A New Nonlinear Compliant Mechanism for Harvesting Energy from Ocean Waves

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Abstract—Traditional linear oscillators, such as cantilevers or pendulums, are only sensitive to specific resonant frequencies. They have then very narrow frequency bandwidths when harvesting energy from ocean waves. In order to enhance the dynamic performance of the wave energy converters (WECs), used to expand the autonomy of Lagrangian Drifters, a statically balanced compliant mechanism (SBCM) is investigated. It is based on finite element analysis (FEA) simulations. The design of the SBCM is introduced and its static force-displacement curve is obtained in FEA. The dynamic response of the SBCM to harmonic base excitations at low frequencies and low accelerations is investigated based on time-domain FEA simulations. The close agreement between simulations, numerical and analytical results verifies that the SBCM is sensitive to ultra-low frequencies with weak accelerations in a wide frequency range. The applicability of the SBCM in WECs is demonstrated by adding PVDF films in the FEA model. In the time-domain simulation, the SBCM-based WEC is excited by the drifter motion pattern obtained from Orcaflex and corresponding to two typical ocean waves (i.e. synthesized Airy and Jonswap models). Relative displacement between the base and mass and the electric outputs are obtained. According to this work, the SBCM provides a structural solution for WECs with enhanced energy harvesting performance.

Keywords—Lagrangian Drifter, Wave Energy Converter (WEC), Compliant mechanism, Stiffness nonlinearity, Wide bandwidth, FEA simulation.

I. INTRODUCTION

Marine biodiversity is highly affected by global warming. Almost 90% of the heat produced during the last decade has been absorbed by oceans, destroying many marine ecosystems. Closely tracking ocean changes helps prevent the effects of this phenomenon and maintain the Earth’s health. Oceanographic sensor platforms provide biological and meteorological data to help understand changes in marine environments. Underwater cabled observatories [1] or autonomous underwater vehicles [2] are sensor platforms that provide a large quantity of data but entail high deployment and maintenance costs.

Lagrangian drifters (Fig. 1) are autonomous floating passive devices used in marine climate research that provide surface marine data [3]. They are low-cost, versatile and easy-to-deploy instrumentation, so many of them can be deployed in large oceanic regions forming a surface sensors network. Drifter deployments can last for years, so autonomy is one of the leading design challenges [4]. Several Energy Harvesting (EH) sources are being explored to reduce costs in battery replacement maintenance tasks. Solar panels have been the most common commercial solution for expanding a drifter’s autonomy (Sofar: Spotter, Fastwave: Voyager Solar). Drifters must avoid the impact of the wind because this may compromise a proper superficial current tracking [5]. Consequently, they must be mostly submerged, interfering with the feasibility of solar harvesting. Depending on a single EH source will have little effect on making the unit more autonomous. For this reason, other EH sources are being explored, including the oscillatory movement of the drifter itself caused by the interaction with the ocean waves.

References [6]–[9] present different Wave Energy Harvesters (WECs) based on electromagnetic techniques to convert vibrational energy into electricity. Specifically in

Fig. 1. Lagrangian Drifter deployed at coastal area, in the Mediterranean Sea, within the tests of the EC-founded MELOA project [3].
[10], a novel pendulum-type WEC which uses the motion of waves and the current flow to generate power from a drifter was presented. The WEC consists of an articulated pendulum arm with a proof mass that transforms the oscillation into rotation and electric outputs are obtained from a DC generator.

In [11], it has been experimentally proven that embedding a moving element in a drifter does not affect its ocean measurements as long as the EH mass is small enough in relation to that of the drifter. Piezoelectric capacitors are also popular choices for energy conversion in WECs [12]. However, the linear oscillators used in all these WEC’s systems lead to an inefficient narrow frequency bandwidth. Since ocean waves have mixed frequencies in a low frequency range with weak accelerations, the resulting performance of the system would be far from its optimum point and would present low conversion efficiency.

Mechanical structures act as interfaces between the drifter vibrations and the energy-conversion capacitors in the WECs [13]. In order to enhance the dynamic performance and the energy generation capability, a Statically Balanced Compliant Mechanism (SBCM) is proposed as a structural solution for WECs embedded in drifters. This SBCM is able to stay in equilibrium in the continuous static-balancing displacement range, while it owns nonlinear stiffness in the wider displacement range. Due to its unique nonlinear force-displacement characteristics, the SBCM responds to ultra-low frequencies with weak accelerations in a wide frequency range. Other advantages of the SBCMs include highly-eliminated friction, less or no assembling procedure, reduced mass, low cost and good manufacturability. They all benefit the application into WECs [14], [15]. This paper investigates the dynamic performance of the proposed SBCM under harmonic excitations based on FEA simulations with COMSOL. The applicability of the SBCM in WECs is also demonstrated utilizing the drifter motion patterns generated from Orcaflex as displacement excitations in FEA simulations.

The paper is organized as follows: Section II describes the design of the SBCM and the analytical results of the dynamic response to harmonic base excitations. Section III presents the FEA simulation on the SBCM model under harmonic base excitations at discrete frequency points in the low frequency range. Section IV presents the simulation of a drifter in the sea using a commercial software (OrcaFlex). The applicability of the SBCM in WECs is demonstrated by adding a PVDF in the SBCM in WECs is demonstrated utilizing the drifter motion patterns generated from Orcaflex as displacement excitations in FEA simulations.

In order to describe the force-displacement link on the SBCM, the force-displacement curve is fitted with a polynomial equation with Polyfit function in Matlab. Fig. 3 shows that the force-displacement curve is symmetric about the origin point. Therefore, only odd order terms exist in theory and odd order terms are neglected in the polynomial equation as shown in Eq. (1). The fitting curve is also shown in Fig. 3 indicated with a dashed line. The $R^2$ coefficient of

\[
\begin{align*}
L_2 & = 42 \text{ mm} \\
H_2 & = 15 \text{ mm} \\
T_2 & = 0.4 \text{ mm} \\
\Delta L & = 2 \text{ mm}
\end{align*}
\]

TABLE I. Geometric parameters of the SBCM with static balancing achieved based on FEA simulation.

<table>
<thead>
<tr>
<th>Positive-stiffness component</th>
<th>Negative-stiffness component</th>
</tr>
</thead>
<tbody>
<tr>
<td>$L_2$</td>
<td>$L_2$</td>
</tr>
<tr>
<td>$H_2$</td>
<td>$H_2$</td>
</tr>
<tr>
<td>$T_2$</td>
<td>$T_2$</td>
</tr>
</tbody>
</table>

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Fig. 2. Schematic structure of the SBCM.

Fig. 3. Force-displacement curve of the SBCM.
determination is 99.94 %, which indicates an accurate fit of this polynomial equation to the force-displacement curve obtained from the FEA simulation.

\[
F(x) = 0.002194x + 0.001774x^3 + 0.000003362x^5
\]  

(1)

B. Theoretical dynamic modeling of the SBCM

The static force-displacement characteristic of the SBCM determines its dynamic response to external excitations. The relative displacement between the mass block and the frame is directly related to the performance of the SBCM in EH applications. Therefore, it is concerned and focused in this work. In order to describe the force-displacement link of the SBCM, a polynomial 5 degree equation with only odd order terms is proposed as Eq. (2).

\[
F(x) = ax^3 + bx^5 + cy^5
\]  

(2)

where \( a, \beta, \text{ and } \gamma \) are the coefficients of the odd-order terms. Based on this general force-displacement equation, the dynamic motion equation of the SBCM under harmonic base excitation can be described as:

\[-m\ddot{z} = m\ddot{x} + cx + ax + \beta x^3 + \gamma x^5\]  

(3)

where \( m \) is mass of the movable block, \( c \) is the damping ratio of the system, \( x \) represents the steady-state relative displacement between the mass block and the frame, \( \ddot{z} \) is the base excitation acceleration assumed to be \( \ddot{z} = A_0\cos(\Omega t) \).

To facilitate analysis, Eq. (3) can be formulated as:

\[-A_0\cos(\Omega t) = \ddot{x} + 2\ddot{\zeta} + k_1x + k_2x^2 + k_3x^3 \]  

(4)

where the individual coefficients can be expressed by the following formulae:

\[ 2\ddot{\zeta} = \dfrac{c}{m}, \quad k_1 = \dfrac{a}{m}, \quad k_2 = \dfrac{\beta}{m}, \quad k_3 = \dfrac{\gamma}{m} \]

Based on the averaging method, the relationship between the relative base-mass displacement (\( H \)) and the excitation frequency (\( \Omega \)) can be obtained. This \( H-\Omega \) relationship can also be obtained numerically based on Eq. (4) with the ODE-45 MATLAB function. In the FEA model created, the mass of the mass block is 88.8 g and the damping ratio (\( \zeta \)) is 1.7. Under the harmonic base excitation in the ultra-low frequency range from 0.25 Hz to 10 Hz with a weak acceleration of 0.25 g and 0.5 g, the analytical and numerical results of the \( H-\Omega \) relationship of the SBCM in its static-balancing status are plotted in Fig. 4. These theoretical results show that this SBCM responds to ultra-low excitation frequencies (theoretically starting from 0 Hz) in a wide frequency range. The maximum relative displacement amplitude can reach 20 mm at 13 Hz and 0.5 g.

III. FEA SIMULATION ON THE SBCM WITH HARMONIC EXCITATIONS.

A. Harmonic base excitation with acceleration of 0.25 g

The dynamic response of the proposed SBCM under sinusoidal excitations with ultra-low frequencies and weak accelerations is explored based on FEA simulations. The excitation frequency range is set from 0.25 Hz to 10 Hz according to the frequency spectrum of ocean waves studied in [18], with two acceleration values of 0.25 g and 0.5 g (1 g equals to 9.8 m/s²). Base excitation is applied on the outer frame of the model by the “Prescribed Displacement” boundary condition in the time domain for 20 periods. Regarding to a given frequency and an acceleration (e.g. 1 Hz, 0.25 g), one simulation is carried out. The simulated relative displacement between the mass and base (\( H \)), the absolute displacement of the base (\( x_{base} \)) and the absolute displacement of the mass (\( x_{mass} \)) are captured and plotted with respect to time (\( t \)).

The displacement curves of the SBCM under the excitation condition of 3 Hz and 0.25 g in time domain are presented in Fig. 5 as an example of the dynamic FEA simulation results. The response displacement of the mass block is illustrated as a blue curve and the average amplitude is about 14 mm. The red curve is the relative displacement between the base and frame and its average amplitude is about 7.57 mm. \( H \) is focused in the FEA simulation since it directly influences the performance of the SBCM. Regarding to the excitation frequencies in the range from 0.25 Hz to 10 Hz with the acceleration of 0.25 g and 0.5 g, \( H \) is collected and summarized in TABLE II. It should be noted that the average relative displacement amplitude of 10 continuous oscillations in its steady state at each frequency point is recorded as the relative displacement amplitude (\( H \)). Based on the data in TABLE II, the \( H-\Omega \) curve is shown in Fig. 6.

### TABLE II. Relative displacement of the SBCM under harmonic base excitations in the dynamic FEA simulations.

<table>
<thead>
<tr>
<th>Base excitation frequency (Hz)</th>
<th>Relative displacement amplitude ( H ) (mm) at 0.25 g</th>
<th>Base excitation frequency (Hz)</th>
<th>Relative displacement amplitude ( H ) (mm) at 0.5 g</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.25</td>
<td>0.25</td>
<td>0.25</td>
<td>7.32</td>
</tr>
<tr>
<td>0.5</td>
<td>5.19</td>
<td>0.5</td>
<td>6.73</td>
</tr>
<tr>
<td>1</td>
<td>5.86</td>
<td>1</td>
<td>6.5</td>
</tr>
<tr>
<td>2</td>
<td>6.67</td>
<td>2</td>
<td>9.4</td>
</tr>
<tr>
<td>3</td>
<td>7.57</td>
<td>3</td>
<td>9.83</td>
</tr>
<tr>
<td>4</td>
<td>8.04</td>
<td>4</td>
<td>10.28</td>
</tr>
<tr>
<td>5</td>
<td>1.26</td>
<td>5</td>
<td>10.93</td>
</tr>
<tr>
<td>6</td>
<td>1.21</td>
<td>7</td>
<td>1.77</td>
</tr>
<tr>
<td>8</td>
<td>0.53</td>
<td>9</td>
<td>1.19</td>
</tr>
<tr>
<td>10</td>
<td>0.35</td>
<td>10</td>
<td>0.44</td>
</tr>
</tbody>
</table>

![Fig. 4. Numerical and analytical results of the dynamic relative displacement response of the SBCM in the ultra-low excitation frequency range from 0.25 Hz to 10 Hz with the accelerations of 0.25 g and 0.5 g.](image-url)
is concluded that the SBCM is sensitive to ultra-low wide bandwidth excitation frequencies with weak accelerations. The SBCM investigated in this paper provides a suitable structural solution in harvesting vibrational energy from ocean waves.

Notice that large displacement amplitudes have not been obtained in FEA simulations at excitation frequencies between the jumping-up and jumping-down frequencies. FEA simulation is carried out at discrete frequencies with no vibrational “history”. I.e. vibrational energy from previous oscillation status is considered as initial conditions. In real operation with SBCM prototypes, external disturbing can be applied to the oscillating mass block to stimulate the oscillation with larger amplitude, while this is not available in FEA simulations.

When the excitation frequency is higher than the jumping-up frequencies (Fig. 6), H jumps significantly and large amplitudes observed in analytical and numerical results cannot be researched in FEA simulations. This is because FEA simulation is carried out at discrete frequencies with no vibrational “history”. In real operation, external disturbing can be applied to the oscillating mass block and the vibration status with larger amplitude can be stimulated from the vibration status with smaller vibration amplitude. The essence of the external disturbing here is imported energy to the oscillation system. However, this operation is not available or very complex in the FEA simulation.

IV. VOLTAGE OUTPUT DEMONSTRATION BASED ON DRIFTER MOTION PATTERNS.

The applicability of the proposed SBCM in energy harvesting from ocean waves is explored in this section based on FEA simulations. The FEA model of a preliminary SBCM-based PVEH is created with piezoelectric materials applied on the flexural beams. PVDF films are used as piezoelectric components for energy conversion due to their good piezoelectric performance and outstanding flexibility. Two pieces of PVDF films (20 mm×15 mm ×0.2 mm for each) are added symmetrically in the near-root area of the upper positive-stiffness beams, on the side close to the central fixing position (Fig. 7). Drifter motion patterns corresponding to typical ocean waves are used as displacement base excitations in the time domain FEA simulation. The voltage output across an external resistance of 1 MΩ and relative displacement of the SBCM are are measured and plotted.

![Displacement curves of the SBCM under the base excitation at 3 Hz, 0.25 g in FEA simulation](image)

*Fig. 6. Displacement curves of the SBCM under the base excitation at 3 Hz, 0.25 g in FEA simulation*

![Numerical results:](image)

*Table III. Ocean drifter parameters*

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Parameter</th>
<th>Value</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>$m_b$</td>
<td>Mass</td>
<td>3.6</td>
<td>kg</td>
</tr>
<tr>
<td>$R$</td>
<td>Radius</td>
<td>0.1</td>
<td>m</td>
</tr>
<tr>
<td>$c_m$</td>
<td>Centre of mass $^4$</td>
<td>-0.05</td>
<td>m</td>
</tr>
<tr>
<td>$d$</td>
<td>SWL-$c_m$ distance</td>
<td>0.05</td>
<td>m</td>
</tr>
<tr>
<td>$I_c$</td>
<td>Horizontal inertia</td>
<td>$9 \times 10^{-3}$</td>
<td>Kg m$^2$</td>
</tr>
</tbody>
</table>

$^4$ CENTER OF MASS BELOW THE DRIFTER’S GEOMETRIC CENTER.
of the wind in the drifter’s shell. Placing the battery pack below the drifter’s geometric center shifts its center of mass \( (c_m) \) downwards by 5 cm, making the drifter stable and thus ensuring the antenna is always above the waterline.

The sea state has been modeled using two sea models to estimate the performance of the WEC in both conditions. On the one hand, a regular sea implemented with the Airy model [19], a sinusoidal-shape trajectory that simply describes the surface particle motion. This is defined by the significant wave height \( (H_S) \) and the significant wave period \( (T_S) \). This sea model has been composed of the superposition of two regular waves. On the other hand, an irregular sea state is described by the JONSWAP model [20]. JONSWAP spectrum is a water wave model that statistically describes the behavior of the water particles in shallow waters, resulting in a bandwidth distribution of frequencies around the main one \( (1/T_S) \), TABLE IV summarizes both models and the shared environmental parameters.

<table>
<thead>
<tr>
<th>Table IV. Environment parameters</th>
<th>Sea model</th>
<th>Symbol</th>
<th>Parameter</th>
<th>Value</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regular</td>
<td>-</td>
<td>h</td>
<td>Ocean depth</td>
<td>20</td>
<td>m</td>
</tr>
<tr>
<td></td>
<td>-</td>
<td>ρ</td>
<td>Ocean density</td>
<td>1024</td>
<td>Kg/m³</td>
</tr>
<tr>
<td></td>
<td>-</td>
<td>g</td>
<td>Gravity accel.</td>
<td>9.81</td>
<td>m/s²</td>
</tr>
<tr>
<td></td>
<td>H_s1</td>
<td>Sig. Wave Height</td>
<td>0.7</td>
<td>m</td>
<td></td>
</tr>
<tr>
<td></td>
<td>T_s1</td>
<td>Sig. Wave Period</td>
<td>3.5</td>
<td>s</td>
<td></td>
</tr>
<tr>
<td></td>
<td>H_s2</td>
<td>Sig. Wave Height</td>
<td>1.5</td>
<td>m</td>
<td></td>
</tr>
<tr>
<td></td>
<td>T_s2</td>
<td>Sig. Wave Period</td>
<td>8</td>
<td>s</td>
<td></td>
</tr>
<tr>
<td>Irregular</td>
<td>H_s3</td>
<td>Sig. Wave Height</td>
<td>0.8</td>
<td>m</td>
<td></td>
</tr>
<tr>
<td></td>
<td>T_s3</td>
<td>Sig. Wave Period</td>
<td>3</td>
<td>s</td>
<td></td>
</tr>
</tbody>
</table>

\*REGULAR SEA MODEL COMPOSED BY THE SUPERPOSITION OF TWO REGULAR WAVES.

Fig. 8 defines also the global axis, where Y is the horizontal axis and Z is the vertical axis. It also defines the concepts of wave height \( (H) \) and period \( (T) \) among the SWL. For simplicity, the wave propagation direction has been aligned with the horizontal drifter’s local axis Y, leading to a simpler model of 2D. The interaction with the wave motion causes the drifter’s vertical displacement \( (D_z) \) which is the vector that has been later used as excitation in FEA simulations.

Simulation results are shown in Fig. 9, where the vertical drifter displacement is shown for both sea models. Orange has been used for the Airy model and blue for the JONSWAP model. The left side of the figure contains the time-domain results and the right side contains the frequency-domain results (FFT function has been used for this purpose). Airy \( D_z \) presents a composition of two sinusoidal waves at a different frequency as its FFT results present two peaks, one at around 0.3 Hz \( (1/T_z) \) and the second at around 0.12 Hz \( (1/T_z) \). Its time-domain peak-to-peak amplitude can reach up to 2 m when both waves align. JONSWAP \( D_z \) presents a lower amplitude than Airy’s because its main \( H_{S3} \) is smaller than the composition of \( H_{S3} \) and \( H_{S2} \). Its frequency-domain results present a frequency distribution around \( 1/T_z \) instead of a peak centered in a single frequency.

B. FEA simulation results

Under the base excitation with drifter motions patterns shown in Fig. 9, the displacement response of the device in the time domain are obtained and presented in Fig. 10. Since the displacement amplitude of the drifter motion patterns are in meters and it is much larger than the dimensions of the SBCM, the displacement curves of the base and mass are almost overlapped with each other as shown in Fig. 10 (a) and Fig. 10 (c). Therefore, relative displacement curves between the frame and the mass block are presented separately for a clear illustration in Fig. 10 (b) and Fig. 10 (d). It is shown that the maximum relative displacement amplitude between the base and mass of the SBCM in the Airy ocean wave is about 9 mm. In the Jonswap ocean wave, the maximum relative displacement amplitude reaches about 10 mm. According to the FEA simulation results, the SBCM designed shows good sensitivity to the ocean waves when it is embedded into drifters to be used as a WEC.

Excited by the drifter motion patterns, voltage outputs across the external resistance are generated in the FEA simulation. The Voltage curves and the calculated instantaneous power curves with respect to time are plotted in Fig. 10 (e) – (h). The relative displacement between the mass and the frame is also plotted in the individual figures as references to highlight the relationship between the deformation of the beams and the piezoelectric attachment. Fig. 10 (e) shows that the AC voltage reaches the maximum of 1.37 V in the excitation condition corresponding to the synthesized airy ocean wave. The maximum instantaneous power is about 1.87 \( \mu \)W as shown in Fig. 10 (f). In the excitation condition corresponding to the Jonswap ocean wave, the maximum AC voltage is about 1.53 V (as shown in Fig. 10 (g)) and the maximum instantaneous power is about 2.34 \( \mu \)W (as shown in Fig. 10 (h)). The electric generation capability of the preliminary SBCM-based PVEH under ocean wave excitations is verified with the FEA simulations in the time domain though the voltage outputs. Instantaneous power dissipated over the load is low due to the non-optimized electric loads and the piezoelectric attachment positions.
Fig. 10. FEA simulation results of the displacement response of the SBCM. (a) Absolute displacements of the frame and mass block and (b) The relative displacement between the frame and the mass block excited by the drifter motion pattern corresponding to ocean wave A; (c) Absolute displacements of the frame and mass block and (d) The relative displacement between the frame and the mass block excited by the drifter motion pattern corresponding to ocean wave B. Right side; (e) Voltage output across the load resistance and (f) Instantaneous power generated over the external resistance together with the relative displacement between the base and mass under the base excitation corresponding to the synthesized air ocean wave in time domain; (g) Voltage output across the load resistance and (h) Instantaneous power generated over the external resistance together with the relative displacement between the base and mass under the base excitation corresponding to the Jonswap ocean wave in time domain.
V. CONCLUSIONS

Ocean waves have mixed frequencies in the low frequency range with weak accelerations. The SBCM provides a structural solution for WECs. The dynamic response of the SBCM to harmonic base excitations with ultra-low excitation frequencies is investigated based on time-domain FEA simulations. The applicability of the SBCM in harvesting energy from ocean waves is then demonstrated with PVDF films added in the FEA model. Using the drifter motion patterns driven by two typical ocean waves, the displacement response and electric outputs are observed in the FEA simulations. Conclusions are drawn as follows.

1) The SBCM responds to an ultra-low excitation frequencies in a wide frequency range, which has been verified by the FEA simulations, analytical results and numerical analysis with a close agreement.

2) According to the electric output generated at the preliminary SBCM-based PVEH, the SBCM can be embedded into a drifter as a WEC to harvest energy from ocean waves.

Future work includes FEA simulation of the SBCM under drifter rotational excitations (pitch and roll), experimental integration of the SBCM prototype with the ocean drifter and real sea test, optimization on the electric circuits etc.

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