the concept of "justice in assessment" that we apply in our case, obeys the following rules:

1) Students with an initial score of <= 10 points are considered suspended regardless of the $D I_{\text {Total }}$ and do not considered in the correction grade.
2) Students with an initial score of $>=90$ points are considered approved regardless of the $d_{i_{\text {total }}}$ and do not considered in the correction grade.
3) Students with an initial score between 11 and 89 points, they will be compensated in function of the $D I_{\text {Total }}$ and the corrected value will be taken.
4) If a student, after correction, obtains a negative grade, the grade will be 0 points.
5) If a student, after correction, obtains a grade higher than 100 , the grade will be 100.

## 4 SUMMARY

This article has proposed a way of, without suppressing any question, making a readjustment of the grades based on fuzzy logic techniques. To do this, it is considered, on the one hand, the initial grade obtained by each student and, on the other, the total difficulty index of the test (overall difficulty index of an entire test, $D I_{\text {total }}$ ). With these two variables, an approximation can be made to a system of linguistic variables that allows correcting the final grades of each student based on the objective difficulty of the test and a set of rules established by the professor. This will revert to greater "justice" in students' mark system, since it will be a function of the difficulty of the test.
The above method tends to benefit students with worse grades when the difficulty of the test is high, while not penalize students who have obtained excellent grades. The MCQ tests allow to obtain the parameter $D I_{\text {total }}$ and, with this index, to be able to establish a re-calculation of the qualification of each student.

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