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# Electrically Driven Varifocal Silicon Metalens

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## Abstract:

**Optical metasurfaces have shown to be a powerful approach to planar optical elements, enabling an unprecedented control over light phase and amplitude. At that stage, where wide variety of static functionalities have been accomplished, most efforts are being directed towards achieving reconfigurable optical elements. Here, we present our approach to an electrically controlled varifocal metalens operating in the visible frequency range. It relies on dynamically controlling the refractive index environment of a silicon metalens by means of an electric resistor embedded into a thermo-optical polymer. We demonstrate precise and continuous tuneability of the focal length and achieve focal length variation larger than the Rayleigh length for voltage as small as 12 volts. The system time-response is of the order of 100 ms, with the potential to be reduced with further integration. Finally, the imaging capability of our varifocal metalens is successfully validated in an optical microscopy setting. Compared to conventional bulky reconfigurable lenses, the presented technology is a lightweight and compact solution, offering new opportunities for miniaturized smart imaging devices.**

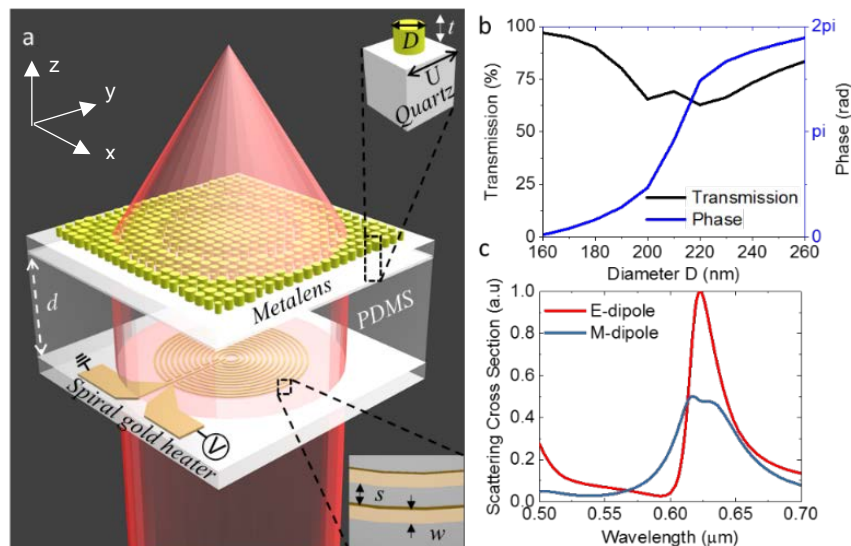
**Keywords: Metasurfaces, Reconfigurability, Varifocal metalens, Dielectric nano-disks, electro-thermo-optical control**

Metasurfaces are 2D metamaterials that have gained enormous attention due to their ability to manipulate light wavefronts at the subwavelength scale, thus enabling planarization of bulky elements.<sup>1-4</sup> Optical metamaterials, in general, are formed by optical scatterers as building blocks, also known as meta-atoms, assembled judiciously to provide operation on demand. Not only these meta-atoms offer planarization, as in case of metasurfaces; they also allow exotic properties, such as cloaking,<sup>5-9</sup> negative refractive index<sup>10-14</sup> and super/hyperlensing,<sup>15-20</sup> which cannot be achieved with conventional optical materials. In recent years, a considerable amount of efforts has been devoted to the design of metalenses.<sup>2,21-28</sup> Based on the geometrical and physical properties, meta-atoms impart a phase, ranging from 0 to  $2\pi$ , on the impinging light and are arranged according to hyperboloid lens phase profile.<sup>27</sup> Metalenses can be made either plasmonic<sup>21-23,28</sup> or dielectrics.<sup>2,24-27,29</sup> Plasmonics-based metalenses tend to suffer from a low efficiency and transmission owing to the intrinsic losses of metallic scatterers in the visible. Conversely, metalenses based on high susceptibility dielectric

materials offer high transmission, efficiency, and compatibility with current microelectronics technology.<sup>30</sup> In addition, both plasmonic and dielectric meta-atoms are also capable of controlling, locally, other properties of light such as polarization, direction and amplitude.

While most progresses so far have focused on static metalens, a further penetration into the industrial sector requires developing reconfigurable metalenses whose focus can be adjusted in real time. In the broad context of metasurfaces, reconfigurability has been achieved by embedding metasurface in liquid crystal,<sup>31,32</sup> electrically driven carrier accumulation/depletion,<sup>33–35</sup> and phase change and phase transition materials including GST,<sup>36–38</sup> VO<sub>2</sub>,<sup>39–42</sup> V<sub>2</sub>O<sub>3</sub>,<sup>43,44</sup> SmNiO<sub>3</sub>,<sup>45</sup> and NdNiO<sub>3</sub>.<sup>46</sup> All these techniques can be potentially employed to design varifocal metalenses. More recent examples of varifocal metalenses are based on a mechanical actuation. For instance, several works have proposed configuration where the metalens stands on a stretchable or elastic substrate allowing the focal length to be changed upon mechanical strain.<sup>47,48</sup> While enabling diffraction limited focusing with large focal distance tuning (> 130 %<sup>47</sup> and > 66 %<sup>48</sup>) and maintaining high efficiency, this approach entails an external mechanical control which may alter the integration and limits the metalens response time. Alternatively, Arbabi and colleagues have recently demonstrated a compact MEMS-based tunable metalens<sup>49</sup> with large optical power tuning and scanning speed reaching up to few kHz. Another strategy recently reported by She *et al.*, relies on electrically tunable dielectric elastomer actuators (DEAs)<sup>50</sup> capable of focal distance tuning of more than 100 %, astigmatism and image shift correction, all simultaneously. While very promising, both configurations require high power/voltage (80 V and 3 kV, respectively) to achieve a substantial focal change.

Here, we present a varifocal metalens formed by cascading a static silicon-on-quartz metalens with electro-thermo-optical control. Focus tuneability is achieved by properly controlling the temperature profile within a thermo-optical material.<sup>51</sup> We fully characterize the system performance, including beam profiling, focus tuneability range and time response. Finally, we demonstrate its suitability for adjustable imaging.



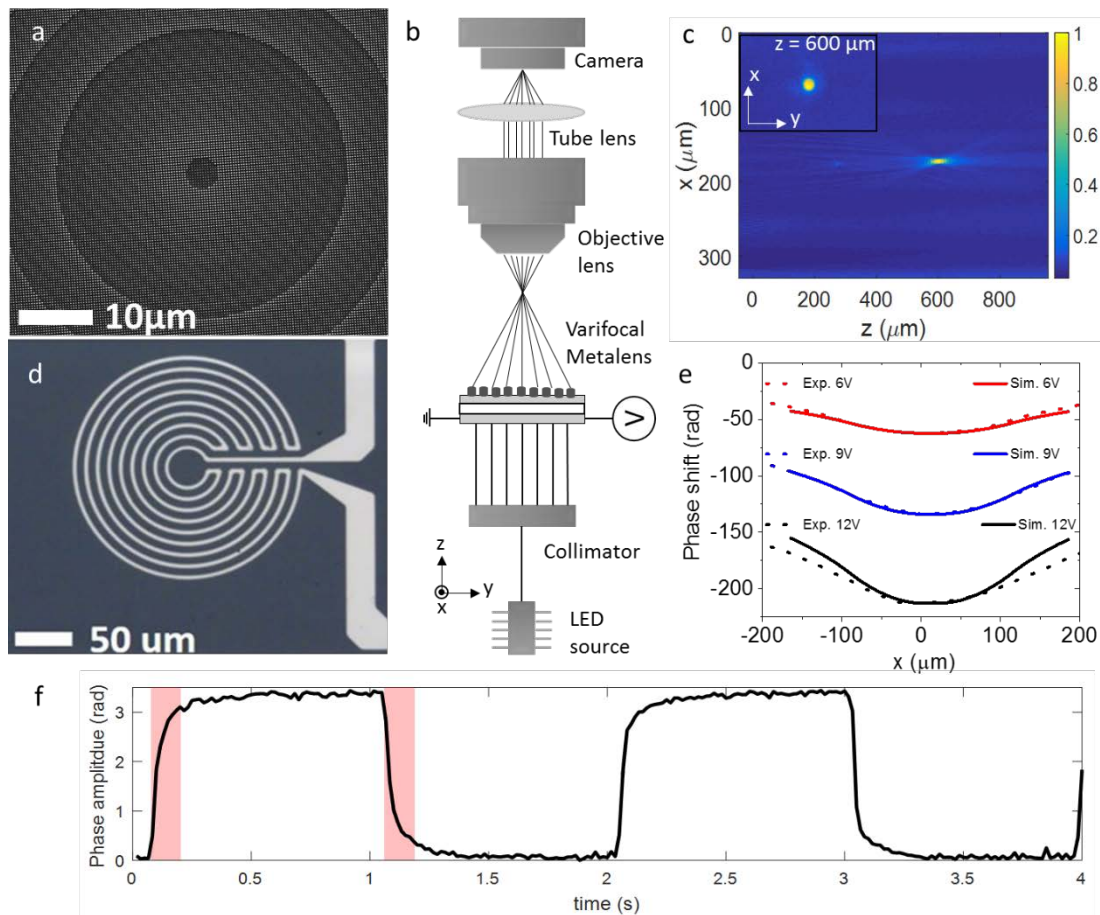
**Figure 1:** Concept of electrically-controlled varifocal metalens. (a) Schematic of the system illustrating both building blocks. (b) Simulated optical transmission and accumulated phase at 632 nm for a silicon nano-disk of varying diameter,  $U = D + 90$  nm, and  $t = 100$  nm. (c) Simulated scattering cross-section contribution of electric and magnetic dipole for a silicon nano-disk with  $D = 210$  nm,  $t = 100$  nm, and  $U = 300$  nm.

Our varifocal system is formed of two building blocks; a high permittivity metalens and an electro-thermo-optical module (Figure 1(a)). The latter, located in the back front of the metalens, enables to

dynamically control the optical phase accumulated by the transmitted light before it is focused. The metalens is 300  $\mu\text{m}$  diameter and made of amorphous silicon-on-quartz cylindrical pillars of 100 nm height. The periodicity of the unit cell  $U$  is equal to  $D + 90$  nm, where  $D$  is the diameter of the silicon nano-disk, optimized to cover the phase from 0 to  $2\pi$  and satisfy 1<sup>st</sup> Kerker condition at visible wavelength of 632 nm.<sup>24,52</sup> Optimal diameters for the silicon nano-disks were identified by using the commercial finite element method (FEM)-based simulation tool COMSOL MULTIPHYSICS (See Supporting Information for detail). Figure 1(b) shows the simulated transmission and phase of silicon nano-disks for diameters  $D$  ranging from 160 nm to 260 nm, at 632 nm wavelength. In addition, we also identified that for a disk diameter of 210 nm, electric and magnetic dipole resonances overlap, enabling to minimize reflection (Figure 1(c)). The scattering cross-section contribution given in Figure 1(c) were calculated using multipole decomposition.<sup>24</sup> To form the metalens, silicon nano-disks were arranged according to the following hyperboloid phase profile<sup>27</sup>:

$$\phi_t(x, y) = 2\pi - \frac{2\pi}{\lambda} \left( \sqrt{x^2 + y^2 + f^2} - f \right) \quad 1$$

Where  $\phi_t(x, y)$  stands as the required phase profile for the nano-disk placed at coordinates  $(x, y)$ ,  $f$  is the focal length, and  $\lambda$  is the wavelength of operation (632 nm).



**Figure 2:** Description and characterization of the fabricated varifocal metalens. (a) SEM image of the central portion of the silicon metalens. (b) Optical setup for the characterization of the varifocal metalens. (c) Optical mapping of the focus created by a silicon metalens with diameter of 300  $\mu\text{m}$  and focal length of 600  $\mu\text{m}$  (without gold spiral heater). The inset shows the spot at focal plane ( $z = 600 \mu\text{m}$ ) and the color bar refers to normalized intensity. (d) SEM image of the gold spiral heater. (e) Simulated (solid lines) and experimental (dashed lines) thermally induced phase shift (in radians) by gold spiral heater with diameter

of 200  $\mu\text{m}$ , as a function of applied voltage. (f) Time response of gold spiral heater for applied square wave signal (0 - 2.5 V). The rise and fall time are highlighted in red areas.

The electro-thermo-optical module consists of a gold spiral resistor of 200  $\mu\text{m}$  diameter covered with a PDMS slab of thickness  $d$  equal to 700  $\mu\text{m}$  (Figure 1(a)). The spiral geometry was chosen in order to introduce a paraboloid shaped refractive index gradient in the PDMS layer. The gold stripes are 4  $\mu\text{m}$  wide, 50 nm thick and spaced by 6  $\mu\text{m}$ , as shown in Figure 1(a) (bottom right inset). We fabricated the electrically varifocal metalens using combination of electron beam lithography and UV lithography technique (see Supporting Information). Figure 2(a) shows the scanning electron microscopy (SEM) image of the central portion of the fabricated metalens with focal length of 600  $\mu\text{m}$  and Figure 2(d) shows an electron micrograph of the fabricated gold spiral heater.

For the characterization of the varifocal metalens, we used a homemade optical setup, sketched in Figure 2(b). A 632 nm LED light source is collimated on the varifocal metalens which is placed on a 3D micrometric stage. All the light transmitted through the varifocal metalens is focused onto an intermediate plane, and re-imaged onto a CCD camera by a custom-built microscope, consisting of a microscope objective (x20 magnification) and a tube lens. DC power supply is used to apply voltage to the spiral resistor. For reference, we first characterized the metalens (theoretically designed to have a focal length of 600  $\mu\text{m}$ ) in absence of gold spiral resistor. Mapping of the optical intensity (Figure 2(c)) shows the experimental focal length to be exactly 600  $\mu\text{m}$  and the focal spot diameter of 7.5  $\mu\text{m}$ .

Subsequently, we also simulated and experimentally characterized the PDMS coated gold spiral heater (without metalens) in order to quantify its effect on the incoming wavefront (see Supporting Information). Simulations were performed for the same applied voltages of 6, 9 and 12 V used in our experiments. We extracted the temperature profile induced into the PDMS from the simulation and calculated the associated refractive index using the following equation:

$$n(T) = n(T_0) + \left(\frac{dn}{dT}\right) * (T - T_0) \quad 2$$

Where,  $n(T)$  is the temperature dependent refractive index of PDMS,  $n(T_0)$  is the refractive index of PDMS at room temperature and is equal to 1.412,<sup>53</sup>  $\left(\frac{dn}{dT}\right)$  is equal to  $-4.5*10^{-4}$  (1/K)<sup>54</sup> and  $T_0$  is the room temperature in Kelvin, i.e. 298 K. Finally, we calculate the thermally induced phase-shift, i.e. the difference in optical path of an incoming planar wave associated to switching on the heater, by integrating the refractive index along the axial direction ( $z$ -axis).

The numerical simulations are compared to experimental wavefront measurements performed on the electro-thermo-optical module (Figure 2(e)). The simulated (solid lines) and experimental phase shift profiles along the  $x$ -axis (dashed lines) show an excellent agreement for applied voltages of 6 and 9 V while further deviation is observed for 12 V.

Once validated the phase profile introduced by the electro-thermo-optical module, we are interested in its time response, which will entirely dictate the operation speed of the varifocal lens. Figure 2(f) shows the maximum amplitude of the thermal phase-shift plotted against time, upon a periodic electrical driving with a square signal at 0.5 Hz and 2.5 V amplitude. Our data give a rise time of 125 ms (10 % to 90 % rise) and a fall time of 130 ms (90 % to 10 % fall) highlighted by the red shading. These values are in good agreement with the time scale of the temperature evolution<sup>55</sup>  $\tau = l_c^2 / (4Ds) \approx 100$  ms, where  $l_c$  is the characteristic length of the system, i.e. the spiral diameter ( $l_c = 200$   $\mu\text{m}$ ), and  $Ds$  the thermal diffusivity of the surrounding ( $Ds \approx 10^{-7}$   $\text{m}^2 \cdot \text{s}^{-1}$  for PDMS). It is noteworthy mentioning that this characteristic time could be significantly reduced by decreasing the spiral

diameter  $l_c$ . For instance, for a spiral diameter  $l_c = 20 \mu\text{m}$ , we expect the response time to decrease to  $\tau \approx 1 \text{ms}$ .

In addition, we also measured the transmittance of the metalenses and the gold spiral heater, separately. For this purpose we used the same optical setup as in Figure 2(b), replacing the camera by a fiber-coupled spectrometer (SHAMROCK - SR-3031-A). By using a pinhole, we made sure that the light coupled to the spectrometer only originated from an aperture size equal to the diameter of metalens or gold spiral heater. The transmittance at 632 nm of metalenses with 600  $\mu\text{m}$  and 1000  $\mu\text{m}$  focal length are listed in Tables 1 and 2, respectively. For the spiral gold heater module the transmittance was measured as a function of the applied voltage, being 73 %, 72 %, 71 % and 69 % for applied voltages of 0, 3, 6, and 9 V, respectively. A transmittance decrease with increasing voltage is expected due to the increase in temperature which leads to increasing absorption losses in gold.

Other important parameters to characterize our device, are the focusing efficiency and Strehl ratio. We determined the focusing efficiency by dividing the amount of light passing through an aperture of radius equal to 3 times the FWHM of the focal spot by the total input light illuminating the metalens.<sup>26</sup> To calculate the Strehl ratio, we followed the same protocol as given by Khorasaninejad *et. al*<sup>56</sup> (also see Supporting Information for details). Both focusing efficiency and Strehl ratio are shown in Table 1 and Table 2 for both of the metalenses.

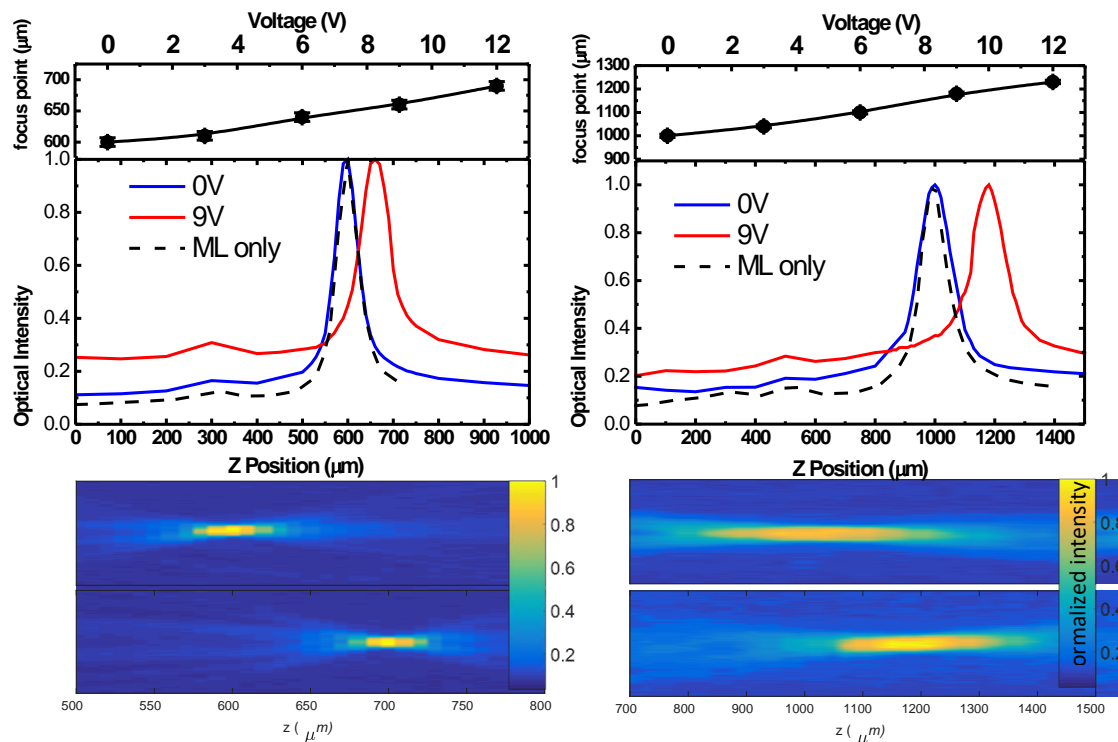


Figure 3: Tuning capability of the varifocal metalens. (a) – (c) refer to the lens with designed focal length of 600  $\mu\text{m}$  and (d) – (f) show the lens with 1000  $\mu\text{m}$  focal length. (a) and (d) Change in the focal lengths vs different voltages. (b) and (e) Axial (z-crosscut) optical intensity distribution comparison of metalens only and varifocal metalens for 0 and 9 V. (c) and (f) XZ map of optical intensities for 0 and 9 V. The scale bar is with arbitrary units.

Now the two building blocks have been characterized separately, we are interested in demonstrating focal length tuning by cascading the metalens with the electro-thermo-optical module. Figures 3(a)

and 3(d) show the focal length tuneability, as a function of the applied voltage, for lenses with focal lengths of 600  $\mu\text{m}$  and 1000  $\mu\text{m}$ , respectively.

For both lenses, the focal length gradually increases as the applied voltage rises (Figures 3(a) and (d)), following a quasi-linear dependence. At 12 V, the focal length has changed by 15 % and 23 %, for the designed 600  $\mu\text{m}$  and 1000  $\mu\text{m}$  lenses, respectively. This corresponds to a focus change that is larger than the actual Rayleigh length of the metalenses (70  $\mu\text{m}$  and 225  $\mu\text{m}$ , respectively). Beyond the efficient control over the focus under low/moderate voltages, we are interested in assessing any potential aberration the electro-thermo-optical module could introduce in the metalens point spread function. To this aim, we map the XZ intensity distribution for 0 and 9 V (Figures 3(c) and (f)) and extract from them the axial focus profiles (Figures 3(b) and (e)). For reference, we also plot the focal profile for the metalens only (without the heating module). Remarkably, the focus profile is not dramatically altered by the thermo-optical control, even between the two extremities of the explored driving voltage range. Still, one can notice some slight changes in the focus size that are not foreseen to be critical for fine refocusing, for instance in an imaging setting.

We measured the overall transmittance, focusing efficiency and Strehl ratio of the whole device (metalens and gold spiral combined) throughout the all tuning range. Tables 1 and 2 summarize the results for the varifocal metalenses with 600 and 1000  $\mu\text{m}$ , respectively. For both metalenses, the Strehl ratio remains similar as compared to the case of metalens only, indicating the gold spiral heater does not introduce significant aberrations. On the other hand, the overall transmittance slightly decreases with increasing voltage. Similarly, the focusing efficiency slightly diminishes with the inclusion of the gold spiral heater and with increasing voltage. It is worth mentioning that the effect of the thermo-optical module on the transmittance and focusing efficiency can be further minimized by using ITO instead of gold (see Supporting Information).

*Table 1: Characterization of the metalens with 600  $\mu\text{m}$  designed focal length*

| Metalens only      |                 | Transmittance (%) | Focusing efficiency (%) | Strehl ratio |
|--------------------|-----------------|-------------------|-------------------------|--------------|
|                    |                 | 69                | 76                      | 0.72         |
| Varifocal metalens | Applied voltage |                   |                         |              |
|                    | 0 V             | 50.4              | 69.5                    | 0.69         |
|                    | 3 V             | 49                | 68.6                    | 0.7          |
|                    | 6 V             | 49                | 68                      | 0.7          |
|                    | 9 V             | 46                | 66.5                    | 0.69         |

*Table 2: Characterization of the metalens with 1000  $\mu\text{m}$  designed focal length*

| Metalens only      |                 | Transmittance (%) | Focusing efficiency (%) | Strehl ratio |
|--------------------|-----------------|-------------------|-------------------------|--------------|
|                    |                 | 66                | 67                      | 0.69         |
| Varifocal metalens | Applied voltage |                   |                         |              |
|                    | 0 V             | 48.1              | 61.1                    | 0.67         |
|                    | 3 V             | 47.5              | 59                      | 0.67         |
|                    | 6 V             | 46                | 56.7                    | 0.65         |
|                    | 9 V             | 45.5              | 55                      | 0.66         |

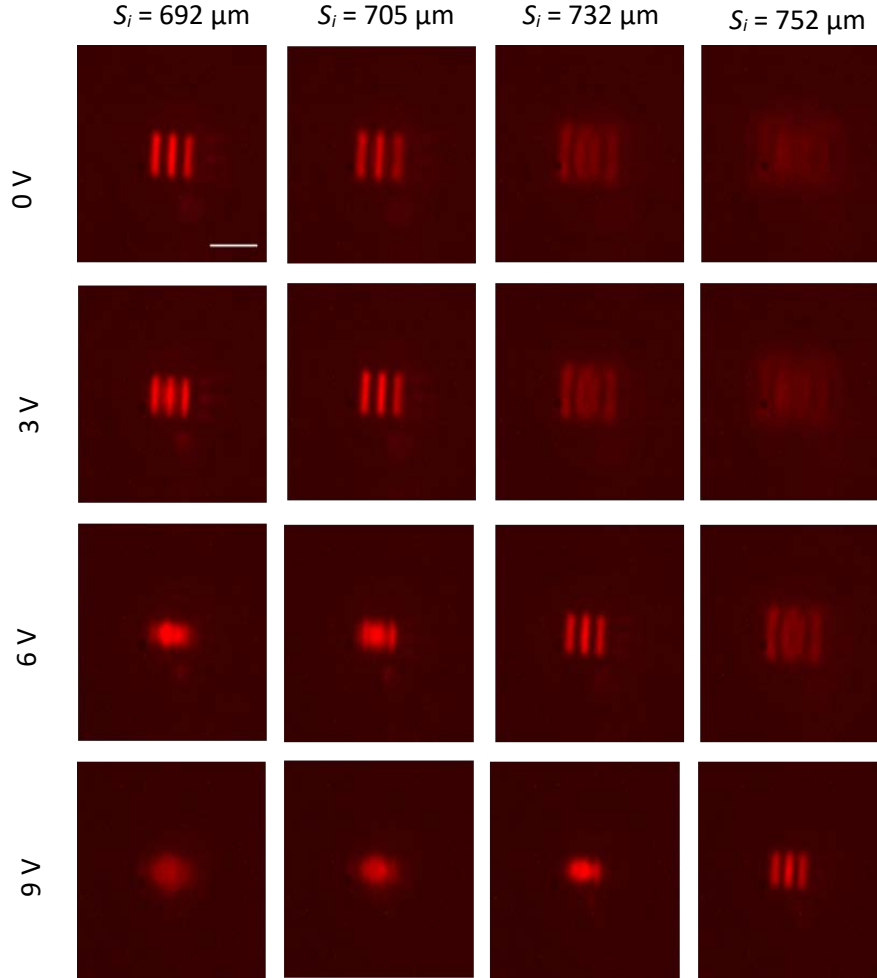


Figure 4: Imaging experiments performed with the 600  $\mu\text{m}$  varifocal metalens. The scale bar is 10  $\mu\text{m}$ . At 0 V, the image is focused at a plane with distance  $S_i$  equal to 692  $\mu\text{m}$ . Additionally, at the same plane we take images for 3, 6, and 9 V to show the image focus shift (1<sup>st</sup> column). In similar manner, we observe image focus at 705  $\mu\text{m}$ , 732  $\mu\text{m}$  and 752  $\mu\text{m}$  for 3, 6, and 9 V, respectively.

Finally, we validate the capability of our varifocal metalens for imaging applications, using a commercially available negative 1951 USAF resolution target (R1DS1N, Thorlabs). For this purpose, we use the same optical setup described in Figure 2(b), with little modifications. The resolution target followed by an aspheric lens was placed in between the collimator and varifocal metalens (Figure 2(b)). In this way, the resolution target is first imaged by the aspheric lens and the varifocal metalens in an intermediate image plane, and re-imaged by our custom-built microscope on the camera. In fact our imaging system is similar to the one used by Arbabi *et al.*<sup>49</sup> However, here we kept the distance between object and aspheric lens constant and we move the objective lens farther away from the varifocal metalens to compensate for the shift in the focal length at different voltages. We denote the distance between the varifocal metalens surface and the image by  $S_i$ . Figure 4 summarizes the imaging data. When no voltage is applied, the image is focused at a distance  $S_i$  equal to 692  $\mu\text{m}$ . By switching on the electro-thermo-optical control, the image becomes out of focus. For an applied voltage of 3 V, the image focus moves to a distance of 705  $\mu\text{m}$ . Similarly, results for 6 and 9 V are also given. It is worth noticing that the image planes are well separated from one voltage to another or in other words, that the varifocal metalens shows good resolving capabilities between different planes. Moreover, we performed imaging with the metalens only (without any heater) and compared it with



the varifocal metalens (with heater) for 0 V and results are presented in Figure S2 of Supporting information.

In conclusion, we presented an electrically-controlled varifocal metalens based on the thermo-optical effect in PDMS. We achieve focal change higher than the Rayleigh length, with voltages as low as 12 V. Our device driving time response is in the 100 ms range but with the potential to reach to 1 ms by suitable engineering of the electro-thermo-optical module. We note that the electro-thermo-optical module in our device does not introduce significant perturbation to the incoming beam. In its current state, the overall transmission of our device is limited by the transmission of the gold based electro-thermo-optical module. However, by using ITO instead of gold, the overall transmission would be substantially improved. The device shows good performance for imaging making it potentially relevant to adaptive vision, bioimaging, wearable technology and displays.

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#### **Supporting Information:**

Simulation of silicon nano-disks and gold spiral heater. Fabrication of the metalens and gold spiral heater. Strehl ratio calculation. Qualitative assessment of imaging of the metalens with and without heating module. Fraunhofer propagation of varifocal metalens with gold and ITO spiral heater.

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