

1 **APPLICATION OF BARCELONA TEST FOR CONTROLLING ENERGY**  
2 **ABSORPTION CAPACITY OF FRS IN UNDERGROUND MINING WORKS**

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12 **ABSTRACT**

13 In recent years in Chile, the use of fiber reinforced shotcrete (FRS) has been widely  
14 extended in underground works, particularly in tunnels for roads, mines and hydroelectric  
15 projects. In these projects, the design of the supports is mainly based on the modified Q–  
16 Barton method, which relates the rock mass quality to the minimum energy absorption  
17 capacity of the FRS, which is determined by the square panel test, with panels filled  
18 during spraying. However, to obtain these specimens, complex procedures must be  
19 followed both on-site and, in the laboratory, and the results obtained present a large  
20 scatter.

21 To improve the execution control of the FRS lining of tunnels, an empirical correlation  
22 has been developed between the square panel test of a synthetic-fiber reinforced concrete  
23 and the double-punch Barcelona test of cylinders, at laboratory level.

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1 The application of such a correlation to a concrete sprayed on-site using the same fiber  
2 has proven satisfactory, with a difference between the experimental and the correlated  
3 measurement of 2.6%. Then, the methodology presented in this paper can be applied to  
4 control the FRS to any other case.

5 **KEYWORDS:** squared panel test, energy absorption capacity, fiber reinforced shotcrete,  
6 tunneling, BCN test.

## 7 **1. INTRODUCTION**

8 In recent years in Chile, the use of shotcrete and fiber reinforced shotcrete (FRS) has been  
9 widely extended in underground works, particularly in tunnels for roads, mining and  
10 hydroelectric projects, as shown in Figure 1. In these projects, the design of the supports  
11 is mainly based on the modified Q-Barton method (Barton *et al.*, 1974; Barton and  
12 Bandis, 1990), which relates the quality of the rock mass to the minimum energy  
13 absorption capacity of the FRS, which is determined using a square panel test with panels  
14 filled during spraying, following the recommendations provided in the "European  
15 Specification for Sprayed Concrete" published in 1996 by the European Federation of  
16 National Associations Representing Producers and Applicators of Specialist Building  
17 Products for Concrete (EFNARC,1996) or according to the EN 14488-5:2006 standard  
18 (CEN, 2006).



19

20

Figure 1. FRS spraying in mining work in Chile.

1 However, these tests require large and heavy specimen samples, which must be filled  
2 while spraying FRS onto the tunnel lining. This often causes the panels to present defects  
3 or damage that alter the results and increase their scatter, with coefficients of variation  
4 (CoV) above 15% and sometimes above 20% between specimens of the same sample  
5 (Carmona and Molins, 2017).

6 On the other hand, the double-punch test (DPT) or Barcelona test (BCN test) proposed  
7 by Molins *et al.* (2006; 2009) has proven to be adequate for the control of fiber reinforced  
8 concrete (FRC) in construction and has been standardized in Spain by AENOR as UNE  
9 83515 (AENOR, 2010). This test has several advantages with respect to other standard  
10 procedures for characterizing FRC toughness, among which is the use of relatively small  
11 samples with large fracture surfaces, which can be cores drilled from the hardened  
12 concrete as presented in Aire *et al.* (2015) and can be tested using conventional testing  
13 machines. This test also presents lower scatter than the common three-point and four-  
14 point bending tests (Carmona *et al.*, 2018).

15 The main objective of this paper is to present a direct correlation between the energy  
16 absorption capacity determined by the square panel test and the BCN test, with the aim  
17 of substituting the square panel test by the BCN test as a control test in tunnel works with  
18 FRS linings. To this end, the results of three extensive experimental investigations are  
19 presented: one developed on samples made in the laboratory and the other two on samples  
20 and cores produced in different tunnel works. The laboratory investigation allowed  
21 proposing a correlation between the energy absorbed by the two tests, whereas the two  
22 on-site investigations allowed the validation of the proposed correlation.

23 This paper is the third of a trilogy, in which the BCN test has been experimentally  
24 correlated with the bending tests given in standards EN – 14651 (Carmona *et al.*, 2018)

1 and ASTM C 1609 (Carmona and Molins, 2019), widely used for the characterization of  
 2 fiber reinforced concretes.

### 3 **2. ENERGY ABSORPTION CAPACITY OF THE FRS**

4 According to the EN 14488–1 standard (CEN, 2005a) and the recommendation of  
 5 EFNARC (1996) for hand spraying, the minimum plan dimensions of the samples  
 6 obtained on-site must be  $500 \times 500$  mm and  $600 \times 600$  mm, respectively. For robotic  
 7 spraying, both standards establish a minimum dimension of  $1000 \times 1000$  mm for panel.  
 8 The energy absorption capacity is determined by testing square panels of  $600 \times 600$  mm  
 9 and 100 mm in thickness, which is supported by a rigid steel frame at their four edges,  
 10 leaving a span of 500 mm between opposite edges. The test is performed under actuator  
 11 displacement control at a central deflection rate of 1.0 mm/min in the case of the EN  
 12 14488–5 standard and of 1.5 mm/min according to the EFNARC recommendation. The  
 13 load is applied at the center of the panel over a contact surface of  $100 \times 100$  mm, as shown  
 14 in Figure 2.

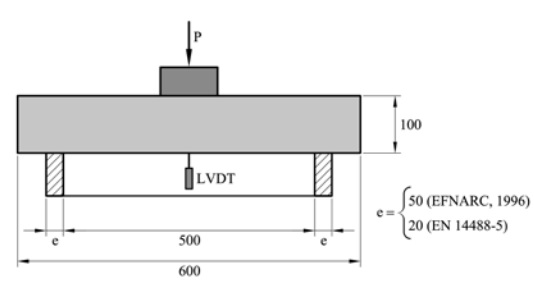


Figure 2. Set up given for square panel.

15 During the test, the load and central deflection are continuously recorded until a central  
 16 deflection of at least 30 mm is achieved. Using that response, the energy absorption  
 17 capacity, up to a central net deflection  $\delta = 25$  mm ( $E_{25}$ ), is calculated as:

$$18 \quad E_{25} = \int_0^{25} P(\delta) \cdot d\delta \quad (1)$$

1 where  $P(\delta)$  is the load as a function of deflection  $\delta$ .

2 The results of square panel tests present high variability, with intra-sample coefficients

3 of variation (CoV) that can exceed 20%. This is due to multiple typical factors of the

4 spraying process such as pressure, distance, and spraying angle as well as sampling,

5 including the support conditions of the mold, curing, transport and subsequent cutting of

6 the panels in the laboratory. In addition to the above, the panels are heavy and difficult to

7 handle, both on-site as well as in the laboratory, which causes many panels to present

8 damage or defects that alter the results.

9 Another source of error is the deflection measuring point. The load-deflection curves

10 obtained by measuring the deflection on the upper and lower faces of a panel are shown

11 in Figure 3a. It can be observed that for a central deflection of 25 mm, as measured on the

12 lower face of the panel, the deflection measured on the upper face is significantly lower,

13 with a consequent effect on the calculation of the absorbed energy.

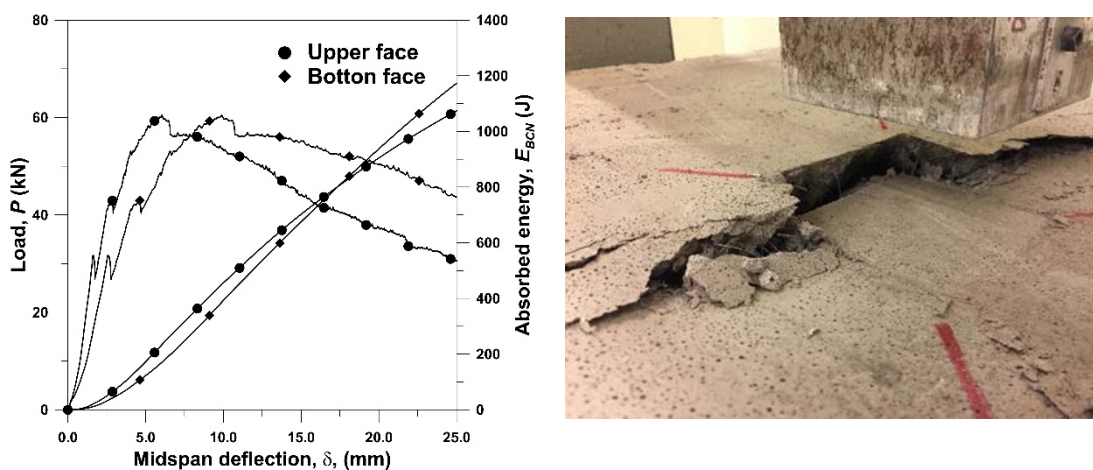


Figure 3. (a) Comparison of the measurement of the central deflection with respect to the lower and upper face of the panel; (b) Final state of the top face of an FRS panel after the test.

14 A punching failure caused by the load on the upper face of the panel, as observed in the

15 concretes reinforced with medium and high fiber contents, is shown in Figure 3b. This

16 failure causes that the loading platen penetrates the upper face of panel, which decreases

1 the displacement measured on that face with respect to the central deflection recorded on  
2 the lower face of the panel.

### 3 **3. DISSIPATED ENERGY IN BCN TEST**

4 As Barcelona (BCN) test is known an indirect tension test proposed by Molins *et al.*  
5 (2009) to determine fiber reinforced concrete properties (ACI, 2016). In this test, a  
6 cylindrical specimen of FRC is subjected to a double punching compression load by  
7 means of two cylindrical steel punches placed at the center of the upper and the lower  
8 faces, respectively, as shown in Figure 4a.



Figure 4. (a) BCN test setup; (b) Typical final state of specimens subjected to double punching tests.

9 According to the UNE 83515 standard (AENOR, 2010), the cylindrical specimen  
10 dimensions are  $d = h = 150$  mm, i.e.,  $h/d = 1$ , and the steel wedges diameter is  $a =$   
11  $d/4$ . In contrast to other indirect tensile tests used for controlling the FRC properties, this  
12 test can be performed in a conventional testing system under stroke displacement control  
13 at a rate of  $0.5 \pm 0.05$  mm/min. During the test, the applied load and the circumferential  
14 deformation measured at half the height of the specimen must be continuously recorded.  
15 On the specimen, the applied load produces a conical volume under triaxial compression  
16 stress beneath the punches, increasing the cylinder diameter and producing tensile stresses  
17 perpendicular to the radial planes of specimen. Due to this tensile stress with cylindrical

1 symmetry, when the stress exceeds the tensile strength of concrete, cracks perpendicular  
2 to the field propagate through the specimen. This allows that the compression cones  
3 penetrate the cylinder increasing the specimen radius and producing two or more cracks.  
4 Then, the final state of the specimen presents two aligned cracks, or three cracks arranged  
5 approximately at 120° or, sometimes, four perpendicular cracks as can be seen in Figure  
6 4b (Carmona *et al.*, 2012).

7 When the specimen cracks, the circumferential dilatation corresponds to the total  
8 circumferential opening displacement (*TCOD*) and the energy dissipated can be  
9 calculated as:

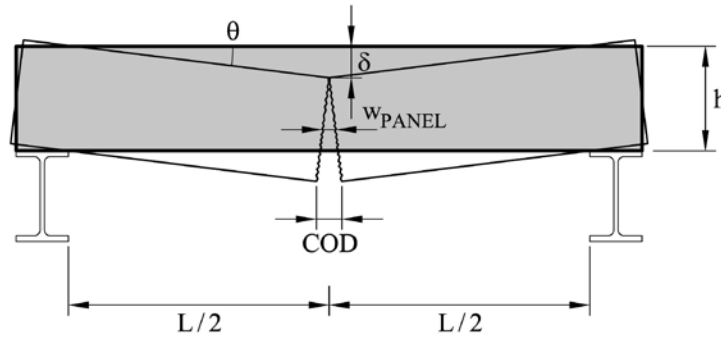
$$10 \quad E_{BCN,x} = \int_0^{R_x} P(Rx) \cdot d(Rx) \quad (2)$$

11 where  $E_{BCN,x}$  is the energy dissipated at a certain value of total circumferential  
12 deformation  $R_x$ . According to the standard UNE 83515, the energy should be determined  
13 at  $R_x = 2.0$  mm, 2.5 mm, 4.0 mm, and 6.0 mm.

14 Due to its simplicity and greater knowledge of the response of the FRC subjected to the  
15 BCN test, supported by a large number of experimental researches (Carmona *et al.*, 2012;  
16 2013; Aire *et al.*, 2015), numerical (Pros *et al.*, 2011; 2012; Pujadas *et al.*, 2013) and  
17 experimental correlations with the bending tests given in the standards EN - 14651  
18 (Carmona *et al.*, 2018) and ASTM C 1609 (Carmona and Molins , 2019), this test has  
19 begun to be used to evaluate the post-cracking behavior of FRC, as can be seen in the  
20 research performed by Chao *et al.*, 2012; Pujadas *et al.*, 2014; Kim *et al.*, 2015; Carmona  
21 *et al.*, 2016; Choumanidis *et al.*, 2017; Rambo *et al.*, 2018, and has been proposed as a  
22 control test for fiber-reinforced shotcrete in some large tunnel projects, such as the Metro  
23 de Lima (Geocontrol, 2015) and Chuquicamata Underground (*Chuquicamata*  
24 *Subterránea*) Project of CODELCO – Chile (Carmona, 2017).

#### 25 **4. EQUIVALENCE BETWEEN PANEL TEST AND DPT**

1 In the last years, different correlations among bending tests and BCN test had been  
 2 proposed by Conforti *et al.* (2017), Carmona *et al.* (2018; 2019) based on crack opening  
 3 ( $w$ ). Then, an equivalence between the square panel test and the BCN test should be  
 4 proposed in terms of  $w$ ; therefore, it is necessary to establish a relationship between the  
 5 midspan net deflection,  $\delta$ , recorded in the panel test and the crack opening displacement  
 6 ( $COD$ ) in the panel,  $w_{PANEL}$ .



7  
 8 Figure 5. Geometric relationship on cracked square panel.

9 For a square panel with a central crack, as shown Figure 5, considering geometric  
 10 relationships and that  $w_{PANEL}$  corresponds to half of the  $COD$  on the surface of the lower  
 11 face of the panel, the following relation can be established:

$$12 \quad w_{PANEL} = \frac{COD}{2} = \frac{2 \cdot \delta \cdot h}{l} \quad (3)$$

13 In the case the standardized square panel, with  $h = 100$  mm, and  $l = 500$  mm, Eq. (3)  
 14 yields  $w_{PANEL} = 0.4 \delta$ .

15 On the other hand, assuming three radial cracks in the failure mechanism of the FRC  
 16 cylinder subjected to a DPT, which opens increasing the diameter,  $\Delta\phi$ , the average crack  
 17 opening,  $w_{BCN}$ , can be estimated with the following expression (Molins *et al.*, 2009):

$$18 \quad w_{BCN} = \frac{TCOD}{3} \quad (4)$$

19 Then, equating Equations (3) and (4), the following relationship can be proposed:

$$20 \quad w_{PANEL} = \frac{COD}{2} = \frac{2 \cdot \delta \cdot h}{l} = w_{BCN} = \frac{TCOD}{3} \quad (5)$$



1 This equation relates the mean crack opening with the crack opening displacement and  
2 the deflection measured in the square panel test with the total crack opening displacement  
3 of cylinders in the BCN test. Therefore, it allows establishing equivalence between both  
4 tests based on similar crack opening.

5 Using equation (5), the crack opening equivalent to a  $TCOD = 6$  mm corresponds to a  
6 net deflection of the panel ( $\delta$ ) of 5 mm. However, there is a low plastic deformation of  
7 the FRC at that deflection of the panel, as can be seen in the curves obtained by Carmona  
8 and Molins (2017). This is because the net deflection in the square panel test includes:  
9 (1) the adaptation of the panel to the support on the frame and (2) the elastic flexural  
10 deformation of the panel, which are about two or more millimeters, as can be seen in the  
11 Figure 3a.

12 In addition, according to the EFNARC recommendation and the EN 14488–5 standard,  
13 the energy absorption capacity of the FRS should be determined at a net midspan  
14 deflection  $\delta = 25$  mm, which represents an advanced cracking and damage state of the  
15 panel with a high plastic deformation. Then, to establish an experimental correlation with  
16 the BCN test, it has been proposed to compare  $E_{25}$  with  $E_{BCN,6}$ , defined here as the energy  
17 dissipated by the cylinder subjected to a DPT at a  $TCOD = 6$  mm, which in the BCN test  
18 is also equivalent to an advanced crack opening state, as can be seen in Fig. 4b. To develop  
19 this proposed correlation, three values of  $E_{25}$  and  $E_{BCN,6}$  corresponding to three different  
20 fibers content were determined experimentally.

## 21 **5. EXPERIMENTAL DETAILS**

22 To establish the proposed experimental correlation between both tests, the following  
23 research was undertaken.

### 24 **5.1. Design of experimental research**

1 The research at laboratory level was designed taking in account the following criteria  
2 based on Chilean tunnel lining construction practice. The concrete matrix was designed  
3 by a supplier of FRS for tunneling works. In fact, it was a concrete mix used in a real  
4 tunneling work where fiber BC – 54 was used. This type of fibers is widely used in FRS  
5 for tunneling in Chile with a fiber contents commonly between 4 kg/m<sup>3</sup> and 5.5 kg/m<sup>3</sup>.  
6 Then, contents of 4 kg/m<sup>3</sup>, 8 kg/m<sup>3</sup> and 12 kg/m<sup>3</sup> were selected to establish the correlation.  
7 Although the last fiber content can be seen as very high, it was chosen to evaluate a  
8 possible saturation effect of fibers in the tension response of FRS when contents are high.  
9 The minimum number of specimens tested *per* determination was fixed in nine because  
10 this is the amount necessary to produce a determination with a probability of 95% of  
11 determining differences of 10% in the mean with a 90% of significance, assuming that  
12 the distribution is normal and the coefficient of variation is 5% (Kuehl, 2001).

### 13 **5.2. Materials**

14 The concretes were prepared with a Portland pozzolanic cement of Type IP (ASTM,  
15 2018) and crushed river sand; the mix dosage is presented in Table 1, and fibers features  
16 are given in Table 2.

17 Table 1. Features and properties of tested FRS.

Material (kg/m <sup>3</sup> )		Concrete		
		FRS – 4	FRS – 8	FRS – 12
Cement type IP		420		
Sand 0/10		1655		
Superplastizicer admixture		2.10		
Superfluidifying admixture		2.10		
Active admixture		2.94		
Water		215		
Fiber content		4	8	12
Number of specimens	BCN test	10	9	10
	Square panel test	10	10	10

	Compressive test	3	3	3
Concrete properties				
Compressive strength, $f_c$ (MPa)		39.5	40.9	42.3
$V_f$ (%)		0.44	0.88	1.32

1

2

Table 2. Synthetic fiber properties (manufacturer's data).

Designation	$l_f$ (mm)	$d_f$ (mm)	$\lambda_f$ $l_f/d_f$	$f_{st}$ (MPa)	E (GPa)	Fibers/kg N°
BC – 54	54	0.84*	64.3	640	12	37000

3

(\*) Equivalent diameter determined with the manufacturer's information.

4

The concretes were prepared at the laboratory using a conventional paddle mixer of 200 liters' capacity. For the BCN test, the specimens were cast in cylindrical molds with a diameter of 150 mm and a height of 150 mm. The panels were cast in steel molds of 600 × 600 × 100 mm. The quantity of specimens for each concrete are given in Table 1. All specimens were demolded after 24 hours and kept in a fog room, until testing. Table 1 also includes the results of the compression tests.

9

### 10 **5.3. Tests and results**

The panel tests were conducted in a hydraulic closed-loop control system of 100 kN capacity, under deformation control. The deflection was measured with a LVDT of 50 mm range, placed in the center bottom face of the specimen. The load and the deflection were recorded continuously by the testing system at a rate of 3 data/s. The mean curves obtained with each tested concrete are shown in Figure 6.

15

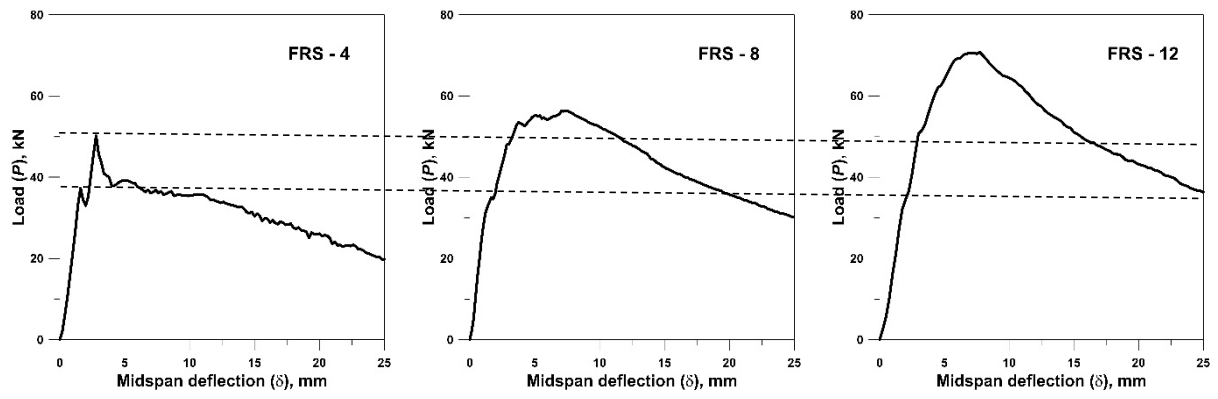


Figure 6. Mean  $P - \delta$  curves obtained with panel tests.



(a)



(b)



(c)



(d)

Figure 7. (a) Crack pattern of FRS-4 panels after the test; (b) Rotation between portions of the panels of the FRS-4 series; (c) Evidence of the friction of the panel on the support framework; (d) Punching shear failure observed in panels with medium and high fiber amounts.

1 In the FRS-4 curve, a first peak was observed at an average load of 37.3 kN, with a central  
2 deflection  $\delta = 1.60$  mm associated with the formation of the first crack, and a second peak  
3 at an average load of 50.2 kN and  $\delta = 2.80$  mm when the second crack was produced. In  
4 these concretes, the cracks were usually oriented in the form of an  $\times$  or  $+$ , as shown in  
5 Figure 7a. After the second peak, a softening was observed, with a gradual decrease in  
6 the load sustained by the FRS, which reached an average load of 19.8 kN at a central  
7 deflection of 25 mm. For advanced deflection levels (see Figure 7b), a high rotation of  
8 the portions of the cracked panel can be observed, with friction between the supporting  
9 edge and the edges of the panel, as shown in Figure 7c.

10 In the FRS-8, the first crack was obtained at an average load of 34.5 kN and  $\delta = 1.77$   
11 mm, and the second crack was produced at a load  $P = 47.8$  kN and  $\delta = 3.06$  mm.  
12 Subsequently, the load continued to increase, with local peaks associated with the  
13 formation of other cracks, until a maximum absolute load  $P = 56.5$  kN was reached at  $\delta$   
14  $= 7.03$  mm. A softening was then observed whereby the load gradually decreased,  
15 reaching a load  $P = 30.0$  kN at a deflection  $\delta = 25$  mm.

16 As can be observed in Figure 6, the loads corresponding to the first and second cracks do  
17 not seem to depend on the amount of reinforcing fiber. However, in the panels reinforced  
18 with medium and high amounts (FRS-8 and FRS-12, respectively), a flexural crack was  
19 initially produced, which caused the first peaks that can be observed in the  $P - \delta$  curves.  
20 However, due to the higher amount of fibers present, the testing system had to increase  
21 the applied load to maintain the established deformation rate, which in addition to the  
22 friction force developed in the supported section of the panel gave rise to a punching

1 failure, which is reflected in the formation of cracks around the loaded section, as can be  
 2 observed in Figure 7d, limiting the work of the fibers in tension and distorting the  
 3 measurement of the deflection performed on the upper face of the panel.  
 4 To explain the failure mechanism of the FRS square panel, the theoretically maximum  
 5 load that must be reached in the test was determined based on a plastic analysis of the  
 6 behavior of a slab subjected to loading. How such loads are evaluated considering the  
 7 plastic bending mechanism plus the arch effect introduced by the friction of the panel  
 8 with the support frame is shown in Appendix 1. It was observed that for the panels with  
 9  $4 \text{ kg/m}^3$  of fiber, such a load is very close to the load resisted in the test. However, for the  
 10 panels with  $8$  and  $12 \text{ kg/m}^3$  of fiber, the estimated loads that must be resisted were  $68\%$   
 11 and  $88\%$  higher than the experiment, respectively. The higher bending capacity of the  
 12 FRS, the greater the difference from the results of the square panel. This shows that there  
 13 is another ultimate mechanism that limits the loading capacity of the panels. It is, without  
 14 a doubt, a mechanism associated with punching.

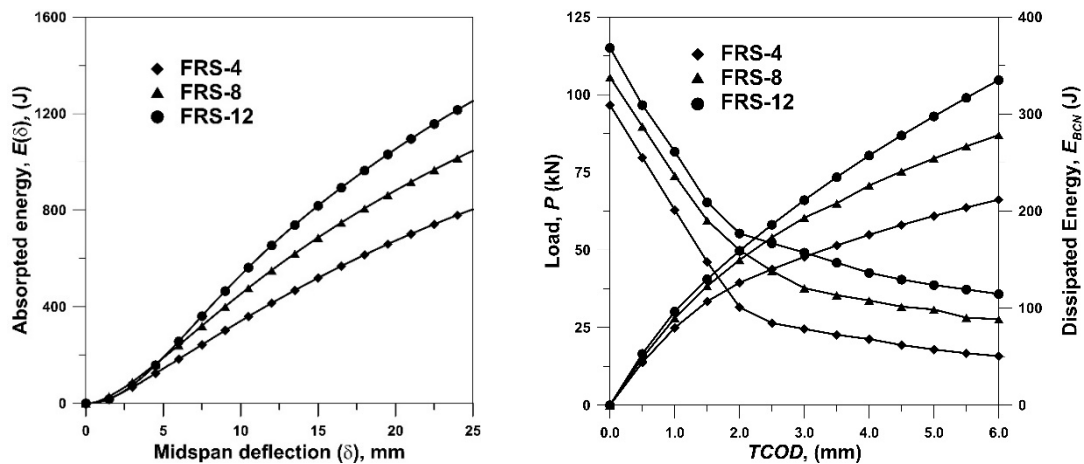


Figure 8. (a) Average  $\delta - E_{25}$  curves obtained testing squared panel of each concrete studied; (b) Mean  $P - TCOD$  and  $E_{BCN} - TCOD$  responses obtained with BCN tests of each tested concrete.

1 The energy absorption capacity of each FRS was calculated using equation (1), obtaining  
2 the curves presented in Figure 8a. Considering that an FRS energy absorption capacity of  
3 1000 J is specified in most projects, it is observed that this capacity is reached in the  
4 laboratory with 8 kg/m<sup>3</sup> of fiber.

5 On the other hand, the BCN tests were carried out using a conventional hydraulic system  
6 of 3 MN capacity controlled by stroke displacement at a constant rate of 0.5 mm/min.  
7 Following the standard UNE 83515, the circumferential dilatation was measured by  
8 means of an extensometer of 12 mm range, fixed to the ends of a chain and placed at half  
9 the height of the specimen. The test data were recorded by a data acquisition system at a  
10 frequency of two data per second. Figure 8b shows the mean  $P - TCOD$  curves recorded  
11 during the BCN tests. In all these curves the  $TCOD$  is close to zero until the maximum  
12 load is reached and, then, increases when cracking of specimen occurs. In the post –  
13 cracking regime the material exhibits a softening, governed by the fiber content.

14 The dissipated energy by the FRS during the cracking process was calculated using  
15 equation (2), obtaining the  $E_{BCN} - TCOD$  curves which are also presented in Figure 8b.

## 16 **6. EXPERIMENTAL CORRELATION BETWEEN TESTS**

17 According to equation (5), the total crack opening of  $TCOD = 6$  mm corresponds to a  
18 net deflection of the panel of  $\delta = 5$  mm. Then, the experimental values of  $E_5$  and  $E_{BCN,6}$ ,  
19 which are given in the Table 3 and plotted in Figure 9a, were processed using the  
20 statistical application XLSTAT ©, obtaining the linear relationship of equation (6).

$$21 \quad E_5(E_{BCN,6}) = 117.35 + 0.205 \cdot E_{BCN,6} \quad (6)$$

22 This equation fits very well the experimental results with a coefficient of determination  
23 ( $r^2$ ) of 0.9628 and absolute differences lower than 1.7%, as can be also seen in Table 3.

24 As proposed in section 4, a correlation between  $E_{25}$  and  $E_{BCN,6}$  was also obtained using  
25 XLSTAT ©. Eq. (7) shows this linear correlation which produced a  $r^2$  of 0.9990.

1 
$$E_{25}(E_{BCN,6}) = 63.55 + 3.479 \cdot E_{BCN,6} \quad (7)$$

2 Table 3 and Figure 9a show the results with this correlation. The very good correlation  
 3 obtained confirms that establishing the correlation between  $E_{25}$  and  $E_{BCN,6}$  is feasible  
 4 and, in fact, better than using Eq. (6).

5 Table 3. Fit of equations (6), (7) and (8) to experimental data.

	exp.	exp.	$E_5(E_{BCN,6})$		exp.	$E_{25}(E_{BCN,6})$ linear		$E_{25}(E_{BCN,6})$ nonlinear	
Concrete	$E_{BCN,6}$ (J)	$E_5$ (J)	Eq. (6) (J)	Diff. (%)	$E_{25}$ (J)	Eq. (7) (J)	Diff. (%)	Eq. (8) (J)	Diff. (%)
FRS-4	212	162	161	1.17	804	800	0.40	799	-0.52
FRS-6	290	174	177	-2.99	1065	1073	-0.77	1074	0.87
FRS-12	340	189	187	1.83	1252	1247	0.40	1247	-0.42

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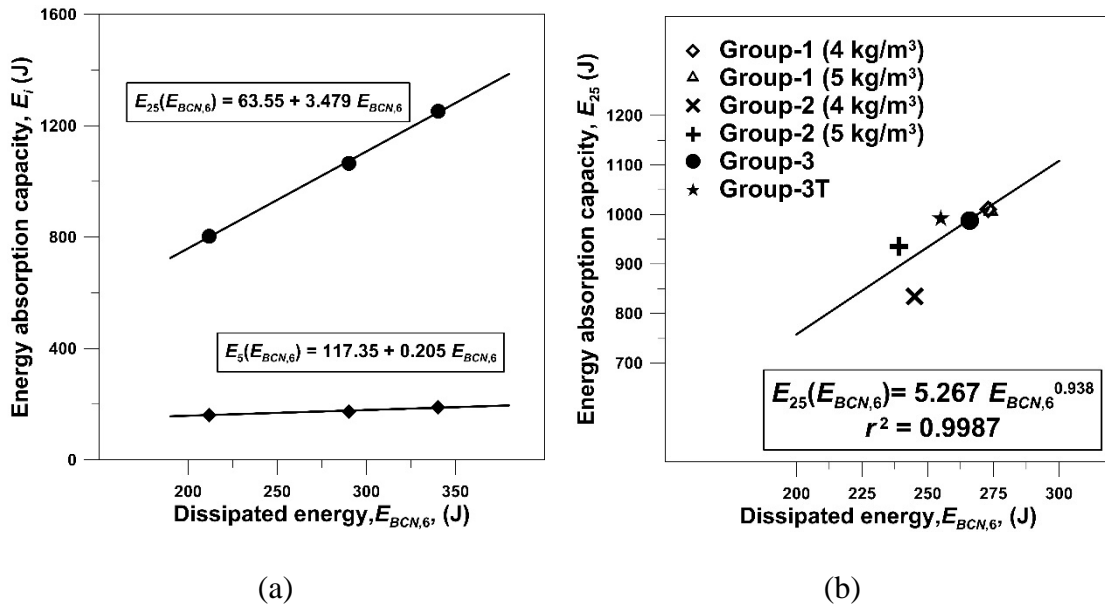


Figure 9. (a) Comparison of linear correlation given by Eq. (6) and Eq. (7) with experimental data; (b) Comparison of Eq. (8) with results of the validation tests.

7 Nevertheless, with the aim to propose a code-type correlation for controlling the energy  
 8 absorption capacity of shotcrete at works by means of BCN test, a nonlinear relationship  
 9 of the form  $y = a x^b$  between  $E_{25}$  and  $E_{BCN,6}$  has been studied. In this equation  $a$ , and  $b$ ,  
 10 are experimental parameters which depend on the type of fibers used to reinforce the



1 concrete. These parameters have been determined using a nonlinear regression analysis  
2 by means of XLSTAT ©, obtaining the following equation:

$$3 \quad E_{25}(E_{BCN,6}) = 5.267 \cdot (E_{BCN,6})^{0.938} \quad (8)$$

4 As can be also seen in Table 3 and Figure 9b, this equation fits very well the experimental  
5 data with a  $r^2 = 0.9987$ .

## 6 **7. VALIDATION OF THE CORRELATION BETWEEN $E_{25}$ AND $E_{BCN,6}$**

7 To replace the panel test by the BCN test in the FRS control in the construction of mining  
8 tunnels in Chile, Eq. (8) was validated using the results obtained with two groups of  
9 samples of FRS prepared by a construction company that executed a section of the  
10 Chuquicamata Underground (*Chuquicamata Subterránea*) Project of CODELCO–Chile.  
11 The FRSs sampled were dosed to reach a compressive strength  $f_c = 25$  MPa at 28 days,  
12 a slump of 24 cm, and reinforced with  $4 \text{ kg/m}^3$  and  $5 \text{ kg/m}^3$  of the same synthetic fibers  
13 BC – 54 used in laboratory research (Table 2). The concretes were mixed at industrial  
14 level and moved to the sprayed front point in mixer trucks and sprayed by mean of robots,  
15 as can be seen in Figure 1.

16 The FRSs were sampled by filling wood molds during the shotcrete spraying in the  
17 construction of the tunnel’s support. After 48 hrs, the molds were transferred to an on-  
18 site laboratory, where cylindrical controls of 153 mm in diameter and variable length and  
19 panels with nominal dimensions of  $600 \times 600 \times 100$  mm were cut. It is worth noting that  
20 the panels were cut through their six faces using a water-cooled diamond saw.  
21 Subsequently, the specimens were transferred to the Laboratory of the Federico Santa  
22 María Technical University, where they were tested following the UNE 83515 standard  
23 and EFNARC recommendation. Prior to the tests, the controls were cut at a ratio of  $H/d$   
24  $\approx 1$ .

1 The results obtained in the BCN and panel tests of each series are presented in Table 4,  
 2 in which are also presented the nominal amount of reinforcing fiber used in each studied  
 3 shotcrete and the value of the energy absorption capacity estimated for each series using  
 4 Eq. (8).

5 Table 4. Results of samples obtained at Chuquicamata Underground Project's works.

Group	Fiber amount (kg/m <sup>3</sup> )	$E_{BCN,6}$ (J)	$E_{25}$ (J)	Eq. (8) (J)	Difference (%)
1	4	273 (9.3)	1011 (5.0)	1016	0.45
	5	274 (15.6)	1007 (13.6)	1019	1.19
2	4	245 (13.4)	835 (19.2)	917	9.88
	5	239 (12.7)	936 (16.2)	896	-4.23

6  
 7 As can be observed in Table 4, the energy absorption capacity of the FRS estimated using  
 8 Eq. (8) fits well with the experimental results obtained with the on-site samples, with a  
 9 maximum difference of 9.88%, which can be graphically observed in Figure 9b. On the  
 10 other hand, it is observed that the scatter of the results of the panel tests is higher than the  
 11 difference in the dissipated energy results obtained with the BCN test, which ratifies one  
 12 of the advantages of this test, and has been widely highlighted by different authors  
 13 (Molins *et al.*, 2009; Carmona *et al.*, 2012; Cavalaro and Aguado, 2015).

#### 14 **8. APPLICATION OF THE PROPOSED CORRELATION**

15 Considering the good fitting of Eq. (8), in the construction of the tunnels support in the  
 16 Underground Chuquicamata Project, the use of the BCN test was proposed to verify the  
 17 energy absorption capacity of the FRS already used in the linings. The dose of this FRS  
 18 was (in kg/m<sup>3</sup>): type IP cement = 450; gravel (5/10) = 81; sand (0/5) = 1533; water = 215;  
 19 high range water reducing and superplasticizing admixture = 3.9; and plasticizer

1 admixture = 3.15. The average slump measured at work was 24.5 cm, and average  
 2 compressive strength at 28 days  $f_c = 39.9$  MPa.

3 For that purpose, the following procedure was used:

- 4 • Identify 15 points where panels were sampled and whose intra-sample absorbed  
 5 energy values have a CoV lower than 20%.
- 6 • Drill at least 2 cores of 150 mm diameter from the shotcrete of the tunnel support  
 7 at each of the selected points.
- 8 • Obtain the dissipated energy at  $TCOD = 6.0$  mm of each core by means of BCN  
 9 test.

10 Following the proposed procedure, the panel sampling points given in Table 5 were  
 11 selected, along with the values of the energy absorption capacity obtained during the  
 12 control.

13 Table 5. Energy absorption capacity and dissipated energy used to validate Eq. (8).

Sample	Sample point	Square panel tests				BCN tests			
		P – 1 (J)	P – 2 (J)	$E_{25,i}$ (J)	CoV (%)	T – 1 (J)	T – 2 (J)	$E_{BCN,6i}$ (J)	CoV (%)
1	7994.77 – 7997.96	978	1028	1003	3.5	276	292	284	4.0
2	68.382 – 73.170	1005	967	986	2.7	218	237	228	5.9
3	681.441 – 671.841	1036	1025	1031	0.8	<b>231</b>	<b>349</b>	<b>290</b>	<b>28.8</b>
4	22.66	986	979	983	0.5	292	258	275	8.7
5	20	1009	998	1004	0.8	305	305	305	0.0
6	85	996	977	987	1.4	244	208	226	11.3
7	40	990	986	988	0.3	<b>172</b>	<b>300</b>	<b>236</b>	<b>38.4</b>
8	124	1023	910	967	8.3	236	200	218	11.7
9	141.196 – 148.801	1000	1001	1001	0.1	230	220	225	3.1
10	50.91 – 53.427	940	1004	972	4.7	191	219	205	9.7
11	208.44 – 212.23	1020	1004	1012	1.1	287	295	291	1.9
12	50	1025	1014	1020	0.8	<b>254</b>	<b>177</b>	<b>216</b>	<b>25.3</b>
13	937	948	931	940	1.3	322	311	317	2.5
14	645.745	923	903	913	1.6	-	-	-	-

15	6809.221	932	904	918	2.2	-	-	-	-
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1

2 At the same sampling points showed in Table 5, two cores of diameter  $d = 153$  mm were  
3 drilled for the BCN test. Before tests, the cores were sawed to obtain a ratio  $H/d \approx 1$ .

4 The tests were performed following the specifications and configuration given in standard  
5 UNE 83515 (Figure 4a) obtaining the results for each sample, also given in Table 5.

6 As can be seen in Table 5, two samples (number 14 and 15) were discarded because they  
7 failed suddenly when cracking load was reached, due to low fiber content. At the same  
8 time, the CoV of four samples, displayed in bold, are higher than 20% and, then, these  
9 results were also discarded.

10 With the mean values of dissipated energy,  $E_{BCN,6} = 257$  J the energy absorption capacity  
11 of shotcrete was determined by using of Eq. (8), obtaining  $E_{25}(E_{BCN,6}) = 961$  J, which is  
12 plotted in Figure 9b as Group 3. This value differs -2.55% with respect to mean  
13 experimental value of  $E_{25} = 986$  J.

14 On the other hand, using all the samples given in Table 8, an average value of dissipated  
15 energy  $E_{BCN,6} = 255$  J is reached. Then, replacing this value in the Eq. (8), the energy  
16 absorption capacity estimated is  $E_{25}(E_{BCN,6}) = 952$  J, which is plotted as Group-3T in  
17 Figure 9b. This value differs by -3.97% with respect to the average  $E_{25} = 992$  J obtained  
18 from the panel tests.

19 **8.1. About the use of 100 mm diameter specimens**

20 Because some shotcrete's thickness of the tunnel's linings of the Chuquicamata  
21 Underground Project are less than 150 mm, it was proposed to evaluate the properties of  
22 the FRS by means of the BCN test executed on 100 mm diameter cores. For this, a  
23 correction factor was developed to use Eq. (8) to determine the energy absorption capacity  
24 of the FRS.

1 Considering that a cylinder subjected to double punch loading fails normally with three  
 2 cracks (Molins *et al.*, 2009), the relationship between the theoretical cracking areas of  
 3 both specimens is 2.25. This factor remains constant for different cracking observed at  
 4 final state of the cylinders after being subjected to DPT, as shown in Figure 4b, it can be  
 5 established the following expression:

$$6 \quad E_{25}(E_{BCN,6-100}) = 5.257 \cdot (2.25 \cdot E_{BCN,6-100})^{0.938} \quad (9)$$

7 Where  $E_{BCN,6-100}$  is the dissipated energy by a 100 mm diameter cylinder at  $TCOD = 6$   
 8 mm.

9 To verify this relationship, an experimental campaign was carried out in which 14 square  
 10 panels, sampled at seven different points when FRS was sprayed in the tunnels, were  
 11 tested. This concrete reached a compressive strength  $f_c = 40.5$  MPa at 28 days and was  
 12 reinforced with  $5 \text{ kg/m}^3$  of synthetic fibers BC-54, obtaining the results shown in Table  
 13 6.

14 Table 6. Testing results used to validate Eq. (9).

Sample	Panel	$E_{25i}$ (J)	$E_{25}$ (J)	$E_{BCN,6-100i}$ (J)	$E_{BCN,6-100}$ (J)
1	1a	849	817	82.5	91.0
	1b	785		99.5	
2	2a	783	784	62.0	67.7
	2b	785		73.4	
3	3a	761	806	84.2	87.2
	3b	851		90.2	
4	4a	884	847	83.0	91.0
	4b	809		99.0	
5	5a	790	813	107.7	104.8
	5a	835		101.8	
6	6a	717	709	82.6	102.8
	6b	701		123.0	
7	7a	969	843	103.43	91.5

	7b	717		79.52	
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1

2 Using the results of Table 6, an average energy absorption capacity  $E_{25} = 803$  J with a  
3 CoV = 5.8% was obtained. From these panels, 100 mm diameter cores were cut, which  
4 were tested following the procedure given in standard UNE 83515, obtaining an average  
5 value of the dissipated energy  $E_{BCN,6-100} = 90.85$  J with a CoV = 13.4%. Replacing this  
6 value in Eq. (9),  $E_{25}(E_{BCN,6-100}) = 803$  J was determined, which differs by 3.86% from  
7 the value of the average energy absorption capacity of the FRS determined before.

8 **9. CONCLUSIONS**

9 An equivalence between cracked square panel and cylinder under DPT was established  
10 based on the crack opening and, using this equivalence, a linear correlation was developed  
11 between energy absorption capacity determined by testing square panels and dissipated  
12 energy obtained with BCN test.

13 An experimental type-code relationship was developed between the EFNARC panel test  
14 and the double-punch Barcelona of a synthetic-fiber reinforced concrete to be used for  
15 controlling the FRS used in tunnel linings.

16 Furthermore, it is justified that a correlation between tests based on relating the fracture  
17 mechanisms is difficult due to the complexity of the failure mechanisms involved in the  
18 EFNARC panel; for light reinforcements, the fracture is predominantly caused by  
19 bending, whereas for significant reinforcements, the fracture is predominantly caused by  
20 punching.

21 The developed expression, as based on the testing of samples made in the laboratory with  
22 different amounts of reinforcing fiber, directly relates the energies of both tests without  
23 requiring other variables, such as the amount of fiber or the concrete's compressive  
24 strength, at least in the range of strengths analyzed.

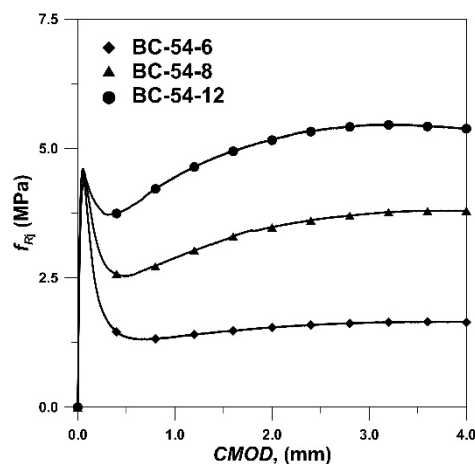
1 The application of such a correlation to a concrete sprayed on-site using the same fiber  
2 has proven satisfactory, with a difference between the experimental and the correlated  
3 measurement of 2.6%. Therefore, it is possible to claim that the criterion and  
4 methodology used can be applied to other cases.

5 The benefit of using much smaller specimens that can be extracted from the actual lining  
6 is going to simplify and improve the quality control of the tunnels' support projects in  
7 addition to reducing the construction cost and the residue of such task.

## 8 **10. APPENDIX – 1 INTERPRETATION OF THE PANEL RESULTS BASED ON** 9 **THE BENDING RESULTS**

### 10 **10.1. Ultimate load of a slab knowing the fiber reinforced concrete bending** 11 **strength**

12 In case the panel breaks under bending, it should develop plastic failure mechanism and,  
13 knowing the sectional response of the concrete with fibers, it would be possible to  
14 calculate the maximum fracture load  $P$  for such a panel. The plastic analysis of the slab  
15 allows determining the plastic failure mechanism and the maximum load assuming that  
16 the moment-curvature diagram is perfectly plastic after cracking. In the  $P - CMOD$   
17 diagrams of the bending tests complementarily developed in the first laboratory  
18 investigation (see Figure 10), it was found that the idealization of a perfectly plastic  
19 behavior is fairly acceptable.



1 Figure 10. Average  $P - CMOD$  curves obtained with the FRC tested.

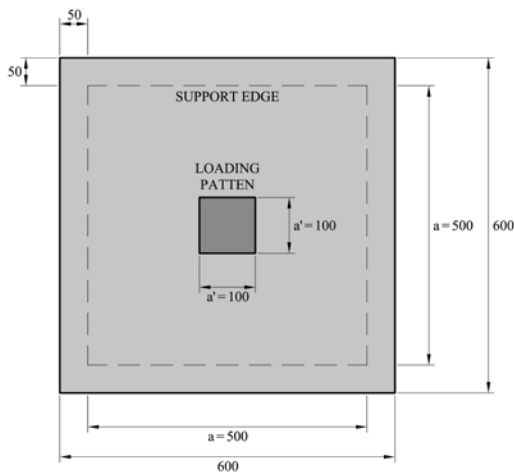


Figure 11. Geometry of the EFNARC panel with its perimeter support and loading plate.

2 A square slab subjected to a point load in its center, of a material whose bending response  
3 is isotropic and remains constant in all directions, develops a collapsing mechanism with  
4 four cracks, which start at the center, reach the midpoint of each side and divide the plate  
5 into four new square slabs (Figure 7a). On the other hand, it is not exactly a point load  
6 but is applied through a square steel plate with sides of 100 mm such that an  
7 approximately uniform load is applied. In this case, there is a direct expression that allows  
8 calculating the fracture load of a square plate with a centered squared uniform load, as is  
9 shown in Figure 11.

10 The analytical expression (Jimenez *et al.*, 2000) is shown in equation (4), where  $m$  is the  
11 plastic bending moment,  $a$  is the side of the slab,  $a'$  is the side of the loading plate, and  $F$   
12 is the maximum load.

13 
$$F = 24 m \left( \frac{2a - a'}{a} \right)^{-2} \quad (10)$$



1 Applying this expression to a square slab with sides of 500 mm and a centered squared  
2 loading area with sides of 100 mm, the following ultimate load is obtained as a function  
3 of the resistant plastic moment:

$$4 \quad F = 7.407 m \quad (11)$$

5 Even though the span between the supports is exactly 500 mm, the hinges extend to the  
6 edge of the slab. To consider this additional bending capacity, the ratio between the length  
7 of the plate's side and that of the support's side is applied, as shown in Eq. (12).

$$8 \quad F = 7.407 m \ 6/5 \quad (12)$$

### 9 **10.2 Obtaining the plastic bending moment per unit of length**

10 To calculate the plastic bending moment, the average maximum residual strength of the  
11 3PB tests on notched beams is adopted. From such residual strength, calculated according  
12 to the EN-14651 standard (CEN, 2005b), the Model Code 2010 (CEB – FIP, 2010)  
13 expression has been adopted for obtaining the residual strength according to Eq. (13).

$$14 \quad f_{Tu} = 0.333F_{R3} \quad (13)$$

15 Once the post-cracking FRS tensile capacity is known, it is possible to calculate the plastic  
16 moment per unit of length assuming that the depth of the neutral axis under simple  
17 bending is negligible (Eq. 14).

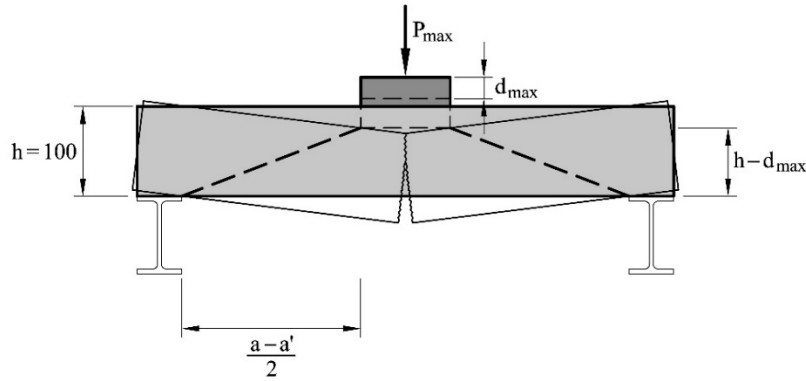
$$18 \quad m = f_{Tu}h^2/2 \quad (14)$$

19 Where  $h$  is the depth of the slab.

### 20 **10.3 Effect of friction in the supports**

21 During the panel test, sliding friction is produced in the supports (Bjøntegaard, 2009).  
22 When the panel rotates to descend under the load's pressure, it tends to separate the initial  
23 support lines. Given that the support frame is horizontally rigid, it is necessary for the  
24 horizontal force to overcome the friction force for movement to take place. The friction  
25 force can be calculated from the friction coefficient ( $\mu$ ) between the panel's concrete and

1 the steel of the support frame upon knowing the vertical force. According to Rabbat and  
 2 Russell (1985), a coefficient of 0.57 has been adopted. Considering that relieving arches  
 3 are formed in the two perpendicular directions of the panel's plane and that the supports  
 4 are on the four sides of the frame, it is straightforward to assume that the normal load on  
 5 each side is a fourth of the total.



6

7 Figure 12. Geometry for the calculation of arch effect in the cracked panel.

8 On the other hand, it should be considered that the relieving arch rise is limited to the  
 9 depth of the panel. However, for significant loads, the panel is already cracked, with a  
 10 significant deflection that reduces the useful depth where the arch can be inscribed.  
 11 Therefore, it will be necessary to consider the deflection at the center of the panel when  
 12 calculating the panel's strength capacity through the arch effect (Figure 12).

13 Finally, the total additional load resisted by the panel through the arches in the two  
 14 orthogonal directions can be estimated as:

15 
$$F_{ARCH} = 2 (\mu(P_{EFN} + W_{panel+platten})/4) \frac{h - d_{max}}{(a - a')/2} \quad (15)$$

16 where  $F_{ARCH}$  is the force of the arch effect,  $P_{EFN}$  is the applied peak vertical load on the  
 17 panel,  $W_{panel+plate}$  is the panel's own weight plus the weight of the steel plate that transmits  
 18 the load onto the concrete,  $h$  is the depth of the panel,  $a$  is the span between supports,  $a'$

1 is the side of the loading plate, and  $d_{max}$  is the deflection corresponding to the peak  
 2 experimental load  $P_{EFN}$ .

3 The resisted vertical load ( $P_{MAX}$ ) can then be estimated as the sum of that resisted by  
 4 bending of the slab and that resisted by the arch effect introduced by the friction force  
 5 with the frame (equation 16).

$$6 \quad P_{MAX} = F + F_{ARCH} \quad (16)$$

7 The results of the loads ( $P_{MAX}$ ) estimated by equation (16) are compared with the  
 8 experimental ones in Table 7. For the panel with 4 kg/m<sup>3</sup> of reinforcement, the estimated  
 9 load ( $P_{MAX}$ ) is similar to experimental one (11% less). However, for the panels with 8 and  
 10 12 kg/m<sup>3</sup>, the estimated loads are significantly larger, 46% and 62%, respectively. The  
 11 difference with the results of the EFNARC panel increases with increasing FRS bending  
 12 capacity. That clearly shows that there is another mechanism that determines the failure,  
 13 which is the FRS punching capacity.

14 Table 7. Estimated and experimental maximum loads,  $P_{MAX}$  and  $P_{EFN}$ , of the FRS panels.

FRS	$F_{Rj}$ (MPa)	$f_{Rj}$ (MPa)	$m$ (Nmm/mm)	$F$ (kN)	$P_{EFN}$ (kN)	$d_{max}$ (mm)	$F_{ARCH}$ (kN)	$P_{MAX}$ (kN)
FRS-4	2.106	0.702	3510	33.70	<b>44.7</b>	6.92	6.06	<b>39.76</b>
FRS-8	5.258	1.753	8763	84.13	<b>63.4</b>	7.60	8.48	<b>92.61</b>
FRS-12	8.807	2.936	14678	140.91	<b>94.3</b>	11.58	12.01	<b>152.92</b>

15

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