A SCALING PROCEDURE FOR MODERN PROPELLER DESIGNS

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Abstract. The extrapolation procedures currently used to scale propeller characteristics tested at model scale to their full scale performances are either based on a statistical [1], the Lerbs-Meyne [2] or the recently developed strip method [3].

With the emergence of so-called unconventional propellers and different design strategies associated with them, it has been questioned whether the assumptions used in these scaling methods are still universally valid. E.g. with tip and root unloading employed, the circulation distribution deviates from the optimum, which is assumed by the Lerbs-Meyne method; more modern profiles show a different camber distribution and hence the drag coefficient must be aligned with the hydrodynamic inflow angle and not with the pitch to diameter ratio as assumed by the strip method (and implicitly by the ITTC 1978 method [4]).

The work presented still uses the assumption of the equivalent profile and will explain a modified scaling procedure showing a way to calculate the hydrodynamic inflow angle solely from one open-water test conducted at a constant Reynolds number. Finally exemplary results comparing a propeller of conventional type with a recent propeller designs will also be shown.

The new proposed method shows a superior performance when compared to other scaling methods.

1 INTRODUCTION

In recent years new propeller design philosophies have emerged into the market. The NPT-, Kappel- and CLT-propellers are examples of these so-called unconventional designs. From the very beginning it was claimed by their designers that full scale predictions based on the existing scaling methods do not reflect the actual performances observed. Based on the data available to the author this holds true for at least one of the above mentioned propeller types: The trial results regularly show a performance above the speeds predicted by different model basins. Generally speaking this behaviour never posed a problem in the past. With everybody now looking for the most efficient configuration, more and more propellers are comparatively tested and the final design is decided on the outcome of the performance predictions. Some propeller manufactures even take the scaling procedure used at the model basin into their consideration when designing a propeller for a comparative test to gain a little advantage over competitors. These tests pose a complete new challenge to the model basins, since tiny

differences – often as small as 0.01 kn – determine who wins the contract. This shows clearly that a more accurate scaling procedure is in high demand.

2 EXISTING SCALING PROCEDURES

Currently four main scaling procedures are used in model basins to scale the measured openwater data to full scale propeller performance:

- 1. No scaling
- 2. ITTC 1978 extrapolation method
- 3. Lerbs-Meyne method
- 4. Strip method

Independently of the scaling method applied, there are some local preferences in the implementation of the open-water tests, mainly concerning the Reynolds number used. Some model basins adheres strictly to the ITTC recommendation that the Reynolds number "must not be lower than $2 \cdot 10^5$ at the open-water test" [4] (some of them just fulfilling the recommendation running the open-water test at a Reynolds number of $2 \cdot 10^5$); some model basins conduct two tests (one at the Reynolds number experienced during the self-propulsion test and one above $2 \cdot 10^5$, using the lower to analyse the self-propulsion test, the other to scale to the full scale open-water curve); at least one model basin arranges for three open-water tests (one at the Reynolds number of the self-propulsion and two higher ones "to assess if the flow is fully turbulent"). If just one open-water test is conducted, it might or might not be scaled down to the Reynolds number experienced at the self-propulsion test.

2.1 No scaling

When predicting the full scale performance, the open-water test is not extrapolated to full scale, but a final correction factor is applied to the performance prediction.

2.2 ITTC 1978 extrapolation method

The ITTC 1978 extrapolation method assumes a linear correlation between the change in friction drag and change in thrust and torque coefficient [4]. But "it should be kept in mind that both the relation between thrust/torque and drag coefficient and the relation between drag coefficient and Reynolds number are based on statistics and the basis for the statistical values is very small" [1]. This very clear warning should always be kept in mind when judging the accuracy of any results using this extrapolation method. With the emergence of new profile types this warning becomes more and more vehemently – especially when comparing propellers using different profile types.

The second problematic characteristics of this scaling method is the linear dependence of the change in the thrust coefficient on the pitch to diameter ratio P/D. To explain the impact of this assumption, let us consider a propeller with a flat camber line and compare it to one, where all the lift is generated by camber alone. The first propeller will have a higher pitch because the lift is only generated by the angle of incidence. Even if this propeller will perform worse than the cambered one, it will be favoured by the extrapolation method and might show a scaled performance superior to the second, cambered propeller.

The ITTC 1978 extrapolation method insists to test the propeller model at a Reynolds

number "not […] lower than $2 \cdot 10^5$ at the open-water test" [4]. If you compared the performance extrapolated from open-water tests conducted at different Reynolds numbers you want to get the same values independently from the starting point. The left picture in figure 2 shows three full scale open-water curves of the same propeller but scaled up from different Reynolds numbers according to ITTC. Evidently the curve calculated from the lowest Reynolds number of about $2.5 \cdot 10^5$ is well above the ITTC 1978 recommendation of $2 \cdot 10^5$. The propeller shown in the right picture in figure 2 exhibits an even worse behaviour: There is a big difference in the extrapolated performances depending on the starting point. The first propeller tested was of a Wageningen B type, the second was of the modern NPT type. Both propellers were tested at the same model basin.

2.3 Lerbs-Meyne method

The Lerbs-Meyne method was published in 1968 [2] and derives a propeller with optimum distribution of circulation and no friction, that is the ideal propeller, from the open-water test at one Reynolds number. With an assumed drag ratio $\varepsilon_{0.7}$ of the so called equivalent profile at radius 0.7*R*, the measured values η and c_{TH} , the open-water efficiency and the thrust coefficient, respectively, can be converted to η_i and c_{THi} of the ideal propeller. However there is only one valid combination of η_i and c_{THi} which can be read of the Kramer diagram [5]. Most likely the calculated $\eta_i(\varepsilon_{0.7})$ and $c_{THi}(\varepsilon_{0.7})$ do not coincide with the valid combination, so $\varepsilon_{0.7}$ has to be adjusted in an iterative process until the valid combination is met. The full scale values are calculated with a friction coefficient of 0.006.

The Lerbs-Meyne method seems to be the perfect scaling method, since the profile drag is calculated from the actually measured open-water values and it is aligned with the inflow. There are only two drawbacks. Firstly, it is based on an equivalent profile which represents the whole propeller blade. Secondly, it assumes that the propeller blade was designed with an optimum circulation distribution. This poses a problem with modern propellers which are almost always wake adapted designs. The designer also often unloads the tip or root region or the diameter is restricted, so the assumption of optimum circulation distribution does not hold for all designs.

The figure 3 shows the scaled open-water tests.

2.4 Strip method

The strip method was developed by H. Streckwall of the HSVA model basin and published in 2013 [3]. When analysing the open-water test, the vector sum of the contributions of each radial section (strip) towards the friction resistance is calculated to get the friction resistance of the whole blade. When doing so, it takes into account the actual Reynolds number and the position of the transition point at the respective radial strip.

The strip method is certainly an advancement of the existing scale methods. The advantages are that it accounts for the actual turbulence in the inflow, e.g. in open-water and behind condition, by using two different friction lines. It also takes into account the actual distribution of chord length and pitch. The main problems are the alignment of the drag forces with the nose-tail pitch line instead of the actual inflow angle (see the respective note in section 2.2 about the ITTC 1978 extrapolation procedure) and the determination of the friction coefficients. As pointed out by Streckwall the calculation of the friction coefficient uses the local friction

coefficients for laminar and turbulent flow as stated by Hoerner [6] and the location of the transition point is derived from CFD calculations. These calculations were done for a set of propellers for two inflow conditions: One with low turbulence for the open-water curve, one with higher turbulence for the behind condition as expected during self-propulsion tests. Final curve fittings result in the two friction resistance curves for the open-water and the behind condition. These derived curves are used for all propellers disregarding of the actual profile used, whereas it is to be expected that the location of the transition point is strongly influenced by the section shape.

The scaled open-water tests can be found in figure 4.

3 ALTERNATIVE SCALING METHOD

In the author's opinion a scaling method which is independent of the propeller geometry can only be realized if the drag coefficient is not parallel to the nose-tail pitch line but aligned with the hydrodynamic inflow as the theory of thin profiles suggests. We will see in the following chapters that it is possible to calculate the hydrodynamic inflow angle from just one open-water test.

3.1 Equivalent profile

Let us imagine that the propeller is built up of circumferential sections stacked on top of each other and each section experiences a lift and drag coefficient c_d and c_l . The direction of action of these coefficients are aligned with the hydrodynamic inflow angle β_i . Geometric considerations lead to the formulae (1a+b) for the thrust and torque coefficients K_T and K_Q :

$$K_{T} = \frac{\pi^{2}Z}{4} \int_{x_{h}}^{1} \frac{c_{l}(x)\cos\beta_{i}(x) - c_{d}(x)\sin\beta_{i}(x)}{\left[\frac{\cos\beta(x)}{\cos(\beta_{i}(x) - \beta(x))}\right]^{2}} \frac{c(x)}{D} x^{2} dx$$

$$K_{Q} = \frac{\pi^{2}Z}{8} \int_{x_{h}}^{1} \frac{c_{l}(x)\sin\beta_{i}(x) + c_{d}(x)\cos\beta_{i}(x)}{\left[\frac{\cos\beta(x)}{\cos(\beta_{i}(x) - \beta(x))}\right]^{2}} \frac{c(x)}{D} x^{3} dx$$

$$(1a)$$

where

Z = the number of propeller blades,

x = the fractional radius r/R,

 x_h = the fractional radius r_h/R of the propeller hub,

c(x) = the length of the section at fractional radius x,

 $\beta(x)$ = the advance angle at fractional radius x,

 $\beta_i(x)$ = the hydrodynamic inflow angle at fractional radius x and

D = the propeller diameter.

At this point we introduce the concept of the equivalent profile: We replace the whole propeller blade with one single section of length \bar{c} located at the fractional radius \bar{x} such that this profile shows the same characteristics as the original blade. Using this equivalent profile we can replace the chord distribution and all hydrodynamic values in the integrand which depend on the fractional radius x with constant values and extract these from the integral. We denote these values of the equivalent profile with the overbar $\bar{}$:

$$K_{T} = \frac{\pi^{2} Z}{4} \frac{\overline{c}_{l} \cos \overline{\beta}_{i} - \overline{c}_{d} \sin \overline{\beta}_{i}}{\left[\frac{\cos \overline{\beta}}{\cos(\overline{\beta}_{i} - \overline{\beta})}\right]^{2}} \frac{\overline{c}}{D} \int_{x_{h}}^{1} x^{2} dx$$
(2a)

$$K_Q = \frac{\pi^2 Z}{8} \frac{\overline{c}_l \cos \overline{\beta}_i + \overline{c}_d \sin \overline{\beta}_i}{\left[\frac{\cos \overline{\beta}}{\cos(\overline{\beta}_i - \overline{\beta})}\right]^2} \frac{\overline{c}}{D} \int_{x_h}^1 x^3 dx$$
(2b)

(For an alternative formulation of the equivalent profile, which takes the distribution of the chord length and pitch into account, see [7].)

Note that for the equivalent profile the thrust and torque coefficients must remain the same as for the whole propeller blade, hence the overbar $\bar{}$ can be omitted.

After integration the equations (2a+b) become:

$$K_{T} = \frac{\pi^{2} Z}{4} \frac{\overline{c}_{l} \cos \overline{\beta}_{i} - \overline{c}_{d} \sin \overline{\beta}_{i}}{\left[\frac{\cos \overline{\beta}}{\cos(\overline{\beta}_{i} - \overline{\beta})}\right]^{2}} \frac{\overline{D}}{D} \frac{1 - x_{h}^{3}}{3}$$
(3a)

$$K_Q = \frac{\pi^2 Z}{8} \frac{\bar{c}_l \sin \bar{\beta}_i + \bar{c}_d \cos \bar{\beta}_i}{\left[\frac{\cos \bar{\beta}}{\cos(\bar{\beta}_i - \bar{\beta})}\right]^2} \frac{\bar{c}}{D} \frac{1 - x_h^4}{4}$$
(3b)

and finally

$$K_T = \varkappa_T B^2 \left(\overline{c}_l \cos \overline{\beta}_i - \overline{c}_d \sin \overline{\beta}_i \right) \tag{4a}$$

$$K_Q = \varkappa_Q B^2 \left(\overline{c}_l \sin \overline{\beta}_i + \overline{c}_d \cos \overline{\beta}_i \right)$$
(4b)

using the following abbreviations for convenience:

$$\varkappa_T = \frac{\pi^2 Z \,\overline{c}}{4} \frac{1 - x_h^3}{D} \tag{4c}$$

$$\varkappa_Q = \frac{\pi^2 Z}{8} \frac{\overline{c}}{D} \frac{1 - x_h^4}{4} \tag{4d}$$

$$\varkappa = \frac{\varkappa_Q}{\varkappa_T} = \frac{3}{8} \frac{1 - x_h^4}{1 - x_h^3} \tag{4e}$$

$$B = \frac{\cos(\overline{\beta}_i - \overline{\beta})}{\cos\overline{\beta}} \tag{4f}$$

Furthermore the advance angle $\bar{\beta}$ is known for a given advance coefficient *J*:

$$\tan\overline{\beta} = \frac{v_0}{\omega\overline{r}} = \frac{J}{\pi\overline{x}} \tag{4g}$$

The theory of aerofoils states that the lift coefficient \bar{c}_l does not change with the Reynolds number [8]. We can (reasonably) assume that if the lift does not change, the induced velocities

will not change either, hence the hydrodynamic inflow angle $\bar{\beta}_i$ does not change with the Reynolds number for any given value of *J*, hence the coefficient *B* and the lift coefficient \bar{c}_l stay constant for a fixed *J*-value. This assumption will certainly hold true as long as no flow separation occurs:

Let us recapitulate the dependencies on the advance coefficient J, the fractional radius \bar{x} and the Reynolds number \overline{Rn} of the equivalent profile of each variable:

$$\vec{c} = \vec{c}(\vec{x})$$

$$K_T = K_T(J, \overline{Rn})$$

$$K_Q = K_Q(J, \overline{Rn})$$

$$\vec{c}_d = c_d(J, \overline{Rn}, \vec{x})$$

$$\vec{c}_l = c_l(J, \vec{x})$$

$$\vec{\beta} = \vec{\beta}(J, \vec{x})$$

$$\vec{\beta}_i = \beta_i(J, \vec{x})$$

$$\kappa_T = \kappa_T(\vec{x})$$

$$\kappa_Q = \kappa_Q(\vec{x})$$

$$\kappa = B(J, \vec{x})$$

3.2 Determination of the hydrodynamic inflow angle $\overline{\beta}_i$ from just one open-water test

The thrust and torque coefficients K_T and K_Q depend on the advance coefficient J and the Reynolds number \overline{Rn} :

$$K_T = K_T(J, \overline{\mathrm{Rn}}) \tag{5a}$$

$$K_Q = K_Q(J, \overline{\mathrm{Rn}}) \tag{5b}$$

Traditionally these equations are looked at with the Reynolds number $\overline{\text{Rn}}$ fixed resulting in the well-known open-water curves $K_T(J)|_{\overline{\text{Rn}}}$, $K_Q(J)|_{\overline{\text{Rn}}}$. If the same propeller were tested at different Reynolds numbers, the three-dimensional surfaces $K_T(J, \overline{\text{Rn}})$ and $K_Q(J, \overline{\text{Rn}})$ can be constructed. Cutting these surfaces at constant *J*-values result in the open-water curves $K_T(\overline{\text{Rn}})|_J$ and $K_Q(\overline{\text{Rn}})|_J$ depending only on the Reynolds number. Omitting $|_J$, which indicates that the *J*-value is fixed, for clarity, equations (4a+b) are written for fixed values of *J* as

$$K_T(\overline{\mathrm{Rn}}) = \varkappa_T B^2 \left[\overline{c}_l \cos \overline{\beta}_i - \overline{c}_d(\overline{\mathrm{Rn}}) \sin \overline{\beta}_i \right]$$
(6a)

$$K_Q(\overline{\mathrm{Rn}}) = \varkappa_Q B^2 \left[\overline{c}_l \sin \overline{\beta}_i + \overline{c}_d(\overline{\mathrm{Rn}}) \cos \overline{\beta}_i \right]$$
(6b)

We can isolate the lift and drag coefficients \bar{c}_l and $\bar{c}_d(\overline{\text{Rn}})$:

$$B^{2} \overline{c}_{l} = K_{Q}(\overline{\mathrm{Rn}}) \frac{\sin\overline{\beta}_{i}}{\varkappa_{Q}} + K_{T}(\overline{\mathrm{Rn}}) \frac{\cos\overline{\beta}_{i}}{\varkappa_{T}}$$
(7a)

$$B^{2} \overline{c}_{d}(\overline{\mathrm{Rn}}) = K_{Q}(\overline{\mathrm{Rn}}) \frac{\cos\overline{\beta}_{i}}{\varkappa_{Q}} - K_{T}(\overline{\mathrm{Rn}}) \frac{\sin\overline{\beta}_{i}}{\varkappa_{T}}$$
(7b)

We differentiate the first equation (7a) with respect to the Reynolds number \overline{Rn}

$$0 = \frac{\mathrm{d}K_Q}{\mathrm{d}\overline{\mathrm{Rn}}} \frac{\mathrm{sin}\overline{\beta}_i}{\varkappa_Q} + \frac{\mathrm{d}K_T}{\mathrm{d}\overline{\mathrm{Rn}}} \frac{\mathrm{cos}\overline{\beta}_i}{\varkappa_T}$$
(8)

and multiply by $d\overline{Rn}$

$$0 = dK_Q \frac{\sin\overline{\beta}_i}{\varkappa_0} + dK_T \frac{\cos\overline{\beta}_i}{\varkappa_T}$$
(9)

Now we can isolate the hydrodynamic inflow angle $\bar{\beta}_i$:

$$\tan \overline{\beta}_i = -\frac{\varkappa_Q}{\varkappa_T} \frac{\mathrm{d}K_T}{\mathrm{d}K_Q} = -\varkappa \frac{\mathrm{d}K_T}{\mathrm{d}K_Q} \tag{10a}$$

or when using absolute thrust and torque figures:

$$\tan \overline{\beta}_i = -\varkappa \frac{D dT}{dQ} \tag{10b}$$

Any of these two last equations determine the hydrodynamic inflow angle $\bar{\beta}_i$ over the whole range of the advance coefficient *J* just from the slope of the $K_T(K_Q)$ -curve. This relationship is strictly speaking only valid if the thrust and torque were measured at a constant Reynolds number (see [7] how this can be achieved). Now the equation (10a) can be rewritten as

$$\tan\overline{\beta}_{i} = -\varkappa \frac{\frac{\partial K_{T}}{\partial I}}{\frac{\partial K_{Q}}{\partial I}}$$
(10c)

which facilitates the calculation, if the K_T and K_Q curves are given in their polynomial form.

With $\bar{\beta}_i$ known, the lift and drag coefficients can be calculated by evaluating equations (7a) and (7b). It is worth noting, that these three values do not depend on the location \bar{x} of the equivalent profile.

4 FULL SCALE EXTRAPOLATION

The analysis presented above yields the values of the lift and drag coefficients \bar{c}_l and \bar{c}_d and the hydrodynamic inflow angle $\bar{\beta}_i$ for a particular open-water test (equations (7a), (7b), and (10a, b or c)). These values can be scaled separately using the theory of aerofoil sections and the corresponding experimental results.

4.1 Scaling the lift coefficient \bar{c}_l

Using results from the profile theory, it can be assumed that the lift coefficient \bar{c}_l remains constant when the Reynolds number changes.

Sometimes it is claimed that this assumption does not generally hold for all cases. There is no reason why the lift coefficient cannot be scaled with any appropriate method already existing or becoming available in the future.

4.2 Scaling the hydrodynamic inflow angle $\overline{\beta}_i$

If the lift coefficient and hence the lift do not change, the induced velocities will not change either. That is equivalent to the statement that the hydrodynamic inflow angle $\bar{\beta}_i$ does not

change with changes in the Reynolds number. If the lift coefficient \bar{c}_l were to be scaled, it is to be assumed that the influence on $\bar{\beta}_i$ is negligibly small and hence can be neglected.

That leaves us with the drag coefficient \bar{c}_d to be scaled.

4.3 Scaling the drag coefficient \overline{c}_d

The drag coefficient of a section can be split into a contribution of the friction and the section form drag, \bar{c}_f and $\bar{c}_{d,2d}$, respectively [1][4][8]:

$$\overline{c}_d = 2\overline{c}_f \cdot \overline{c}_{d,2d} \tag{11}$$

Abbott and von Doenhoff [8] give the section form drag as

$$\overline{c}_{d,2d} = 1 + 2\frac{\overline{t}}{\overline{c}} + 60\left(\frac{\overline{t}}{\overline{c}}\right)^4 \tag{12}$$

(Often the term $60(\bar{t}/\bar{c})^4$ is not taken into account, because its contribution is very small.) The ITTC [4] recommends the following friction line:

$$\overline{c}_f = \frac{0.04}{\overline{\mathrm{Rn}}^{1/6}} - \frac{5}{\overline{\mathrm{Rn}}^{2/3}}$$
(13)

Analyzing the data available to the author using these two empirical formulae show that the drag coefficients calculated with equations (7b) and (11) differ substantially. Kuiper mentions in his book [1] that van Oossanens introduces a drag coefficient \bar{c}_{d3} to account for "three-dimensional effects", which is added to the profile drag:

$$\overline{c}_d = 2\overline{c}_f \cdot \overline{c}_{d,2d} + \overline{c}_{d3} \tag{14}$$

According to these authors this three-dimensional added drag coefficient \bar{c}_{d3} does not change with the Reynolds number.

In the author's opinion a proportional factor $\bar{c}_{d,3d}$ is more suitable and would fit into the concept of the (two-dimensional) section form drag $\bar{c}_{d,2d}$:

$$\overline{c}_d = 2\overline{c}_f \cdot \overline{c}_{d,2d} \cdot \overline{c}_{d,3d} \tag{15a}$$

If no flow separation occurs, the section form drag $\bar{c}_{d,2d}$ only depends on geometrical features but neither on the Reynolds number nor on the advance coefficient, hence it is constant. The factor $\bar{c}_{d,3d}$ accounts for the three-dimensional effects of the flow around the propeller and hence depends only on the advance coefficient. (Strictly speaking there will be an influence of the Reynolds number as well, since the thickness of the boundary layer changes and hence the three-dimensional flow around the propeller. For the moment we deliberately disregard this small effect.) The friction drag coefficient \bar{c}_f depends strongly on the Reynolds number:

$$\overline{c}_d(J,\overline{\mathrm{Rn}}) = 2\overline{c}_f(\overline{\mathrm{Rn}}) \cdot \overline{c}_{d,2d} \cdot \overline{c}_{d,3d}(J)$$
(15b)

If the friction coefficient \bar{c}_f were known, the three-dimensional drag $\bar{c}_{d,3d}$ can be calculated from the model test. Finally the drag coefficient \bar{c}_d for any scale can be reassembled with the friction coefficient \bar{c}_f for the selected Reynolds number, e.g. full scale propeller or self-propulsion test.

4.4 Scaling the friction drag coefficient \bar{c}_f

The scaling of the friction drag with the Reynolds number is a matter of ongoing discussion. In the scope of this paper only some observations or suggestions should be made.

The difficulty of scaling propellers stems from the fact that the Reynolds numbers reached during open-water tests fall into the transitional region where the flow over the blades is not fully turbulent yet and the laminar region spreads over a substantial part of the propeller blade.

The traditional way to scale the friction drag coefficient \bar{c}_f is to use friction lines derived from experiments. One line which is universally used in the field of naval architecture is the ITTC 1978 friction line, equation (13). The note made in section 2.2 should always be kept in mind.

For alternative approaches see [7].

5 EXAMPLARY RESULTS

A NPT propeller designed by Stone Marine Propulsion and a conventional propeller of the Wageningen B type were tested at three different Reynolds numbers at the model basin of SSPA in Gothenburg (table 1 and figure 1). All six open-water curves were scaled according to the ITTC 1978 (figure 2), the Lerbs-Meyne (figure 3), the strip method (figure 4) and the proposed alternative method (figure 5). The new method uses the ITTC 1978 friction line to calculate \bar{c}_f .

	Conventional	NPT	
D	7.3	6.8	m
P/D	0.673	0.902	_
$\overline{c}_{0.7}$	1.9563	1.799	m
A_e/A_0	0.53	0.460	_
Z	4	4	_
λ	33.1818	27.143	_
Туре	Wageningen B	New Profile Technology	

Table 1: Main particulars of the propellers analyzed.

It is noticeable that the lowest Reynolds numbers of $2.5 \cdot 10^5$ and $3.5 \cdot 10^5$ is too low for all methods. The first three methods work reasonably well for the conventional propeller, whereas the scaled values for the NPT propeller shows a noticeable gap between the efficiencies extrapolated from the different Reynolds numbers.

Applying the new method to the conventional propeller moves the efficiency curves scaled from the two higher Reynolds numbers on top of each other. For the NPT propeller the difference between these efficiency curves decreases noticeably.

6 CONCLUSIONS

An alternative method to extrapolate open-water performance data was presented. It makes use of the concept of the equivalent profile. It is entirely independent of the propeller geometry or the blade loading and works for all propellers which do not experience flow separation. By calculating the hydrodynamic inflow angle from just one set of open-water curves, it is able to align the drag and friction forces to the actual inflow as the theory of wings suggests. This alternative method has the potential to replace the existing methods as shown in the exemplary results.

This new method should be applied to as many performance predictions as possible and compared with the respective trials data to validate its suitability. This can only be done by a model basin which has the extensive data base to make this comparison reliable.

It was also shown that the ITTC 1978 recommendation for a minimum Reynolds number of $2 \cdot 10^5$ might be too low and it should be considered to be raised.

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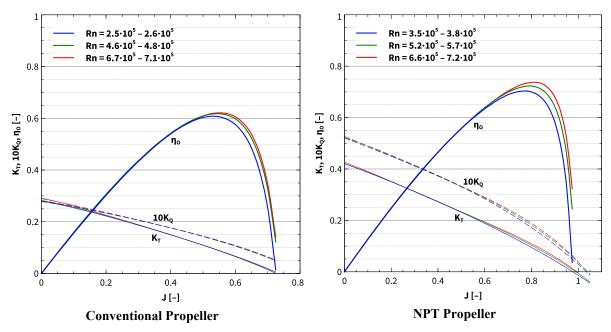


Figure 1: Open-water characteristics, measured values.

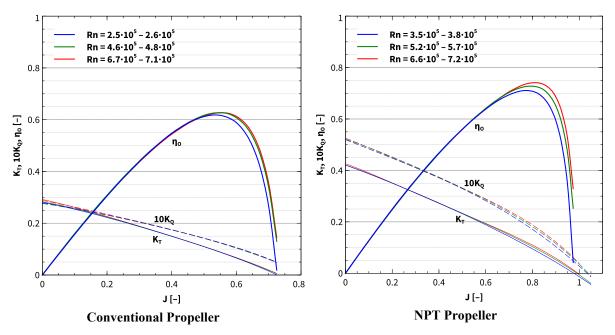


Figure 2: Open-water characteristics scaled according to the ITTC 1978 method.

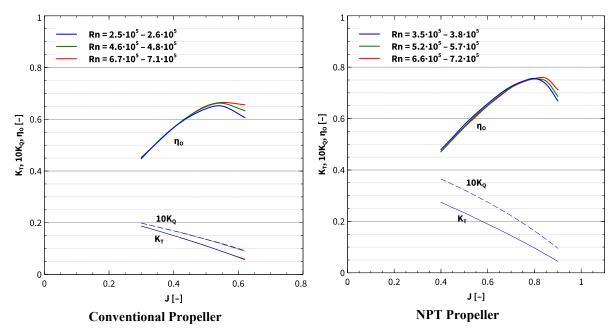


Figure 3: Open-water characteristics scaled with the Lerbs-Meyne method. (Courtesy of H. Streckwall.)

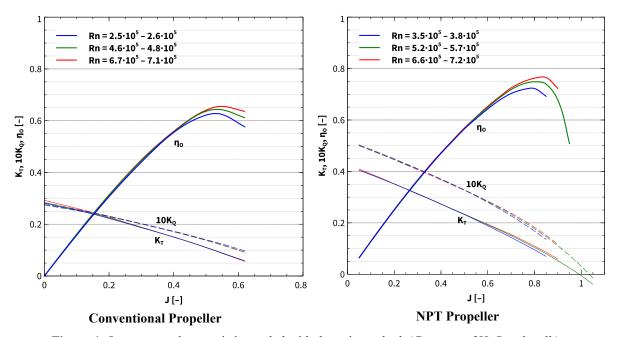


Figure 4: Open-water characteristics scaled with the strip method. (Courtesy of H. Streckwall.)

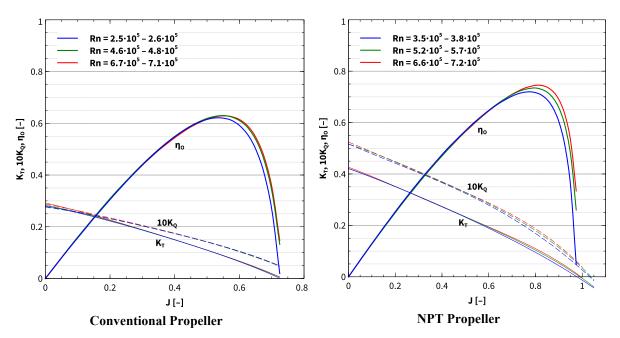


Figure 5: Open-water characteristics of the conventional propeller, scaled with the new method.