Fault Detection Algorithm for Wind Turbines’ Pitch Actuator Systems

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Abstract: A fault detection innovation to wind turbines’ pitch actuators is an important subject to guarantee the efficiency wind energy conversion and long lifetime operation of these rotatory machines. Therefore, a recent and effective fault detection algorithm is conceived to detect faults on wind turbine pitch actuators. This approach is based on the interval observer framework theory that has proved to be an efficient tool to measure dynamic uncertainties in dynamical systems. It is evident that almost any fault in any actuator may affect its historical-time behavior. Hence, and properly conceptualized, a fault detection system can be successfully designed based on interval observer dynamics. This is precisely our main contribution. Additionally, we realize a numerical analysis to evaluate the performance of our approach by using a dynamic model of a pitch actuator device with faults. The numerical experiments support our main contribution.

Keywords: fault detection; interval observer; pitch actuator; wind turbines

1. Introduction

Nowadays, wind turbines are essential machines to produce green energy from the natural air current. One way to increase this green energy is by increasing the wind-turbine blade dimensions. Hence, its price is increased too. Therefore, to ensure a good feasibility and long lifetime operation of the wind turbines blade-dynamics to effectively capture the wind, a fault detection system design for the pitch actuator systems of a wind turbine results in being virtually mandatory [1–4].

Recently, the benefit impact of wind turbines on earth and, in a near future, on Mars too is well accepted [5,6]. In wind turbine literature, an important topic is to improve its performance. In [7], a study on misalignment of the wind turbine nacelle with respect to the wind direction is presented, and a study [8] on the major driven force on the mooring line tension of offshore wind turbines. In [9], the effect of age in the performance of wind turbine is investigated. The damage effects caused by the fatigue of the wind turbine components is an important issue to perform the behavior of wind turbines [10]. In addition, improving the design can be an effective way to ameliorate the performance of the whole system [11]. For example, the blade aerodynamic design of the wind turbine is studied in [12]. Moreover, vibration control and fatigue reduction are studied to develop new strategies with the objective of increasing the performance and decreasing pitch actuator usage [13,14]. To fulfill this objective, stochastics models can be built to study fatigue loads [15], or to predict drive-train vibrations [16]. Furthermore, it is crucial to prevent system failures in order to ensure the performance. Innovative fault detection and diagnosis are essential to realize the required levels of reliability in recent wind turbines [17–19]. To assure efficient operation on energy conversion of these wind systems, an efficient pitch actuator fault detection methodology is mandatory [20]. Fault detection techniques can be classified into two major categories: model-based methods and signal processing-based methods.
For model-based fault detection, the system model could be mathematical [21]. Faults are detected based on the residual generated by state variable or model parameter estimation (see [22] and a reference on it). For signal processing-based fault detection, mathematical or statistical operations are performed on the measurements (see, for example, [23]).

Hence, the main objective of this paper is to present a recent algorithm to detect a fault in pitch actuators of wind rotary mechanisms. In the presence of pitch actuator faults, pitch systems may present changes on its behavior, affecting the pitching performance with the possibility of oscillation on the generator speed and making the turbine system unstable and unsafe [24]. A fault on pitch actuator induces changes on dynamics, as high air content in oil, pump wear, or hydraulic leakage [22]. In literature, there are many contributions on it. Some are based on data analysis [25], others are based on the frequency response of the system actuator to a given input signal [26], and so on [27]. On the other hand, the use of interval observers has proved to be an excellent tool to measure uncertainties in dynamical systems [28–31]. Taking advantage of this, we use the main interval observer statement to postulate our fault detection method. Then, and by using a given training input signal, the performance of our approach is numerically validated. According to these numerical experiments, a pitch actuator fault is highlighted.

The rest of this paper is structured as follows. Section 2 shows the theoretical frame on interval observers design and our general fault detection algorithm for any linear dynamic system. Then, in Section 3, the application to wind turbine system is presented, along with the novel fault detection and fault classification algorithms. A set of numerical experiments support the main contribution of this paper. We use a wind turbine pitch actuator under three common faults. According to these numerical experiments, our approach is able to to discern the faulty stages from the healthy one. Finally, a brief conclusion and future work are discussed in Section 4.

**Notation 1.** For a real matrix $M$ or a vector, $M > 0$ means that its components are positive, and $M \geq 0$ means that its components are non-negative. Additionally, $\mathbb{R}^{n \times m}_{+}$ denotes that the set of real $n \times m$ matrices have non-negative entries [28]. In consequence, $\mathbb{R}^{n \times m}_{-}$ denotes the set of real $n \times m$ matrices having non-positive entries.

### 2. Fault Detection Algorithm: Interval Observer Approach

This section presents the first approach to our main objective: to design a rule for a fault detection on a pitch actuator of a wind turbine system by using the residual signals of interval observers. To achieve this objective, we consider a linear dynamic system and we design a general fault detection algorithm. To succeed, first some definitions and results on interval observer theory are presented. Then, our general result is stated.

#### 2.1. Interval Observers Design

First of all, we present some definitions [32]:

(i) The relation $M_1 \leq M_2$ must be understood at the element-wise.

(ii) A matrix $M$ is a Metzler matrix if its off-diagonal elements are non-negative ones.

(iii) A matrix $M$ is Hurwitz (or stable) if every eigenvalue of $M$ has strictly negative real part.

We also need the next theorem, where the non-negative solutions to a linear dynamic system is characterized.

**Theorem 1 ([28]).** Given a Metzler matrix $M$, the system $\dot{z} = Mz + r(t)$, $z \in \mathbb{R}^n$, $r(t) \geq 0$, is called cooperative or non-negative system if due to $z(0) \geq 0$, then $z(t) \geq 0$, $\forall t \geq 0$.

On the other hand, it is well-known that any system may present uncertainties, due to model parameters variation or unknown input disturbances. An option to estimate an uncertainty in a
A linear dynamic system is by invoking the classical approach on constructing a Luenberger observer. For example, consider the system
\[ \dot{x}(t) = Ax(t) + Bu(t), \quad x(0) = 0 \in \mathbb{R}^n, \]
where \( x \in \mathbb{R}^n \) is the state, \( A \in \mathbb{R}^{n \times n} \) is a constant matrix, \( B > 0 \in \mathbb{R}^n \) is a vector, and \( u(t) \in \mathbb{R} \) is the input excitation signal and assumed bounded. To detect or observe the state variable \( x(t) \), with input \( u(t) \), a Luenberger observer can be constructed (see [33] for an introduction to observers):
\[ \dot{z}(t) = Az(t) + Bu(t) + L(x(t) - z(t)). \] (2)

Variable \( z(t) \) observes \( x(t) \), in the sense that the state error dynamic \( z(t) - x(t) \) is stable. Then, if the matrices \( A \) and \( B \) in Equation (1) present uncertainties, a natural question is how to modify the observer structure to overcome these uncertainties. Broadly speaking, it can be inferred that there are two main approaches: (1) by employing adaptive laws for an estimation on the system parameters variation [34], and (2) by designing interval observers [35,36]. The main advantage of using interval observers is its dynamic response to give a finite range of possible values for the state variable [29].

For a basic reference, next we introduce the general definition of interval observer for linear systems.

**Definition 1 ([35]).** For system (1), the dynamical system
\[
\begin{bmatrix}
\dot{z}(t) = a(z,u) \\
\dot{x}(t) = Ax(t) + Bu(t)
\end{bmatrix}^T = b(z,u)
\] (3)
is an interval observer for (1), if \( \underline{x}(0) \leq x(0) \leq \overline{x}(0) \), then \( \infty < \underline{x}(t) \leq x(t) \leq \overline{x}(t) < \infty \) for all \( t \geq 0 \).

The functions \( a(\cdot,\cdot) \) and \( b(\cdot,\cdot) \) in (3) are carefully designed to capture the state dynamics of the given system with a required performance. Usually, they are defined based on Luenberger observer structure (2). Therefore, a Luenberger matrix \( L \) must be constructed. Additionally, the stability of the interval observer dynamic \( z(t) \) in (3) must be ensured too. By accurately defining the functions \( a(\cdot,\cdot) \) and \( b(\cdot,\cdot) \), this stability issue can be accomplished. In a general approach, the residual errors \( \varepsilon(t) = x(t) - \overline{x}(t) \) and \( \delta(t) = \underline{x}(t) - x(t) \) are usually studied to evaluate the observer design performance. Hence, if these dynamics are stable, then the inclusion condition \( \underline{x}(t) \leq x(t) \leq \overline{x}(t) \) is ensured.

Now, suppose that system matrices \( A \) and \( B \) in Equation (1) are faulty but bounded by known matrices \( A_L \) and \( A_U \), and \( B_L \) and \( B_U \), respectively:
\[ A_L \leq A \leq A_U, \quad B_L \leq B \leq B_U. \] (4)

An approach to determine an interval for the system state variable \( x(t) \) is by using the inequalities stated in (4), allowing for structuring an interval observer. That is, the functions \( a(\cdot,\cdot) \) and \( b(\cdot,\cdot) \) (in Equation (3)) will depend not only on \( A_L, A_U, B_L \) and \( B_U \), but also on the Luenberger observer matrix \( L \).

### 2.2. General Fault Detection Algorithm

In this section, a new faulty algorithm based on interval observers is presented. It is based on the fact that interval observers allow for detecting if the observed variable overcomes a prefixed healthy value. To do that, we introduce a slight modification on the classical Luenberger observer stated in Equation (2). The main idea is to monitor interval (4) as a possible faulty interval: the nominal value \( A \) takes values in \([A_L, A_U]\) when a fault is present in the system (the same for \( B \)). Moreover,
the observer dynamic depends only on a nominal value of matrices $A$ and $B$. That is, the interval observer is designed despite inequation (4). If a fault occurs, matrices in system (1) reflect this faulty scenario. However, the observers do not depend on it, as expected due to the faulty scenario being unknown. In fact, we do not need the interval state observer for the detection alert, and we work directly with the observed residual signals $\varepsilon(t)$ and $\hat{\varepsilon}(t)$ to confirm a fault. This is realized below.

We now present a novel interval observer by introducing a design function $g(t)$, with a design parameter $a \in R^+$ into an state-observer Luenberger frame-scheme Equation (2):

$$
\dot{w}(t) = Aw(t) + Bu(t) + L(x(t) - w(t)) - aBg(t), \quad w(0) \in R^n_+,
$$

(5)

$$
\dot{z}(t) = Az(t) + Bu(t) + L(x(t) - z(t)) + aBg(t), \quad z(0) \in R^n_+,
$$

(6)

with $w(0) \leq x(0) \leq z(0)$. The additional term $\pm aBg(t)$ is an artificial external perturbation that uses the same canal as $u(t)$. The term $a$ is introduced to tune the dynamic observer to accurately detect a faulty case on our system. Consider now the residual signals of these observations (also named observed errors), defined as:

$$
e_L(t) = x(t) - w(t),
$$

$$
e_U(t) = z(t) - x(t).
$$

(7)

Hence, the process monitoring is realized by manipulating these residual observed signals (7) in comparison to the nominal (non-faulty) case. Therefore, under a faulty system scenario, the system matrices (1) are affected, but the observer systems (5) and (6) only depend on the non-faulty system data giving its ability to claim a fault on the system if it occurs. To fulfill this objective, we first need to ensure the stability of the proposed method.

**Proposition 1 (Lower and Upper bounds).** Consider the system (1), with $a \in R^+$, and a non-negative function $g(t)$. If there exists matrix $L$ such that $A - L$ is Metzler, then

$$
w(t) \leq x(t) \leq z(t), \quad t \geq 0,
$$

(8)

$w(t)$ and $z(t)$ being solutions to the systems (5) and (6). Moreover, if $g(t)$ is bounded and $A - L$ is Hurwitz, the bounded-input bounded-output (BIBO) stability is ensured.

**Proof.** From definition in (7), it suffices to note that the errors $e_L(t)$ and $e_U(t)$ are non-negative, and then concluding by using Theorem 1. Then, differentiating Equation (7) with respect $t$, we obtain:

$$
\dot{e}_L(t) = \dot{x}(t) - \dot{w}(t) = A\dot{x}(t) + Bu(t) - (Aw(t) + Bu(t) + L(x(t) - w(t)) - aBg(t))
$$

$$
= A\dot{x}(t) - Aw(t) - L(x(t) - w(t)) + aBg(t) = (A - L)e_L(t) + aBg(t).
$$

Taking into account that $A - L$ is Metzler, and $aBg(t) \geq 0$, by Theorem 1, we have $e_L(t) \geq 0$, and conclude that $x(t) \geq w(t)$. Moreover, if $A - L$ is Hurwitz, $\dot{e}_L(t)$ is BIBO stable. Consider now the upper error $e_U(t)$ defined in Equation (7):

$$
\dot{e}_U(t) = \dot{z}(t) - \dot{x}(t) = Az(t) + Bu(t) + L(x(t) - z(t)) + aBg(t) - (Ax(t) + Bu(t))
$$

$$
= Az(t) + L(x(t) - z(t)) + aBg(t) - Ax(t) = (A - L)e_U(t) + aBg(t).
$$

Again, from Theorem 1, we conclude that $e_U(t) \geq 0$, so $z(t) \geq x(t)$, and, if the Hurwitz condition is verified, BIBO stability is ensured. \(\square\)
Note that, in order to design the interval observers (5) and (6), it is necessary to know the nominal value of system matrices $A$ and $B$ in Equation (1). This is the case for the wind turbine [37,38]. The interval observer (8) in Proposition 1 may not be the best interval observer. This is not the purpose of this work: we only ensure that the error is BIBO to construct an algorithm for fault detection. That is, no optimization process is involved. Our aim is to detect a fault on the system, and not really to determine an interval to the system state vector. Algorithm 1 summarizes the fault detection algorithm. Thus, in the healthy scenario, we determine its maximum value and then take it as a threshold for comparison. Thus, if this threshold is violated, then a fault is presented. Moreover, we may also be able to classify the kind of fault, an important issue in wind-turbines. We summarize this in a general fault detection algorithm based on the interval observers (5) and (6). Its stability is ensured by Proposition 1.

**Algorithm 1:** General fault detection algorithm.

Step 1: Define $L$, $g(t)$ and $\alpha$ such Proposition 1 holds.

Step 2: Healthy case: Find a threshold $T_h$ for residual errors (7).

Step 3: General scenario: evaluate residual errors (7) and compare with $T_h$.

### 3. Interval Observer Statement Applied to Fault Detection in a Pitch-Actuator of a Wind-Turbine

We now present a fault detection algorithm applied to a wind turbine. To succeed, we first need to present the wind turbine mathematical model, and then adapt the general fault detection algorithm presented in Section 2, in order to obtain a rule allowing for discerning if a fault on pitch actuator appears or not.

The pitch-actuator dynamic behavior, see Figure 1, of a wind-turbine can be captured by using the next representation [20,37,38]:

$$\frac{\beta(s)}{u(s)} = \frac{w_n^2}{s^2 + 2\zeta w_n s + w_n^2},$$

(9)

where $\beta(t)$ is the pitch angle related to its actuator, $u(t)$ is the reference command signal supplied by the control power management system, and $s$ represents the Laplace variable of a related signal in time-domain, $t$. Additionally, $w_n$ and $\zeta$ represent the natural frequency and the damping ration of the pitch actuator, respectively. On the other hand, in hydraulic pitch actuators, its degradation performance comes from different faulty operation cases, such as pump wear, hydraulic leakage, and high air oil content [20,37]. For a general report on fault detection in wind turbine, see [1,2], and Ref. [3] presents a faulty scenario classification. In the present paper, we only consider the pitch actuator faults. Access to real wind turbine data sets is usually proprietary, and therefore they may not be openly accessible. To overcome this difficulty, in this work, numerical data were obtained from existing literature, presented in Table 1 [37,38], where the nominal (H) and faulty ($F_1$, $F_2$ and $F_3$) scenarios’ values of $w_n$ and $\zeta$ in Equation (9) under study in this work are defined.

**Table 1.** System parameters for a hydraulic pitch actuator under common faulty scenarios [37,38].

<table>
<thead>
<tr>
<th>Scenario</th>
<th>$w_n$ (rad/s)</th>
<th>$\zeta$</th>
</tr>
</thead>
<tbody>
<tr>
<td>No fault (H)</td>
<td>11.11</td>
<td>0.6</td>
</tr>
<tr>
<td>High air oil content ($F_1$)</td>
<td>5.73</td>
<td>0.45</td>
</tr>
<tr>
<td>Hydraulic leakage ($F_2$)</td>
<td>3.42</td>
<td>0.9</td>
</tr>
<tr>
<td>Pump wear ($F_3$)</td>
<td>7.27</td>
<td>0.75</td>
</tr>
</tbody>
</table>
System (9) can be transformed into the state-space scheme as:

\[
\dot{x}(t) = Ax(t) + Bu(t)
\]

(10)

with

\[
A = \begin{pmatrix} 0 & 1 \\ -w_n^2 & -2\zeta w_n \end{pmatrix}, \quad B = \begin{pmatrix} 0 \\ w_n^2 \end{pmatrix}.
\]

Here, \(x_1(t) = \beta(t)\), and \(x_2(t) = \dot{\beta}(t)\) such as \(x^T(t) = [x_1(t) \quad x_2(t)]\). To apply Proposition 1, and ensure stability, we need to define \(L\), \(\alpha\), and \(g(t)\) for wind turbine system (10). The next lemma collects it.

**Lemma 1.** The system (5) and (6), with

\[
L = \begin{pmatrix} 1 & 1 \\ -w_n^2 & 1 - 2\zeta w_n \end{pmatrix},
\]

(11)

define an interval observer (8) for the pitch actuator system (10) with \(g(t) = |u(t)|\) and \(\alpha = 0.01\).

The value of \(\alpha\) is tuned to discriminate the pitch dynamic if a fault occurs (see Table 1). Function \(g(t)\) is designed to fulfill the hypothesis of Proposition 1, ensuring BIBO stability. Note that, if we define \(g(t) = 0\) in Equations (5) and (6), the residual signals (13) vanish because both systems (1), (5), and (6) consider the same matrices \(A\) and \(B\), obtaining Luenberger observers.

Observe that the dynamic of the interval observer (5) and (6) is defined under the non-faulty scenario (\(H\) in Table 1). Hence, the system matrices \(A\) and \(B\) in system (10), and \(L\) in Equation (11), take values given by \(w_n = w_H = 11.11\) and \(\zeta = \zeta_H = 0.6\); and then labeled as \(A_H, B_H\) and \(L_H\), as follows:

\[
A_H = \begin{pmatrix} 0 & 1 \\ -w_H^2 & -2\zeta_H w_H \end{pmatrix}, \quad B_H = \begin{pmatrix} 0 \\ w_H^2 \end{pmatrix}, \quad L = \begin{pmatrix} 1 & 1 \\ -w_H^2 & 1 - 2\zeta w_H \end{pmatrix}.
\]

(12)

Therefore, to detect a fault, we can go on analyzing the related residual signals:

\[
e_{l_2}(t) = x_2(t) - w_2(t),
\]

\[
e_{u_2}(t) = z_2(t) - x_2(t),
\]

(13)

where the variable \(x_2(t)\) is selected because, besides representing the pitch system, \(\dot{\beta}(t)\) is the dynamical variable most sensitive to faults. We can now present an algorithm to design the fault detection system.

Next, we present some simulations to test our proposal fault detection method. First, the total time of simulation is set to 250 s, sufficiently enough to evaluate our fault detection design. Then, we program the system observers (5) and (6) and applied to the pitch actuator process (9). This observer just uses the healthy parameters of the pitch actuator prototype. In our testing numerical experiments,
we program the input prove signal as shown in Figure 2; jointly, we have the response of the state variables for the healthy actuator. Here, we set $x_1(0) = 0, x_2(0) = 0, w_1(0) = -1, w_2(0) = -1, z_1(0) = 1, \text{ and } z_2(0) = 1$ for each test and then hereafter.

By following the FD-Algorithm stated in Algorithm 2, we need to define $T_h$ from the nominal case $H$, as stated in Table 1. We obtain Figure 3, where both errors (13) for this case are displayed. Then, we can define a threshold (third step of FD-Algorithm): $T_h = 2.5$ (this value can be obtained from Figure 3 or evaluating a bound for $\sup_t \{e_{L2}(t), e_{U2}(t)\}$). Finally, we can use it to obtain a fault detection system (step 4 in Algorithm 2): faulty system (10) is considered and residual signals $e_{L2}(t)$ and $e_{U2}(t)$ are evaluated. The obtained simulation results for each faulty scenario are shown in Figures 4–6. By using the stated excitation signal (or input signal), the occurrence of a fault is simple to realize: if $\sup_{0 \leq t \leq 250} e_{L2}(t) \geq T_h$, then a fault has occurred. Figures 4–6 picture both errors (13), proving that it is necessary to consider $e_{L2}(t)$ and $e_{U2}(t)$ in Equation (13) to detect a fault because they do not detect a system fault at the same time. Thus, the designer has to evaluate (13) and the first to overcome $T_h$ detects a system fault.

**Algorithm 2: Wind turbine fault detection algorithm (FD-Algorithm)**

<table>
<thead>
<tr>
<th>Step</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Consider the healthy parameters shown in Algorithm 1, and then define matrix $L$ (11).</td>
</tr>
<tr>
<td>2</td>
<td>Define a non-constant excitation signal $u(t)$.</td>
</tr>
</tbody>
</table>
| 3    | From the nominal plant ($H$), define a threshold $T_h$ as a bound to the system dynamic (13):
| 3.1  | Solve (10) for $A_H, B_H$ and $L_H$ (12), along with (5) and (6). |
| 3.2  | Define a threshold $T_h$ to the dynamic in (13). |
| 4    | Decision rule.
| 4.1  | Solve (10) for faulty $A$ and $B$. |
| 4.2  | Solve (5) and (6), with $A_H, B_H$ and $L_H$ (12). |
| 4.3  | If residual signals (13) are greater than the set threshold $T_h$, then a fault is detected. |

We can state $T_h = 2.5$ as a bound for the residual signals (dashed). Note that both errors are identical because no fault is present.
In Figure 3, the positiveness of the residual signal can be shown. When the faulty system is considered, the Metzler condition can be lost, so the non-negativeness of $e_U(t)(t)$ and $e_L(t)(t)$ in Equation (7) is not ensured. For instance, this can be noted in Figure 4, where both errors take negative values.

Figure 4. Fault F1 scenario. Residual signals $e_{U_2}(t)$ and $e_{L_2}(t)$. Once one of the two errors overcomes the dashed line, a fault is detected.

Figure 5. Fault F2 scenario. The first fault detection for both residual signals or observed error is in red.

Figure 6. Fault F3 scenario. In this case, the residual signal $e_{U_2}$ allows for detecting a fault faster than $e_{L_2}$. 
On the other hand, an important experimental issue is to evaluate how fast our detection system responds. Table 2 presents when the first fault is detected, for each case, and for both residual signals $e_{L2}(t)$ and $e_{U2}(t)$:

\[
\begin{align*}
t_L &= \min_{0 \leq t \leq t_f} \{ e_{L2}(t) > T_h \}, \\
t_U &= \min_{0 \leq t \leq t_f} \{ e_{U2}(t) > T_h \},
\end{align*}
\] (14)

where $t_f$ is the total time of simulations.

**Table 2.** Time estimation of the first detection by using the residual signals (13).

<table>
<thead>
<tr>
<th>Scenario</th>
<th>$t_U$ (seconds)</th>
<th>$t_L$ (seconds)</th>
</tr>
</thead>
<tbody>
<tr>
<td>High air oil content ($F_1$)</td>
<td>79.9382</td>
<td>58.0804</td>
</tr>
<tr>
<td>Hydraulic leakage ($F_2$)</td>
<td>31.3493</td>
<td>13.1228</td>
</tr>
<tr>
<td>Pump wear ($F_3$)</td>
<td>42.3287</td>
<td>55.9148</td>
</tr>
</tbody>
</table>

Note that it takes less than a minute to detect a fault. In comparison to the technique stated, for instance in [20], our approach may be considered as a fast response method for detecting a fault. Moreover, from Figures 4 and 5 and Table 2, a classification of a system fault can be stated, once the threshold value $T_h$ is defined. In a general scenario, once $e_{L2}(t)$ or $e_{U2}(t)$ are greater than the stated value $T_h$, a fault is detected. However, how may we classify it as $F_1$, $F_2$ or $F_3$? From Table 2, a response to this question can be inferred using (14). A classification algorithm is stated in Algorithm 3.

**Algorithm 3: Fault classification algorithm (FC-Algorithm)**

- **Step 1**: Nominal plant: determine $T_h$.
- **Step 2**: General plant: Evaluate the first value of $t$ (14) such that $e_{L2}(t)$ or $e_{U2}(t)$ (13) verify:
  - 2.1 If $e_{L2}(t) > T_h$ for $t \leq 15$: then $F_2$
  - 2.2 If $e_{U2}(t) > T_h$ for $15 < t \leq 55$: then $F_3$
  - 2.3 If $e_{U2}(t) > T_h$ for $58 \leq t$: then $F_1$.

Finally, in real applications, even when we are actuating by using a known control signal to the pitch-actuator system of the wind turbine, there may exist a wind on the blades and then inducing of random dynamics on our structure. Hence, we repeat the previous simulations by adding a random signal to our control action as shown in Figure 7. The obtained results are shown in Figures 8–11. From these figures, we see that the same fault detection algorithm is still possible.

**Figure 7.** Top: Input signal with random noise; Down: variables of wind turbine system (10).
Figure 8. Residual signals $e_{U_2}(t)$ and $e_{L_2}(t)$ for the nominal case H when a random noise is present on the input reference signal, similar to non-random input (see Figure 3). Again, the programmed threshold is $T_h = 2.5$ (dashed).

Figure 9. Fault F1 scenario under a random noise. Residual signal $e_{U_2}$ detects a faulty behavior due to high air oil content, despite noise on the input signal.

To test the proposed FD-Algorithm (Algorithm 2) and FC-Algorithm (Algorithm 3), a set of 500 numerical experiments with random input data are carried out. The accuracy of the algorithms is displayed in Table 3, where the percentage of right fault classification is over detected ones.

Table 3. Random sample test: Fault detection and classification percentage.

<table>
<thead>
<tr>
<th>Fault Cases</th>
<th>F1</th>
<th>F2</th>
<th>F3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Detection</td>
<td>62%</td>
<td>80%</td>
<td>91%</td>
</tr>
<tr>
<td>Classification</td>
<td>83%</td>
<td>100%</td>
<td>100%</td>
</tr>
</tbody>
</table>

Comparing the achievement of the proposed algorithm related to others in literature [22,25], our approach is robust to noisy data, which would be a serious problem, for instance, to the fault detection technique in [25]. Thus, the image to process is obtained by reading a one-dimensional sensor in discrete-time domain. Moreover, our approach does not rely on accurate discrete-time modeling of the pitch system as the one stated in [22], for which its performance depends on the discrete-time sampling too. On the other side, among the different approaches on monitoring the mechanical
structures on a wind turbine, there is the stochastic method focused to predict, for instance, vibrations at the tower top of wind turbine and fatigue loads due to the wind [15,16]. This stochastic approach resulted robustly against changing conditions and was able to separate the response dynamics of the system response from the deterministic one.

Figure 10. Fault F2 scenario under a random noise, with similar behavior of non-random input case (see Figure 5).

Figure 11. Fault F3 scenario under a random noise. Note that $e_{L_2} > T_h$ before $e_{U_1}$, but the same non-noisy classification rule still works because cases 2.1 or 2.3 in FC-Algorithm are not accomplished.

4. Concluding Remarks and Future Work

In this work, pitch actuator faults were studied due to these systems having the highest failure rate in wind turbines. A fault in a pitch actuator may change the dynamics of the pitch system by varying the damping ratio and natural frequencies from their nominal values, thus affecting the whole performance of a costly wind turbine. Thus, a fast and stable fault detection algorithm is an important key to study.

By using the interval observer theory, an original algorithm on fault detection to wind-turbine pitch actuators was successfully realized. This algorithm is based on knowing the healthy parameters of the plant. Then, we assume that, even if a fault occurs, the values of these parameters are not far away from the healthy one. Thus, we can consider an interval observer for a healthy region. Under a general scenario, from the residual errors, we can determine if the system fits this region or not. Thus, a fault detection system is obtained. On the other hand, in this paper, we focus on detecting faults on wind turbine pitch actuators. Therefore, the fatigue load damage estimation, and other wind-turbine structures’ metric performances, are not studied here. The efficiency of this method was numerically
validated by using a wind turbine pitch actuator under three common fault stages. For each one, our fault detection method was able to discern. Moreover, the time response of our approach fault detection method can be considered fast.

As in [39], a Fourier theory can be used to study the principal harmonics of the residual signals. Comparing Figures 3 and 8, where residual signals for healthy scenario are pictured, the behavior is almost the same. However, when a fault occurs, note that a faulty system with a random component on the input signal presents more harmonics than the non-random one. Thus, as future work, a possible algorithm to detect a fault is to study the presence of harmonics in the residual signals by using the Fourier transform.

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**Abbreviations**

The following abbreviations are used in this manuscript:

- **BIBO** Bounded-Input Bounded-Output
- **FD** Fault Detection
- **FC** Fault Classification

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