

1 Flexural Failure of Fabric Reinforced Cementitious Mortar (FRCM) Plates under 2 Punctual Loads: experimental test, analytical approach and numerical simulation

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7 Abstract

8 Fabric-reinforced cementitious matrix (FCRMs) are composites that produce lighter and
9 more durable strengthening solutions. In this study, carbon and basalt fabrics were used
10 to manufactured FRCM plate specimens. These plates were subjected to a centered
11 punctual load with different punch diameters. Flexural failure mode was observed.
12 Experimental tests showed that carbon and basalt fabrics improved notably the load
13 capacity and the stiffness of mortar plates compared to unreinforced ones. Moreover,
14 failure in the reinforced plates was progressive, preventing the sudden brittle failure of
15 the unreinforced ones. Analytical and numerical models were adjusted and validated from
16 experimental results, and both have proved to be effective calculation tools. What is more,
17 numerical model allowed to determine a sliding tensile stress for the carbon fabric used
18 in this study.

19 **Keywords:** Plates, FRCM, Cementitious matrix, Carbon fibres, Basalt fibres, Flexural
20 test, Analytical model, Numerical model

21 1 Introduction

22 Concrete plates or slabs are one of the most used structural elements in building
23 construction, especially the well-known concrete reinforced flat slabs, that give the
24 advantages of providing more free space [1].

25 The problem of concrete plates subjected to punctual loads has been studied from the very
26 beginning. Punctual loads may produce flexural failures but also punching failures, which
27 are sudden and extremely dangerous. The transition way one to other is not clear and there
28 are still a lot of research about this issues.

29 Currently, there are some articles aimed at studying the behavior of reinforced
30 cementitious matrix plates, see [2][3]. Of particular interest is the work of [4], this paper
31 presented experimental tests conducted on square cementitious slabs simply supported on
32 four edges and subjected to patch load. The test results showed that adding a wire mesh
33 to ordinary reinforcement increases significantly the punching resistance. Moreover, as
34 the loaded area size increases both ductility and stiffness increase and the bridging effect
35 due to the difference in the reinforcement ratio in orthogonal directions was clearly
36 noticed.

37 In order to know the difference between flexural and punching failure, the research
38 presented by [5] carry out an experimental campaign. In this was observed that the failure
39 load is raised with increasing cross-section of the reinforcement. The load–displacement
40 curves illustrated that after the maximum load was reached, a flexural failure is
41 characterized by a smooth decrease of the carrying load with increasing displacement. In
42 the opposite case, a punching failure results in a sudden decrease of the carrying load after
43 the maximum load. These results clearly illustrate the difference between both failure
44 mechanisms for traditional steel reinforcement.

45 The fabric cementitious matrix (FRCM) is well known as a strengthening system used to
46 improve the mechanical behavior from structural elements [6][7][8][9][10][11][12]. This
47 emerged as a promising alternative to organic matrix based fibre reinforced polymers
48 (FRPs), and also this is an evolution of ferrocement used for manufacturing plate or flat
49 slab.

50 FRCM consists of a fabric embedded in an inorganic mortar matrix. This fabric can be
51 made of diverse materials such as glass, carbon, basalt [13,14], PBO (Polyparaphenylene
52 benzobisoxazole), and vegetal fibre [15].

53 It is essential to understand that FRCM provides tensile strength thanks to the fabrics, and
54 that these fibres only bear the loads that the mortar is capable of transmitting [16].
55 Therefore, the transmission of matrix-mesh stresses is one of the main requirements to be
56 considered, as well as the geometric adaptability of the fabric and its chemical stability
57 (durability) within the matrix.

58 In the case of cementitious plates with fabrics of synthetic fibres, in the research presented
59 by [17], specimens of carbon fabric reinforced cementitious matrix (FRCM) with
60 chopped carbon fibre were developed. A series of three-point bending tests were
61 conducted to investigate the effects of chopped carbon fibre content and the carbon mesh.
62 The results show that the carbon mesh is effective as reinforcement of cementitious
63 matrix, where during in the bending test the loads of the specimens continued to increase
64 after the occurrence of visible cracks, which indicated that the carbon mesh in the center
65 of FRCM plates enhances the plasticity of cementitious matrix.

66 From the studies presented above, it can be seen that most of these investigations are
67 aimed at the study of steel reinforced concrete plates whereas it seems there are no records
68 of experimental campaigns aimed to demonstrate the flexural behavior of FRCM plates.
69 The present work is an experimental campaign aimed to analyze the behavior of different
70 FRCM materials (carbon and basalt fibres) in the shape of small plates. From the test
71 results it is aimed to develop analytical and numerical models capable of reproducing the
72 flexural failure of FRCM plates under simple supported boundary conditions. It is
73 expected that this study will raise the possibility of replacing steel with synthetic fiber
74 fabrics, which would reduce the thickness of the plates, making them lighter and avoiding
75 the durability drawbacks caused by the steel corrosion. Nevertheless, the investigation is
76 mainly oriented to the material performance and results are prevented to be directly
77 extended to real size slabs.

78

79 **2 Materials and specimens**

80 In order to face the experimental campaign some samples of small FRCM plates were
81 produced according next conditions.

82

83 **2.1 Mortar**

84 A single type of commercial mortar was used in this study. It was an auto-levelling mortar
85 which includes organic additives (plasticiser polymer). The manufacturing of samples
86 was performed with a single batch and some test on compression and flexural. The control
87 mortar specimens were tested to flexion in an electromechanical press of 50 kN, and then
88 the resulting halves were tested under compression with a hydraulic actuator of 100 kN
89 capacity. These tests were performed according to EN 1015-11: 2000 [18].

90

91

Table 1. Mortar properties

<i>Mortar</i>	<i>Flexural strength (MPa)</i>		<i>Compressive strength (MPa)</i>	
	<i>Average</i>	<i>C.V.</i>	<i>Average</i>	<i>C.V.</i>
A	8.84	(11%)	36.60	(7%)

92

93 **2.2 Fabrics**

94 Two type of fabrics were used to manufacture the FRCM plates: carbon and basalt fibres.
 95 The averaged results of a tensile tests and other mechanical properties (supplied by the
 96 manufacturer) are summarized in Table 2. These experimental data were previously
 97 determined in [19] and they were obtained from tests of 5 tows of the each fabric (carbon
 98 and basalt) using the same procedure presented in [20].

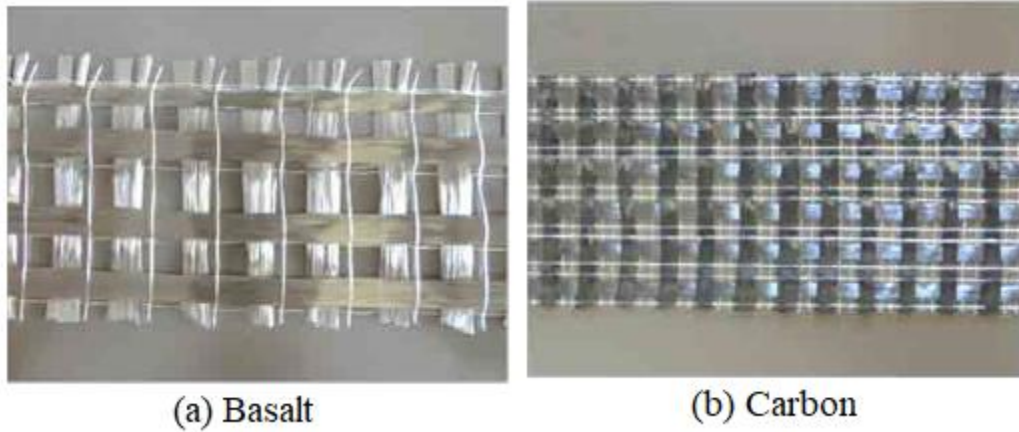


Figure 1. Fabrics

Table 2. Fibres and fabric properties

	Property	Units	Basalt (B)	Carbon (C)
Fibres	Ultimate tensile strength ⁽¹⁾	$f_{fib,u}$ [MPa]	3080	4320
	Elastic modulus ⁽¹⁾	E_{fib} [GPa]	95	240
	Ultimate strain ⁽¹⁾	$\epsilon_{fib,u}$ [%]	3.15	1.80
	Fibre orientation ⁽¹⁾		Bidirectional	Bidirectional
Fabric	Equivalent thickness ⁽¹⁾	t_{tex} [mm]	0.053	0.047
	Distance between tows ⁽¹⁾	d_{tows} [mm x mm]	15x15	10x10
	Elastic modulus ⁽²⁾	E_{tex} [GPa]	87.81	235.69
	Ultimate tensile strength ⁽²⁾	$f_{fab,u}$ [MPa]	763.7	1915.74

(1) Supplied by manufacturer; (2) results of tensile test [19].

103

104 2.3 Specimens

105 The experimental program included 27 samples of FRCM plates. There is no specific
 106 norm about specimen dimensions for assessing the response to a punctual centered load.
 107 The closer to this research might be a reference related to punching shear on ferrocement
 108 by [4]. This author used plates of effective dimensions 400 mm x 400 mm with thickness
 109 from 40 to 60 mm. He reinforced slabs with a wire mesh and some steel rods. In the
 110 present research the reinforcement is by fabric, with less strength than steel
 111 reinforcement. Therefore the dimensions of the specimens can be taken half of 400 mm
 112 that is enough to create a relevant flexural deformation. Hence, every plate had
 113 dimensions of 200 mm x 200 mm and a thickness of 20 mm.

114



Figure 2. Manufacturing of specimens and traceability labels

115

116

117

118 There were three types of plates, the ones without any reinforcement, the ones with carbon
 119 fabric and finally, the ones with basalt fabric. One of the objectives was to compare the
 120 different performance according the nature of fabric.

121 All plates were manufactured at the same time in a single batch in three molds. Every
 122 mold produced all plates of the same type. Each specimen is labeled with the
 123 reinforcement material: None, Carbon or Basalt and the punching diameter: D16, D30,
 124 D63 in this manuscript.

125 Every mold was prepared with a grid of wooden strips defining 200 mm x 200 mm gaps.
 126 These strips had only a height of 10 mm, just the half of the total plate thickness, so to
 127 place one continuous reinforcement fabric for all the plates in a mold. Fabric was placed
 128 “as-it-is”. Therefore, bonding was only achieved by chemical and friction with no special
 129 treatment or mechanical device placed at the edge of the samples. A second layer of
 130 wooden strips was placed on the first one to reach the 20mm plate thickness. The
 131 manufacturing procedure was as follows:

- 132 ✓ Preparing the mold basis with demolding agent.
- 133 ✓ Mixing the mortar and pouring it up to fill the mold and level it. For unreinforced
 134 plates the procedure was over.
- 135 ✓ Cover the whole mold with the reinforcement grid and bond it lightly to the
 136 wooden strips using stitches and adhesive tape.
- 137 ✓ Place a second layer of wooden strips and nail them lightly to the mold.
- 138 ✓ Pour mortar up to fill the mold and level it.
- 139 ✓ Manually shake the mold to vibrate mortar.
- 140 ✓ Cover the mold with a plastic cover to maintain moisture. And keep it in
 141 laboratory conditions for 10 days.
- 142 ✓ Demold and leave samples to cure in laboratory conditions for other 18 days. After
 143 that the plates were ready to be tested

144 All samples were measured to ensure the proper dimensions. It was found that square size
 145 was perfect but thickness had some small deviations at a certain point, less than 1 mm,
 146 and it was considered acceptable (less than 5%).

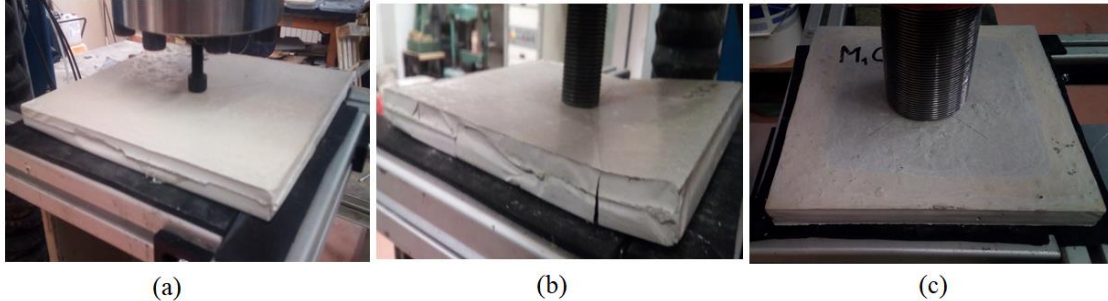
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148

149 **3 Experimental campaign**

150 3.1 Test setup and instrumentation

151 The test is based on placing the plate over a rigid boundary frame and press the top surface
152 with a concentrate load. Load is applied with a cylindrical tool in the middle of the
153 sample. For each type of plate three different punching tools were used. One with
154 diameter 15.9 mm (named D16), other 30 mm (named D30) and finally, 63.5 mm (named
155 D63).



156
157
158

Figure 3. Test setup: (a) D16, (b) D30, (C) D63

159 Rigid frame was made of connected aluminium profiles. In the contact between the plate
160 and the frame a very thin rubber strip was placed to avoid stress concentrators that may
161 modify the crack pattern. Plate was simply supported at every edge (see Figure 3).
162 A universal electromechanical machine applied the load with displacement control at a
163 speed 1mm/s. Continuous measurement included displacement and load from the
164 machine sensors. The test ended when the load decreases 10% of the peak load.

165

166 3.2 Experimental results

167 3.2.1 Crack patterns

168 The results of the different tests are shown in Figure 4. In all tests first cracks started at
169 the bottom side of the specimen under the loading area. Later cracks propagated
170 diagonally to the boundary condition. The crack pattern followed the classical distribution
171 of a yield line flexural failure.

172 The FRCM-plates presented two type of failures:

- 173 ✓ Fabric sliding failures [21,22]: this occurred in carbon-FRCM, where the fabric
174 starts to slide when the maximum load was reached. This showed that the bonding
175 interaction between fabric-mortar was not perfect (mortar debonding, see Figure
176 4. Carbon D16, D30, D63) after the fabric reached some sliding tensile stress.
- 177 ✓ Fabric rupture failures: this occurred in the basalt-FRCM, where the fabric reach
178 its tensile strength. Final crack thickness is wider than for carbon-FRCM
179 specimens (see Figure 4. Basalt D16, D30, D63). This means perfect interaction
180 between the fabric and the mortar.

181 The unreinforced specimens break with a sudden mechanism. As soon as the yield
182 lines appeared, the sample broke down. Little number of wide cracks were developed
183 (see Figure 4. None D16, D30, D63). On the contrary, all reinforced specimens
184 showed a smooth decrease in the applied load while the cracks grew and developed.

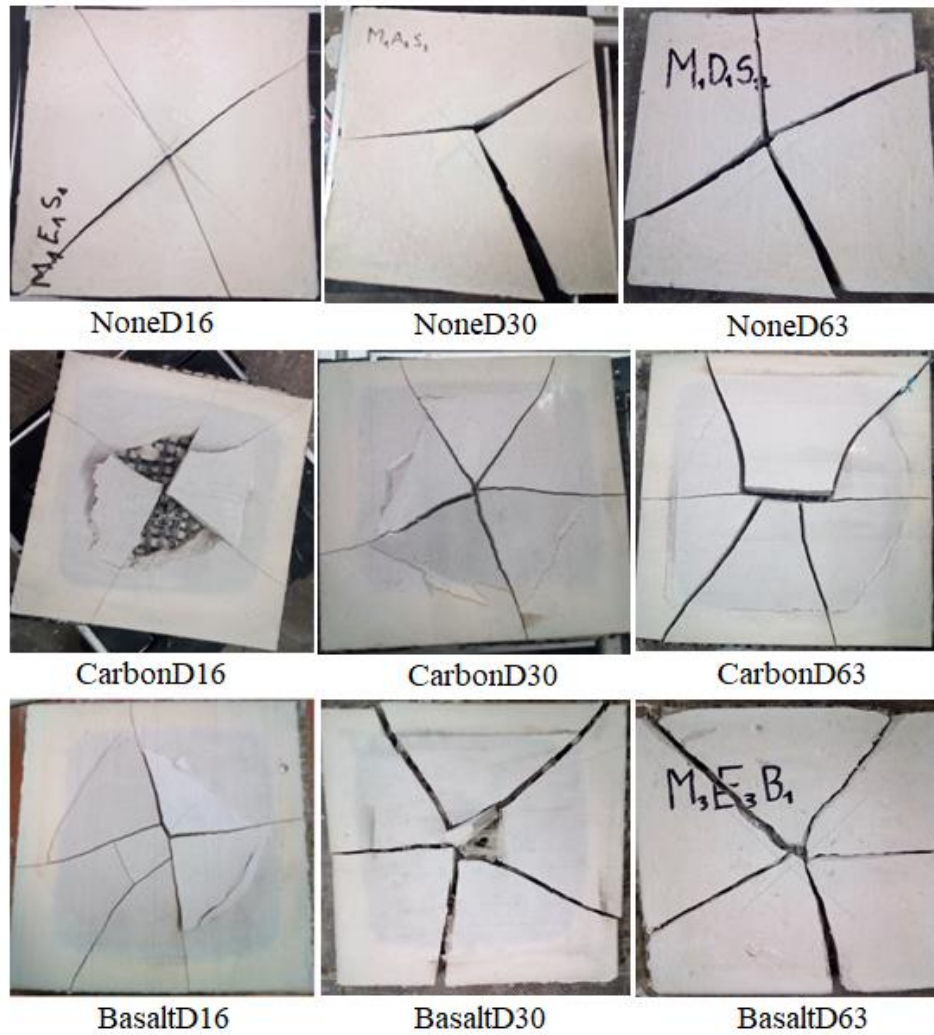


Figure 4. Crack pattern

3.2.2 Maximum load and stiffness coefficient

Table 3 shows the experimental results of maximum load (P_{max}) and the initial stiffness coefficient (K_i) for all the specimens. The initial stiffness was calculated from the first slope in the load-displacement curve presented in Figure 6.

Table 3. Experimental results

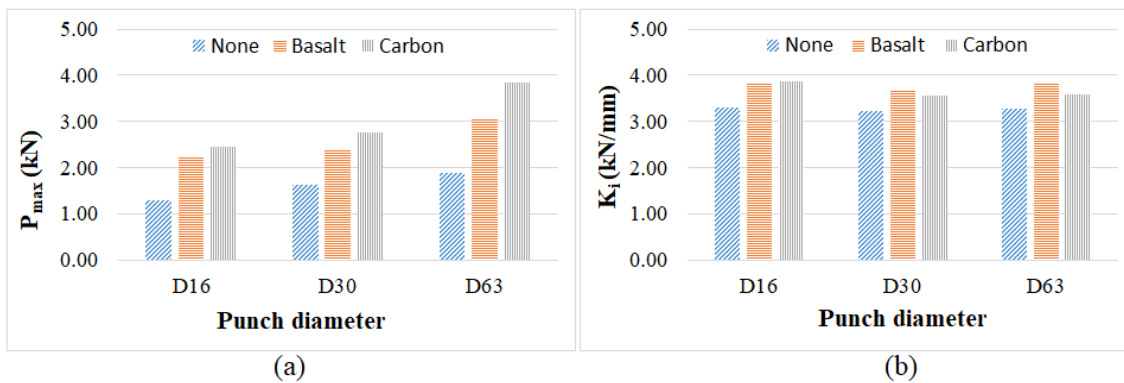
Punch diameter	None		Basalt		Carbon		
	P_{max} (kN)	K_i (kN/mm)	P_{max} (kN)	K_i (kN/mm)	P_{max} (kN)	K_i (kN/mm)	
D16	M1	1.71	4.06	2.15	4.06	2.49	3.65
	M2	1.00	2.90	2.17	3.24	2.22	3.84
	M3	1.16	2.95	2.43	4.16	2.61	4.15
	Average	1.29	3.30	2.25	3.82	2.44	3.88
	C.V.	24%	16%	6%	11%	7%	5%
D30	M1	1.05	2.84	2.39	3.39	2.68	3.29
	M2	1.89	3.80	2.22	4.09	2.55	3.24
	M3	1.92	3.04	2.49	3.57	3.05	4.13
	Average	1.62	3.23	2.37	3.68	2.76	3.56
	C.V.	25%	13%	5%	8%	8%	12%

M1	1.42	2.75	2.84	4.27	3.97	2.64
M2	2.44	3.30	3.19	3.37	3.73	4.54
D63 M3	1.82	3.76	3.14	3.87	3.82	3.54
Average	1.89	3.27	3.06	3.84	3.84	3.57
C.V.	22%	13%	5%	10%	3%	22%

193

194 The results presented in Table 3 show coefficients of variation between 3% and 25%.
 195 The unreinforced samples showed the greatest scattering of data, as it was expected for a
 196 single mortar material. On the contrary, the reinforced ones limited its scattering at 10%
 197 which represents good repeatability of the experiments.

198 Figure 5 shows the variation of the maximum load and initial stiffness for each type of
 199 specimen and punch diameter. In Figure 5a, it is appreciated that the maximum load
 200 increased with the increase of the punch diameter. The load-bearing capacity was greater
 201 for larger punch diameter because the punch area was nearer to the support, so to reach
 202 the same flexural moment it was necessary to apply a greater load. Also Figure 5a shows
 203 that the basalt and carbon fabrics increased the maximum load in all the specimens,
 204 especially in the case of carbon-FRCM (D63) where this improved 103%.
 205



206

207

208

Figure 5. Experimental results

209 Figure 5b shows a negligible change (slightly larger) of the initial stiffness in the FRCM
 210 plates compared to the plates without fabric. Basalt and carbon FRCM did not contribute
 211 with significant stiffness. This is an expected result because the reinforcement modifies
 212 the strength of the specimen but its deformation depends mostly on the mortar stiffness
 213 and the specimen geometric inertia, two parameters that the fabric did not modify.

214 Figure 6 show the average of the load-displacement curves of the experimental results. In
 215 the case of unreinforced plates (“none” in Figure 6) it is shows a sudden decrease of the
 216 carrying load after the maximum loads, in change in the case of FRCM specimen it is
 217 shows a smooth decrease of the carrying load when the maximum loads is reached [5],
 218 this is due to friction between materials that prevents brittle breakage and dissipates more
 219 energy. This confirms the flexural failures showed in the specimens (Figure 4).

220 Also in the case of FRCM specimen Figure 6 shows a first slope where the fabric and the
 221 mortar have the same deformation, however when the mortar reach the carking stress,
 222 they start a stage of fabric-mortar interaction, and after that there are a stiffness change
 223 controlled by the fabric stiffness. This behavior meets the three lineal tensile model
 224 presented by [23].

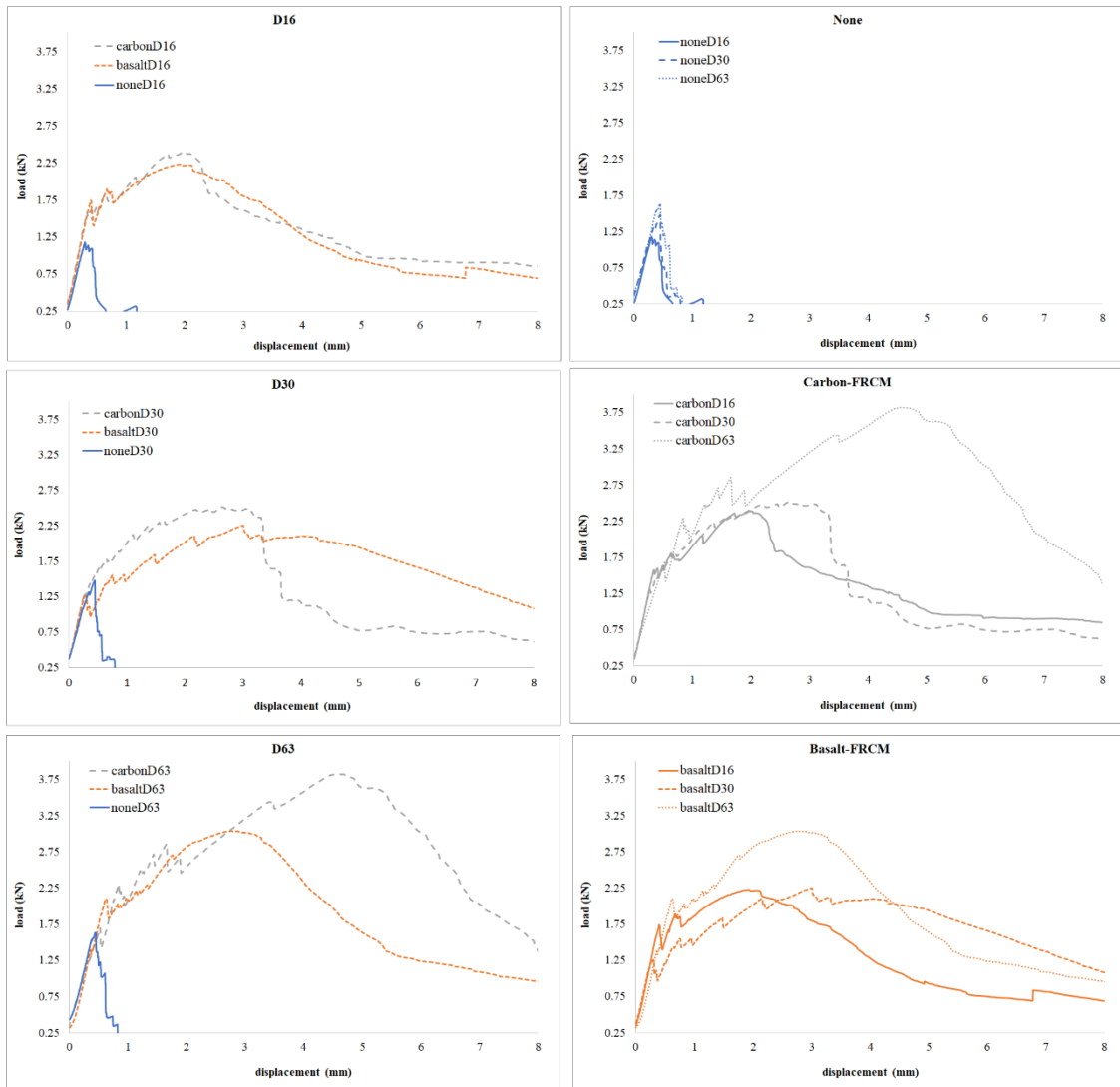


Figure 6. Average of the experimental load-displacement plots

4 Analytical model

4.1. Analytical unreinforced model

In the case of unreinforced plate, the symmetric model presented in Figure 7 was considered, from this model it was possible to obtain the following equations (eq. 1-2).

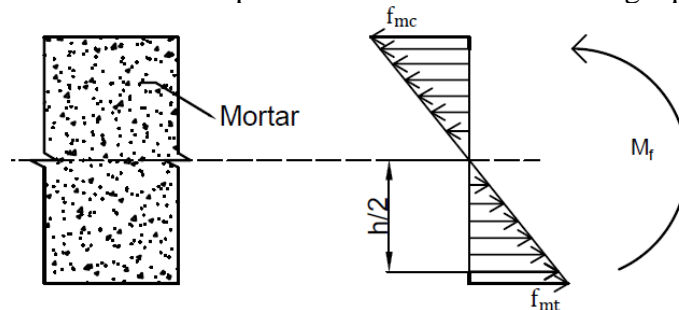


Figure 7. Analysis of cross-section for unreinforced section

Constitutive behaviour of concrete (mortar for this case), is shown in Figure 7 and Figure 8 and according to classical plate theory of yield lines of Johansen.

Where the maximum force (F_{max}) is:

$$F_{max} = \frac{f_{mt,u}h}{4} \quad \text{Eq. 1}$$

$$M_u = F_{max} \times d \quad \text{Eq. 2}$$

$$d = \frac{2h}{3} \quad \text{Eq. 3}$$

238

239 $f_{mt,u}$: is the tensile strength

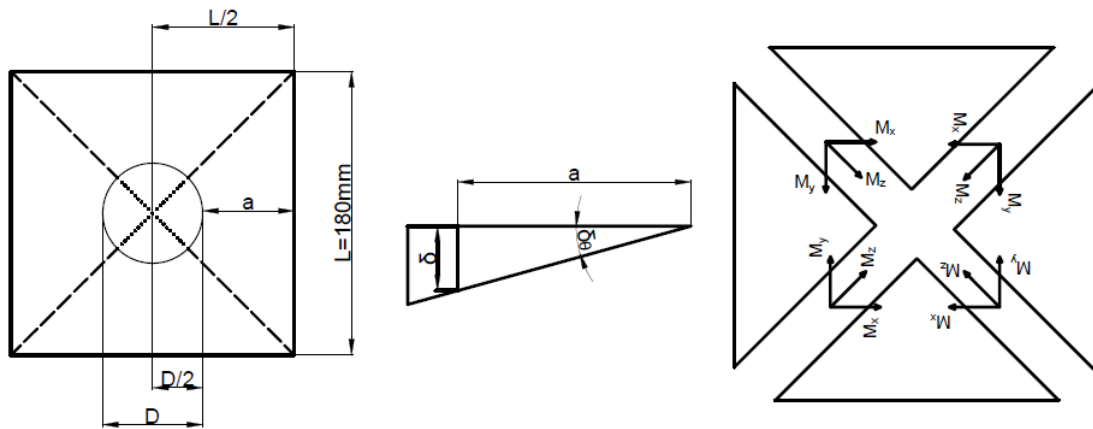
240 M_u : is the ultimate moment

241 d : is the distance since the concentrate maximum force until the neutral fiber (lever arm)

242 The tensile strength was determined from the equation 4 until 7 (which were extracted

243 from the yield lines method presented in Figure 8). This was possible with the

244 maximum load (p) obtained from the experimental test.



245

246

247

Figure 8. scheme representative based in yield lines plate theory

$$U = 4 \times M_u \times L \times \delta_\theta \quad \text{Eq. 4}$$

248

$$\delta_\theta = \frac{\delta}{a} \quad \text{Eq. 5}$$

249

$$W = p \times \delta \quad \text{Eq. 6}$$

250

$$p = \frac{4 \times M_u \times L}{a} \quad \text{Eq. 7}$$

251 Where:

252 U : is the sectional theory energy

253 δ_θ : is the angular distortion (Figure 8)

254 δ : is the vertical displacement (Figure 8)

255 a : is the horizontal distance from the plate extreme until the punch extreme (Figure 8)

256 W : is the work of external forces

257 From the equations 1-7 was obtained the tensile strength, equivalent to 2.31 MPa, that

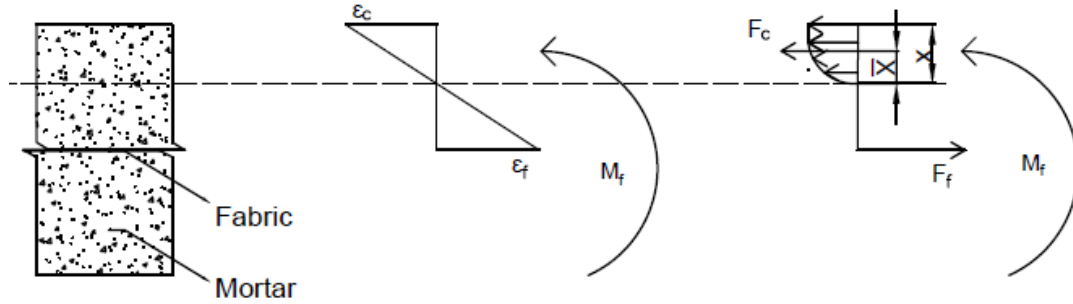
258 was validated by the 3 maximum load average obtained experimentally by the 3 different

259 punch used in this study (D16, D30, D63), with percentage variation of 4, 9 and 0 %
 260 respectively. This tensile strength was used in the analytical model of the FRCM plates,
 261 and their numerical simulation.

262

263 4.2. Analytical reinforced model

264 The analytical method to determine the ultimate flexural capacity of the reinforced plate
 265 is based on the following assumptions: (1) strain compatibility during the loading process,
 266 (2) equilibrium of forces of the load-bearing cross-section. The mortar tensile strength
 267 was not considered, because after the cracks formation the fabric is which support the
 268 tensile stress.



269

270

Figure 9. Analysis of cross-section for reinforced section

271

272 The proposed analytical approach is based on the assumptions presented in Figure 9. The
 273 fabric was assumed to behave linear-elastic until failure, and the stresses in the mortar
 274 compression block followed a parabolic-rectangular distribution according to Eurocode
 275 [24].

276 The contribution of the fabric is an effective strength over the total strength of the cross
 277 section. Figure 9 shows the internal force equilibrium and the strain distribution of a
 278 rectangular FRCM-plate cross-section at maximum bending moment stage. According to
 279 Figure 9, the analytical maximum flexural moment ($M_{max,an}$) is calculated as the following
 280 (Eq. 1 and 2):

$$M_{max,an} = M_c + M_{fib} \quad \text{Eq. 8}$$

281 where M_c and M_{fib} are the ultimate flexural contributions by compression strength of the
 282 mortar, and the ultimate flexural contributions of the fibres. The contributions of each
 283 withstanding material and neutral axis depth (x) can be determined according to the
 284 following equations (Eq. 9 - Eq. 17):

- 285 • Ultimate flexural contribution of the compressive stresses on mortar:

$$f_c = f_{cd} \left[1 - \left(1 - \frac{\varepsilon_c}{\varepsilon_{c0}} \right)^n \right]; \text{ if } 0 \leq \varepsilon_c \leq \varepsilon_{c0} \quad \text{Eq. 9}$$

$$f_c = f_{cd}; \text{ if } \varepsilon_{c0} \leq \varepsilon_c \leq \varepsilon_{cu} \quad \text{Eq. 10}$$

286 The values of mortar breakage deformation (ε_{c0}) and ultimate deformation (ε_{cu}) in
 287 compression are set to 0.002 and 0.0035 respectively, both suggested by Eurocode 2 [24].
 288 These values are valid for concrete with a characteristic compressive strength $f_{ck} \leq$
 289 50MPa. Hence the used mortar is assumed to fit into this definition. The compressive
 290 strength of the mortar, f_{cd} , as described in section 2.1.

291 The moment produced by the compression block will be equal:

$$M_c = f_c x \bar{x} \quad \text{Eq. 11}$$

292 Where x is the distance from the neutral fiber to most compressed fiber (see Figure 9) and
 293 \bar{x} is the distance from center of gravity the compression block to the neutral fiber.

294

- 295 • Ultimate flexural contribution of the fibre fabric:

$$M_{fib} = f_{fib} A_{fib} (h/2 - x) \quad \text{Eq. 12}$$

296 It is known that for the tested FRCM-plates the fabrics failure occurred before reaching
 297 the maximum compressive mortar deformation. The ultimate fabric deformation ($\varepsilon_{f,u}$,
 298 experimental in [19] and Table 2) is taken to calculate the strain in concrete when the
 299 maximum load is reached. Strain compatibility is imposed:

$$\varepsilon_c = \frac{\varepsilon_{f,u} \cdot x}{h/2 - x} \quad \text{Eq. 13}$$

300 Once the deformations of the materials at the specimens' failure state are known, the
 301 following condition must be fulfilled to validate the calculation of the bending capacity
 302 of the FRCM-plates:

303 ✓ $\varepsilon_c \leq 0.0035$ (Code [24])

304

305 4.3. Analytical model results

306 The results obtained from the analytical model are presented in Table 4. This shows the
 307 results of maximum load (P_{max}) and the ultimate flexural moment (M_u) supported by the
 308 FRCM-plate. Also, this shows the analytical fabric and mortar ultimate strain when is
 309 reached the maximum experimental load of the FRCM-plate.

310

311

Table 4. Analytical model results

Punch diameter	Carbon-FRCM				Basalt-FRCM			
	M_u (MPa)	P_{max} (KN)	ε_f	ε_c	M_u (MPa)	P_{max} (KN)	ε_f	ε_c
D16	296.71	2.60	0.0031	0.0008	257.00	2.26	0.0061	0.0011
	-(5%)				(0.4%)			
D30	296.71	2.85			257.00	2.40		
	(3%)							
D60	296.71	3.67			257.00	3.09		
	(7%)							
(%) : variation with the experimental results								

312

313 The first data to highlight in Table 4 is that the strain of the carbon fibres are less than the
 314 ultimate strain calculated ($\frac{f_{fib}}{E_f} = 0.0031$). This because the fibres sliding before the reach
 315 the ultimate strain. The carbon fibres strain presented in table 4 is the 38% of the ultimate
 316 carbon strain. In the case of basalt-FRCM the fabric reaches 70% of the ultimate strain,
 317 in this case is no reach the ultimate strain, like in the experimental results (fabric rupture).

318 Also is observed that the mortar ultimate strain (0.0035) is not reached in both cases,
319 whereby, is fulfilled the analytical limit imposed.
320 The analytical model results were properly approximated to the experimental results, with
321 fitting between 0.4 and 7 % of variation.

322

323 **5 FRCM numerical simulation**

324 Commercial mechanical simulation software Abaqus® 6.14-4 [26] was used to
325 implement numerical simulations. This choice was based on the aim of using a general
326 purpose-widely available simulation tool that was capable of representing complex
327 material models. In addition, many previous studies for the analysis of FRCM and
328 reinforced concrete successfully used this software (see, for example, [27][28]).

329

330 5.1. General material's constitutive formulations

331 One of the most used approaches for the simulation of FRCM subjected to tensile loads
332 is based on assuming a concrete plastic damage model for cementitious matrix. While
333 fabric is considered an elastic material only dependent from Young's modulus.

334 Plastic damage model is characterized by the definition of two modulus of elasticity: one
335 corresponding to the elastic zone, and another depending on damage coefficient, which
336 is function of the cracking situation or the plastic degree achieved. In this model, it is
337 assumed that the two main failure mechanisms are tensile cracking and compression
338 crushing of the concrete. The evolution of the yield surface (or failure) is controlled by
339 two plasticity variables ε_t^{pl} y ε_c^{pl} , linked to the failure mechanisms under tension and
340 compression, respectively. These are defined as the plastic deformations equivalent to
341 tension and compression, respectively.

342 In addition, this model assumes that the strain-stress response for the uniaxial
343 compression of the concrete is characterized by damaged plasticity, as shown in Figure
344 10. Under uniaxial tension, the stress-strain response follows a linear elastic relationship
345 until the cracking stress value is reached (σ_{t0}). The cracking stress corresponds to the
346 appearance of microcracks in the material. From this point, the tensile tension that
347 transmits the material does not disappear, but it gradually decreases as the deformation
348 increases. Damage variable d_t , whose minimum value is 0 (intact material) and whose
349 maximum value is 1 (totally damaged material), defines the slope of the discharge branch.
350 So, if E_0 is the modulus of elasticity of the elastic material, the module of the discharge
351 branch becomes $(1-d_t) E_0$.

352 Under uniaxial compression, the response is linear up to the value of initial yield (σ_{c0}).
353 In the plastic zone, the response is typically characterized by stress hardening followed
354 by stress weakening beyond the final stress (σ_u). This representation, although somewhat
355 simplified, captures the main characteristics of the concrete response and it is also valid
356 for mortar. As in the case of tension there is a damage parameter d_t that varies between 0
357 and 1 which reduces the stiffness of the discharge branch.

358 This model is useful to simulate the interaction between reinforcement and concrete
359 (fabric and mortar for the case of FRCM), and also provides numerical stability improving
360 convergence.

361

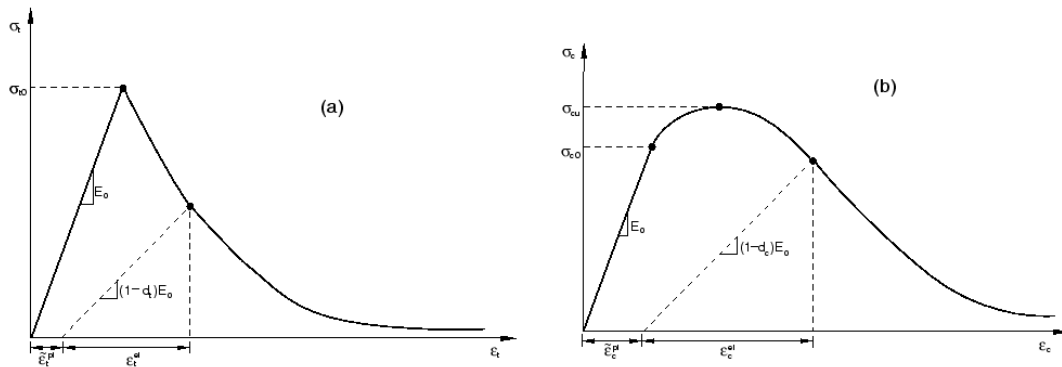


Figure 10. Uniaxial model [26]: (a) tension, (b) compression

5.2. Unreinforced plates modelling

The unreinforced plate specimens were modeled to determine the mortar elasticity modulus and to calibrate the mortar properties for the FRCM-plate simulations. The particularities to model these specimens is described.

First, the geometry of the specimens was defined based on the geometry of the specimens manufactured. These were area of 180×180mm (support positioning) and thickness of 20mm. This geometry was defined as a deformable solid part.

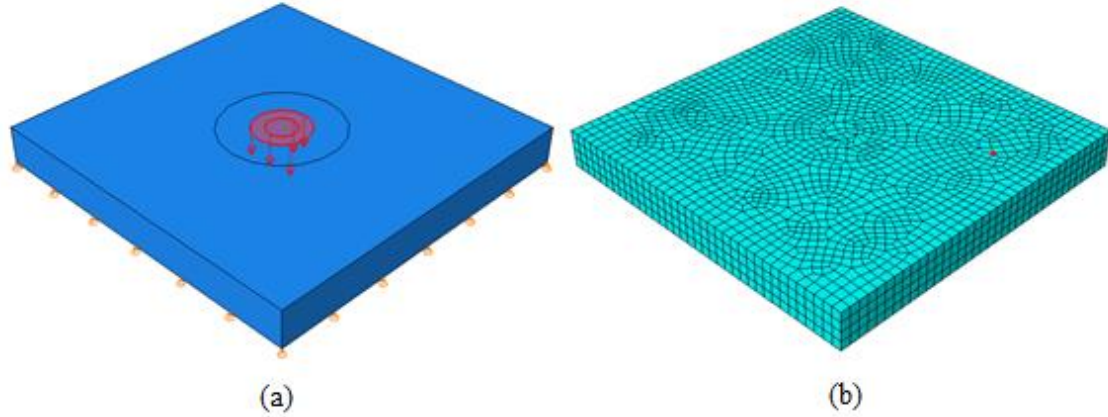
To define the material of the cementitious matrix, the aforementioned plastic damage model was chosen. The elastic behavior of the cementitious matrix was defined by: i) the elasticity model, which was calibrate with the maximum loads and stiffness coefficients obtained experimentally (section) , and ii) the Poisson coefficient, which was set to 0.2 as suggested by EHE [25].

Regarding the plastic zone of the cementitious matrix in tension and compression, it was necessary to define the following parameters:

- a) Dilatation angle: This controls the quantity of the plastic volumetric deformation developed during the plastic shear and is assumed constant during the plastic flexibilization. The first value used for this parameter was 13 according [28], but in our simulations we saw that a value of 31 performed better and facilitate the convergence of the computations.
- b) Eccentricity: This parameter defines the speed at which the function approaches the maximum stress asymptote. The predetermined eccentricity suggested by Abaqus is 0.1, which implies that the material has almost the same angle of expansion in a significant range of confining pressure values.
- c) Form parameter of the plasticizing surface K: This is the ratio of the second invariant tension in the meridian, to that of the compression meridian, in the initial yield for any given value of the invariant pressure. Default value is equal to 2/3.
- d) Relationship between the maximum uniaxial and biaxial compression stress at the beginning of the loading process. Default value is equal to 1.16.
- e) Viscoplastic regularization: models of materials that exhibit a smoothing behavior and a degradation of rigidity often lead to serious convergence difficulties in implicit analysis programs. A common technique for overcoming some of these convergence difficulties is the use of a viscoplastic regularization of the constitutive equations, which causes the constant tangent stiffness of the softening material to become positive during sufficiently small increments of time. In a range from 0.001 to 0.004, 0.003 proved to be the most stable and provided convergence.

Once these materials properties were defined, the matrix stress-strain curves and the corresponding damage variables were calculated using the procedure from [28].

403 Next step was defining boundary conditions. The inferior perimeter of the deformable
 404 solid was simply supported (restriction of vertical displacements), and the maximum
 405 displacement obtained experimentally was imposed on the center of the opposite face, in
 406 a superficial circular area, defined by the three different punch diameter used in this study
 407 (see Figure 11) .



408 Figure 11. (a) Boundary conditions and (b) Mesh size of deformable solid

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410

411 Then the mesh was defined. Three meshes of 2.5 mm, 5 mm and 10 mm characteristic
 412 size were tested for results convergence analysis, resulting that no significant difference
 413 was observed between the results of meshes of 2.5 and 5 mm (2% variation of the
 414 maximum load). Hence, the size of elements used was set to 5 mm to reduce calculation
 415 cost.

416

417 5.2.1. Determining of elasticity modulus of mortar

418

419 Mortar's modulus of elasticity was not known. Hence, it was necessary to calibrate this
 420 property with the aim of reproducing the experimental stiffness and maximum load of
 421 the unreinforced plates. With this purpose, 4 different moduli for each punch diameter
 422 were numerically tested, interpolating or extrapolating the value that best fits
 423 experimental results with a parabolic fitting (Figure 12), excepting in the case of the
 424 D30 punch, where the results obtained with the modulus of 2388 MPa gave variation
 425 with experimental results of 1%. Finally, the three fitted values (one per punch
 diameter) were averaged. The results are presented in

426

Table 5.

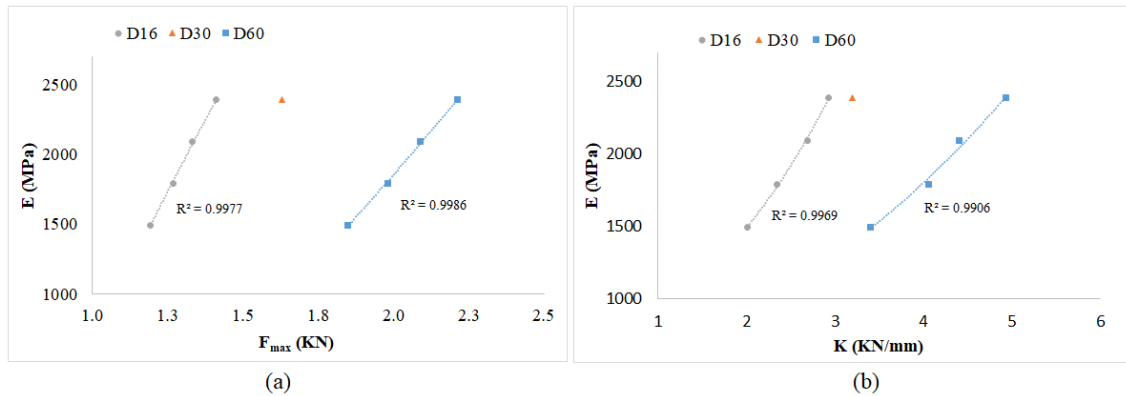
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428

Table 5. Determining of elasticity modulus

E (MPa)	D16		D30		D60	
	K _i (KN/mm)	P _{max} (KN)	K _i (KN/mm)	P _{max} (KN)	K _i (KN/mm)	P _{max} (KN)
2388.00	2.92	1.41	3.19	1.63	4.94	2.21
2089.50	2.69	1.33	-	-	4.41	2.09
1791.00	2.34	1.27	-	-	4.06	1.98
1492.50	2.01	1.19	-	-	3.40	1.85
E_m (MPa)	2098.14					

429



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432

Figure 12. Tendency of elasticity modulus

433 5.3.FRCM-plates modelling

434 Two FRCM-plates were modeled, one for each type of fibres used in the experimental
435 campaign (carbon and basalt). Here, the particularities to model these specimens is
436 described.

437 The geometry and properties of the deformable solid was the same that the used in the
438 unreinforced plate simulation, with the elasticity modulus previous determined (E_m).

439 To simulate the fabrics, truss elements were chosen, like in other studies [29]. These are
440 long and thin structural members that can transmit axial force only. These are typically
441 used to model thin, line-like structures that support loading only along the axis or the
442 center line of the element and no moments or forces perpendicular to the center line are
443 considered. Truss elements were used in this case to reduce the high computational costs
444 that the use of three-dimensional elements would cause, as well as to avoid convergence
445 problems.

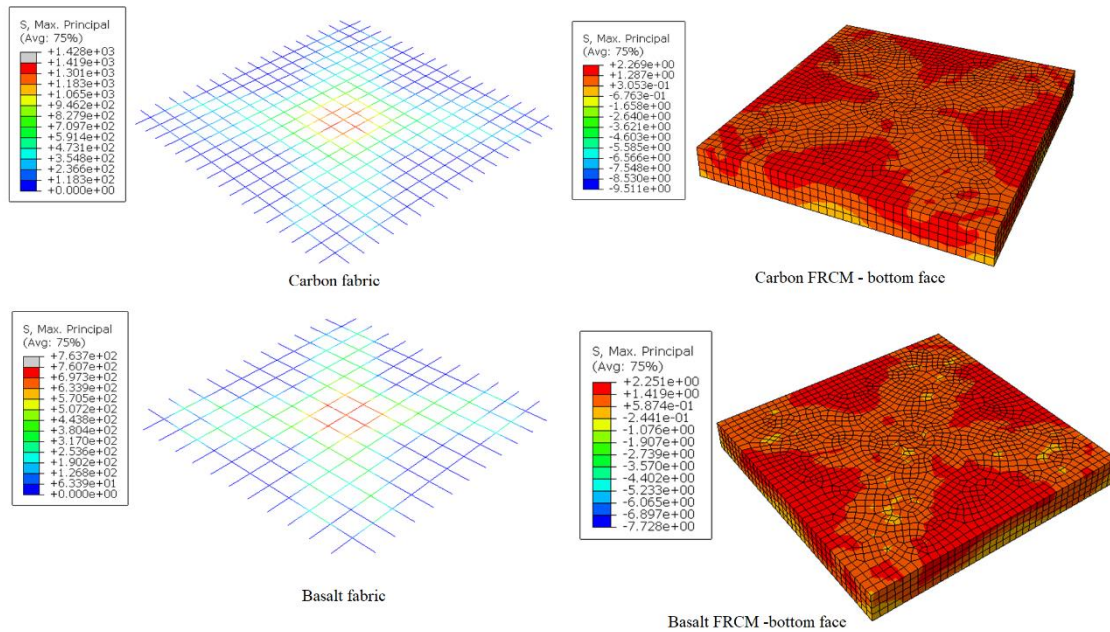
446 In carbon-FRCM model, 34 "truss" elements were used (17 in weft direction and 17 in
447 warp direction), and in the basalt-FRCM were used 22 elements (11 in each directions).
448 These simulated tows in the FRCM-plates. These were defined as elastic material, where
449 the Young modulus was the presented in Table 2. Due that the bonding interaction
450 between the mortar and the fabrics was not known, it was considered the fabric totally
451 bonded to the matrix (embedded) without allowing slipping in the fabric-matrix interface.
452 The same boundary condition than for the unreinforced plate were imposed (section 5.2).
453 The mesh size used was set to 5 mm, the same than the deformable solid modelling in
454 section 5.2.

455

456 5.4. FRCM-plate results

457 Figure 13 shows the stress contour plots of the matrix and the reinforcement fabric at the
458 state when the fabric reached the tensile stress taken as failure criterion. The tensile stress
459 taken as failure criteria was determined for each type of fibres by comparing the mean
460 maximum load from the experimental results with the numerical analysis results for each
461 punch size loading. From this initial result it was possible to determine the average tensile
462 stress in the fibres when the numerical analysis reached the experimental maximum load
463 (see Figure 13).

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Figure 13. Stress state of the fabric and mortar simulation at the time to reach the failure criteria

470 The principal stress in the matrix of the FRCM plates shown in Figure 13 describes
471 failures mode similar to the experimental results.

472 The tensile stress of carbon fabric was 1419.33 MPa (coefficient of variation of 4% for
473 the three punch size used), and 763.7 MPa (0%) for the basalt fabric. These values are
474 74% of the carbon-fabric tensile strength, and exactly the tensile strength of the basalt-
475 fabric (reaching the tensile rupture). In the case of carbon-FRCM this result can be mean
476 that for this percentage of fabric tension strength, the fabric sliding starts.

477 The fabric sliding (carbon-FRCM) and the fabric rupture (basalt-FRCM) were the type
478 of failure observed in the experimental campaign (section 3.2.1). Although, in the
479 analytical model (section 4.3) the percentage of carbon tensile strength when the fabric
480 sliding started was 38%. The difference between the numerical and analytical results may
481 be due to the fact that the numerical model considers a full 3D that allows to increase the
482 bidirectional fabric contribution in contrast to the 1D simplification of the analytical
483 model.

484 Also this sliding failures were presented in a previous experimental tensile study of
485 carbon-FRCM [30], where the sliding tensile stress was 57% of the tensile fabric strength.
486 This mean that the flexural behavior of the FRCM-plate improves 17% the fabric sliding
487 stress, maybe because of the out-of plane normal stress induced friction.

488 The results obtained from the numerical model are presented in Table 6. This shows the
489 results of maximum load (P_{max}) and the initial stiffness coefficient (K_i) for all the punch
490 diameters. The initial stiffness was calculated from the first slope in the load-displacement
491 curve presented in Figure 14.

492
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Table 6. Numerical model results.

Fibres	Properties	D16	D30	D63
Basalt-FRCM	F_{max} (KN)	1.95	2.25	3.07
	Δ_{exp}	-13%	-5%	0%
	K_i (KN)	2.28	3.18	4.47

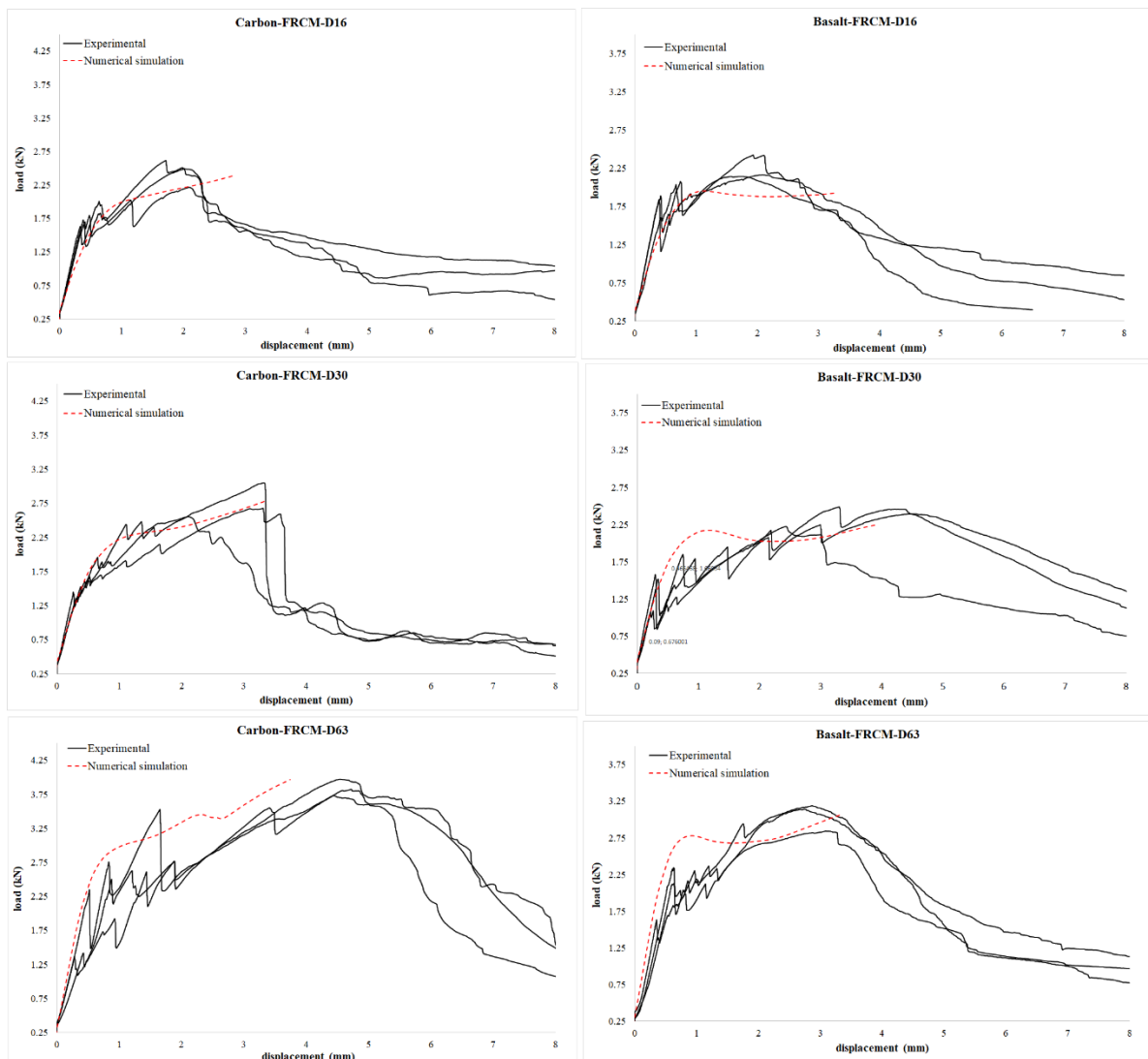
	Δ_{exp}	-40%	-14%	16%
	F_{max} (KN)	2.38	2.78	3.97
Carbon-FRCM	Δ_{exp}	-2%	1%	3%
	K_i (KN)	2.29	2.62	4.41
	Δ_{exp}	-41%	-26%	24%

Δ_{exp} : variation with the experimental results

494

495 The results presented in Table 6 show that maximum load results of the numerical model
 496 fit better the experimental results than the initial stiffness output.

497 Figure 14 show the contrast of the load-displacement diagrams of the experimental and
 498 numerical results. These demonstrate that the proposed numerical models are able to
 499 reproduce the experimental response with sufficient approximation. However, this
 500 numerical model is not capable to reproduce the sliding process. Including frictional
 501 and/or cohesive contacts may led to a more accurate model of the post-critic sliding
 502 response. Nevertheless, it is far beyond the scope of the current research.
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Figure 14. Contrast of the experimental and numerical load-displacement plots.

5 Conclusions

508 In this work, an experimental, analytical and numerical research was conducted to
509 investigate the flexural performance of FRCM plates. According the achieved results:

- 510 • The basalt and carbon fabrics improve the flexural capacity in load and stiffness.
511 Especially in the case of carbon-FRCM (D63) that improves 103% the maximum
512 load.
- 513 • The carbon-FRCM presented fabric sliding failures and the basalt-FRCM
514 presented fabric rupture failures. These types of failures were related to the degree
515 of bonding behavior between the different materials (fabric-mortar).
- 516 • The maximum load increased with the increase of the punch diameter. However,
517 the stiffness was not affected significantly by the increase of the punch diameter.
- 518 • The analytical and numerical analysis of FRCM may be performed similarly to
519 reinforced concrete. Concrete formulations and models were useful to calculate
520 the experimental results of this research.
- 521 • The mortar tensile strength and Young modulus were obtained from fitting the
522 analytical calculation of the load-bearing capacity of mortar plates without
523 fabrics. These values were successfully used to FRCM's numerical simulation
524 proving that unreinforced mortar properties are representative to the proposed
525 model.
- 526 • The tensile sliding stress of the carbon fabric was obtained by comparing the
527 experimentally determined maximum loads with the numerical results. The
528 carbon fabric started to slide when it reached the 74 % of its tensile strength.
- 529 • The proposed numerical model was able to reproduce the experimental maximum
530 load with sufficient approximation (between 0-13%). However, this numerical
531 model is not yet capable to reproduce the sliding process.

532

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538

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