Multicellular feedback control of a genetic toggle-switch in microbial consortia

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Abstract—We describe a multicellular approach to control a target cell population endowed with a bistable toggle-switch. The idea is to engineer a synthetic microbial consortium consisting of three different cell populations. In such a consortium, two populations, the Togglers, responding to some reference input, can induce the switch of a bistable memory mechanism in a third population, the Targets, so as to activate or deactivate some additional functionalities in the cells. Communication among the three populations is established by orthogonal quorum sensing molecules that are used to close a feedback control loop across the populations. The control design is validated via in-silico experiments in BSim, a realistic agent-based simulator of bacterial populations.

I. INTRODUCTION

The main goal of Synthetic Biology is the design of reliable genetic circuits able to endow living cells with new functionalities [1]. Examples include the development of bacteria able to sense and degrade pollutants (like hydrocarbons or plastic) in the environment [2], or cells that can track and kill cancer cells by releasing drugs at specific locations, limiting dangerous side effects [3].

Biological systems capable of carrying out these complex tasks require the integration of advanced functional components analogous to those of an autonomous robotic systems [4]. Specifically, sensors are needed to perceive stimuli from the environment, actuators to interact with the environment (e.g. production and delivery of desired molecules or drugs), and more importantly, some control logic with a memory mechanism able to make decisions and regulate the cell behavior. However, due to current technological and biological limitations, e.g. metabolic burden and retroactivity, it is hard to implement the entire control system inside a single cell [5].

A promising solution to overcome this problem is to assign the required functionalities to different cell populations such that each of them carries out a specific task [6], [7]. For example, one population can be specialized to sense a certain molecule in the environment and to communicate its presence to the rest of the consortium by secreting signaling molecules in its surroundings. In this way, more complex tasks can be carried out by multicellular systems as the result of the mutual interactions between their components [6].

In this letter we present a novel multicellular feedback control strategy involving a microbial consortium consisting of three cellular populations, in which the activity of one of them is governed by the other two. Specifically, the state of a genetic toggle-switch endowed in one of the populations, the Targets, can be controlled by providing or removing a reference input to the other two, the Togglers, which communicate with the Targets via orthogonal quorum sensing molecules. In this way, it can be possible to toggle additional functionalities in the Targets, as required in a number of applications, e.g. production and secretion of some desired molecule or drug in the environment [3], [8].

The relationship between the three cell populations in the consortium and their molecular signals can be schematically represented as a sequential logic circuit [9] (Fig. 1). The two controller cells sense the concentration in the environment of the reference signal Ref and of the Targets’ output y, which is high (y = 1) only when the Targets are active. The controllers then generate two control signals u₁ and u₂ according to the following logic functions

\[ u_1 = \text{Ref} \text{ AND } (\neg y), \]  
\[ u_2 = (\neg \text{Ref}) \text{ AND } y, \]  

Fig. 1. Representation as a sequential logic circuit of the relationship between the cell populations and their molecular signals. The Target receives ON commands (u₁ = 1) only when Ref = 1 AND y = 0, and OFF commands (u₂ = 1) only when Ref = 0 AND y = 1. In this way, the input signals u₁ and u₂ are equal to 1 only when there is disagreement between Ref and y.
they perceive the presence of a specific reference chemical signal in the environment and the Targets are inactive, while the other controller population, the Deactivators, inhibit the activity of the Targets when they are active and the reference signal is no longer present in the environment. In this way, the Targets are active only when the reference signal is present in the environment.

The crucial challenge we address in this letter is the biological implementation of this novel multicellular control scheme. After proposing a possible realization of all the functions required, we model the three populations and investigate analytically how to engineer the consortium parameters so as to guarantee its desired operation. We then provide in-silico experiments in a realistic agent-based simulator of bacterial populations confirming the viability of the approach.

II. MULTICELLULAR CONTROL SYSTEM

A schematic biological implementation of the multicellular control strategy we propose is illustrated in Fig. 2. The superscripts e, t, a, d are used in the rest of the paper to denote quantities in the environment, Target cells, Activator cells and Deactivator cells, respectively.

Activation and repression of each species is governed by Hill functions with dissociation coefficient $\theta$ and exponent $n$. Moreover, we denote with $\alpha_{X}^{0}$ and $\alpha_{X}$ the basal and maximal expression rates of species $X$, and with $\gamma^{n}$ the degradation rate of a species within a domain $v$.

A. Target population

We assume that the bistable memory regulating the activation of the Target cells is implemented by an inducible genetic toggle-switch [10], [11]. This genetic network consists of two proteins, $X_{1}$ and $X_{2}$, each repressing the expression of the other, so that at steady state only one is fully expressed. Without loss of generality, we assume full expression of $X_{1}$ corresponds to the “active” state of the cell where some desired functionalities are turned on, while full expression of $X_{2}$ corresponds to its inactive state.

We focus here on the problem of toggling the Target population between the two states. Other works in the literature have considered the alternative control problem of stabilizing the toggle-switch about some intermediate expression levels of $X_{1}$ and $X_{2}$, see e.g. [11]–[15]; a problem we do not address in this paper.

The dynamical model of the toggle-switch can be given as

$$\dot{x}_{1} = \frac{\alpha_{x_{1}}^{0}}{1 + (\frac{x_{1}}{\theta})^{n_{x_{1}}}} - \gamma^{n} x_{1} + u_{1} \quad (3)$$

$$\dot{x}_{2} = \frac{\alpha_{x_{2}}^{0}}{1 + (\frac{x_{2}}{\theta})^{n_{x_{2}}}} - \gamma^{n} x_{2} + u_{2} \quad (4)$$

where the state variables $x_{1}$ and $x_{2}$ denote concentrations of molecules $X_{1}$ and $X_{2}$ inside the cell and we assume $u_{1}$ and $u_{2}$ capture the effect of two inputs that can be used to toggle the switch between one state and the other.

We assume that the parameters of the toggle-switch are chosen such that in the absence of external inputs, i.e. $u_{1} = u_{2} = 0$, the system is bistable [16], with well separated equilibria and sufficient transversality of the nullclines [17]. Specifically, system (3)-(4) admits two stable equilibria, $x_{1}^{\text{eq}} = [x_{1}^{+}, x_{2}^{+}]$ and $x_{2}^{\text{eq}} = [x_{1}^{-}, x_{2}^{-}]$, associated to high expression of species $X_{1}$ or $X_{2}$, respectively. We also assume, that there exists some positive value $\hat{u}_{1} (\hat{u}_{2})$ such that, when $u_{1} > \hat{u}_{1}$ ($u_{2} > \hat{u}_{2}$) and $u_{2} = 0$ ($u_{1} = 0$), system (3)-(4) converges to a unique equilibrium point corresponding to high expression of $X_{1}$ ($X_{2}$) and remains therein when the inputs are switched off.

As shown in Fig. 2, we associate each of the inputs of the toggle-switch (3)-(4) in the Targets to the concentration of a quorum sensing molecule coming from the Activator and Deactivator cells. Specifically, we capture the promoting action of the signaling molecule $Q_{u}$ on the expression of $X_{1}$ by setting

$$u_{i} := \beta_{i}, \frac{(q_{t}^{u})^{n_{u_{i}}}}{\theta_{u_{i}}^{n_{u_{i}}} + (q_{t}^{u})^{n_{u_{i}}}} + (Q_{t})^{n_{u_{i}}}, \quad i = 1, 2, \quad (5)$$

where $q_{t}^{u}$ denotes the concentration of molecule $Q_{u}$ inside the Target cell, and $\beta_{i}, \theta_{u_{i}}$, and $n_{u_{i}}$ are the maximal promoter activity, activation and Hill coefficients, respectively.

In our design, Target cells can signal their state to the other cells by means of another, orthogonal, quorum sensing molecule $Q_{y}$ that is produced at rate $f_{y}^{+}$ assumed to be proportional to $X_{1}$ [7], that is

$$f_{y}^{+} := k_{y} x_{1}, \quad k_{y} > 0. \quad (6)$$

Hence, at steady state, when the cell is active, $f_{y}^{\text{ON}} = k_{y} x_{1}$.

B. Toggler populations

The two controller implement the same logic circuits (Fig. 1) and therefore they also share similar biological implementations. However, since the reference molecule $R$ and signaling molecule $Q_{y}$ have inverted roles, the biochemical reactions describing the Activator and Deactivator cells are
in general different. For the sake of brevity, we next describe only the biological implementation of the Deactivator cells in Fig. 2, which is directly taken from [7].

The logic function (2) is realized in the Deactivators by means of an antithetic motif. Specifically, the expression of $Z_1$ is regulated by two independent and competing species, $R$ and $Q_y$. $R$ represses $Z_1$, while $Q_y$ activates $Z_1$ and reacts with it forming the complex $Z_1 : Q_y$. $Q_{u_2}$ is then produced through a synthesis process catalyzed by $Z_2$, which is promoted only by the active compound $Z_1 : Q_y$. As a result, the control signal molecule $Q_{u_2}$ is produced and released only when the concentration of $R$ inside the Deactivator cells is low while that of $Q_y$ is high.

By denoting with $z_1$ and $z_2$ the concentrations of the species $Z_1 : Q_y$ and $Z_2$ in the Deactivators, their dynamics can be written as

$$
\dot{z}_1 = \left( \alpha^0_{z_1,r} + \alpha_{z_1,r} \frac{\theta^{m_{z_1,r}}_{r,z_1}}{\theta^{m_{z_1,q}}_{q,z_1} + (r^0_{m_{z_1}})^{m_{z_1,q}}_{q}} \right) \cdot \left( \alpha^0_{z_1,q} + \alpha_{z_1,q} \frac{\theta^{m_{z_1,q}}_{q,z_1} + (q^0_{m_{z_1}})^{m_{z_1,q}}_{q}}{\theta^{m_{z_1,q}}_{q,z_1} + (q^0_{m_{z_1}})^{m_{z_1,q}}_{q}} \right) - \gamma^d z_1 
$$

(7)

and

$$
\dot{z}_2 = \alpha^0_{z_2} + \alpha_{z_2} \cdot \frac{z_1^{1/2}}{\theta^{m_{z_2}}_{r,z_2} + z_1^{1/2}} - \gamma^d z_2 
$$

(8)

The output signaling molecule $Q_{u_2}$ is produced through a synthesis process catalyzed by $Z_2$, and so at a rate $f^d_{u_2}$ proportional to the concentration of $Z_2$, that is

$$
f^d_{u_2} := k_{u_2} z_2, \quad k_{u_2} > 0. 
$$

(9)

Moreover, the substrates required to synthesize $Q_{u_2}$ are assumed to be in excess and therefore this process does not directly affect $Z_2$ [7].

Similarly, another antithetic motif is embedded in the Activators so that by denoting with $w_1$ and $w_2$ the concentrations of the species $W_1 : R$ and $W_2$ therein, their dynamics can be written as

$$
\dot{w}_1 = \left( \alpha^0_{w_1,q} + \alpha_{w_1,q} \frac{\theta^{m_{w_1,q}}_{q,w_1}}{\theta^{m_{w_1,q}}_{q,w_1} + (q^0)^{m_{w_1,q}}_{q}} \right) \cdot \left( \alpha^0_{w_1,r} + \alpha_{w_1,r} \frac{(r^0)^{m_{w_1,r}}_{r}}{\theta^{m_{w_1,r}}_{r,w_1} + (r^0)^{m_{w_1,r}}_{r}} \right) - \gamma^a w_1 
$$

(10)

and

$$
\dot{w}_2 = \alpha^0_{w_2} + \alpha_{w_2} \cdot \frac{w_1^{1/2}}{\theta^{m_{w_2}}_{w_1} + w_1^{1/2}} - \gamma^a w_2 
$$

(11)

The Activators will then generate a quorum sensing molecule $Q_{u_1}$ at a rate $f^a_{u_1}$ proportional to the concentration of $W_2$, that is

$$
f^a_{u_1} := k_{u_1} w_2, \quad k_{u_1} > 0. 
$$

(12)

C. Intercellular communication

The intercellular communication between the three populations is realized by means of three pairwise orthogonal quorum sensing molecules. Namely, $Q_{u_1}$, $Q_{u_2}$ and $Q_y$, which are produced by Activators, Deactivators and Targets, respectively. For the sake of brevity, in what follows we use the placeholder superscript $j$ to denote concentrations of signaling molecules in a generic cell type, where $j = a$ for Activators, $j = d$ for Deactivators and $j = t$ for Targets. The quorum sensing molecules and the reference signal molecule $R$ diffuse across the cell membrane of the genetic cell of type $j$ with diffusion rate $\eta^j$. The evolution of the concentrations of the signaling molecules inside the genetic cell of type $j$ can then be given as

$$
\dot{r}^j = \eta^j (r^e - r^j) - \gamma^j r^j 
$$

(13)

$$
\dot{q}^j_{u_1} = f^j_{u_1} + \eta^j (q^j_{u_2} - q^j_{u_1}) - \gamma^j q^j_{u_1} 
$$

(14)

$$
\dot{q}^j_{u_2} = f^j_{u_2} + \eta^j (q^j_{u_2} - q^j_{u_1}) - \gamma^j q^j_{u_2} 
$$

(15)

$$
\dot{q}^j_y = f^j_y + \eta^j (q^j_y - q^j_{u_1}) - \gamma^j q^j_y 
$$

(16)

where the production functions $f^a_{u_1}$, $f^d_{u_2}$ and $f^t_y$ are defined in (12), (9) and (6), and $f^d_{u_1} = f^d_{u_2} = f^a_{u_1} = 0$, $f^d_{u_2} = f^a_{u_2} = 0$, and $f^t_y = f^d_y = 0$.

The concentrations of the reference signal molecule and of the quorum sensing molecules secreted by the three cell populations in the environment can be described by the following set of ODEs:

$$
\dot{r}^e = r_{in} (t) + \eta^a \Delta q^a_{u_2} + \eta^d \Delta q^d_{u_2} + \eta^t \Delta q^t_{u_2} - \gamma^e r^e 
$$

(17)

$$
\dot{q}^e_{u_1} = \eta^a \Delta q^a_{u_1} + \eta^d \Delta q^d_{u_1} + \eta^t \Delta q^t_{u_1} - \gamma^e q^e_{u_1} 
$$

(18)

$$
\dot{q}^e_{u_2} = \eta^a \Delta q^a_{u_2} + \eta^d \Delta q^d_{u_2} + \eta^t \Delta q^t_{u_2} - \gamma^e q^e_{u_2} 
$$

(19)

$$
\dot{q}^e_y = \eta^a \Delta q^a_y + \eta^d \Delta q^d_y + \eta^t \Delta q^t_y - \gamma^e q^e_y 
$$

(20)

where $\Delta q^a_{u_1}, \Delta q^a_{u_2}, \Delta q^a_y$ are defined in (17), and similarly are defined $\Delta q^d_{u_1}, \Delta q^d_{u_2}, \Delta q^d_y$, and the function $r_{in} (t)$ represents the concentration of the reference signal provided externally to influence the cell behavior. In the above equations, $\gamma^e$ and $\gamma^j$ are the degradation rate in the environment and in the generic cell of type $j$ (assumed to be the same for all species for the sake of simplicity).

III. CONSORTIUM ENGINEERING

In this section, we show that, for the control loop to be effectively closed across the three populations, the parameters characterizing each of the cell populations and the intercellular communication channels must fulfill a set of necessary conditions.

In particular, a set of constraints on the parameters can be derived by analyzing the model equations at steady state, assuming that spatial effects are negligible and the number of cells in the three populations are equally balanced, which implies $\eta^j = \eta$ for all $j \in \{a, d, t\}$. These assumptions will then be relaxed in the next section where in-silico experiments are carried out also in the presence of cell-to-cell variability and spatio-temporal effects.

a) Feedback loop pathways: We start by making the realistic assumption that $\eta \gg \gamma^j$, $j \in \{a, d, t\}$, that is, the signaling molecules diffuse through the cellular membrane faster then they are degraded. Hence, when the reference signal fed to the environment is constant and large enough (i.e. $r_{in} (t) = r^{ON}_{in} = \text{const}$.) and the Target cells are not active (i.e. $Q_y$ is not expressed), it is easy to verify that at steady state the concentrations of the signaling molecules $R$
and \( Q_{u_1} \) reach the same value in every cells, that is, for all \( j \in \{ a, d, t \} \) we have
\[
\hat{r}^a = r_{in}^{ON} / \Gamma, \quad \hat{q}_{u_1} = k_{u_1} \bar{w}_2 / \Gamma, \quad (21)
\]
where \( \Gamma := \gamma^r + \gamma^l + \gamma^a + \gamma^d \), and \( \bar{w}_2 \) denotes the steady-state value of \( w_2 \) when it is fully expressed.

Analogously, for \( Q_y \) and \( Q_{u_2} \), when the reference signal \( r_{in} \) is absent (i.e. \( r_{in}(t) = r_{in}^{OFF} = \text{const.} \)) and the Target cells are initially active (i.e. \( Q_y \) is expressed), at steady state for all \( j \in \{ a, d, t \} \) we have
\[
\hat{q}_{u_2} = k_{u_2} \bar{z}_2 / \Gamma, \quad (22)
\]
where, similarly, \( \bar{x}_1 \) and \( \bar{z}_2 \) denotes the steady-state values of \( x_1 \) and \( z_2 \) when they are fully expressed.

b) Toggler cells: To guarantee that the Activators and Deactivators implement at steady state the logic functions (1)-(2), it is necessary that only the Activators produce their control signal when the concentrations in the cells of the reference molecule \( R \) and \( Q_y \) are sufficiently high and low, respectively. Therefore, it must hold that
\[
\theta_{r,u_1} \ll \hat{r}^a \quad \text{and} \quad \theta_{r,z_1} \ll \hat{r}^d, \quad (23)
\]
Similarly, when the concentrations of \( R \) and \( Q_y \) are sufficiently low and high, respectively, then, in order that only the Deactivators generate their control signal, it must hold that
\[
\theta_{q,u_1} \ll \hat{q}_y^a \quad \text{and} \quad \theta_{q,z_1} \ll \hat{q}_y^d. \quad (24)
\]

c) Target cells: In order for the signaling molecules coming from the controllers to toggle the switch within the Targets, the input functions (5) must be such that
\[
\beta_i > 2 \hat{u}_i, \quad i = 1, 2, \quad (25)
\]
and the concentrations of the quorum sensing molecules within the Targets must be sufficiently high
\[
\theta_{u_i} \ll \hat{q}_{u_i}, \quad i = 1, 2, \quad (26)
\]
so that the control input is strong enough to trigger the transition from one state to the other and render the toggle-switch monostable.

d) Parameters’ constraints: Substituting equations (21)-(22) in conditions (23), (24) and (26), we obtain that, at steady state, the Toggler can activate or deactivate the Targets in response to the presence or absence of the external reference signal \( r_{in}(t) \) (if the system parameters satisfy (25) and the following conditions are satisfied:
\[
\Gamma \theta_{r,w_1} \ll \gamma^ON, \quad \Gamma \theta_{r,z_1} \ll \gamma^ON, \quad (27)
\]
\[
\Gamma \theta_{q,w_1} \ll k_y \bar{x}_1, \quad \Gamma \theta_{q,z_1} \ll k_y \bar{x}_1, \quad (28)
\]
\[
\Gamma \theta_{u_1} \ll k_{u_1} \bar{w}_2, \quad \Gamma \theta_{u_2} \ll k_{u_2} \bar{z}_2. \quad (29)
\]
Using similar arguments, it is also possible to obtain lower bounds for the \( \theta_s \), yielding the parameter constraints
\[
r_{in}^{OFF} \ll \Gamma \theta_{r,w_1} \ll \gamma^ON, \quad r_{in}^{OFF} \ll \Gamma \theta_{r,z_1} \ll \gamma^ON, \quad (30)
\]
\[
k_y \bar{z}_1 \ll \Gamma \theta_{q,w_1} \ll k_y \bar{x}_1, \quad k_y \bar{z}_1 \ll \Gamma \theta_{q,z_1} \ll k_y \bar{x}_1, \quad (31)
\]
\[
k_{u_1} \bar{w}_2 \ll \Gamma \theta_{u_1} \ll k_{u_1} \bar{w}_2, \quad k_{u_2} \bar{z}_2 \ll \Gamma \theta_{u_2} \ll k_{u_2} \bar{z}_2. \quad (32)
\]
where \( \bar{x}_1, \bar{w}_2 \) and \( \bar{z}_2 \) denote the steady-state values of the corresponding species when they are completely repressed.

The previous conditions represent a set of necessary conditions for the consortium to exhibit its desired multicellular control functions.

Remark. Conditions (30)-(32) depend on steady-state values of \( x_1, w_2 \) and \( z_2 \), which in general would need to be estimated in-silico or quantified experimentally. However, at the price of having more relaxed bounds, conditions not depending on these values can be obtained by approximating Hill functions with step functions (i.e. by letting their coefficient \( n \to \infty \) yielding \( \bar{x}_1 = \alpha_{x_1}^{\alpha} / \gamma^a \), \( \bar{w}_2 = \alpha_{w_2}^{\alpha} / \gamma^a \), \( \bar{z}_2 = \alpha_{z_2}^{\alpha} / \gamma^d \), \( \bar{x}_1 = \alpha_{x_1}^{\alpha} + \alpha_{z_1}^{\alpha} / \gamma^a \), \( \bar{w} = \alpha_{w_2}^{\alpha} + \alpha_{z_2}^{\alpha} / \gamma^a \) and \( \bar{z}_2 = \alpha_{z_2}^{\alpha} + \alpha_{z_2}^{\alpha} / \gamma^d \).

IV. IN-SILICO EXPERIMENTS
A. Agent-based simulations

To validate the effectiveness of our multicellular control design, we implemented a set of in-silico experiments via BSim, a realistic agent-based simulator of bacterial populations [18], [19]. In so doing, we modeled a microfluidics
its robustness to perturbations in the parameters. consortium due to poor intercellular communication, and (ii) imbalances between populations affect the operation of the illustrative case of no population growth, to evaluate (i) how B. Robustness to parameter variations be done by means of other methods, such as in [20].) The in-vivo implementation of the consortium we propose is currently beyond what is technologically possible but is not unrealistic given that each of the controller population is similar to the comparator implemented experimentally in [21] and the antithetic feedback controller recently presented in [22]. Also, orthogonal communication channels able to set in place the required interaction between the three populations are available and have been tested in [23]. Due to different growth rates of the strains involved, a crucial open problem of toggling a memory mechanism in a target cell population. The approach we presented consists in engineering a synthetic microbial consortium of three populations, where two of them act as controllers able to induce activation or deactivation of an inducible genetic switch in the third population, in response to some external reference input. After modeling all the essential components of our design, we discussed some feasibility issues before presenting a careful in-silico investigation of the proposed approach and its robustness to changes in the ratios between the cell populations in the consortium and to perturbation in the parameter values. Our results confirm that the solution we propose is theoretically viable.

Finally, we tested robustness of our design when all parameters of Targets, Activators and Deactivators are perturbed from their nominal values. As shown in Fig. 6, even in the presence of a consistent parameter mismatch (CV = 0.2), the Togglers are able to activate or deactivate a large fraction of the Targets’ population with the Activators showing better performance of the Deactivators in the parameters’ region we selected.

V. DISCUSSION AND CONCLUSIONS

We have presented a multicellular control solution to the problem of toggling a memory mechanism in a target cell population. The total cell population in the consortium is set to $N = 50$. For each cell type $n_j = N_j/N$, $j = \{t, a, d\}$, is its relative ratio within the consortium, and such that $n_t + n_a + n_d = 1$.

Table I. The nominal values of the parameters used in simulations are reported in Table I. They have been chosen similarly as those reported in [7], [15], and satisfying conditions (25) and (30)-(32). Cell-to-cell variability was modeled by assigning a different set of parameters to daughter cells when they split from their mothers. Specifically, each of their parameters, say $\mu$, was drawn independently from a normal distribution centered at its nominal value $\bar{\mu}$ and with coefficient of variation $CV = 10\%$.

Figs. 3 and 4 show the results of a typical in-silico experiment where the Toggler cells (depicted in red and green) successfully flip the Target cells from their active state (depicted in blue) to their inactive state (depicted in black) and vice versa, following changes in the reference signal $r_{in}$. The amplitude and the duration of the reference pulse $r_{in}$ have been heuristically set to 43 $\mu$M and 1140 min, respectively. (A more accurate tuning of the pulse can be done by means of other methods, such as in [20].)

B. Robustness to parameter variations

Next, we performed numerical analysis in Matlab, in the illustrative case of no population growth, to evaluate (i) how imbalances between populations affect the operation of the consortium due to poor intercellular communication, and (ii) its robustness to perturbations in the parameters.

Fig. 5 shows the values at steady state of the ratio $x_{1}/x_{2}$ when the Targets are switched OFF (bottom-left panel) and ON (top-right panel), respectively, following the application of the corresponding reference signal $r_{in}$, as the ratios of the cell populations in the consortium are being varied. In this scenario, we see that for a wide range of population densities (black region for Deactivators in bottom-left panel, non-black region for Activators in top-right panel of Fig. 5), the Togglers are effectively able to flip the state of Targets.

Finally, we tested robustness of our design when all parameters of Targets, Activators and Deactivators are perturbed from their nominal values. As shown in Fig. 6, even in the presence of a consistent parameter mismatch (CV = 0.2), the Togglers are able to activate or deactivate a large fraction of the Targets’ population with the Activators showing better performance of the Deactivators in the parameters’ region we selected.
We wish to emphasize that a simpler implementation of our design can be obtained by considering a consortium comprising the Target cells and only one population of Activators (or Deactivators), so that the modular control strategy is still able to activate initially inactive Targets (or deactivate initially active ones, respectively). With this respect our modular multicellular design is resilient as some functions of the consortium will still be present if one controller population is lost (e.g., becomes extinct or washed out), allowing also for more flexible deployment of the strains in the environment.

A possible future application of the design we propose could be its use for the controlled delivery of active molecules or drugs synthesized by the Targets when they are active. Indeed, the consortium is designed so that the drug or active molecule of interest is only produced and secreted when a specific reference chemical signal is perceived by the controller cells with production being stopped when such a reference is removed and the Targets are deactivated. By using a cancer biomarker as the reference signal, the Togglers could then be used to activate the Targets to deliver chemotherapy drugs in situ only when the biomarker is detected in the tissue, providing a multicellular feedback control alternative to the open-loop design proposed in [8]. Also, if the reference signal was linked to the presence of some pollutant in the environment, the controlled activation of the Targets cells could be used to synthesize active molecules for bioremediation when and where they are needed.

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