Probabilistic mapping of earthquake-induced submarine landslide susceptibility in the South-West Iberian margin

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ABSTRACT

The SW Iberian continental margin is well recognized as a tectonically active area, where major canyons and mass wasting events are both present. Earthquake triggered submarine landslides may cause tsunami and result in catastrophic damage to bordering coastal areas. In this setting, submarine landslide susceptibility mapping represents a major step towards a regional risk mitigation strategy. Landslide susceptibility mapping in large offshore areas presents significant challenges as a result of the limited information on controlling variables, large uncertainties in triggering mechanisms and limited geotechnical data. In this study, a geotechnical model-based approach has been followed that narrows the range of controlling factors and, within a probabilistic framework, allows a systematic treatment of parameter uncertainties. This model-based analysis covers the whole SW Iberian margin increasing by three orders of magnitude the areal extent of precedent offshore slope stability susceptibility studies. This jump in spatial scale is facilitated by application of a systematic Bayesian updating procedure, to combine geotechnical information from global databases and that available from regional sites. Seismic shaking is estimated using an available regional database of seismogenic faults. These tools are implemented within a GIS to generate, via Montecarlo simulations, probabilistic landslide susceptibility maps based on two different analytical seismic infinite slope stability models. These models differ mainly in the form of their final results, either as distributions of slope stability safety factors or as distributions of seismic-triggered slope displacements. Receiving Operator Curves are used to assess the different landslide susceptibility predictions obtained against a comprehensive regional database of submarine landslides. It turns out that the models analyzed correctly predict 92% and 82% of the mapped landslide subset chosen for validation for pseudo-static and displacement-based method respectively. This suggests that, within the limits of the currently available databases, seismic events are the dominant factor at the origin of the submarine landslides mapped in the study area. An advantage of the framework presented is that it can quickly incorporate new regional geological information or better regional landslide databases, as they become available.

1. Introduction

Submarine landslides are widespread in all continental margins and compared to their subaerial counterparts, they have larger magnitude and frequently occur on gentler slopes (Hüherbach et al., 2004; Chaytor et al., 2009; Urgeles and Camerlenghi, 2013; Behrmann et al., 2014; Huhn et al., 2019). Submarine landslides may impact directly on underwater structures and are also capable of generating destructive tsunami waves (Synolakis et al., 2002; Lavhol, 2019). Several historical and instrumental examples prove the connection between earthquakes and submarine landslides (e.g., Piper et al., 1999; Geist, 2000; Sassa and Takagawa, 2018) and earthquakes are generally recognized as the main triggering mechanism for tsunami-generating offshore landslides (ten Brink et al., 2009; Grilli et al., 2009).

Incorporation of landslide generated tsunamis into probabilistic tsunami hazard assessments is considered particularly difficult (Grezio et al., 2017), as large uncertainties affect the probability and location of slope failures. Susceptibility maps are used to predict where a landslide...
is likely to occur (Guzzetti et al., 2006) and are recognized as a key step in onshore landslide hazard analyses (Corominas et al., 2014). The intensity of seismic shaking is an important component for landslide susceptibility maps, both onshore (Jibson et al., 2000; van Westen et al., 2008) and offshore (Lee et al., 1999; Urgeles et al., 2002).

There are different approaches to map landslide susceptibility (Reichenbach et al., 2018), including heuristic (or index-based), statistical and probabilistic methods. Heuristic or index-based methods have been applied to map susceptibility offshore (Hitchcock et al., 2010; Leon and Somoza, 2011). However, they express landslide susceptibility in qualitative terms. Statistical methods are used onshore to map landslide susceptibility at regional scales, quantifying the probability of failure (Zhu and Huang, 2006; Chauhan et al., 2010). The application of similar methods offshore (Borrell et al., 2016; Piedade et al., 2018) faces severe difficulties, because the number of thematic variables available for prediction is limited by the scarcer data available.

Quantitative probabilistic prediction is also possible using a process-based approach to map susceptibility (Jibson et al., 2000; Reichenbach et al., 2018). In this approach models are used to represent the physical process producing landslides. For earthquake triggered submarine landslides suitable models may be based on the infinite slope concept with effective stress-normalized undrained strength parameters (Lee and Edwards, 1986).

Lee et al., (1999) integrated a simplified infinite slope model with GIS technology to map spatial variability of slope failure susceptibility in a relatively small area (approx. 400 km²) offshore California; Urgeles et al., (2002) produced a landslide susceptibility map for the Saguenay Fjord (140 km² in Quebec, Canada); Mackenzie et al. (2010) used GIS-based landslide hazard analysis in offshore oil and gas projects with development areas of over 1,000 km²; Strasser et al. (2011) presented a landslide susceptibility map for the whole of Lake Lucerne (114 km²). In all these examples the slope stability models were treated deterministically, using best estimates and/or worst-case scenarios, as relevant. Nevertheless, it is desirable to move from deterministic to probabilistic susceptibility assessments, as they offer a more consistent framework to express the effect of inevitable input uncertainties in the results. Probabilistic assessment is also consistent with the needs of tsunami hazard studies (Pampell-Manis et al., 2016; Grezio et al., 2017). Precedent probabilistic approaches using infinite slope models include Carlton et al. (2017) and Puzrin et al. (2017) who mapped landslide hazards for areas not larger than a few hundred km² in the Lofoten Islands and Caspian Sea respectively. Puzrin et al. (2017) used a more complex model incorporating the concept of shear band propagation in the analysis.

The challenge addressed here is to extend that previous work to the much larger areas involved in regional mapping. For this purpose, the SW Iberian margin has the advantage of counting with relatively good databases of both potential earthquake sources and observed submarine landslides. On the other hand, the geotechnical information currently available for the region is rather sparse, as is often the case in most marine studies. This limitation is addressed here, for the first time in mapping landslide susceptibility in the offshore environment, using a Bayesian methodology to combine the existing regional information and that given by worldwide-sourced databases. Bayesian methods are useful because they allow a systematic treatment of uncertainties and they can easily incorporate newly obtained information. These advantages are now widely recognized, both in the field of geotechnical characterization (Wang et al., 2016) and in that of tsunami hazard studies (Grezio et al., 2017).

2. Geological setting

The SW Iberian continental margin is characterized by the interplay of complex tectonic activity between the Iberian and African plates. Seismicity is characterized by shallow to deep earthquakes of low to moderate magnitude ($M_w < 5.5$) (Buforn et al., 1995, 2004; Stich et al., 2005; Stich et al., 2007; Stich et al., 2010), but also includes the largest and most destructive earthquakes in Western Europe (1531 CE, 1722, 1755 and 1969) (Fukao, 1973). The 1755 Lisbon Earthquake (estimated $M_w > 8.5$) destroyed the city (intensity X-XI MSK) and was accompanied by tsunamis that devastated the SW Iberian and NW African coasts (Baptista et al., 1998; Baptista and Miranda, 2009). Wide angle seismic data shows that most seismicity is due to onset of subduction west of the Gulf of Cadiz Imbricated wedge (Martínez-Lorente et al., 2014). Active fault structures there correspond to NE-SW trending west-verging folds and thrust faults (Gracia et al., 2003; Zitelli et al., 2004; Terrinha et al., 2009). In addition, long WNW-ESE dextral strike-slip faults are also present (Zitelli et al., 2009; Terrinha et al., 2009; Bartolome et al., 2012; Hensen et al., 2015).

Submarine landslides are also ubiquitous in Gulf of Cadiz (Urgeles and Camerlenghi, 2013). Infrequent large volume events are capable of tsunami generation (Lo Iacono et al., 2012). In the Gulf of Cadiz (Fig. 1), landslides and turbidites have been used as a proxy for off-fault
paleoseismic seismology. For instance, landslides such as the Marques de Pombal slide and the North Gorringe debris avalanche (Vizzaino et al., 2006; Lo Iaco, Lo Iacono et al., 2012), are associated to active faults and were likely seismically triggered.

3. Data sources

The SW Iberian margin covers an area of approximately 458,400 km² from 33°0′ to 38.7°0′N and from 15.6°0′ to 6°0′ W, including the coasts of Spain, Portugal and Morocco. Available data for the area include a digital elevation model (DEM) (Fig. 1) constructed from multibeam bathymetric data (spatial resolution 115x115 m) that was collected in a total of 19 cruises from different European institutions (Zitellini et al., 2009) and compiled as part of the EMODnet bathymetry initiative (EMODnet Bathymetry Consortium, 2018).

The fault database used in this study is the European Database of Seismogenic Faults (EDSF; Basili et al., 2013). This database includes faults that are deemed to be capable of generating earthquakes of magnitude equal to or larger than 5.5 $M_s$ and contains fault plane geometry information and a series of fault parameters such as strike, dip, rake, slip and earthquake magnitude information. In this study, the database was restricted to include only faults whose possible quake epicenters are mostly located offshore. This criterion is in line with that applied in the evaluation of probabilistic seismic hazard in the offshore scenario for structures in Portugal (Costa et al., 2008; Sousa and Oliveira, 1997).

A continuously updated landslide catalogue for the SW Iberian margin is being compiled at the Institute of Marine Sciences (CSIC) of Barcelona, systematically gathering previous data in the area (e.g., Baraza et al., 1999; Pajarón et al., 2015; Gracía and Lo Iacono, 2008; Leon and Somoza, 2011; Mulder et al., 2009; Hanquez et al., 2007). An earlier version of this catalogue is presented in Urgelles and Camerlenghi (2013). The landslide inventory includes information on typology, area, volume, thickness and depth of failure initiation.

Geotechnical data for the SW Iberian margin was gathered from different sources. Site location, water depth, and type of measurements are listed in Table 1; referenced locations are reported in Fig. 1.

4. Methodology

4.1. Overview

A dedicated GIS project was built for this study. Bathymetric data from the Gulf of Cadiz as well as information on submarine landslides, faults and geotechnical properties from the various databases were all imported into it. Operations within the GIS project are implemented using Python scripts with all input and output based on grid cells that represent 1 km x 1 km. Grid resolution was selected as a compromise amongst physical relevance, computational efficiency and possible loss of information due to averaging (Rodriguez-Peces et al., 2011).

A Montecarlo procedure (MC) is employed to obtain probabilistic landslide susceptibility maps using two different geotechnical slope stability assessment models. Two key aspects of the Montecarlo method are the selection of the stochastic inputs and the definition of probability density distributions for those inputs. In this work the stochastic input variables selected are slope gradient ($\alpha$), horizontal peak ground acceleration (PGA) and two geotechnical variables (i.e. normalized undrained shear strength $\gamma'_{undr}$ and normalized soil unit weight $\gamma'$).

In the precedent, $\gamma'_{undr}$ represents mobilized undrained shear strength, $\sigma'_{vo}$ effective vertical stress, $\gamma'$ total soil unit weight and $\gamma'$ effective soil unit weight. All the stochastic inputs are represented through density distributions that are different at each cell of the map. From these individual cell distributions random samples of the stochastic variables are drawn at each run.

To set up the individual cell distributions different procedures are employed, because the nature of the uncertainties represented is also different. The information available on slope gradient (i.e. bathymetric) is exhaustive in its coverage, but affected by measurement error. The probability distribution that accounts for this uncertainty can be set up once and for all at each cell.

Local -i.e. cell- distributions of PGA represent uncertainties in earthquake magnitude at the source and attenuation due to varying distance to the source. Assuming that the source catalogue (the EDSF; Basili et al., 2013) is also exhaustive, these effects can be computed and a PGA distribution set up once and for all at each cell. Note that any limitations of the source database (e.g. its completeness) add a layer of uncertainty to the results, which is not explicitly represented in the model.

When addressing the uncertainty in geotechnical parameters the situation is different. Each 1 km$^2$ cell may be thought of as representing a “geotechnical site”. At that cell-size, inherent ground variability in a site, even within the restricted soft soil classes assumed by the geotechnical models, is always significant (Dreyfus et al., 2013). That local variability is what is directly represented by the parameter distributions set up at each cell. However, this opens up the question of how to choose the statistics of those local distributions, since the regional geotechnical database is very sparse.

The answer given is to combine the available regional information with that contained in global databases to set up a regional-scale distribution of plausible statistics to describe geotechnical site variability. At each cell in the map any of these plausible geotechnical sites is something that is assumed to be random. Therefore, two levels of sampling are needed in each Montecarlo round to initialize geotechnical model inputs. First, the statistics for the cell distributions are selected or, in other words, a plausible “geotechnical site” is assigned to each cell. Afterwards those local distributions are themselves sampled to obtain parameter values.

Once cell input distributions are initialized (i.e., at each grid cell density distributions of $\gamma'_{undr}$, $\gamma'$, PGA are defined), they are sampled at each simulation to obtain single values of slope gradient, PGA, normalized sediment density and normalized undrained shear strength (Fig. 2). Using these inputs two slope stability models are computed at each cell in each run.

The first slope stability model represents seismic loading as a quasi-static action, but with quasi-static coefficients calibrated using permanent-displacement Newmark-type analyses (Rampello et al., 2010). The Montecarlo output, at each grid cell, is a lognormal distributed pseudo-static factor of safety $F_{Sp - stat}$. The probability of failure $P_f$ is simply evaluated as the number of simulated $F_{Sp - stat}$ lower than 1 over N simulations. Fig. 2a summarizes the workflow for this model.

In the second approach, the outputs are seismically induced Newmark displacements (Newmark, 1965), which are estimated using regressions with seismic ground motion, slope and geotechnical characteristics (Jibson, 2007). Direct application of the Newmark approach is computationally demanding for large-area mapping purposes and different indirect methods are used instead (Jibson, 2011). The Montecarlo output for each grid cell is a Newmark displacement probability density function PDF ($D_n$), which is also fitted to a lognormal distribution. This distribution may be used to compute exceedance probabilities for any chosen displacement $D_n$ threshold (i.e. $P_{\text{exceedance } D_n}$). Fig. 2b summarizes the workflow for this model.

4.2. Slope stability assessment models

4.2.1. Pseudo-static approach

The pseudo-static approach is frequently used for regional landslide hazard mapping (Jibson, 2011). In this approach, an equivalent seismic coefficient $k_s$ is introduced within a conventional limit equilibrium analysis. The infinite slope stability model can be expressed as (Lee and Edwards, 1986; Morgenstern, 1967):
<table>
<thead>
<tr>
<th>Type of data</th>
<th>Site Location</th>
<th>Cores</th>
<th>Water and subsurface depth information</th>
<th>Lithology description</th>
<th>Measurement methodology</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cu⁴⁺[v0]</td>
<td>Continental margin of Gulf of Cadiz.</td>
<td>37 118</td>
<td>From 30 m to 800 m water depth (cores up to 250 cm length from seabed)</td>
<td>Thin upper sand layer overlying a grayish olive, massive mud unit with bioturbation interlayered by silt unit</td>
<td>Vane shear measurements on the end of sections and for some split cores at 10-cm intervals.</td>
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<tr>
<td></td>
<td>Cores location: failed upper slope; stable upper slope; shelf mud-layer.</td>
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<td></td>
<td>Lee and Baraza, 1999, Fig. 1</td>
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<tr>
<td></td>
<td>Marquês de Pombal landslide.</td>
<td>4 287</td>
<td>From 2700 m up to 4000 m water depth (cores up to 500 cm length from seabed)</td>
<td>Mostly composed by silt and clay content with small sand fraction.</td>
<td>Fall cone penetrometer (Wykeham Farrance WF 21600) at 5-cm distance.</td>
</tr>
<tr>
<td></td>
<td>Cores location: Head scarp; Landslide body; Most distal lobe.</td>
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<td></td>
<td>Minning et al., 2006, Fig. 1</td>
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<td></td>
<td>ICM - 2018INSIGHT cruise</td>
<td>10 25</td>
<td>From 930 m up to 2667 m water depth (cores up to 264 cm length).</td>
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<td>Handheld vane shear measurements.</td>
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<td>Lower slope (Fig. 1)</td>
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<tr>
<td></td>
<td>Continental margin of Gulf of Cadiz.</td>
<td>7 14</td>
<td>From 30 m to 800 m water depth (cores up to 250 cm length from seabed)</td>
<td></td>
<td>Derived from water content.</td>
</tr>
<tr>
<td></td>
<td>Cores location: Failed upper slope; Stable upper slope; Shelf mud-layer.</td>
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<td></td>
<td>Lee and Baraza, 1999, Fig. 1</td>
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<tr>
<td></td>
<td>Marquês de Pombal landslide.</td>
<td>4 174</td>
<td>From 2700 m up to 4000 m water depth (cores up to 50 cm length from seabed).</td>
<td></td>
<td>Quantachrome pentapycnometer on 5 cm³ samples.</td>
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<tr>
<td></td>
<td>Cores location: Head scarp; Landslide body; Most distal lobe.</td>
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<td>Minning et al., 2006, Fig. 1</td>
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<td></td>
<td>Expedition 339: Gulf of Cadiz-W Iberian margin (Stow et al., 2013).</td>
<td>67 60</td>
<td>Up to 150 mbsf.</td>
<td>Uniform lithology composed mostly by bioturbated calcareous mud and calcareous clays.</td>
<td>Water content measurements on core specimens of 8 cm³. Volume of specimens measured by gas pycnometry.</td>
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<td></td>
<td>U1385 (Fig. 1)</td>
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<tr>
<td></td>
<td>Borehole location: SW Iberian margin</td>
<td>18 197</td>
<td>Up to 586 mbsf.</td>
<td>Nannofossil mud, calcareous silty mud, and silty bioclastic sand lithologies.</td>
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<td>U1386 (Fig. 1)</td>
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<td>Borehole location: Continental margin of Gulf of Cadiz: middle slope — 25 km south-southeast of the Portuguese city of Faro. Middle-slope contemporaneous deposits</td>
<td>86 275</td>
<td>Up to 870 mbsf.</td>
<td>Nannofossil mud, calcareous silty mud, and silty bioclastic sand lithologies generally organized as bi-gradational sequences.</td>
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<td>U1387 (Fig. 1)</td>
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<td>Borehole location: Continental margin of Gulf of Cadiz: middle slope, companion to Site U1386</td>
<td>24 47</td>
<td>Up to 1550 mbsf.</td>
<td>Strongly heterogeneous media mostly composed by silty mud, calcareous clay, sand, silty sand.</td>
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<td>U1388</td>
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<td>Borehole Location: This site is the site closest to the Strait of Gibraltar gateway.</td>
<td>107 278</td>
<td>Up to 990 mbsf.</td>
<td>Calcareous mud, silty mud, sandy mud, and silty bioclastic sand lithologies.</td>
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<td></td>
<td>U1389</td>
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<td>Borehole location: ~ 90 km west of the Spanish city of Cádiz. Site in the “channels and ridges” sector of Cadiz margin.</td>
<td>38 121</td>
<td>Up to 350 mbsf.</td>
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<td></td>
<td>U1390</td>
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<td></td>
<td>Borehole location: Second of two sites drilled in the channels and ridges sector of Cadiz margin.</td>
<td>56 188</td>
<td>Up to 672 mbsf.</td>
<td>Calcareous mud with minor lithologies including silty mud, sandy mud, nannofossil mud, and biosiliceous mud clayey foraminiferal nannofossil ooze.</td>
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<td>U1391</td>
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<td></td>
<td>Borehole location: 50 km northwest of Cape São Vicente, gently inclined middle-slope region.</td>
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<td></td>
<td>Total</td>
<td>5447 m</td>
<td>1166</td>
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<td></td>
<td>Total</td>
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<tr>
<td></td>
<td>DSDP Leg 79–546,79–545: Hinz et al., 1984, Fig. 1</td>
<td>60 76</td>
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</tr>
</tbody>
</table>

(continued on next page)
FS_{p-stat} = \frac{Cu}{\gamma'z \sin \alpha \cos k \cos \frac{p_{stat}}{h}} \quad (1)

with:
\( \alpha \): slope gradient;
\( \frac{Cu}{\gamma'z} \): normalized undrained shear strength.
\( \frac{p_{stat}}{h} \): normalized sediment unit weight;
\( k \): horizontal acceleration coefficient.

The horizontal acceleration coefficient is obtained as:

\( k_h = \eta \cdot PGA \) \quad (2)

where the coefficient \( \eta \) is applied to obtain a performance-based value of \( k_h \).

Values of \( \eta \) coefficients used here are taken from the work of Rampello et al. (2010). Following a well-established methodology (Bray and Rathje, 1998; Stewart et al., 2003), Rampello et al. (2010) provided a suite of \( \eta \) values by correlation with the output of stochastic permanent-displacement Newmark type analyses. Different \( \eta \) values are obtained for different levels of Newmark displacement \( D_n \) values and for different site conditions. In this work the \( \eta \) values used are those associated to 15 cm permanent Newmark displacement for subsoil conditions described as loose-to-medium cohesionless soil and/or soft-to-firm cohesive soil (see Bisch et al., 2012). Newmark displacement values are used as indicative thresholds at which slope failure might occur (Jibson et al., 2000). Table 2 shows that resulting \( \eta \) values are slightly dependent on \( PGA \) values. All Newmark analyses in Rampello et al. (2010) used an Italian strong-motion database (Scassera et al., 2009) resulting from records generated by shallow crustal earthquakes with \( M_w > 3.7 \). Lacking more specific studies for the SW Iberian margin, \( \eta \) values derived from the Italian database were considered as appropriate for the SW Iberian margin.

4.2.2. Displacement-based approach

In the Newmark method the slide mass is represented as a rigid block (Newmark, 1965). In absence of inertial forces, the stability of the block is given by the static factor of safety \( FS_{stat} \), here computed as:

\( FS_{stat} = \frac{\gamma'z \sin \alpha \cos k \cos \frac{p_{stat}}{h}}{\gamma'z} \) \quad (3)

with \( \frac{Cu}{\gamma'z} \) and \( \alpha \) previously described in eq. 2. Due to the seismic shaking, the critical acceleration, defined as the one that allows the block to glide (i.e., \( FS_{p-stat} = 1 \) in eq. 2) is then expressed as:

\( a_c = (FS_{stat} - 1) \tan(\alpha) \frac{\gamma'}{g} \) \quad (4)

Given an earthquake acceleration time history, values in excess of \( a_c \) are applied to the failing mass. Two integrations of the filtered acceleration history results in a cumulative permanent displacement of the sliding block relative to its base. The method used here (Jibson, 2007) evaluates Newmark displacements from correlation with a ratio between the critical acceleration of eq. 4 and \( PGA \):

\( \log_{10}(D_n) = 0.215 \log \left[ 1 - \frac{a_c}{PGA} \right]^{1.241} - 1.438 + \varepsilon_{log(D_n)} \) \quad (5)

where:
\( D_n \): Newmark permanent displacement [cm];
\( a_c \): critical acceleration in g;
\( \varepsilon_{log(D_n)} \): model uncertainty, given by a normal distribution \( N(0, \sigma_{log(a_c)}) \), with a standard deviation \( \sigma_{log(D_n)} = \pm 0.51 \);
\( PGA \): horizontal peak ground acceleration in g’s, which accounts for soft sediments ground motion amplification effects.
Fig. 2. a) Flow chart for pseudo-static slope stability probability model. b) Flow chart for displacement-based slope stability probability model.
Table 2

<table>
<thead>
<tr>
<th>Horizontal Peak Ground Acceleration (PGA) [g]</th>
<th>$\eta$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.3–0.4</td>
<td>0.22</td>
</tr>
<tr>
<td>0.2–0.3</td>
<td>0.22</td>
</tr>
<tr>
<td>0.1–0.2</td>
<td>0.25</td>
</tr>
<tr>
<td>$\leq0.1$</td>
<td>0.17</td>
</tr>
</tbody>
</table>

4.3. Treatment of model input uncertainties

4.3.1. Slope angle

Implicit in any DEM there is measurement error that propagates into slope angle uncertainty. Each multibeam system from which the DEM was obtained will introduce a slightly different error depending mostly on factors such as water depth, beam angle, bottom type and sea bottom geomorphology. As a consequence, the error in depth measurements would vary within a range of 0.04% to 0.15% for shallow water systems and from 0.2% to 0.5% for medium to deep water systems. A simplified approach has been taken in this study, and an average error value of 0.25% of the water depth is assumed throughout the DEM. Following Mudron et al. (2013), evaluation of the slope uncertainty in a DEM is quantified through a separate Monte Carlo procedure (Fig. 3a). Assuming a normal distribution for the DEM error, with 0 mean and quantified through a separate Monte Carlo procedure (Fig. 3a). As-Mudron et al. (2013), evaluation of the slope uncertainty in a DEM is 0.25% of the water depth is assumed throughout the DEM. Following Mudron et al. (2013), evaluation of the slope uncertainty in a DEM is quantified through a separate Monte Carlo procedure (Fig. 3a). Assuming a normal distribution for the DEM error, with 0 mean and standard deviation $\sigma_{\text{DEM}}$ equal to 0.25% of the water depth, a randomly perturbed DEM is generated for each Monte Carlo run (see example in Fig. 3b). The corresponding slope field is then evaluated using the $3 \times 3$ cell method as implemented in ArcGIS. After N simulations, a normally distributed slope angle is obtained for each cell. Convergence in slope statistics was observed after $N = 130$ simulations.

4.3.2. Horizontal peak ground acceleration

PGA values are usually derived from ground motion attenuation relationships, i.e. empirical correlations between maximum ground acceleration observed during an earthquake event at a given location and earthquake magnitude. The significant influence of magnitude in attenuation relationships is well recognized (Bommer et al., 2007). In particular, equations derived from large-magnitude events should not be extrapolated for prediction of ground motion from smaller events and vice versa. Mezcua et al., (2008) presented an attenuation relationship for the Iberian Peninsula, but cautioned against their use for the Gulf of Cadiz, as it was largely based in smaller magnitude events compared to those expected there. In the Gulf of Cadiz, shallow crustal earthquakes associated to $M_w$ greater than 5 are frequently recorded. For this reason, the PGA is evaluated using a more general approach proposed by Ambraseys et al. (2005), derived using Europe and Middle East large-magnitude events ($M_w > 5$). For soft soils this correlation reduces to:

$$\log(\text{PGA}) = 2.6595 - 0.142M_w + (-3.184 + 0.314M_w) \log \frac{d^2}{7.6} - 0.084F_N + 0.062F_T - 0.044F_D + \varepsilon$$

where:

- $\log(\text{PGA})$: logarithm of the horizontal peak ground acceleration [m s$^{-2}$];
- $M_w$: moment magnitude;
- $d$: Joyner-Boore distance [km] (i.e. distance to the surface projection of the fault);
- $F_N = 1$ for normal faulting, 0 otherwise;
- $F_T = 1$ for thrust faulting, 0 otherwise;
- $F_D = 1$ for other styles of faulting, 0 otherwise.
- $\varepsilon$: transformation uncertainty, modeled as $\sim N(0, \sigma_{\text{PGA}})$;
- $\sigma_{\text{PGA}} = \sqrt{(0.665 - 0.065M_w)^2 + (0.222 - 0.022M_w)^2}$.

This relation introduces a small dependency on fault mechanism that is taken into account in our determination of the PGA, as the EDSF (Basili et al., 2013) includes such information for all faults. The coefficients to the terms $F_N$, $F_T$ and $F_D$ imply that thrust faults will provide the most intense shaking compared to normal and strike-slip faults given an earthquake of the same magnitude ($M_w$) and at the same distance from the fault. The uncertainty introduced is clearly dependent on the $M_w$. For a magnitude range between 5.8 and 7.6, as for the case study, the uncertainty in ground motion prediction falls in the interval 0.31–0.18. The PGA for events in the upper range is therefore determined with somewhat higher accuracy.

For each fault, the catalogue provides 10 different estimates of maximum earthquake $M_w$ derived from different correlations. In the EDS catalogue all these estimates are computed assuming full-length fault activation. The seismic events considered in this study as landslide triggers would then all be associated with relatively large return periods. Considering such long return periods is also justified by the submarine landslide catalogue used to validate the analysis. Even if the date of the events in this catalogue is not always well constrained, their position in the uppermost sedimentary sequences indicates that they are all Quaternary.

![Flow chart for slope uncertainty quantification](a)

![Random DEM perturbation](b)

Fig. 3. a) Flow chart for slope uncertainty quantification, adapted from Mudron et al., 2013. b) Random DEM perturbation for $\sim N(0,0.25\%$ water depth). Axes show degrees latitude and longitude.
For each fault, the probabilistic description of $M_w$ is given by a uniform distribution covering the entire range of estimates. As a result, uncertainty associated to the PGA at a site is given by the combination of that in the Ambraseys et al. (2005) correlation and that of the $M_w$.

Again, a separate Montecarlo procedure is employed to build a lognormal distribution of PGA values at each map cell. The main steps in the procedure are depicted in Fig. 4. At each simulation a random seismic source is activated. For such fault a random value of $M_w$ is sampled from its uniform probability distribution to evaluate a PGA according to eq. 6 at all grid cells. The distribution statistics stabilizes after some 400 runs.

### 4.3.3. Geotechnical properties

The geotechnical information available for the study area is scarce. Some preliminary screening is possible: areas in which rock outcrops have been clearly identified (e.g. seamounts) are excluded from the analysis (Fig. 1). These areas appear as white spots in the maps (e.g. Fig. 3b). In addition to this, we assume that soft relatively fine sediments prevail, such that an undrained response to earthquake loading is plausible.

Given the large area (1 km$^2$) represented by each model cell, it is realistic to treat those as if they were different geotechnical sites. This, in turn, makes useful a conceptual scheme proposed by Zhang et al. (2004) in which the overall spatial inherent variability of geotechnical parameters is decomposed into within-site variability and cross-site variability. Within-site variability is embedded in the statistical distribution assigned to a particular geotechnical parameter in a cell. Cross-site variability is represented by the variability of statistical parameters describing different local (i.e. cell-based) distributions. For each of the geotechnical parameters involved $X_o$ (i.e. sediment unit weight or normalized undrained shear strength) lognormal distributions at each cell are used to represent within-site variability. The first step in each Montecarlo run (see Fig. 2) is, then, to set up these distributions at each cell, i.e. to randomly assign a “site” to every cell in the model. To do so, statistical distributions of means and variances for the different geotechnical properties are sampled. Such statistical distributions of means and variances (i.e. of statistics) are themselves described as lognormal random variables.

The available data from the site investigations in the area (Table 1) provide a starting point to evaluate the density distributions for different geotechnical parameter statistics. However, given their non-uniform spatial distribution and reduced overall number, direct extrapolation to the whole area seems unwarranted. To circumvent this problem, a Bayesian framework is adopted to integrate this regional information with more general soil parameter information –i.e., a worldwide sourced database.

In the scheme adopted, information from the global databases is used to set up prior distributions for statistics of geotechnical parameters. Making use of Bayes' rule such prior information is then integrated with the SW Iberian margin regional data (i.e. Data) to obtain updated probability density functions (i.e. posterior distribution) of the relevant statistics, − the mean and standard deviations for the local distributions of geotechnical parameters. Following Straub and Papaioannou (2015), Bayes' rule for a generic random variable $X$ is expressed as:

$$ f'(x) = aL(x)f'(x) $$

where:

- $f'(x)$ is the Prior probability density function for $X$.
- $f'(x)$ is the Posterior or updated probability density function for $X$, taking into account the Data.
- $L(x)$ is the likelihood or conditional probability of observing the Data when $X = x$.

### Table 3

Statistical inputs to the Bayesian updating procedure of geotechnical parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Mean</th>
<th>Standard Deviation</th>
<th>Prior Distribution</th>
<th>Posterior Distribution</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\mu_{Tc}$</td>
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<td>–</td>
<td>Uniform $[5.2-1.95]$</td>
<td>Uniform $[0.4-0.1]$</td>
</tr>
<tr>
<td>$\mu_{Tc}/\mu_T$</td>
<td>0.0086</td>
<td>0.0048</td>
<td>Uniform $[1.45-0.1]$</td>
<td>Uniform $[0.3-0.01]$</td>
</tr>
<tr>
<td>$\sigma_{Tc}$</td>
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<td>–</td>
<td>Uniform $[0.75-0.02]$</td>
<td>Uniform $[0.12-0.02]$</td>
</tr>
<tr>
<td>$\sigma_{Tc}/\mu_T$</td>
<td>0.4</td>
<td>0.22</td>
<td>Uniform $[1.75-0.1]$</td>
<td>Uniform $[0.4-0.01]$</td>
</tr>
</tbody>
</table>

Fig. 4. Flow chart for PDF(PGA) and PDF(\(\mu\)) estimation.

Fig. 5. Example of ROC curve for landslide susceptibility model.
is a normalizing constant; In this application, the random variables $X$ are the statistics (mean and standard deviation) of the geotechnical parameters. The two geotechnical parameters used in the models, normalized sediment unit weight and undrained shear strength, are considered mutually independent. The likelihood function can be expressed as:

$$L(x) = P(Data | \mu_x, \sigma_x) = \prod_{i=1}^{N_r} \frac{1}{\sqrt{2\pi}\sigma_x} \exp \left\{-\frac{1}{2} \left[ \frac{x_i - \mu_x}{\sigma_x} \right]^2 \right\}$$

with:

- $x_i$: statistics from geotechnical data (i.e. logarithms of mean or standard deviations obtained at each regional site), computed from data reported in Table 1;
- $N_r$: number of regional sites considered in the updating operation;
- $\mu_x$: logarithm of a possible mean for the variable $X$;
- $\sigma_x$: logarithm of a possible standard deviation value for the variable $X$;

The Bayesian updating scheme is computed numerically. This is done using a Markov Chain Monte Carlo (MCMC) method, using a Metropolis-Hasting algorithm implemented through a dedicated MATLAB script. The Montecarlo method is used to obtain a probability distribution for the target parameter, sampling the prior distribution. To guarantee statistical robustness, this Montecarlo computation is repeated in sequence, setting up a Markov chain in which the posterior of
the previous step is taken as new prior. See Wang and Cao (2013) for a detailed explanation of MCMC in a geotechnical context.

The computation of statistics at each site needs to account for different techniques used during data acquisition. In some cases, an empirical correlation was applied to transform the originally acquired data to a different strength measure (i.e. from fall cone test to vane shear strength). Such process adds a transformation error to the strength estimate. In such cases the original variability of a given dataset, represented by its standard deviation, $\sigma_0$, is increased by that of the transformation error, $\sigma_T$, to give (Phoon and Kulhawy, 1999a):

$$\sigma_f = \sqrt{\sigma_0^2 + \sigma_T^2}$$

(9)

The transformation error only affects part of the relevant collection of regional datasets. Therefore, a weighted average approach was used to account for this in the likelihood function:

$$\sigma_{f,T^*} = \frac{N_f}{N_T} \sqrt{\sigma_0^2 + \sigma_T^2}$$

(10)

with $N_T$ number of relevant data, and $N_f$ number of data affected also by the transformation error.

4.3.3.1. Normalized sediment unit weight. Regional sediment density
measurements are obtained from deep IODP boreholes (Table 1), as well as from short core data from other sources. Data obtained in the IODP boreholes at depths below 350 m.b.s.f. was excluded, because that is the maximum excavation depth of landslides in the catalogue. Fig. 6a presents histograms of normalized sediment unit weight data from all available cruises that collected geotechnical data in the area. The values indicate significant variability within a range of 2 to 3.2, (equivalent to $14.55 \leq \gamma_{\text{bulk}} [\text{kN/m}^3] \leq 20$). Fig. 6b presents adjusted lognormal distributions to the different datasets. From these adjusted curves a population of means and variances of site normalized unit weight is obtained. Normalized sediment unit weight (i.e. $\gamma_{\text{sw}}$) was determined using a variety of methods (Table 1). However, we missed specific information on the statistics of conversion rules between the different methods employed to derive soil unit weight measurements, so they all were deemed equivalent and, as indicated in Table 3, no transformation was applied.

Mayne (2014) collected a global database of soil unit weights containing 1049 values representative of 88 sites with different soil types. Amongst those, sites representative of soft clays, offshore soft clays, offshore firm clays and offshore stiff clays were selected to build a new dataset (i.e., clay-offshore dataset), to be used as Prior Information in the Bayesian updating procedure. For each site in that restricted clay-offshore dataset the mean and variance of bulk density was estimated. Histograms of the means and variances thus obtained are depicted in Fig. 7a. The mean values in the clay-offshore dataset lie mostly in the range [1.9–3.97], except for some outliers. Considering now the standard deviations (Fig. 7b), it appears that within-site variability for the clay-offshore dataset lies generally below 0.4, with only a few outliers having larger values.

The offshore-clay normalized unit weight statistics are fitted with uniform prior distributions, illustrated in Fig. 7. It was decided to use the uniform distribution as Prior as it represents a less strong

Fig. 10. a) Local mean maximum PGA expected values assuming that the fault activates at full-length. b) Local PGA estimated variability.
Maximum and minimum values of statistics adopted in the uniform distribution are reported in Table 3. Regional data are also presented in Fig. 7 alongside a fitted lognormal distribution that will be employed to compute likelihood in the Bayesian update scheme.

4.3.3.2. Normalized undrained shear strength. When considering normalized undrained strength, the CLAY/10/7490 database (Ching and Phoon, 2014) is used to define the prior knowledge. Relevance of this prior knowledge was checked comparing regional data with the global dataset in terms of Liquidity index (LI) and Plasticity index (PI) (Fig. 8). This global database includes data from 251 sites. Normalized Cuvane is considered herein as reference, since it closely corresponds to the strength mobilized in slope failures (Mesri and Huvaj, 2007). The range of statistics (mean and variance) of normalized Cuvane data from the different case studies in the global database is used to define uniform prior distributions for the Bayesian updating procedure (see Table 3).

The regional undrained shear strength data from the SW Iberian margin sites is also dominated by vane strength measurements (e.g. Lee and Baraza, 1999). To consider also the fall cone measurements of Minning et al., 2006, a transformation is necessary. An empirical correlation for marine clays (Lu and Bryant, 1997) is used, namely

\[ \mu_{\text{Cvane}} = 0.275 \mu_{\text{Cu vane}} + \mu_Y \]

(11)

where \( \mu_Y \) represents the transformation error of the regression. This error is normally distributed with mean \( \mu_{\mu_Y} = 0 \) and \( \sigma_{\mu_Y} = 0.0086 \).

4.4. Assessment of model performance

To quantify the model performance, the model outputs (probabilistic susceptibility maps) are compared with the observations (i.e. grid cells with mapped landslide). Results of the comparison are expressed by means of Receiver Operating Characteristic (ROC) curves (Begueria, 2006; Frattini et al., 2010). ROC curves (Fig. 5) visualize model performance representing the True Positive fraction (TP) vs False positive fraction (FP) for given cut-off values (e.g. specified probability of failure value). TP is the proportion of positive cases correctly predicted by the model, while FP is the proportion of false positive (unstable grid-cells predicted as stable). Cut-off values are given by a certain probability of failure – for the quasi-static model- and for a certain displacement value – for the displacement-based approach. The area between the ROC curve and the diagonal in the graph (Area Under the Curve or AUC) gives a measure of potential discriminating power for the model, with more powerful models resulting in larger areas. Since the landslide catalogue used does not differentiate between source area and deposit (mostly spread on flat areas), only reported landslide grid-cells with slope angles greater than 3° are considered for model validation. This left 4007 cells available for model evaluation.

5. Results

5.1. Slope gradient statistics

As previously described, the slope root mean square error (RMSE) for each cell grid is a function of both water depth and slope angle magnitude. For a fixed ratio of bathymetric measurement uncertainty, the slope gradient error is inversely proportional to the magnitude of...
5.3. Normalized sediment unit weight

A total of sixteen regional data groups were available from which mean and variances of normalized unit weight distributions could be extracted. For this purpose, the information from deep boreholes in the Iberian margin (i.e., IODP Exp. 339 in Table 1) was split into seven locations, as the boreholes were performed at large distances from one another. As detailed in Table 4, the datasets from twelve sites were selected for the updating operation, leaving 4 aside for validation.

Fig. 11 presents the Bayesian updating results for the assumed prior distributions of normalized unit weight statistics. The figures present the Equivalent Samples generated during the MCMC run, as well as the resulting updated distributions. Comparing likelihoods and updated distributions it can be seen that the Bayesian approach has been effective in reducing the spread of the distributions that will feed the analysis to the map cells. The most relevant distribution values are reported in Table 5. Finally, it may be noted that the validation data points lie unambiguously within the bounds of the updated distributions.

5.4. Normalized undrained shear strength

As indicated in Table 4, nine regional site datasets, out of the thirteen used to evaluate $\mu(C_{\text{vane}})$ and $\sigma(C_{\text{vane}})$, were used as input to the Bayesian updating procedure and four were reserved for validation. Results in terms of updated PDF of $\mu(C_{\text{vane}})$ and updated PDF of $\sigma(C_{\text{vane}})$ are presented in Fig. 12. The most relevant distribution values are reported in Table 5. Concerning $\mu(C_{\text{vane}})$, all the four validation data fall within the 90% inter-percentile range of $[0.19–0.79]$. A 90% inter-percentile range of $[0.17–0.8]$ is derived instead for $\sigma(C_{\text{vane}})$, which also includes the four-validation data. Statistics of the Updated PDFs are reported in Table 5.

5.5. Landslide susceptibility map: pseudo-static approach

Having obtained the PDFs for all input parameters required by the seismic slope stability calculation the Monte Carlo procedure in Fig. 2a was run. A total of 1000 simulations were performed to achieve a failure probability precision of around 0.01 (Wang et al., 2011). The local mean value of the pseudo-static factor of safety is obtained and reported in Fig. 13a. As expected, lower values of factor of safety (i.e. slopes prone to failure) are associated to sites with high values of predicted PGA and slope gradient. A minimum value of 0.4 appears in the most susceptible areas (nearby Cape Sao Vicente, Marques de Pombal fault and Gorringe bank fault), while $F_{S_p-\text{stat}}>20$ are obtained for flat areas offshore the Iberian margin. The precision of the derived factor of safety is quantified by its local variability expressed in terms of the square root of the variance of $F_{S_p-\text{stat}}$ (Fig. 13b). The latter is given by the combination of morphological, geotechnical and PGA uncertainties.

A noteworthy result is that uncertainty in the $F_{S_p-\text{stat}}$ decreases for low values of the FS. Therefore, unstable sites are quantified more precisely than stable ones. This is in apparent contrast with PGA results reported in Fig. 10, where higher uncertainties are associated to greater PGA values. A plausible explanation for this result may be obtained applying a first order second moment method (FOSM) derivation (Baecher and Christian, 2005) to the slope stability (Eq. 1).

$$\sigma_{F_{S_p-\text{stat}}}^2 = \frac{C_{\text{u}}}{y_E^2} \left[ \frac{1}{\sin^2 \pi \cos^2 \pi x + k_0 \frac{\pi}{\cos^2 \pi x}} \right] \frac{y}{\gamma} \cos^2 \pi \sigma_{F_{S_p-\text{stat}}}^2$$

where:

$$\sigma_{F_{S_p-\text{stat}}}^2 = \frac{C_{\text{u}}}{y_E^2} \left[ \frac{1}{\sin^2 \pi \cos^2 \pi x + k_0 \frac{\pi}{\cos^2 \pi x}} \right] \frac{y}{\gamma} \cos^2 \pi \sigma_{F_{S_p-\text{stat}}}^2$$

5.2. Peak ground acceleration

Seismogenic faults incorporated in the Montecarlo procedure are labeled in Fig. 1. Fig. 10 reports the statistics (i.e. mean and variance) of the local probability distribution functions of the aggregated maximum PGA that these faults can deliver. The local mean $\mu_{PGA}$ is a function of the relative distance of the faults to the particular cell. This implicitly assumes a temporal dimension large enough so that all faults will be active at one moment or another along their entire length. The faults incorporated in the Basili et al. (2013) catalogue are all considered active faults and therefore such assumption is reasonable. A maximum mean value of 0.23 g is obtained for sites nearby the Horseshoe abyssal plain (i.e. Horseshoe fault Fig. 1). Along the Portuguese margin values between 0.15 and 0.13 g have been obtained. Such values are in agreement with those available in the current seismic hazard zonation for Portugal (Costa et al., 2008) for a similar seismic scenario and a probability of exceedance of 10% in 50 years (i.e. 475 years return period). The PGA variability, $a_{PGA}$ (Fig. 10b) is also greater in the proximity of the Horseshoe fault.
Fig. 13. a) Mean estimates of Factor of safety. b) Uncertainty in Factor of safety estimation. c) Probability of failure map considering the η factor from Rampello et al. (2010). Outlined in blue in figures (a) and (b) are the landslides in the SW Iberian margin inventory. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Therefore, \( P_f = 0.22 \) and \( P_{exceedance} (7\text{cm}) = 0.135 \) may be used as model output boundaries to classify susceptible and unsusceptible grid cells. These criteria were checked using the landslide subset randomly selected for validation. The results are summarized in Table 6. The quasi-static model predicts correctly 92% of the cells in the validation subset and the displacement-based method 82%.

6. Discussion

6.1. Limitations affecting the results

There are several strong assumptions inherent to the slope stability models that are at the core of the methodology presented in this study. From the geometrical viewpoint there is no clue in the model about the lateral extent or volume of the sliding mass. From the material viewpoint the models assume that the sliding mass is a soft sediment, normally consolidated, which would shear undrained when subject to seismic shaking. The assumption of normally consolidated material may not represent well the sediment strength and density profile in areas of significant erosion such as submarine canyons. With regard to in-situ stresses, it should be noted also that excess pore pressures induced by rapid sedimentation are not considered. Although in most marine deposits it is correct to assume that conditions are hydrostatic (Lee and Edwards, 1986), overpressure is possible in areas where the sedimentation rates are relatively high (e.g., Urgeles et al., 2006; Llopart et al., 2015). Alternatives to address these model limitations are outlined in section 6.3 below.

Other limitations to the results presented are inherent to the databases employed. In particular, the magnitude estimates in the European Database of Seismogenic Faults assume full-length fault dislocation. This assumption implies relatively large return periods for the ground shaking events. However, such long return periods are justified by the submarine landslide catalogue that is used to validate the analysis, as the date of the events in this catalogue is not well constrained in many instances but, because of their position in the uppermost sedimentary sequences, they can all be assumed to be Quaternary.

A strong limitation of the submarine landslide database employed is that it does not distinguish between source area and deposit. Because submarine landslides may travel long distances from the area that initially failed (e.g., Elverhøi et al., 2000; De Blasio et al., 2004) a data-base that identifies the landslide source area will be better adapted to highlight the factors linked to the failure without the influence of the landslide dynamics. The slope-angle based filtering criteria that has been applied to get around this limitation is a relatively crude solution.

6.2. Model performance

Despite all the limitations signaled above overall model performance, as measured by the AUROC curves, is noteworthy. This good performance suggests that, within the limits of the employed databases, seismic triggers are the dominant cause of submarine slope failure in the SW Iberian margin.

The (slightly) better performance of the quasi-static model should not come as a surprise. Both the quasi-static and the displacement-based approach applied here are ultimately based on statistical regressions of Newmark method outputs for a given set of input seismic motions and slope descriptors. In the displacement-based method that regression directly gives an estimated displacement, whereas in the quasi-static method the regression is used to establish the mobilization factor \( \eta \). The statistical work of Rampello et al. (2010) is based on seismic motion records from Italy, which from a tectonic viewpoint is a
(a) 

(b) 

(c)
reasonable proxy for the Gulf of Cadiz. The displacement-based model performance might also be improved by using richer descriptions of seismic ground motion, for instance using models that also include Arias intensity within the predictor variables (Jibson, 2007).

The calibration of the quasi-static method using dynamic effects affects the performance of the method. Fig. 16 shows the estimated probability of failure using a non-calibrated reduction factor value frequently used in practice (i.e., \( \eta = 0.5 \)). When compared with the calibrated method (Fig. 13c) the new results show a general increase in slope failure susceptibility.

Model performance should be reevaluated in the future, as the landslide catalogue is updated and becomes more precise. A particularly significant improvement in this respect may be a landslide catalogue that distinguishes between landslide source and landslide deposits. By using the polygons of the landslide source areas only, we will ensure that the input in the model performance and validation through the ROC curves will not be contaminated by portions of the polygons

where the slope stressors, factor of safety and probability of failure are not related to the slope failure conditions.

6.3. Enhancing the susceptibility maps

The susceptibility maps might be further enhanced if other conditioning factors are included. An additional input factor that could be considered is the occurrence of overpressure. In a first approximation this may be explored using very similar models. For example, following (Carlton et al., 2017) the pseudo-static slope stability model might be reformulated as:

\[
FS_{\text{p-stat}} = \frac{Cu}{\gamma'\left[\sin \alpha \cos \alpha + k_h \frac{1}{\gamma} \cos^2 \alpha\right]} (1 - \tau_c)
\]

(13)

Table 4

Regional datasets employed as input and validation for the Bayesian updating procedure. SdG068-XX are measurements performed on samples collected in 2019 during the INSIGHT Leg-1 cruise. See Stow et al. (2013) for details of IODP Exp. 339 Sites.

<table>
<thead>
<tr>
<th>Variables</th>
<th>Input data</th>
<th>Validation data</th>
</tr>
</thead>
<tbody>
<tr>
<td>9 Sites</td>
<td>- 4 sites Minning et al., 2006</td>
<td>SdG068–11</td>
</tr>
<tr>
<td></td>
<td>- 3 sites, Lee and Baraza, 1999</td>
<td>SdG068–14</td>
</tr>
<tr>
<td></td>
<td>- SdG068–02</td>
<td>SdG068–15</td>
</tr>
<tr>
<td></td>
<td>- SdG068–03</td>
<td>SdG068–16</td>
</tr>
<tr>
<td>12 Sites</td>
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<td>SdG068–11</td>
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</table>

Fig. 14. a) Mean value of Newmark displacement. b) Square root of variance of Newmark displacement. c) Probability of exceedance a Dn threshold equal to 7 cm. Outlined in blue are the landslides in the SW Iberian margin inventory. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Fig. 15. ROC curve and Optimal thresholds for Pseudo-static model and Displacement-based method.

Fig. 16. Probability of failure map obtained using a naïve quasi-static slope stability model (\( \eta = 0.5 \)).
with:

\[ r_{ex} = \frac{\sigma'_{uo}}{u} \] being the excess pore pressure ratio.

The \( r_{ex} \) is a new variable that may be integrated in the spatial model using a similar procedure to that applied here to the slope gradient and PGA variables. A local (i.e. grid cell dependent) distribution of overpressure across SW the Iberian margin could be derived from spatially distributed inputs such as sedimentation rate and/or sediment accumulation over a reference horizon of known age. Correlations may be established between sedimentation rate and maximum pore water pressure at a cell, by exploiting systematic 1D simulations of sedimentation and consolidation, with a parametric coverage relevant for the SW Iberian margin. Uncertainties in hydromechanical parameters (e.g., permeability and coefficient of consolidation) may be treated if the amount of erosion can be estimated and characterized by the model outputs (i.e. the connectivity of failed cells for source events of similar magnitude at given location) may be exploited to define an aerial event size. Areal sizes thus estimated would require transformation into volumetric landslide characteristics making use of regional correlations. Considering the spatial correlation structure of outputs might, however, require more detailed consideration of spatial correlations of geotechnical inputs. This can be facilitated by using a random field approach (Fenton and Griffiths, 2008), which is already implemented in the code.

### 7. Conclusion

This study, using the SW Iberian margin as an example, is the first attempt to assess in a systematic probabilistic manner earthquake-induced submarine landslide susceptibility for a large offshore region. A grid cell-based methodology using infinite slope models is applied at this regional-scale. While similar mapping efforts have been previously presented, the area addressed here is orders of magnitude larger than that of the precedents.

The expected seismic shaking across the study area is computed assuming that faults dislocate their entire length, a constrain given by the source database. Therefore, the seismic scenario considered is defined by severe magnitude earthquakes implying long return periods. Given the temporal scale of the landslide catalogue used for validation of the method this appears as a valid assumption.

Despite the jump in scale introduced, well-established evaluation methods for susceptibility maps suggest that the models employed achieve good accuracy. It appears that most landslides included in the database employed to validate the output were earthquake-triggered by the faults collected in the source database. Naturally, this conclusion should be revised and confirmed as both databases are enlarged and/or improved.

The methodology employed has been deliberately developed to facilitate re-evaluation, as the database of mapped landslides, the seismic source catalogue or the regional geotechnical information is extended and updated. The method can be also extended to include additional contributing factors such as overpressure. Probabilistic susceptibility maps like the ones presented here are one significant step towards landslide-generated tsunami hazard estimation at the regional scale. However, further work is still necessary to that end, particularly in order to link spatial susceptibility and overall event magnitude.

### Notation

The following symbols are used in this paper:

- \( \sigma_{\text{rem}} \) standard deviation of DEM error
- \( \mu_{\log(\text{PGA})} \) mean value of logarithm of PGA
- \( H_L = P_{LV} \times P_N \times S \) (14)

For earthquake triggering the occurrence of landslides is directly connected to the recurrence of seismic shaking. Gutenberg-Richter laws have been proposed for several zones offshore Portugal for seismic hazard studies in that country (Costa et al., 2008). These laws may be easily coupled to the model to provide a starting point to evaluate submarine landslide recurrence until better studies become available. A more complex issue is that of landslide size. Regional magnitude-frequency relations for submarine landslides (Urgeles and Camerlenghi, 2013) might be useful to constrain the parameters affecting the predicted hazard. It is also attractive to explore if the spatial coherence of model outputs (i.e. the connectivity of failed cells for source events of similar magnitude at given location) may be exploited to define an aerial event size. Areal sizes thus estimated would require transformation into volumetric landslide characteristics making use of regional correlations. Considering the spatial correlation structure of outputs might, however, require more detailed consideration of spatial correlations of geotechnical inputs. This can be facilitated by using a random field approach (Fenton and Griffiths, 2008), which is already implemented in the code.

### 6.4. From submarine landslide susceptibility to submarine landslide hazard

As noted in the introduction susceptibility maps onshore are frequently conceived as steps towards hazard evaluation. Landslide generated tsunami is the more relevant hazard at the regional scale discussed here.

From a general viewpoint, landslide hazard \( H_L \) can be expressed as the conditional probability of landslide size \( P_{LV} \), of landslide occurrence in an established period \( P_N \) and of landslide spatial occurrence \( S \) (Guzzetti et al., 2005). Assuming independence amongst the three probabilities, the landslide hazard can therefore be expressed as:

\[ H_L = P_{LV} \times P_N \times S \] (14)

<table>
<thead>
<tr>
<th>( \mu_{\log(\text{PGA})} )</th>
<th>( \sigma_{\text{rem}} )</th>
<th>( \mu_{\log(\text{PGA})} \times \sigma_{\text{rem}} )</th>
<th>( \mu_{\log(\text{PGA})} \times \sigma_{\text{rem}} \times S )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.22</td>
<td>0.135</td>
<td>0.28</td>
<td>0.45</td>
</tr>
</tbody>
</table>

Table 6

Percent of landslide-grid-cells predicted by the models.

- \( P_L = 0.22 \)
- \( P_{\text{exceedance}} [\text{Dn}=5.2cm] = 0.135 \)
- 92%
- 82%

Table 5

Summarized statistics of normalized geotechnical parameters after a Bayesian procedure.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Prior range [max-min]</th>
<th>Likelihood Estimate</th>
<th>Updated</th>
<th>90% inter-percentile</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \mu_{\log(\text{PGA})} )</td>
<td>[5.2-1.95]</td>
<td>[2.28]</td>
<td>[2.26]</td>
<td>[2.83-1.81]</td>
</tr>
<tr>
<td>( \sigma_{\text{rem}} )</td>
<td>[0.4-0.1]</td>
<td>[0.28]</td>
<td>[0.23]</td>
<td>[0.72-0.19]</td>
</tr>
<tr>
<td>( \mu_{\log(\text{PGA})} \times \sigma_{\text{rem}} )</td>
<td>[1.45-0.1]</td>
<td>[0.42]</td>
<td>[0.41]</td>
<td>[0.17-0.6]</td>
</tr>
<tr>
<td>( \mu_{\log(\text{PGA})} \times \sigma_{\text{rem}} \times S )</td>
<td>[0.32-0.06]</td>
<td>[0.10]</td>
<td>[0.43]</td>
<td>[0.8-0.17]</td>
</tr>
</tbody>
</table>

The following symbols are used in this paper:

- \( P_L \) probability of landslide occurrence
- \( P_{\text{exceedance}} [\text{Dn}=5.2cm] \) probability of exceedance at a cell, by exploiting systematic 1D simulations of sedimentation and consolidation, with a parametric coverage relevant for the SW Iberian margin.
\( \sigma_{\log(PGA)} \) standard deviation of logarithm of PGA
\( \mu_{\log(PGA)} \) mean value of PGA
\( \sigma_{PGA} \) standard deviation of PGA
\( X \) statistics of interest (mean and standard deviation) modeled as random variable
\( f_{X}(x) \) Prior probability density function for \( X \)
\( f_{X}(x) \) Posterior probability density function for \( X \)
\( L(x) \) Likelihood or conditional probability of observing the Data when \( X = x \)
\( \log \) logarithm of a possible mean for the variable \( X \)
\( \sigma_X \) logarithm of a possible standard deviation value for the variable \( X \)
\( \xi_i \) i-th data on geotechnical statistics
\( \sigma_{\xi_i} \) original standard deviation of \( \xi \)
\( \varepsilon_i \) transformation error due to regression used
\( \sigma_{\varepsilon_i} \) standard deviation of data statistics \( \xi \) due to transformation error used
\( \sigma_{\log} \) original standard deviation of the Likelihood \( L(x) \)
\( \sigma_{\log,w} \) weighted standard deviation of data statistics \( \xi \) due to transformation error used
\( \mu_{T} \) mean value of transformed data statistics
\( \sigma_{T} \) standard deviation of \( \mu_{T} \)
\( \mu_{0} \) mean value of undrained vane shear strength
\( \mu_{0,\text{uc}} \) mean value of undrained fall-cone strength
\( N_r \) number of regional sites considered in the updating operation
\( N_{\text{tot}} \) number of relevant data
\( N_T \) number of data affected also by the transformation error

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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