

1 **ABSTRACT**

2 **Background:** Experimental and modeling errors can lead to dynamically inconsistent results when
3 performing inverse dynamic analyses of human movement. Adding low-value residual pelvis actuators
4 could deal with such a problem. However, in certain tasks, these residuals may remain quite large, and
5 strategies based on motion or force variation must be applied.

6 **Research question:** Can the dynamic inconsistency be handled by an optimal control algorithm that
7 changes the measured kinematics in the preparatory phase of the single leg triple hop test, a relatively
8 high-speed and torque-demanding task, so that residuals are kept within a low range?

9 **Methods:** The proposed optimal control algorithm was developed as a tracking problem, in which the
10 implicit form of dynamics was used. Equations of motion were introduced as path constraints, as well as
11 residual forces and moments acting on the pelvis. To do so, GPOPS-II and IPOPT were employed to solve
12 the optimization problem. Furthermore, OpenSim API was called at each iteration to solve the equations
13 of motion through an inverse dynamic analysis.

14 **Results:** Results presented a high reduction in all six components of residual actuators during the entire
15 task. Moreover, resulting motion after the optimization showed a very similar evolution than the
16 reference motion before the ascending phase of the task. Once the ascending phase started, some
17 coordinates presented a more significant discrepancy compared to the reference, such as the pelvis tilt
18 and lumbar extension.

19 **Significance:** The findings suggest that the proposed algorithm can deal with dynamic inconsistency in
20 high-speed tasks, obtaining low residual forces and moments while keeping similar kinematics. Hence, it
21 could complement other optimal control algorithms that simulate new motions, relying on dynamically
22 consistent data.

23 **KEYWORDS**

24 Biomechanics; Residual reduction; Optimal control; Triple hop test; Inverse dynamics.

25 **INTRODUCTION**

26 Optimal control simulation of human movement allows analyzing and assessing the biomechanics of
27 specific tasks. Based on measurements of kinematics and contact forces, the balance between external
28 and inertial forces and moments becomes inconsistent due to several sources of experimental and
29 modeling errors [1]. Strategies to cope with such dynamic inconsistency are based on adding low-value
30 residual force and torque actuators to the pelvis segment [2]. However, in high-speed tasks these residual
31 actuators values usually remain large [3], which might invalidate the conclusions of the dynamic analysis.

32 In such those cases, procedures based on modifying force and motion data are employed. One way is to
33 maintain kinematics and modify experimental external forces, for instance using a sharing force
34 assumption during the double support phase of gait [4]. Another approach consists in keeping external
35 forces and varying kinematics and the torso's center of mass position, such as the Residual Reduction
36 Algorithm (RRA) in OpenSim [5]. Finally, other strategies consider changing both kinematics and external
37 forces with a least square estimation [6].

38 This paper presents an optimal control algorithm for solving the dynamic inconsistency problem, *i.e.*,
39 minimizing the residual actuators, at the price of introducing variations to the measured kinematics. The
40 proposed algorithm is tested against a previous published solution by Alvim *et al.* [3], which uses RRA.

41 **METHODS**

42 Reference motion, joint torques and ground reaction forces (GRF) from 6 healthy subjects performing the
43 single leg triple hop (SLTH) test, as well as their respective scaled OpenSim skeletal models, were taken

44 from [3] before applying the RRA. The preparatory phase of the SLTH test, a relatively high-speed and
 45 torque-demanding task, was used to compare the presented algorithm with that applied in [3].

46 The proposed residual reduction procedure was formulated as an optimal control problem that tracked
 47 reference data. Joint coordinates and velocities were states of the problem ($\mathbf{x}^T = [\mathbf{q}, \dot{\mathbf{q}}]$), and joint
 48 accelerations and torques were introduced as controls ($\mathbf{u}^T = [\ddot{\mathbf{q}}, \boldsymbol{\tau}]$). The cost functional consisted of the
 49 minimization of squared differences between design variables (\mathbf{x}, \mathbf{u}) and their respective reference data
 50 ($\mathbf{x}_{ref}^T = [\mathbf{q}_{ref}, \dot{\mathbf{q}}_{ref}]$, $\mathbf{u}_{ref}^T = [\ddot{\mathbf{q}}_{ref}, \boldsymbol{\tau}_{ref}]$). Moreover, to ensure that the stance foot did not slip in the
 51 optimal solution found, an additional term tracking three points along that segment was added. Those
 52 three points (\mathbf{p}_{ref}) were introduced as virtual markers equidistantly positioned between the heel and the
 53 big toe, and its corresponding position (\mathbf{p}) computed from the state variables was added to track them.

$$\begin{aligned}
 [MIN] J = \int_{t_0}^{t_f} (\mathbf{x} - \mathbf{x}_{ref})^T \mathbf{W}_x (\mathbf{x} - \mathbf{x}_{ref}) + (\mathbf{u} - \mathbf{u}_{ref})^T \mathbf{W}_u (\mathbf{u} - \mathbf{u}_{ref}) \\
 + (\mathbf{p} - \mathbf{p}_{ref})^T \mathbf{W}_p (\mathbf{p} - \mathbf{p}_{ref}) dt
 \end{aligned} \tag{1}$$

54 being \mathbf{W}_x , \mathbf{W}_u and \mathbf{W}_p diagonal weight matrices. Moreover, a set of constraints were considered,
 55 employing the implicit form of dynamics [7]. First, dynamic constraints were applied to ensure time
 56 derivative relationships among kinematic variables:

$$\begin{bmatrix} \dot{\mathbf{q}} \\ \ddot{\mathbf{q}} \end{bmatrix} = \frac{d}{dt} \begin{bmatrix} \mathbf{q} \\ \dot{\mathbf{q}} \end{bmatrix} \tag{2}$$

57 An inverse dynamic analysis (IDA) was solved to obtain the joint torques ($\boldsymbol{\tau}_{IDA}$) and residuals (\mathbf{R}_{IDA}), using
 58 design variables related to motion ($\mathbf{q}, \dot{\mathbf{q}}, \ddot{\mathbf{q}}$) and imposing experimental GRF (\mathbf{GRF}_{exp}). Two path
 59 constraints were introduced. The first, equaling control torques ($\boldsymbol{\tau}$) to the resulting torques of the IDA
 60 ($\boldsymbol{\tau}_{IDA}$). The second, limiting the residuals (\mathbf{R}_{IDA}) within an interval of tolerances ($\boldsymbol{\epsilon}_R$) set to ± 2 N and ± 2
 61 Nm, respectively:

$$\boldsymbol{\tau} - \boldsymbol{\tau}_{IDA}(\mathbf{q}, \dot{\mathbf{q}}, \ddot{\mathbf{q}}, \mathbf{GRF}_{exp}) = \mathbf{0} \quad (3)$$

$$-\boldsymbol{\varepsilon}_R \leq \mathbf{R}_{IDA}(\mathbf{q}, \dot{\mathbf{q}}, \ddot{\mathbf{q}}, \mathbf{GRF}_{exp}) \leq \boldsymbol{\varepsilon}_R \quad (4)$$

62 The optimal solution reported in this study was obtained using GPOPS-II [8] and IPOPT [9]. Also, OpenSim
63 API was called during the optimization to solve the IDA.

64 In order to assess results and compare both algorithms, the reduced residuals and the obtained joint
65 coordinates were contrasted with the corresponding results presented in [3]. Furthermore, the mean and
66 standard deviation of the root-mean-square (RMS) of the residuals for each subject were calculated.

67 RESULTS

68 Before applying the reduction algorithms, residual forces and moments presented the highest average
69 RMS values over 90 N and 90 Nm, and the lowest values of almost 17 Nm (Table 1, left column). After
70 applying the optimal control algorithm, residuals were reduced within the limits set on the problem, being
71 the maximum RMS of 1.91 N in the vertical residual force. Moreover, standard deviations in all
72 components presented results under 0.4 N or Nm, indicating small variability between the different
73 subjects (Table 1, middle column).

74 Furthermore, differences were appreciated depending on the residual reduction procedure used.
75 Reductions obtained performing the RRA changed depending on the residual component, having a
76 reduction of 95% in the vertical force but a reduction of 12% in the mediolateral moment (Table 1, right
77 column). In the case of the proposed algorithm, reductions were above 90% in all components. Also,
78 applying the RRA maintained bounded residual values before starting the ascending phase of the test, but
79 higher values once the subject was ascending. Contrarily, residuals were kept within the range of ± 2 N
80 and ± 2 Nm during the entire task, when the presented residual reduction approach was used (Figure 1).

81 [TABLE 1]

82

[FIGURE 1]

83 Joint coordinates after applying the optimal control algorithm manifested a very similar evolution than
84 the reference motion until 50% of the task, moments prior starting the ascending phase of the test. As
85 soon as the ascending phase started, some coordinates showed a different behavior from the captured
86 motion, being the pelvis tilt and lumbar extension coordinates the ones that differed the most. At 50% of
87 the task, pelvis tilted anteriorly slower than the captured motion and then, at 75%, faster. On the other
88 hand, torso started to extend at 50% of the task, contrarily to the reference coordinate, which started at
89 80% of the task (Figure 2). Compared to the motion obtained from the RRA, changes in kinematics were
90 in general higher. Nevertheless, coordinates such as pelvis list or left ankle flexion presented lower RMS
91 error. Overall, considering the six subjects, the mean RMS error of angular coordinates was 1.33° for the
92 RRA solution and 1.97° for the optimal control solution.

93

[FIGURE 2]

94 **DISCUSSION & CONCLUSIONS**

95 This study presented an approach to reduce residual forces and moments based on optimal control
96 theory. Tracking reference data while introducing experimental GRF allowed the algorithm to successfully
97 reduce the residual actuators during the preparation phase of the SLTH test, a high-speed and torque-
98 demanding task. Compared to the residual reduction performed in [3] applying RRA, it can be concluded
99 that lower values of residual components were reached using the presented method. Introducing the
100 residuals as a constraint, instead of adding them to the cost function, allowed always to fulfill the
101 tolerances set on the problem, even in tasks involving high torque efforts. Additionally, low variability
102 among the results for each subject was obtained.

103 The reduction was achieved by varying the reference kinematics obtained from the measurements. It was
104 observed that coordinates that changed the most were the ones that may have had more effect on

105 changing the pose of the body segments with higher inertia. Hence, the dynamic consistency was achieved
106 by the modified kinematics, which allowed to compensate both modelling and experimental errors. Note
107 that unlike RRA in OpenSim, the proposed optimal control method does not change the torso center of
108 mass position to reduce residuals, which yields larger changes in kinematics with respect to the reference
109 motion than in RRA. Nevertheless, the solution presented in this study shows that the discrepancy in terms
110 of RMS error, which has an overall mean of 1.93° , is similar to the maximum values tolerated in previous
111 published motion tracking studies [10, 11].

112 The higher changes in kinematics and the need of imposing experimental GRF could be denoted as two
113 limitations of the algorithm. Depending on the initial residuals and the kinematics of the task, the final
114 motion could change in a manner that would produce unrealistic movements, such as slipping or losing
115 ground contact with the stance foot. Consequently, if the algorithm relies on the experimental GRF, it
116 must include constraints or a term in the cost function (such as in this study, the additional foot tracking
117 term) to avoid these issues. Conversely, incorporating a foot-ground contact model would directly
118 produce realistic movements and GRF that would be dynamically consistent.

119 In conclusion, this study contributed to introduce a suitable approach to reduce residuals that presented
120 satisfactory results in a high-speed and torque-demanding task. Hence, it could be used as a
121 complementary tool for other optimal control algorithms that simulate new motions, relying on
122 dynamically consistent data. Furthermore, future work is contemplating the adaptation of the presented
123 algorithm to develop a foot-ground contact model, which at the same time, will be introduced to improve
124 the performance of the proposed method.

125 **CONFLICTS OF INTEREST**

126 The authors disclose that there are no financial and personal relationships with other people or
127 organizations which could inappropriately influence this work.

128 **ACKNOWLEDGMENTS**

129 The authors acknowledge the financial support of CNPq, CAPES, and FINEP.

130 **REFERENCES**

- 131 [1] J. L. Hicks, T. K. Uchida, A. Seth, A. Rajagopal, S. L. Delp. Is My Model Good Enough? Best Practices
132 for Verification and Validation of Musculoskeletal Models and Simulations of Movement, *J. Biomech.*
133 *Eng.* 137 (2015) 020905. doi:10.1115/1.4029304.
- 134 [2] S. R. Hamner, S. L. Delp. Muscle contributions to fore-aft and vertical body mass center accelerations
135 over a range of running speeds, *J. Biomech.* 46 (2013) 780 – 787.
136 doi:10.1016/j.jbiomech.2012.11.024.
- 137 [3] F. C. Alvim, P.R.G. Lucareli, L. L. Menegaldo. Predicting muscle forces during the propulsion phase of
138 single leg triple hop test, *Gait Posture.* 59 (2018) 298 – 303. doi:10.1016/j.gaitpost.2017.07.038.
- 139 [4] U. Ligrís, J. Carlín, R. Pàmies-Vilà, J. M. Font-Llagunes, and J. Cuadrado. Solution methods for the
140 double-support indeterminacy in human gait. *Multibody Syst. Dyn.* 30 (2013) 247 – 263.
141 doi:10.1007/s11044-013-9363-x.
- 142 [5] S. Delp, F. C. Anderson, A. S. Arnold, P. Loan, A. Habib, C. T. John, E. Guendelman, and D. G. Thelen.
143 OpenSim: open-source software to create and analyze dynamic simulations of movement. *IEEE*
144 *Trans. Biomed. Eng.* 54 (2007) 1940 – 1950. doi: 10.1109/TBME.2007.901024.
- 145 [6] C. D. Remy and D. G. Thelen. Optimal Estimation of Dynamically Consistent Kinematics and Kinetics
146 for Forward Dynamic Simulation of Gait. *Journal of Biomechanical Engineering* 131(3):031005
147 (2009). doi: 10.1115/1.3005148.
- 148 [7] F. De Groote, A. L. Kinney, A. V. Rao and B.J. Fregly. Evaluation of Direct Collocation Optimal Control

- 149 Problem Formulations for Solving the Muscle Redundancy Problem. *Annals of Biomedical*
150 *Engineering* (2016) 44: 2922. doi:10.1007/s10439-016-1591-9.
- 151 [8] M. A. Patterson, and A. V. Rao. GPOPS-II: A MATLAB Software for Solving Multiple-Phase Optimal
152 Control Problems Using hp-Adaptive Gaussian Quadrature Collocation Methods and Sparse
153 Nonlinear Programming. *ACM Transactions on Mathematical Software (TOMS)* 41 (2014).
154 doi:10.1145/2558904.
- 155 [9] A. Wächter and T. B. Lorenz. On the implementation of an interior-point filter line-search algorithm
156 for large-scale nonlinear programming. *Mathematical Programming* 106 (2006) 25 – 27.
157 doi:10.1007/s10107-004-0559-y.
- 158 [10] Y. Lin and M. G. Pandy. Three-Dimensional Data-Tracking Dynamic Optimization Simulations of
159 Human Locomotion Generated by Direct Collocation. *Journal of Biomechanics* 59 (2017) 1 – 8.
160 doi:10.1016/j.jbiomech.2017.04.038.
- 161 [11] Y. Lin, J. P. Walter and M. G. Pandy. Predictive Simulations of Neuromuscular Coordination and Joint-
162 Contact Loading in Human Gait. *Annals of Biomedical Engineering* 46 (2018) 1216 – 1227.
163 doi:10.1007/s10439-018-2026-6.

LIST OF FIGURES

Figure 1. Comparison of residual force and moment components of one subject after performing the reduction through the optimal control problem (black line) and the RRA in [3] (grey line). Residual forces (F) and moments (M) are expressed in anatomical directions: Anteroposterior (AP), Vertical (V) and Mediolateral (ML).

Figure 2. Evolution of joint coordinates after applying the optimal control algorithm (black lines) and the RRA in [3] (grey lines) compared to the reference motion (dashed black lines) for one subject. Each plot presents the RMS error (RMSE) between the obtained joint coordinates and the reference motion performing the optimal control algorithm (black) and the RRA (grey).

FIGURES

Both gray-scale, no need for color.

Figure 1:

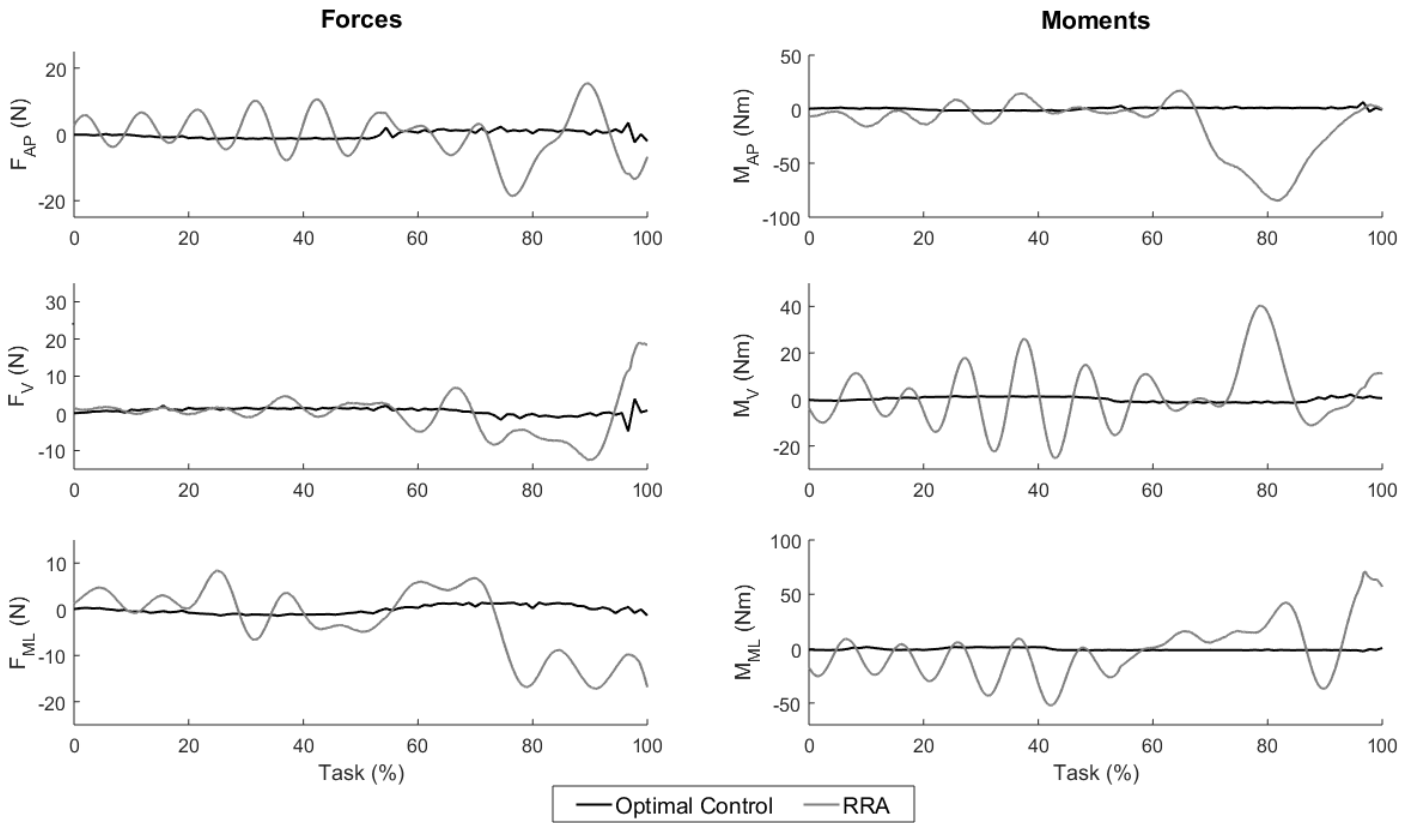


Figure 2:

