



Project of an UAV of infinite autonomy

APPENDIX

AUTHOR

Sánchez Bravo, Àlex

DIRECTOR

Pérez Llera, Luis Manuel

ESEIAAT

Polytechnic University of Catalonia

Delivery date

10/06/2019

Contents

A	Conceptual Design Code	1
A.1	Input Data	1
A.2	Main	2
A.3	Incident Energy from the Sun	3
A.4	Weight of the Batteries	3
A.5	Calculate start and end of the day	4
A.6	Postprocess	5
B	Weight Refinement Code	7
B.1	Input Data	7
B.2	Main	8
B.3	Calculate Weight and Position of the elements of the Airframe	9
B.4	Read Profile Points	10
B.5	Calculate the perimeter of the airfoil	10
B.6	Calculate the area of the airfoil	11

A Conceptual Design Code

This section of the Appendix presents the code employed to choose an optimum configuration for the UAV in the Conceptual Design stage.

A.1 Input Data

```

1  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2  %%THIS IS THE INITIAL DATA SCRIPT%%
3  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
4
5  %% AERODYNAMICS
6
7  %RG15
8  %Cl=0.638;%Re=200k, alpha=5,73
9  %Cd=0.0115;%Re=200k, alpha=5,73
10
11 %S7012
12 %Cl = 0.857;
13 %Cd = 0.0131;
14 %SD7003
15 Cl = 0.645;
16 Cd = 0.013;
17
18 v=13;%m/s
19 rho=0.1815;%kg/m^3
20 mi=12.83e-6;%Pa*s
21 e = 0.89;%Span planform efficiency factor (not oswald's)
22 %% EFFICIENCY
23 eta.p=0.7;%Propulsive efficiency
24 eta.sc=0.3;%Solar Cell efficiency: it theory, it considers the loss of efficiency ...
    due to packaging
25 eta.bat.in = 0.837; %loss of energy entering the batteries
26 eta.bat.out = 0.837; %loss of energy going out of the batteries
27 eta.motor = 0.97; %Efficiency of the electric motor
28 %% POWER CONSUMPTION
29 P.avionics = 2.5 + 6.5 + 2.3;%W ->Controller, Datalink, 4Servos
30 %% WEIGHT -> All the weights should be in Newtons
31 W.avionics= (0.18 + 0.18 +0.14)*9.81;%N ->Controller, Datalink, 4 Servos
32 EdW.batteries = 1.8e6/9.81;%J/N (Sion Batteries)
33 %WdP_propulsion = 0.032;%N/W ->taken from the "HELIPLAT" document.
34 WdP_propulsion = 0.08; %(Noth, 2008)
35 %Power control of the batteries??
36 WdS.sc = 0.35*9.81;%N/m^2 -> weight of the solar cells (MicroLink devices)
37 %% DESIGN FACTORS
38 n = 2; %limit load factor ->Altman, p.38 states that n=2 is a reasonable number.

```

A.2 Main

```

1  %P : "Power"
2  %W : "Weight"
3  %E : "Energy"
4  %EdP: Energy/Power ->Energy divided Power
5  clear;close all;clc
6  run('input_data');
7  %% First Iteration
8  AR_vec = linspace(7,11,5);
9  Sw_vec = linspace(5,25,30);
10 %AR_vec = linspace(9.5/1.05,9.5/1.05,1);
11 %Sw_vec = linspace(9.975,9.975,1);
12 L_vec = zeros(length(AR_vec),length(Sw_vec)); %AR rows, Sw columns
13 W_vec = zeros(length(AR_vec),length(Sw_vec)); %AR rows, Sw columns
14 for i=1:length(AR_vec)
15     for j=1:length(Sw_vec)
16         AR = AR_vec(i);
17         Sw = Sw_vec(j);
18         %% Initial Calculations
19         CL = Cl; L = 1/2*rho*v^2*Sw*CL;
20         CDi = CL^2/(pi*AR*e);CD = Cd + CDi;
21         D = 1/2*rho*v^2*Sw*CD;
22
23
24         W_airframe = 0.022*Sw^1.55*AR^1.3;
25
26         S_sc = Sw*1;
27         W_sc = WdS_sc*S_sc; % "1": Sw = S_sc
28         %% Power consumption
29         P_propulsion = D*v/(eta_p*eta_motor);
30         %% Estimate the Weight (not iterative)
31
32         W_propulsion = WdP_propulsion*P_propulsion;%N
33         W_constant = W_sc + W_airframe + W_avionics + W_propulsion; %f(AR,Sw,v)
34         [E_rad,ts] = IntegrateRadiation();
35         [W_batteries, SparePower] = WeightBatteries(E_rad, P_propulsion, S_sc, eta_sc,...
36             eta.bat.out, EdW_batteries, P_avionics);
37
38         W = W_batteries + W_constant;
39
40         L_vec(i,j) = L;
41         W_vec(i,j) = W;
42         W_airframe_vec(i,j) = W_airframe;
43         W_sc_vec(i,j) = W_sc;
44         W_avionics_vec(i,j) = W_avionics;
45         W_propulsion_vec(i,j) = W_propulsion;
46         W_batteries_vec(i,j) = W_batteries;
47     end
48 end
49 c_max = sqrt(max(Sw_vec)/min(AR_vec));
50 c_min = sqrt(min(Sw_vec)/max(AR_vec));
51 Re_min = rho*v*c_min/mi;
52 Re_max = rho*v*c_max/mi;
53
54 PostProcess(L_vec,W_vec,AR_vec,Sw_vec, W_airframe_vec, W_sc_vec, ...
55     W_avionics_vec, W_propulsion_vec, W_batteries_vec);%AR files, Sw columns
56 save('data');

```

A.3 Incident Energy from the Sun

```

1 function [E_rad,ts] = IntegrateRadiation()
2 %E_rad is the energy per square meter from the radiation
3 div = 5;%divisions each hour
4 P_rad = readtable('RadiationJune.xlsx');
5     hours=size(P_rad,1);%amount of hours (24 hopefully)
6     pos = div*hours;%number of positions of E_rad
7 E_rad = zeros(pos,2);% time ; radiation
8
9 cont = 0;
10 for i=1:hours
11     if i<hours
12         fst = P_rad.radiation(i);%radiation this hour
13         scd = P_rad.radiation(i+1);%radiation next hour
14         in = (scd - fst)/div;%radiation increase each step
15     else
16         fst = P_rad.radiation(i);
17         scd = P_rad.radiation(1);
18         in = (scd - fst)/div;
19
20     end
21
22     for j=1:div
23         cont = cont +1;
24         E_rad(cont,2) = 1800/div*(2*fst + in*(2*j -1));%J/m^2
25         E_rad(cont,1) = P_rad.hour(i) + (j-1)/div; %hours
26         E_rad(cont,1) = E_rad(cont,1)*3600; %seconds
27     end
28 end
29 ts = 3600/div; %timestep (seconds)
30 plot(E_rad(:,1),E_rad(:,2),'color',[0 0 0])
31 end

```

A.4 Weight of the Batteries

```

1 function [W_batteries, SparePower] = WeightBatteries(E_rad, P_propulsion, S_sc, ...
2     eta_sc,...
3     eta.bat.out, EdW_batteries, P_avionics)
4
5 %CALCULATE W_batteries
6 [t1,t2,E_night,E_day] = EnergySwitch(P_avionics, P_propulsion, S_sc, eta_sc, E_rad);
7 tn = 24*3600 - (t2 - t1);%Night Duration
8 E_batteries_night = ((P_avionics + P_propulsion)*tn ...
9     -E_night*S_sc*eta_sc)*1/eta.bat.out;
10 W_batteries = E_batteries_night/EdW_batteries;
11 if E_day - (P_avionics + P_propulsion)*(t2 - t1) < E_batteries_night
12     warning('The batteries have not filled up!!')
13 end
14 SparePower = E_day-E_batteries_night-(P_avionics + P_propulsion)*(t2 - t1);
15 end

```

A.5 Calculate start and end of the day

```

1 function [t1,t2,E_night,E_day] = EnergySwitch(P_avionics, P_propulsion, S_sc, ...
    eta_sc, E_rad)
2 close all;
3 %P_avionics = 11;P_propulsion = 69; Sw = 10; eta_sc = 0.3;
4 %[E_rad,ts] = IntegrateRadiation();
5 ts = E_rad(2,1)-E_rad(1,1);%timestep
6 b1=false;%we start the loop when there isn't enough energy from solar cells -> ...
    false==night
7 E_night = 0; E_day = 0;
8 t1=0;t2=0;
9 for i=1:length(E_rad)
10
11 b2 = S_sc*eta_sc*E_rad(i,2) - ts*(P_avionics + P_propulsion)>0; %b2=true if energy ...
    balance >0
12
13 %Obtaining t1 and t2;
14 %From t1 -> t2 the batteries are filling up.
15     if b2≠b1 && b1==0
16         t1 = E_rad(i,1);
17         pos1 = i;
18     elseif b2≠b1 && b1==1
19         t2 = E_rad(i,1);
20         pos2 = i;
21     end
22 b1 = b2;
23
24 %Total energy obtained during night and during day
25     if b2 == 0
26         E_night = E_night + E_rad(i,2);
27     elseif b2 ==1
28         E_day = E_day + E_rad(i,2);
29     end
30
31
32 end
33
34 if t1==0 ||t2==0
35     warning('no hi ha prou potencia propulsiva! t1 o t2 no shan assignat');
36
37 end
38 %postprocess
39 %{
40 figure(1)
41 plot(E_rad(pos1:pos2,1),E_rad(pos1:pos2,2),'color',[0.5 0.5 ...
    0.5],'LineWidth',1,'DisplayName','Batteries filling up')
42 hold on
43 plot(E_rad(1:pos1,1),E_rad(1:pos1,2),E_rad(pos2:24*5,1),E_rad(pos2:24*5,2),'color',[0 ...
    0 0],'LineWidth',2,'DisplayName','Batteries providing energy')
44 hold on
45 %plot(E_rad([1:pos1,pos2:120],1),E_rad([1:pos1,pos2:120],2),'color',[0 0 ...
    0],'LineWidth',2,'DisplayName','Batteries providing energy')
46 legend
47 %}
48
49
50 end

```


A.6 Postprocess

```

1 function PostProcess(L_vec,W_vec,AR_vec,Sw_vec, W_airframe_vec, W_sc_vec, ...
2     W_avionics_vec, W_propulsion_vec, W_batteries_vec)
3 %load('data')->If you want to use the function as an independent code
4 %% Figure 1: W/L vs AR and Sw
5 figure(1)
6
7 for i=1:length(AR_vec)
8     lgd = ['AR = ', num2str(AR_vec(i))];
9
10    LdW = L_vec(i,:)./W_vec(i,:);
11    clr = [0.1 0.1 0.1]*(i-1)*9.5/(length(AR_vec)-1);
12    wdth = 2-1*(i-1)/(length(AR_vec)-1);
13    plot(Sw_vec,LdW, 'DisplayName',lgd,'color',clr,'linewidth',wdth);
14    hold on;
15 end
16 xlabel('Sw (m^2)')
17 ylabel('L/W')
18 title('Spare Weight of the UAV vs AR and Sw')
19 legend
20     hor = linspace(min(Sw_vec),max(Sw_vec),10);
21     ver = ones(10,1);
22     plot(hor, ver, '—', 'DisplayName','n=1','color',[0 0 0])
23     hold on;
24
25 %% Figure 2: W_airframe vs AR and Sw
26 figure(2)
27
28 for i=1:length(AR_vec)
29     lgd = ['AR = ', num2str(AR_vec(i))];
30
31     clr = [0.1 0.1 0.1]*(i-1)*9.5/(length(AR_vec)-1);
32     wdth = 2-1*(i-1)/(length(AR_vec)-1);
33     plot(Sw_vec,W_airframe_vec(i,:), 'DisplayName',lgd,'color',clr,'linewidth',wdth);
34     hold on;
35 end
36 xlabel('Sw (m^2)')
37 ylabel('W_{airframe} (N)')
38 title('Weight of the Airframe vs AR and Sw')
39 legend
40
41 %% Figure 3: W_batteries vs AR and Sw
42 figure(3)
43
44 for i=1:length(AR_vec)
45     lgd = ['AR = ', num2str(AR_vec(i))];
46
47     clr = [0.1 0.1 0.1]*(i-1)*9.5/(length(AR_vec)-1);
48     wdth = 2-1*(i-1)/(length(AR_vec)-1);
49     plot(Sw_vec,W_batteries_vec(i,:), 'DisplayName',lgd,'color',clr,'linewidth',wdth);
50     hold on;
51 end
52 xlabel('Sw (m^2)')
53 ylabel('W_{batteries} (N)')
54 title('Weight of the Batteries vs AR and Sw')
55 legend
56
57 %% Figure 4: W_propulsion vs AR and Sw
58 figure(4)

```

```

59
60 for i=1:length(AR_vec)
61     lgd = ['AR = ', num2str(AR_vec(i))];
62
63     clr = [0.1 0.1 0.1]*(i-1)*9.5/(length(AR_vec)-1);
64     wdh = 2-1*(i-1)/(length(AR_vec)-1);
65     plot(Sw_vec,W_propulsion_vec(i,:), 'DisplayName',lgd,'color',clr,'linewidth',wdh);
66     hold on;
67 end
68 xlabel('Sw (m^2)')
69 ylabel('W_{propulsion} (N)')
70 title('Weight of the Propulsion vs AR and Sw')
71 legend
72
73 %% Figure 5: W_sc vs AR and Sw
74 figure(5)
75
76 for i=1:length(AR_vec)
77     lgd = ['AR = ', num2str(AR_vec(i))];
78
79     clr = [0.1 0.1 0.1]*(i-1)*9.5/(length(AR_vec)-1);
80     wdh = 2-1*(i-1)/(length(AR_vec)-1);
81     plot(Sw_vec,W_sc_vec(i,:), 'DisplayName',lgd,'color',clr,'linewidth',wdh);
82     hold on;
83 end
84 xlabel('Sw (m^2)')
85 ylabel('W_{sc} (N)')
86 title('Weight of the Solar Cells vs AR and Sw')
87 legend
88
89 %% Figure 6: W_avionics vs AR and Sw
90 figure(6)
91
92 for i=1:length(AR_vec)
93     lgd = ['AR = ', num2str(AR_vec(i))];
94     clr = [0.1 0.1 0.1]*(i-1)*9.5/(length(AR_vec)-1);
95     wdh = 2-1*(i-1)/(length(AR_vec)-1);
96     plot(Sw_vec,W_avionics_vec(i,:), 'DisplayName',lgd,'color',clr,'linewidth',wdh);
97     hold on;
98 end
99 xlabel('Sw (m^2)')
100 ylabel('W_avionics (N)')
101 title('Weight of the avionics vs AR and Sw')
102 legend
103
104 %% Figure 7: W vs AR and Sw
105 figure(7)
106
107 for i=1:length(AR_vec)
108     lgd = ['AR = ', num2str(AR_vec(i))];
109     clr = [0.1 0.1 0.1]*(i-1)*9.5/(length(AR_vec)-1);
110     wdh = 2-1*(i-1)/(length(AR_vec)-1);
111     plot(Sw_vec,W_vec(i,:), 'DisplayName',lgd,'color',clr,'linewidth',wdh);
112     hold on;
113 end
114 xlabel('Sw (m^2)')
115 ylabel('W (N)')
116 title('Total Weight as a function of AR and Sw')
117 legend
118 end

```

B Weight Refinement Code

This section of the Appendix presents the code employed to refine the weight of the UAV in the second stage of the design — the Preliminary Design. This code is also a tool to calculate the center of gravity of the aircraft, indispensable for the aerodynamic study of stability.

B.1 Input Data

```
1 bw = 9.5; %wing span (m)
2 cw = 1.05; %wing chord (m)
3
4 bht = 2.57; %horizontal tail span (m)
5 cht = 0.43; %horizontal tail chord (m)
6
7 bvt = 1.15; %vertical tail span (m)
8 cvt = 0.38; %vertical tail chord (m)
9
10 lwt = bw/2; %Distance between aerodynamic centers of the tail and the chord
11 dwt = cw/4 + lwt - cht/4;%Distance between the LE of the wing and the LE of the ...
    horizontal tail
12
13 M.battery = 0.154; %154g each battery
14 n.batteries = 20;M.batteries = n.batteries*M.battery;
15
16 M.avionics = 4.9/9.81;%(kg)
17
18 M.sc.w = bw*cw*0.7*0.35;
19 M.sc.t = bht*cht*0.7*0.35*0;
20
21 M.propulsion = 6.9/9.81;%kg
22 %% Design parameters
23
24 xcg.batteries = 6/100;
25 xcg.avionics = 6/100;
26 xcg.propulsion = -5/100;% a negative xcg for the propulsion is sensible
27 xcg.sc.w = 0.5*cw;
28 %this also accounts for the weight of the control surfaces
29 xcg.sc.t = 0.55*cht + dwt;
```

B.2 Main

```

1 clear;clc;
2 %This function calculates the center of gravity of the plane
3 [M.airframe,xcg_skin_w,M_skin_w,xcg_skin_ht,M_skin_ht,xcg_skin_vt,M_skin_vt,...
4 xcg_profile_w,M_profile_w,xcg_profile_ht,M_profile_ht, xcg_profile_vt, M_profile_vt,...
5 M.mspar,M_tespar, M_htspar, M_vtspar, M_tetspar, M_tevtspar, M_boom] = ...
   WeightsPositions();
6
7 %% Input Data
8 %% Data
9 run('InputData_CG');
10
11 %CG referenced from the LE of the wing
12 % NOTE -> The xcg's of the wing and the tail are referred to their respective LE
13 %COMPUTE THE AIRFRAME MASS:
14 num_xcg_airframe = xcg_skin_w*M_skin_w + (xcg_skin_ht + dwt)*M_skin_ht + ...
   (xcg_skin_vt + dwt)*M_skin_vt...
15 +xcg_profile_w*M_profile_w + (xcg_profile_ht + dwt)*M_profile_ht + ...
   (xcg_profile_vt + dwt)*M_profile_vt...
16 +cw/4*M.mspar + (cw - 2.5/1000)*M_tespar + (dwt + cht/4)*M_htspar + (dwt + ...
   cvt/4)*M_vtspar...
17 + (dwt + cht - 1/1000)*M_tetspar + (dwt + cvt/4 - 1/1000)*M_tevtspar + ((dwt - ...
   cw)/2 + cw)*M_boom;
18 xcg_airframe = num_xcg_airframe/M.airframe;
19
20
21 num_xCG = xcg_airframe*M.airframe + xcg_batteries*M.batteries + ...
   xcg_avionics*M.avionics...
   + xcg_sc_w*M.sc_w + xcg_sc_t*M.sc_t + xcg_propulsion*M.propulsion + 1*6/100;
22 M = M.airframe + M.batteries + M.avionics + M.sc_w + M.sc_t + M.propulsion + 1;
23 xCG = num_xCG/M
24
25
26 M_vt = M_skin_vt + M_vtspar + M_tevtspar + M_profile_vt;
27 xcg_vt = ((xcg_skin_vt+dwt)*M_skin_vt + (dwt + cvt/4)*M_vtspar + (dwt + cvt/4 - ...
   1/1000)*M_tevtspar + (xcg_profile_vt + dwt)*M_profile_vt)/M_vt
28
29 M_ht = M_skin_ht + M_htspar + M_tetspar + M_profile_ht;
30 xcg_ht = ((xcg_skin_ht + dwt)*M_skin_ht + (dwt + cht/4)*M_htspar + (dwt + cht - ...
   1/1000)*M_tetspar + (xcg_profile_ht + dwt)*M_profile_ht)/M_ht
31
32 M_w = M_skin_w + M.mspar + M_tespar + M_profile_w;
33 xcg_w = (xcg_skin_w*M_skin_w + cw/4*M.mspar + (cw - 2.5/1000)*M_tespar + ...
   xcg_profile_w*M_profile_w)/M_w
34
35 xcg_boom = ((dwt - cw)/2 + cw)

```

B.3 Calculate Weight and Position of the elements of the Airframe

```

1 function ...
2     [M.airframe,xcg_skin_w,M.skin_w,xcg_skin_ht,M.skin_ht,xcg_skin_vt,M.skin_vt,...
3     xcg_profile_w,M_profile_w,xcg_profile_ht,M.profile_ht, xcg_profile_vt, ...
4     M_profile_vt,...
5     M.mspar,M.tespar, M.htspar, M.vtspar, M.tehtspar, M.tevtspar, M.boom] = ...
6     WeightsPositions()
7 run('InputData');
8 %Read Profile Coordinates (wing)
9 profilew = 'sd7003.dat';
10 [xw,yw] = ReadProfile(profilew);
11
12 %Read Profile Coordinates (tail)
13 profilet = 'sd8020.dat';
14 [xt,yt] = ReadProfile(profilet);
15
16 %% Xcg, Ycg, Mass of the skin
17 [xcg_skin_w, ycg_skin_w, perimeter_w] = PerimeterProfile(xw*cw, yw*cw);
18 M_skin_w = perimeter_w*bw*rho_skin*t_skin;
19 [xcg_skin_ht, ycg_skin_ht, perimeter_ht] = PerimeterProfile(xt*cht, yt*cht);
20 M_skin_ht = perimeter_ht*bht*rho_skin*t_skin;
21 [xcg_skin_vt, ycg_skin_vt, perimeter_vt] = PerimeterProfile(xt*cvt, yt*cvt);
22 M_skin_vt = perimeter_vt*bvt*rho_skin*t_skin;
23
24 M.skin = M.skin_w + M.skin_ht + M.skin_vt;
25 %% Xcg, Ycg, Mass of the profiles
26 [xcg_profile_w, ycg_profile_w, area_w] = AreaProfile(xw*cw, yw*cw);
27 [xcg_profile_vt, ycg_profile_vt, area_vt] = AreaProfile(xt*cvt, yt*cvt);
28 [xcg_profile_ht, ycg_profile_ht, area_ht] = AreaProfile(xt*cht, yt*cht);
29
30 M_profile_w = rho_profile*area_w*t_profile*n_profiles_w;
31 M_profile_vt = rho_profile*area_vt*t_profile*n_profiles_vt;
32 M_profile_ht = rho_profile*area_ht*t_profile*n_profiles_ht;
33
34 M_profiles = M_profile_w + M_profile_vt + M_profile_ht;
35 %% Xcg, Ycg, Mass of the spars
36 area_mspar = pi/4*diameter_mspar^2 - pi/4*(diameter_mspar - t_spar)^2;
37 M_mspar = area_mspar*bw*rho_spar;
38 area_tespar = t_spar*5/1000;%the te spar will be 5x0.9 mm
39 M_tespar = area_tespar*bw*rho_spar;
40 area_ttspar = pi/4*diameter_ttspar^2 - pi/4*(diameter_ttspar - t_spar)^2;%the two ...
41     tails will have the same spar
42 M_htspar = area_ttspar*bht*rho_spar;
43 M_vtspar = area_ttspar*bvt*rho_spar;
44 area_tetspar = t_spar*2/1000; %the tail te spar will be 2x0.9mm
45 M_tehtspar = area_tetspar*bht*rho_spar;
46 M_tevtspar = area_tetspar*bvt*rho_spar;
47
48 M.spars = M.mspar + M.tespar + M.htspar + M.vtspar + M.tehtspar + M.tevtspar;
49
50 area_boom = pi/4*diameter_boom^2 - pi/4*(diameter_boom - t_spar)^2;
51 M.boom = area_boom*(bw/2-3/4*cw-3/4*cht)*rho_spar;
52
53 M.airframe = M.skin + M_profiles + M.spars + M.boom;
54
55 end %function

```

B.4 Read Profile Points

```

1 function [x,y] = ReadProfile(namefile)
2 profile = fopen(namefile);
3 k= textscan(profile, '%f');
4 a=k{1};
5 x=zeros(length(a)/2,1);
6 y=zeros(length(a)/2,1);
7 for i=1:length(a)
8     par = ~ mod(i,2);
9     if par == 1
10        y(i/2) = a(i);
11    else
12        x((i+1)/2) = a(i);
13    end
14 end
15 end

```

B.5 Calculate the perimeter of the airfoil

```

1 function [xcg, ycg, perimeter] = PerimeterProfile(x, y)
2 %xcg = Int_num_x/Perimeter; ycg = Int_num_y/Perimeter
3 perimeter = 0;
4 Int_num_x = 0;
5 Int_num_y = 0;
6 for i=1:length(x)
7     if i==length(x)
8         p_i = sqrt((x(1) - x(i))^2+(y(1) - y(i))^2);
9         num_x_i = 1/2*(x(i) + x(1))*p_i;
10        num_y_i = 1/2*(y(i) + y(1))*p_i;
11    else
12        p_i = sqrt((x(i+1) - x(i))^2 + (y(i+1) - y(i))^2);
13        num_x_i = 1/2*(x(i) + x(i+1))*p_i;
14        num_y_i = 1/2*(y(i) + y(i+1))*p_i;
15    end
16    perimeter = perimeter + p_i;
17    Int_num_x = Int_num_x + num_x_i;
18    Int_num_y = Int_num_y + num_y_i;
19 end
20 xcg = Int_num_x/perimeter;
21 ycg = Int_num_y/perimeter;
22 end

```

B.6 Calculate the area of the airfoil

```

1  %Input: (B, rho, x, y,
2  %Output: [M, xcg, ycg,
3  function [xcg, ycg, area] = AreaProfile(x, y)
4
5  %xcg = Int_num_x/Int_den;   ycg = Int_num_y/Int_den;
6  Int_den = 0; %Area of the profile // Denominator in xcg and ycg calculus
7  Int_num_x = 0; %Numerator in xcg calculus
8  Int_num_y = 0; %Numerator in ycg calculus
9  for i=1:length(x)
10     if i==length(x)
11         A_i = 1/2*(x(i) - x(1))*(y(i) + y(1)); %Area of the portion i: y(x)*dx
12         num_x_i = 1/2*(x(i) + x(1))*A_i; %x*A_i = x*y(x)*dx
13         num_y_i = 1/2*(y(i) + y(1))*A_i; %y(x)*A_i = y(x)*y(x)*dx
14     else
15         A_i = 1/2*(x(i) - x(i+1))*(y(i) + y(i+1));
16         num_x_i = 1/2*(x(i) + x(i+1))*A_i;
17         num_y_i = 1/2*(y(i) + y(i+1))*A_i;
18     end
19     Int_den = Int_den + A_i;
20     Int_num_x = Int_num_x + num_x_i;
21     Int_num_y = Int_num_y + num_y_i;
22 end
23
24 xcg = Int_num_x/Int_den;
25 ycg = Int_num_y/Int_den;
26 area = Int_den;
27
28 end

```