

A Simple Nonlinear Observer for State and Unknown Input Estimation: DC Motor Applications

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Abstract—The contribution of this work is to propose a method based on a simple nonlinear observer with an easy-to-compute observer gain, in order to achieve both state and unknown input estimation. Since the structure of the original model of the process does not require any transformation, the nonlinear dynamics are preserved. This allows an accurate estimation of the states and the unknown inputs or faults. Two particular cases involving DC motors are illustrated in simulation and an experiment using a permanent magnet DC motor is presented.

Index Terms—Nonlinear observer, unknown input, fault, DC motor.

I. INTRODUCTION

From the point of view of automatic control, many problems involving DC motors must be solved in the design stage before prototyping (i.e. modeling [1], control design [2], state/parameter estimation [3]) or at the operation stage (i.e. fault diagnosis [4], fault tolerant control [5], prognosis [6]). When a DC motor operates, it is subject to different operating conditions (predictable or not) caused by exogenous variables, disturbances, noise or faults, which can be induced by many causes such as vibrations, friction, overload, and voltage variations. Most of these conditions or phenomena unrelated to the ideal behavior are collectively known as unknown inputs (UI) [7]–[9].

Typically an unknown input is an unmeasured signal affecting a dynamical system. Many times, the knowledge of these signals is crucial to predict, compensate or to monitor the consequences of them over the system dynamics. Several authors have shown that the observer-based approaches are the most successful methods used to estimate unknown inputs, e.g., [10]–[12]. For instance, the authors in [10] use a high-order sliding mode observers for leak estimation in pipelines where pressure and input-output flow rate measures are available. The case of UI observers for linear parameter variant (LPV) systems is recently treated in [11], where the computation of the observer gains via linear matrix inequalities (LMI's) is not a trivial task. The authors in [12] propose a disturbance observer-based controller for a direct-drive servo control system. In [5] and [13] UI observers are proposed for fault and state estimation for Takagi-Sugeno (T-S) fuzzy systems. In these cases, the observer design

requires to transform the original nonlinear representation of the system into a T-S representation.

The contribution of this work is focused on proposing a method based on a simple nonlinear observer for state and unknown input estimation in DC motor applications (Section III). Two particular cases (Section II) for state and UI estimation involving DC motors are illustrated in simulation (Section IV). In order to demonstrate the practical applicability of the proposed approach, an experiment using a permanent magnet DC motor is presented in Section V.

II. PROBLEM STATEMENT

Two problems associated with unknown input estimation in DC motors are presented. For this end, two different mathematical models are selected from literature and used in this study: (1) a DC motor controlling an inverted pendulum [13] and (2) a permanent magnet DC motor [14].

1) *Case 1. DC motor controlling an inverted pendulum:* Consider the model of a DC motor controlling an inverted pendulum via gear train [13].

$$\begin{aligned}\dot{x}_1 &= x_2 \\ \dot{x}_2 &= \frac{g}{l} \sin(x_1) + \frac{NK_m}{ml^2} x_3 \\ \dot{x}_3 &= -\frac{K_b N}{L_a} x_2 - \frac{R_a}{L_a} x_3 + \frac{1}{L_a} u\end{aligned}\quad (1)$$

where $x_1 = \varphi_p$ is the motor shaft position, $x_2 = w_p$ is the motor shaft velocity, $x_3 = I_a$ is the armature current, u is the voltage input. $K_m = 0.1 \text{ Nm/A}$ is the motor torque constant, $K_b = 0.1 \text{ Vs/rad}$ is the back emf, $g = 9.8 \text{ m/s}^2$ is the gravity, $N = 10$ is the gear ratio, $l = 1 \text{ m}$ is the shaft length, $m = 1 \text{ kg}$ is the mass, $R_a = 1 \Omega$ is the armature resistance and $L_a = 0.1 \text{ H}$ is the armature inductance.

Assume that there is an unknown additive fault Δu in the input of system (1). In such a case, the input u is replaced by $u + \Delta u$, where Δu can be an undesired variation of the voltage input which needs to be estimated in order to compensate it. Besides, assume that the motor shaft velocity w_p and the armature current I_a are not measured.

Assumption 1. The voltage input variation Δu is unknown.

Assumption 2. The shaft position $x_1 = \varphi_p$ is measurable.

Assumption 1 implies that although the process input u is assumed to be known, actuators that provide this signal can be affected by faults Δu , i.e. non measurable signals. Assumption

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2 implies that x_1 is the system output, i.e. $y = x_1$. Then, system (1) can be represented as:

$$\begin{aligned}\dot{x} &= Ax + g(y, u) + F\theta \\ y &= Cx\end{aligned}\quad (2)$$

where $x = (x_1 \ x_2 \ x_3)^T = (\varphi_p \ w_p \ I_a)^T$, $y = x_1 = \varphi_p$, $\theta = \Delta u$ and

$$A = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & \frac{NK_m}{ml^2} \\ 0 & -\frac{K_b N}{L_a} & -\frac{R_a}{L_a} \end{pmatrix}, \quad g(y, u) = \begin{pmatrix} 0 \\ \frac{g}{l} \sin x_1 \\ \frac{1}{L_a} u \end{pmatrix}, \quad (3)$$

$$C = \begin{pmatrix} 1 & 0 & 0 \end{pmatrix}, \quad F = \begin{pmatrix} 0 & 0 & \frac{1}{L_a} \end{pmatrix}^T. \quad (4)$$

The authors in [13] propose a Takagi-Sugeno observer in order to estimate the states and faults simultaneously. However, the computation of the gains is not a trivial task. In the following sections, an alternative method for state and unknown input estimation is proposed.

2) *Case 2. Permanent magnet DC motor:* Consider the following model of a permanent magnet DC motor [14].

$$\begin{aligned}\dot{i}_a &= -\frac{R_a}{L}i_a - \frac{K_e}{L}v_m + \frac{1}{L}u \\ \dot{v}_m &= \frac{K_T}{J_1}i_a - \left(\frac{f_r - f_p v_m}{J_1}\right)v_m - \frac{T_0 - T_2}{J_1}\end{aligned}\quad (5)$$

where i_a is the armature current, v_m is the rotational speed (rpm), u is the armature voltage (the input of the system), T_0 and T_2 are respectively the no-load and load torque. $R_a = 1\Omega$ is the armature resistance, $L = 0.9H$ is the inductance, $K_e = 13.5 \times 10^{-3}V/rpm$ is the back-emf coefficient, $K_T = 0.1Nm/A$ is the torque-current coefficient, $J_1 = 66.9 \times 10^{-4}Nm s$ is the normalized inertial moment, $f_r = 1.4 \times 10^{-4}Nm/rpm$ is the friction coefficient (lubrication), $f_p = 7.5 \times 10^{-8}Nm/rpm^2$ is the friction coefficient (aerodynamics) and $T_2 = 22.9 \times 10^{-2}Nm$ is the load torque.

Assumption 3. The rotational speed v_m and the armature voltage u are measurable.

Assumption 3 implies that v_m and u are two known signals, i.e. they do not need to be estimated. Besides, v_m is the measured output of the system, i.e. $y = v_m$. It should be noted that the armature current i_a and the no-load torque T_0 are unknown and they need to be estimated. Then, system (5) has the form of system (2), where $x = (x_1 \ x_2)^T = (i_a \ v_m)^T$, $y = x_2 = v_m$, $\theta = T_0$ and

$$A = \begin{pmatrix} -\frac{R_a}{L} & 0 \\ \frac{K_T}{J_1} & 0 \end{pmatrix}, \quad C = \begin{pmatrix} 0 & 1 \end{pmatrix}, \quad F = \begin{pmatrix} 0 \\ -\frac{1}{J_1} \end{pmatrix}, \quad (6)$$

$$g(y, u) = \begin{pmatrix} -\frac{K_e}{L}v_m + \frac{1}{L}u \\ -\left(\frac{f_r - f_p v_m}{J_1}\right)v_m + \frac{T_2}{J_1} \end{pmatrix}. \quad (7)$$

III. THE PROPOSED OBSERVER

Consider a nonlinear system having the following form:

$$\begin{aligned}\dot{x} &= Ax + g(y, u) + F\theta \\ y &= Cx\end{aligned}\quad (8)$$

where $x \in \mathbb{R}^n$ is the state of the system, $g(y, u) \in \mathbb{R}^n$ is a vector field depending on the system input u and the output y . A , F and C are constant matrices of appropriate dimensions and $\theta \in \mathbb{R}^d$ is an unknown constant or slow-varying input, i.e. $\dot{\theta} \approx 0$.

Assumption 4. The following rank conditions are satisfied

- $\text{rank}(F) = d$.

- $\text{rank}(O) = n$, where $O = \begin{pmatrix} C \\ CA \\ \vdots \\ CA^{n-1} \end{pmatrix}$

The first rank condition $\text{rank}(F) = d$ in Assumption 4 implies that vector $\theta \in \mathbb{R}^d$ can be estimated. On the other hand, $\text{rank}(O) = n$, implies that system (8) is observable.

Theorem 1. Assume that Assumption 4 holds. A nonlinear Luenberger-like observer for state and unknown input estimation for nonlinear systems having the form in Eq. (2) is:

$$\begin{aligned}\dot{\hat{x}} &= A\hat{x} + g(y, u) + F\hat{\theta} + K_1(y - \hat{y}) \\ \dot{\hat{\theta}} &= K_2(y - \hat{y}) \\ \hat{y} &= C\hat{x}\end{aligned}\quad (9)$$

if there exist two matrices K_1 and K_2 such that $A_s = \begin{pmatrix} A - K_1 C & F \\ -K_2 C & 0 \end{pmatrix}$ is a stability matrix.

Proof. Define the estimation errors $e_x = x - \hat{x}$ and $e_\theta = \theta - \hat{\theta}$. The time derivative of e_x and e_θ are, respectively:

$$\dot{e}_x = \dot{x} - \dot{\hat{x}} = (A - K_1 C)e_x + F e_\theta \quad (10)$$

$$\dot{e}_\theta = \dot{\theta} - \dot{\hat{\theta}} = -K_2 C e_x \quad (11)$$

Eqs. (10) and (11) can be written in a compact form as

$$\dot{e} = A_s e \quad (12)$$

where:

$$A_s = \begin{pmatrix} A - K_1 C & F \\ -K_2 C & 0 \end{pmatrix} \quad (13)$$

and $e = (e_x \ e_\theta)$. If K_1 and K_2 are selected in such a way that A_s is a stable matrix, then system (12) is stable, i.e. the observer converges. \square

Matrix (13) can be rewritten as:

$$A_s = (A - KC) \quad (14)$$

where

$$A = \begin{pmatrix} A & F \\ 0 & 0 \end{pmatrix} \quad K = \begin{pmatrix} K_1 \\ K_2 \end{pmatrix} \quad C = \begin{pmatrix} C & 0 \end{pmatrix}$$

Eq. (14) can easily be solved to compute the observer gain vector K by any pole placement algorithm. Asymptotic convergence of the observer, i.e. $\lim_{t \rightarrow \infty} e = 0$ is guaranteed if the eigenvalues of matrix A_s have positive real part, where e is the estimation error in Eq. (12).

IV. OBSERVER DESIGN AND SIMULATION RESULTS

In this section, the proposed observer in Section III is used for state and UI estimation of the processes described in Section II.

1) *Case 1. DC motor controlling an inverted pendulum:* Consider the system given in Eq. (2).

Remark 1. It should be noted that $\theta \in \mathbb{R}^1$ and $x \in \mathbb{R}^3$, then $d = 1$ and $n = 3$. In consequence Assumption 4 is verified, i.e. $\text{rank}(F) = 1$, $\text{rank}(O) = 3$, where

$$O = \begin{pmatrix} C \\ CA \\ CA^2 \end{pmatrix}.$$

Then, an observer having the form (9) is designed to estimate the unmeasured states and the unknown input Δu :

$$\begin{aligned} \dot{\hat{x}} &= \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & \frac{NK_m}{ml^2} \\ 0 & -\frac{K_b N}{L_a} & -\frac{R_a}{L_a} \end{pmatrix} \hat{x} + \begin{pmatrix} 0 \\ \frac{g}{l} \sin x_1 \\ \frac{1}{L_a} u \end{pmatrix} \\ &+ \begin{pmatrix} 0 \\ 0 \\ \frac{1}{L_a} \end{pmatrix} \hat{\theta} + K_1(y - \hat{y}) \\ \dot{\hat{\theta}} &= K_2(y - \hat{y}) \\ \hat{y} &= C\hat{x} = \hat{\varphi}_p \end{aligned} \quad (15)$$

where matrices K_1 and K_2 are computed by pole placement of the stability matrix A_s given in Eq. (13).

A numerical simulation is carried out in MATLAB[®] to show the performance of the observer. If the eigenvalues of matrix A_s are located at $\lambda_1 = 2.2$, $\lambda_2 = 2.8$, $\lambda_3 = 2.9$ and $\lambda_4 = 4$, then $K_1 = (1.90 \quad 23.26 \quad -151.09)$, $K_2 = 7.14$. The initial conditions of the model and the observer are: $x^0 = (\varphi_p^0 \ w_p^0 \ I_a^0)^T = (0.01 \ 0 \ 0)^T$, $\hat{x}^0 = (\hat{\varphi}_p^0 \ \hat{w}_p^0 \ \hat{I}_a^0)^T = (0.065 \ 0.215 \ 0.12)^T$ and $\hat{\theta}^0 = 0$. The input voltage $u = 1.5 \text{ V}$. Eqs. (5) and (16) are integrated using a Runge-Kutta first order method (Euler) with an integration step $T_s = 0.05 \text{ s}$. Δu is simulated as follows:

$$\theta = \Delta u = \begin{cases} 0 \text{ V}, & 0 \leq t < 35 \text{ s} \\ 0.5 \text{ V}, & 35 \leq t < 75 \text{ s} \\ 0.8 \text{ V}, & 75 \leq t \end{cases}$$

As displayed in Fig. 1 the estimated states $\hat{x}_2 = \hat{w}_p$ and $\hat{x}_3 = \hat{I}_a$ (dotted lines) asymptotically converge to the corresponding simulated values $x_2 = w_p$ and $x_3 = I_a$ (solid lines), despite the increments in the input Δu (see Fig. 2) at $t = 35 \text{ s}$ and $t = 75 \text{ s}$. The motor shaft position $x_1 = \varphi_p$ is not displayed because it is the measured variable and it does not need to be estimated. Fast convergence for state x_2 can be appreciated, whereas a convergence time of about 5 s is required to estimate state x_3 after each voltage increment in Δu . Convergence time can be modified/improved by selecting different stable eigenvalues of matrix A_s . On the other hand, the estimation of $\Delta \hat{u}$ is depicted in Fig. 2 (dotted line). As expected, the observer asymptotically converges to the simulated unknown input Δu (solid line).

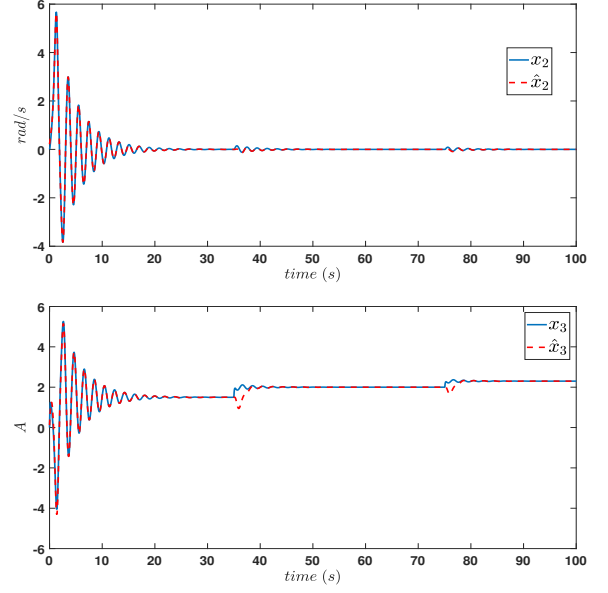


Fig. 1. Estimation of the states φ_p , w_p and I_a in Case 1.

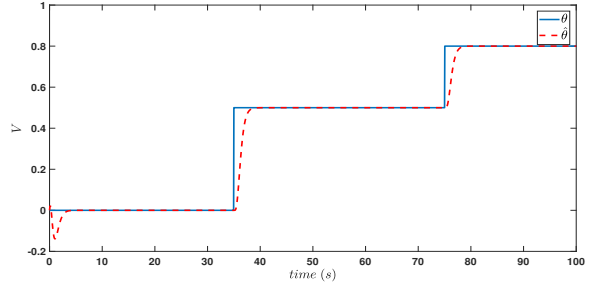


Fig. 2. Estimation of the UI $\theta = \Delta u$ in Case 1.

2) *Case 2. Permanent magnet DC motor:* Consider the system given in Eq. (2) and described by matrices given in (6)-(7).

Remark 2. It should be noted that $\theta \in \mathbb{R}^1$ and $x \in \mathbb{R}^2$, then $d = 1$ and $n = 2$. In consequence Assumption 4 is verified, i.e. $\text{rank}(F) = 1$, $\text{rank}(O) = 2$, where $O = \begin{pmatrix} C \\ CA \end{pmatrix}$.

By considering Remark 2, an observer having the form of system (9) can be designed to estimate the unmeasured state i_a and the unknown input T_0 as follows:

$$\begin{aligned} \dot{\hat{x}} &= \begin{pmatrix} -\frac{R_a}{L} & 0 \\ \frac{K_T}{J_1} & 0 \end{pmatrix} \hat{x} + \begin{pmatrix} -\frac{K_e}{L} y + \frac{1}{L} u \\ -\left(\frac{f_r - f_{py}}{J_1}\right) y + \frac{T_2}{J_1} \end{pmatrix} \\ &+ \begin{pmatrix} 0 \\ -\frac{1}{J_1} \end{pmatrix} \hat{\theta} + K_1(y - \hat{y}) \\ \dot{\hat{\theta}} &= K_2(y - \hat{y}) \\ \hat{y} &= C\hat{x} \end{aligned} \quad (16)$$

where the observer gains K_1 and K_2 are constant matrices of

appropriate dimensions. These matrices are easily computed by pole placement of the stability matrix A_s given in Eq. (13).

A numerical simulation is carried out in MATLAB[®] in order to show the observer performance for state and unknown input estimation, i.e. the armature current i_a and the no-load torque T_0 . The process model (5) and the observer (16) are simulated using the parameter values given in section II. If the eigenvalues of matrix A_s in Eq. (13) are required to be located at $\lambda_1 = 0.41$, $\lambda_2 = 0.42$ and $\lambda_3 = 0.40$, then the observer gains are: $K_1 = (0.027 \ 0.030)$, $K_2 = -3.84 \times 10^{-4}$. The initial conditions are $x^0 = (i_a^0 \ v_m^0)^T = (4 \ 0.02)^T$, $\hat{x}^0 = (\hat{i}_a^0 \ \hat{v}_m^0)^T = (2 \ 0.10)^T$ and $\hat{\theta}^0 = 0.04$. The input voltage $u = 10 \text{ V}$. Integration of Eqs. (5) and (16) are performed using a Runge-Kutta first order method (Euler) with an integration step of 0.01 s . Two step changes of the no-load torque T_0 are considered as follows:

$$T_0 = \begin{cases} 0.023 \text{ Nm}, & 0 \text{ s} \leq t < 50 \text{ s} \\ 0.040 \text{ Nm}, & 50 \text{ s} \leq t < 100 \text{ s} \\ 0.050 \text{ Nm}, & 100 \text{ s} \leq t \end{cases}$$

Simulation results are depicted in Figs. 3-4. In Fig. 3, it can be appreciated that the estimated current \hat{i}_a (dotted lines) asymptotically converges to the simulated process variable i_a (solid line). The rotational speed $x_2 = v_m$ is not displayed because it is the measured variable and it does not need to be estimated. Besides, the estimated no-load torque $\hat{\theta} = \hat{T}_0$ (dotted line in Fig. 4) converges even if the simulated value $\theta = T_0$ (solid line in Fig. 4) undergoes significant step changes.

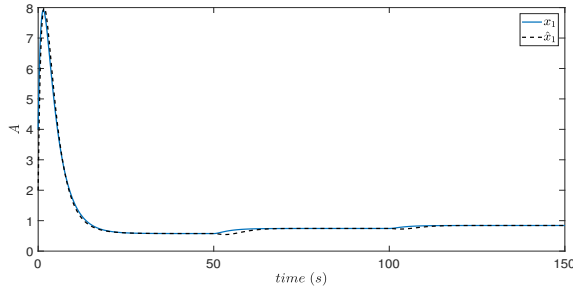


Fig. 3. Estimation of $x_1 = i_a$ in Case 2.

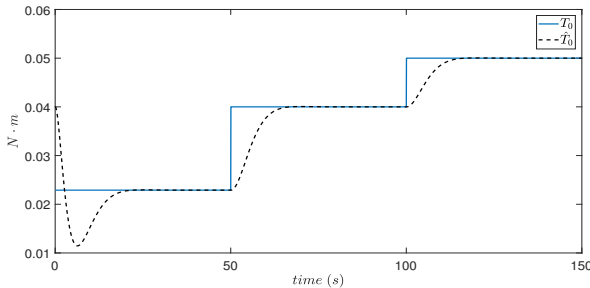


Fig. 4. Estimation of the unknown input $\theta = T_0$ in Case 2.

V. EXPERIMENTAL RESULTS

Several experiments were carried out in a laboratory prototype for estimation of the armature current i_a and the no-load torque T_0 . A typical operation is presented in this section.

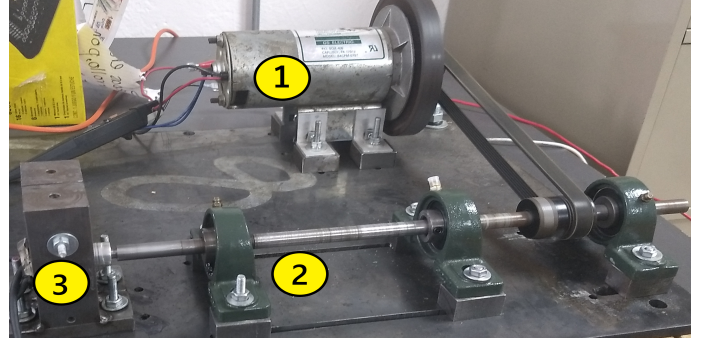


Fig. 5. Laboratory prototype. DC motor connected to a bearing train.

The prototype consists of a DC motor (labeled as 1 in Fig. 5) coupled to a bearing train (labeled as 2 in Fig. 5). The physical parameters according to the employed DC motor are given in Section II, Case 2. These parameters were obtained by direct physical measurements, or they were approximately deduced and verified through laboratory experiments.

The rotational speed of the shaft v_m was measured by coupling a 1000 pulses per revolution incremental encoder (Koyo TRD-S1000-VD, labeled as 3 in Fig. 5). The frequency signal provided by this encoder was acquired and treated by a NI myRIO-1900 card with a sampling time $T_s = 1 \mu\text{s}$ to deliver a proportional signal to the speed of the motor in r.p.m. The voltage input, provided by a Magna-Power programmable DC power supply was constant at $u = 15 \text{ V}$.

Assume (as in the previous simulation) that the armature current i_a is not measured and the no-load torque $\theta = T_0$ is unknown. Then, the implemented observer has the form of system (16). The observer gains K_1 and K_2 are

$$K_1 = \begin{bmatrix} 0.02747 \\ 0.33446 \times 10^{-4} \end{bmatrix} \quad K_2 = -3.83967 \times 10^{-4}$$

By using these gains, the observer stability matrix A_s , defined in Eq. (13), has suitable eigenvalues $\lambda_1 = -0.63$ and $\lambda_{2,3} = -0.28 \pm 0.17i$, ensuring an adequate observer convergence. The initial conditions of the observer are $\hat{x}^0 = [1.4 \ 700]^T$, $\theta^0 = \hat{T}_0^0 = 0.23$.

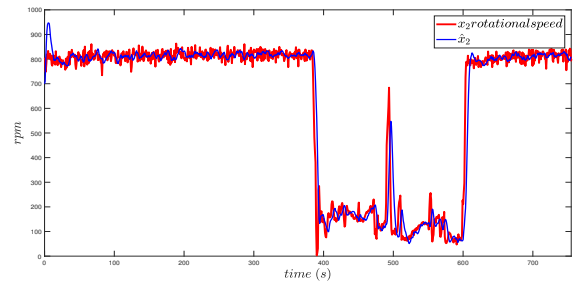


Fig. 6. Measurement and estimation of the rotational speed.

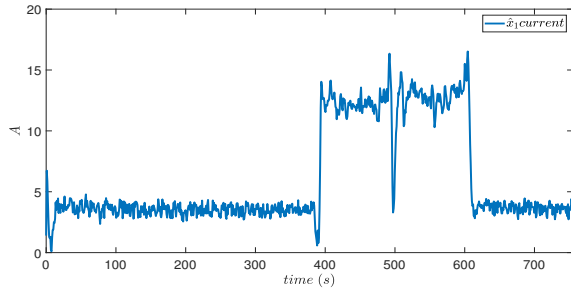


Fig. 7. Estimation of armature current.

The experiment was performed as follows. Once the motor speed reaches the steady-state value (around 800 r.p.m. as illustrated in Fig. 6), a mechanically-induced friction force is generated from around $t = 390\text{s}$ to $t = 600\text{s}$. This action emulates a faulty scenario, probably due to unhealthy bearings. In this way, a variation on the value of T_0 is expected.

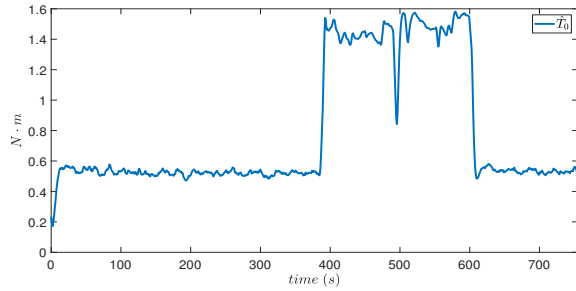


Fig. 8. Estimation of T_0 .

Experimental results are depicted in Figs. 6-8. In Fig. 6, it can be appreciated that the estimated rotational speed $\hat{x}_2 = \hat{v}_m$ (blue line) asymptotically converges to the measured value (red line) despite the fault occurrence and measurement noise. As expected, the armature current i_a increases when the friction force is induced. The corresponding estimated armature current $\hat{x}_1 = \hat{i}_a$ is depicted in Fig. 7. Finally, the unknown input occurrence is reflected as an increasing variation in T_0 , whose estimated value of \hat{T}_0 is depicted in Fig. 8.

VI. CONCLUSION

A simple nonlinear observer for state and UI estimation is presented in this paper. Two cases are presented in order to illustrate its applicability to DC motors. Preliminary results in simulation demonstrate asymptotic convergence of the observer. Besides, a laboratory experiment is performed with a laboratory prototype, consisting in a DC motor coupled to a bearing supported shaft, where faults (like these appearing when bearings become faulty) are induced, to test the fault detection and estimation capabilities of the proposed observer. The two main advantages of the proposed observer, compared with [13], and similar works dealing with Takagi-Sugeno systems are: (i) the easiness to compute the observer gain, because

a simple pole placement procedure is required to calculate the observer gain and (ii) the mathematical model of the processes does not require any transformation, preserving the original nonlinear dynamics of the model. Thus, an accurate estimation of the non-measurable states and the unknown inputs and faults can be guaranteed. On the other hand, the main limitation of this observer is that it can only be applied for nonlinear systems having the form of system (8) where all variables in the nonlinear vector $g(y, u)$ must be measurable. Fortunately, in practice, many systems can be modeled in this form.

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