

## Measurement of the group velocity of light in sea water at the ANTARES site

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## ABSTRACT

The group velocity of light has been measured at eight different wavelengths between 385 nm and 532 nm in the Mediterranean Sea at a depth of about 2.2 km with the ANTARES optical beacon systems. A parametrisation of the dependence of the refractive index on wavelength based on the salinity, pressure and temperature of the sea water at the ANTARES site is in good agreement with these measurements.

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## 1. Introduction

The ANTARES neutrino telescope is located on the bottom of the Mediterranean Sea (42°50' N, 6°10' E) at a depth of 2475 m, roughly 40 km offshore from Toulon in France. The main objective of the experiment is the observation of neutrinos of cosmic origin in the southern hemisphere sky. Sea water is used as the detection medium of the Cherenkov light induced by relativistic charged particles resulting from the interaction of neutrinos. The particle trajectory is reconstructed from the measured arrival times of the detected photons. The detector consists of 885 photomultiplier tubes (PMTs) mounted on twelve vertical lines with a length of about 450 m. The horizontal separation between lines is about 70 m. Further details can be found elsewhere [1–3].

Charged particles traveling through sea water produce the emission of Cherenkov light whenever the velocity of the particle exceeds that of light in water. The Cherenkov photons are emitted at a characteristic angle,  $\theta_c$ , with respect to the particle direction. This angle is related to the index of refraction of the medium as  $\cos \theta_c = \frac{1}{\beta n_p}$ . In this,  $\beta$  is the velocity of the particle relative to the speed of light in vacuum. The index of refraction,  $n_p$ , corresponds to the ratio between the speed of light in vacuum and the phase velocity of light in water. The individual photons then travel through the water at the group velocity. Both the phase and the group velocity depend on the wavelength of the photons. This is usually referred to as chromatic dispersion. The group velocity is related to its phase velocity in the following way:

$$n_g = \frac{n_p}{1 + \frac{\lambda}{n_p} \frac{dn_p}{d\lambda}} \quad (1)$$

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where  $\lambda$  is the wavelength of light. The index of refraction,  $n_g$ , corresponds to the ratio between the speed of light in vacuum and the group velocity of light in water.

Since the PMTs cannot distinguish the photon wavelength, the variation of the photon emission angle and the group velocity due to chromatic dispersion cannot be accounted for on the individual photon level. Nevertheless, the average effect of the wavelength dependencies are accounted for in the algorithm used to reconstruct the particle trajectory [4,5].

A measurement of the group velocity of light has been made using the optical beacon system of ANTARES. This system consists of a set of pulsed light sources (LEDs and lasers) which are distributed throughout the detector and illuminate the PMTs with short duration flashes of light. The refractive index is deduced from the recorded time of flight distributions of photons at different distances from the sources for eight different wavelengths between 385 nm and 532 nm.

## 2. Experimental setup

The PMTs of ANTARES are sensitive to photons in the wavelength range between 300 nm and 600 nm. The maximum quantum efficiency is about 22% between 350 nm and 450 nm. The arrival time and integrated charge of the analogue pulse from the PMT are measured by the readout electronics [6]. The transit time spread of single photo-electrons of the PMT is around 3.5 ns (FWHM) [7].

The group velocity of light has been measured using the ANTARES optical beacon system. This system was primarily designed to perform time calibration *in situ* [7,8]. There are two types of optical beacons, the LED optical beacons and the laser beacons. There are four LED optical beacons distributed along each detector line and two laser beacons at the bottom of two central lines. The *in situ* measurement of the temperature and salinity is provided by some conductivity/temperature/depth sensors.<sup>5</sup>

<sup>5</sup> SEABIRD CTD (SBE37-SMP), <http://www.seabird.com/>.

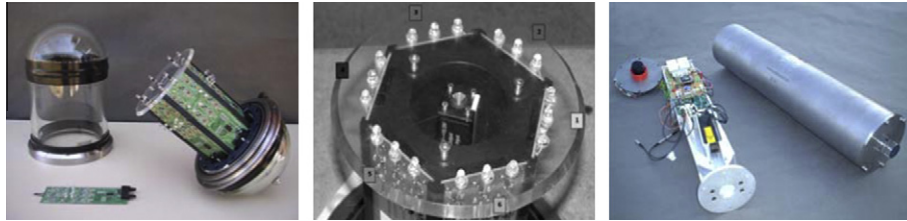


Fig. 1. Picture of a standard LED optical beacon (left), the modified LED optical beacon (middle) and a laser beacon (right).

A standard LED optical beacon contains 36 individual LEDs distributed over six vertical faces forming a hexagonal cylinder housed in a pressure resistant glass enclosure (Fig. 1, left). On each face, five LEDs point radially outwards and one upwards. All LEDs emit light at an average wavelength of 469 nm, except the two LEDs located on the lowest LED optical beacon of Line 12 which emit light at an average wavelength of 400 nm. A modified LED optical beacon was installed in 2010 on Line 6. This LED optical beacon has three LEDs per face instead of six, all of them pointing upwards (Fig. 1, centre). The three LEDs of each face emit light of the same colour. The average wavelength of the light from the six faces are 385, 400, 447, 458, 494 and 518 nm. The LEDs emit light with a maximum intensity of about 160 pJ and a pulse width of about 4 ns FWHM. The intensity of the emitted light can be varied changing the voltage feeding the LEDs.

The laser beacon consists of a Nd-YAG solid state laser (Fig. 1, right). It can emit pulses of light with an intensity of about 1  $\mu$ J and pulse width of about 0.8 ns FWHM. The average wavelength is 532 nm. This light is spread out by an optical diffuser, so that the light can reach the surrounding lines. During calibration runs, the LEDs and lasers flash at a frequency of 330 Hz. Further details about the optical beacon system can be found elsewhere [7–9].

The wavelength spectra of the light sources used for this analysis were measured using a calibrated spectrometer<sup>6</sup> (see Fig. 2a). The typical width of each spectrum is around 10 nm except for the green LED (518 nm), which is larger, and the laser (532 nm), which is much smaller.

Due to the wavelength dependence of the absorption of light in water, the spectra change as a function of the distance travelled by the light. The expected wavelength distributions as a function of distance have been estimated by Monte Carlo simulations using the dependence of absorption length on wavelength given by Smith and Baker [10]. In Fig. 2b the spectra at a distance of 120 m are shown for the different light sources. In particular, absorption has a large effect for wavelengths above 500 nm. Notice that the distributions have been renormalised to unity in each peak and therefore the relative effect of absorption between sources is not observed. This renormalisation is performed in order to show the change in the shapes of the distributions, which is what influences the velocity measurement. The evolution of the spectra is taken into account in the final results (Section 4), in particular the uncertainty assigned to the wavelengths has been taken to be the root mean square (RMS) of the wavelength distribution given by the simulation.

### 3. Data acquisition and analysis

In order to measure the optical properties of the deep sea water, designated data taking runs were performed using the optical beacon system. During these runs, one single LED located in the lowest optical beacon of a line and pointing upward was flashed. Only the signals recorded by the PMTs along the same line are used in the

analysis. As a result, the line movements due to the sea currents can safely be ignored.

The runs used in this analysis were taken between May 2008 and April 2011. Each run contains typically more than 100,000 light flashes. Each flash is detected by a small PMT inside the optical beacon. The time of the flash and the arrival times of the photons on the PMTs were recorded within a time window from 1500 ns before to 1500 ns after the flash. The integrated charge of the analogue pulses of the PMTs were also recorded. Only runs were used when the average rate of background light was below 100 kHz.

In Fig. 3, the distribution of the arrival times of photons on a PMT located 100 m above the LED optical beacon ( $\lambda = 469$  nm) is shown. The time,  $t = 0$  ns, corresponds to the time of the flash. A clear peak at  $t = 470$  ns can be seen which corresponds to the shortest propagation time of the light. The tail with late photons can be attributed to light scattering. The flat background arises from the optical background due to <sup>40</sup>K decays and bioluminescence.

A convolution of a Gaussian and an exponential distribution on top of a flat background is fitted to the data. The Gaussian distribution reproduces the transit time spread of the PMTs, the duration of the light flash and the effect of the chromatic dispersion in water. The exponential distribution takes into account the effect of the scattering of photons in water. The fit function can be formulated as:

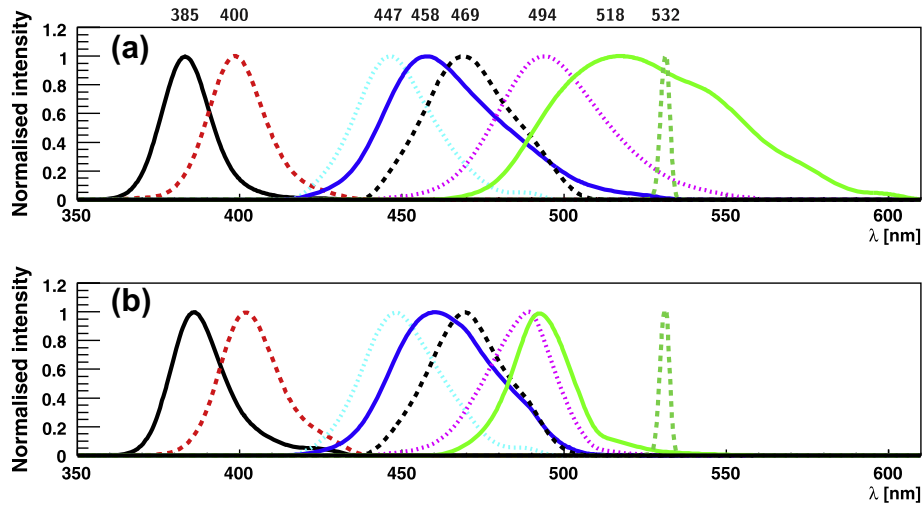
$$f(t) = B + S \cdot e^{-\frac{t-\mu}{\tau}} \times \text{erfc}\left(\frac{1}{\sqrt{2}}\left(\frac{\sigma}{\tau} - \frac{t-\mu}{\sigma}\right)\right) \quad (2)$$

where  $t$  is the arrival time of the photons. The fit parameters are the optical background,  $B$ , the signal strength,  $S$ , the mean,  $\mu$ , and width,  $\sigma$ , of the Gaussian distribution and the exponential decay constant,  $\tau$ . In Eq. 2,  $\text{erfc}(t)$  is the complementary error function distribution. An example of the fit is shown in the inset of Fig. 3. The fit is determined in the range from 200 ns before the most populated bin and 20 ns after. The arrival time of the light flash at each PMT is estimated by the fitted mean value of the Gaussian distribution.

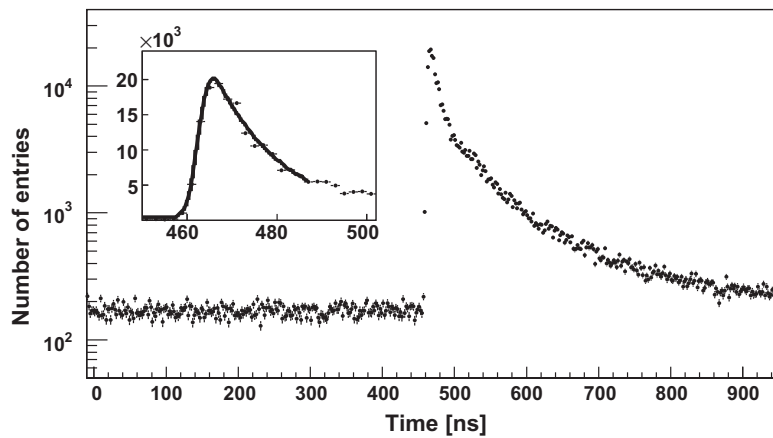
An example of the measured arrival times as a function of the distance between the optical beacon and the PMT is shown in Fig. 4a. A linear function has been fitted to the data to extract the group velocity of the light. In the fitting procedure, the distance between the light source and the PMT has been restricted to the range between 50 m and 250 m in order to limit the effects of time slewing [7] and optical background on the measurement.

A Monte Carlo simulation of the response of the detector to LED flashes has been made. The analysis method was performed to validate the analysis procedure and to study the systematic effects due to the assumed light absorption and scattering parameters. Table 1 shows the different contributions to the systematic uncertainty in the measurement of the refractive index. These contributions have been determined as follows. For the wavelength values of 400 nm, 470 nm and 532 nm, the difference of the refractive index obtained after the fitting procedure with respect to the input refractive index is shown in the first row of Table 1. This variation, which has been computed for the default values of absorption and

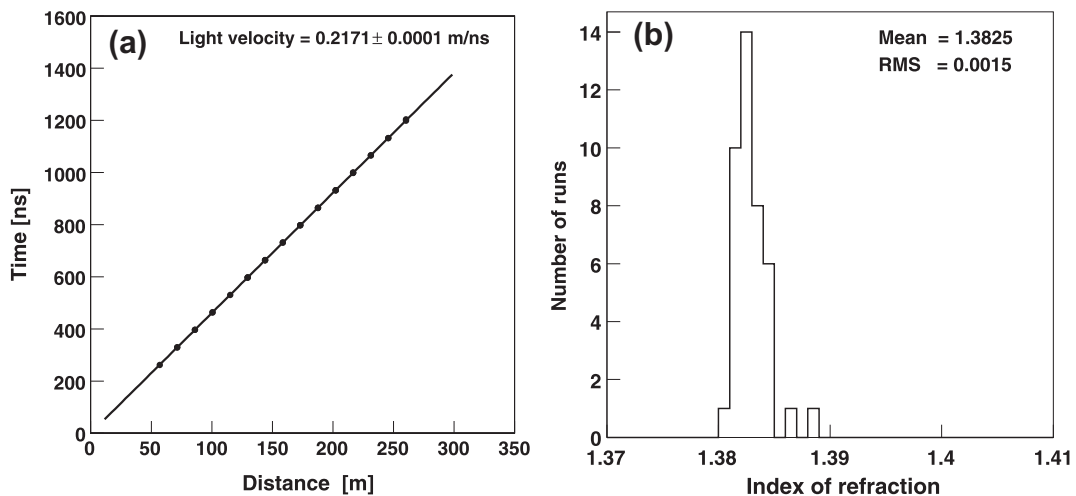
<sup>6</sup> Ocean Optics HR4000CG-UV-NIR, <http://www.oceanoptics.com/>.



**Fig. 2.** (a) Wavelength spectra of the light sources used in this work as measured with a calibrated spectrometer. The spectrometer measurements are made in air. The data points have been smoothed and the highest value of each spectrum is set equal to one. On the top of the Figure the peak wavelengths are indicated in units of nm. (b) Simulated light spectra at a distance of 120 m in sea water with the highest value renormalized to one. The differences between the spectra are due to the variation of the absorption length as a function of the wavelength.



**Fig. 3.** Example of a distribution of arrival times observed at a distance of 100 m from an LED. The inset shows a zoom around the signal region. The solid curve corresponds to a fit function as described in the text and given in Eq. 2.



**Fig. 4.** (a) Arrival time as a function of the distance between the LED ( $\lambda = 469$  nm) and the PMT for one single run. The solid line corresponds to a fit of a linear function to the data (see text). (b) Distribution of the measured refractive index for a total of 42 runs.

**Table 1**

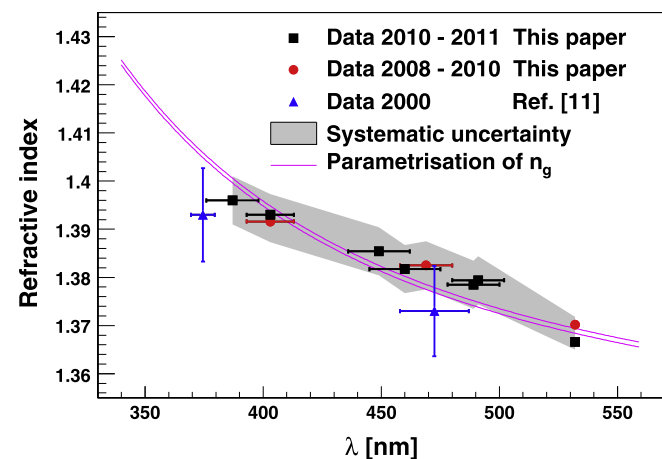
The systematic uncertainty of the refractive index measurement is estimated for three different wavelengths by varying the absorption length and the scattering length (see text).

Wavelength [nm]	400	470	530
Source of uncertainty	Variation in [%]		
Method	0.27	0.13	0.04
Absorption length	0.11	0.05	0.07
Scattering length	0.22	0.34	0.24
Total systematic uncertainty [%]	$\pm 0.37$	$\pm 0.37$	$\pm 0.25$

scattering lengths, is termed “Method”. In the second row, the variation in percentage of the fitted value is shown when the absorption length changes by  $\pm 50\%$ . Finally, in the third row the variation in percentage of the fitted value is shown when the scattering length is varied between 20 m and 70 m [11]. As can be seen, the latter is the largest contribution to the systematic uncertainty. Adding in quadrature these values one obtains a systematic error that varies from 0.25% to 0.37% depending on the wavelength.

#### 4. Determination of the refractive index

Between May 2008 and March 2010, a total of 42 runs were taken using an LED with an average wavelength of 469 nm. Three different LED intensities were used. For a high, middle or low intensity run the range of distances between the optical beacon and the PMT used in the fit were 50–250 m, 40–220 m and 10–130 m, respectively. The measured refractive index values of these runs are shown in Fig. 4b. In addition to these runs, 14 runs using an LED with an average wavelength of 400 nm and 13 runs using an LED with an average wavelength of 532 nm were taken. Between November 2010 and April 2011 eight runs with a modified optical beacon were taken, extending the measurements with six additional wavelengths. The index of refraction is estimated at each wavelength by the mean of the distribution. The measured refractive indices with the systematic uncertainty are shown in Fig. 5 and tabulated in Table 2. As mentioned in Section 2, the uncertainties in the wavelengths have been taken to be the RMS of the corresponding distribution at the middle of the distance ranges. The variation of the RMS values in this range with respect to the middle is  $\pm 2$  nm.



**Fig. 5.** Index of refraction corresponding to the group velocity of light as a function of the wavelength. Also shown are results from measurements made in [11]. The grey band shows the systematic uncertainty. The two solid lines correspond to a parametrization of the index of refraction evaluated at a pressure of 200 atm (lower line) and 240 atm (upper line) (see text).

**Table 2**

Summary of the refractive index results for the 2008–2011 data shown in Fig. 5. For the refractive index first the statistical uncertainties are shown. They are computed as the RMS of the measured refractive index for each wavelength divided by the square root of the number of runs. In addition, there is a total systematic uncertainty of  $\pm 0.005$ .

Wavelength (nm)	Refractive index	Number of runs	Time period
$403 \pm 10$	$1.3916 \pm 0.0007$	14	2008–2010
$469 \pm 12$	$1.3825 \pm 0.0002$	42	2008–2010
$532 \pm 1$	$1.3702 \pm 0.0007$	13	2008–2010
$387 \pm 11$	$1.3960 \pm 0.0007$	8	2010–2011
$403 \pm 10$	$1.3930 \pm 0.0007$	8	2010–2011
$449 \pm 13$	$1.3854 \pm 0.0003$	8	2010–2011
$460 \pm 15$	$1.3817 \pm 0.0003$	8	2010–2011
$489 \pm 11$	$1.3785 \pm 0.0003$	8	2010–2011
$491 \pm 11$	$1.3794 \pm 0.0006$	8	2010–2011
$532 \pm 1$	$1.3666 \pm 0.0006$	8	2010–2011

The velocity of light in sea water at a given wavelength depends on the temperature, the salinity and the pressure of the water, because the density of sea water depends on these variables. A parametrization of the light velocity proposed by Quan and Fry [12] is based on data from Austin and Halikas [13]. This parametrization was modified to incorporate a correction for pressure [11]. During the data taking period, the temperature and salinity were measured *in situ* at a depth of 2250 m. At an ambient temperature of  $T = 12.9 \pm 0.1^\circ\text{C}$  and salinity of  $S = 38.48 \pm 0.01 \text{‰}$ , the refractive index corresponding to the phase velocity as a function of wavelength is expressed as:

$$n_p(\lambda, p) = 1.32292 + (1.32394 - 1.32292) \times \frac{p - 200}{240 - 200} + \frac{16.2561}{\lambda} - \frac{4382}{\lambda^2} + \frac{1.1455 \times 10^6}{\lambda^3} \quad (3)$$

where  $\lambda$  is the wavelength (in units of nm) and  $p$  is the pressure (in units of atm). Using Eq. 1, the result of this parametrization can be compared to the measurements (see Fig. 5).

From the known variations of temperature, salinity and pressure, the refractive index for a particular wavelength and at a given depth can be determined with an accuracy of better than  $4 \times 10^{-5}$ . The parametrization is in good agreement with the measurements.

As mentioned in Section 1, the PMTs are unable to distinguish the wavelength of the incoming photons, so the effect of this chromatic dependence can only be taken into account on average. The spread of the arrival time residuals with respect to the expected arrival time of a 460 nm photon have been computed by means of a standalone Monte Carlo simulation using the phase velocity for the emission angle and the group velocity (as given by the Eqs. 3 and 1) for the arrival time. This simulation indicates that the spread of the time residual is 0.6 ns at 10 m, 1.6 ns at 40 m, 2.7 ns at 100 m and 3.6 ns at 200 m. The time uncertainty introduced by this spread is unavoidable and is taken into account in the ANTARES official simulation program [14,15]. Even though the exact influence of the medium depends on the particular Cherenkov photon (wavelength, distance to the hit PMT) and therefore requires a full simulation, a rough estimate of the average effect can be obtained assuming that a majority of hits are between 40 m and 100 m from the track, which gives a value of  $\sim 2$  ns for the uncertainty introduced by the transmission of light in sea water, including chromatic dispersion. This value is to be compared with  $\sim 1.3$  ns coming from the PMTs transit time spread and to  $\sim 1$  ns from time calibration. Monte Carlo simulation studies show also that an additional uncertainty of  $\sim 2$  ns on the spread of the time residual degrades the neutrino pointing accuracy about 0.1 degrees.

## 5. Summary

Using pulsed light sources with wavelengths between 385 nm and 532 nm the group velocity of light in sea water at the ANTARES site has been measured as a function of wavelength. The emission spectra determined in the laboratory for the different pulsed sources have been used as input to a Monte Carlo simulation in order to correct for the effect of absorption on the corresponding velocity measurement. Except for two sources these corrections are in general small. Likewise, a Monte Carlo simulation has been used to evaluate the systematic uncertainties and to check, that the procedure to obtain the speed of light is robust and unbiased. The results obtained for the dependence of the group refractive index on wavelength are in agreement with the parametrisation as a function of salinity, pressure and temperature of sea water at the ANTARES site.

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