ABSTRACT: Metal nanoparticles have been used for coloring glass since antiquity. Colors are produced by light scattering and absorption associated with plasmon resonances of the particles. Recently, dewetting at high temperature has been demonstrated as a straightforward high-yield/low-cost technique for nanopatterning thin metal films into planar arrays of spherical nanocaps. Here, we show that by simply tuning the contact angle of the metal dewetted nanocaps one can achieve narrow resonances and large tunability compared with traditional approaches such as changing particle size. A vast range of colors is obtained, covering the whole visible spectrum and readily controlled by the choice of film thickness and materials. The small size of the particles results in a mild dependence on incidence illumination angle, whereas their high anisotropy gives rise to strong dichroism. We also show color tuning through interference by simply adding an ultrathin metal film at a designated distance from the dewetted particle array. Our measurements are quantitatively well explained through analytical theory, which enables fast optimization of fabrication parameters. Good agreement between theory and experiment requires incorporating the effect of plasmon peak broadening caused by the finite size distribution of the particle. The proposed designs and techniques hold great potential for large-scale production of colored and dichroic glass with application to optical windows, filters, and displays.

KEYWORDS: structural colors, dewetting, plasmonics, glass coloring

Received: February 10, 2016

DOI: 10.1021/acsphotonics.6b00090

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ACS Photonics XXXX, XXX, XXX--XXX
approaches, for example, relying on changing particle size. A wide chromatic range is also accessible through varying the initial film thickness. The structures display a high degree of dichroism, with radically different colors on transmission and reflection. We mainly focus on silver-on-silica, for which the contact angle determines the nanocap morphology, although

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Figure 1. Color tuning through particle size and shape. Top: Geometry and parameters of a silver ultrathin metal film (UTMF) of thickness $t$, along with nanocaps of various shapes and sizes (base diameter $D$ and contact angle $\beta$), produced upon dewetting of the film. The metal is embedded in silica. We assume the nanocaps to be distributed in a triangular lattice with spacing $8t$ and total metal volume equal to that of the homogeneous UTMF in all cases. Bottom: Calculated normal-incidence reflection spectra for particles of varying shape (horizontal direction) and size (vertical). Each curve is given the RGB color extracted from the spectrum that it represents.

(a) 4 nm  
(b) 7 nm  
(c) 10 nm  
(d)  
(e)  
(f)  
(g) Photographs for the three samples with measured spectra corresponding to (d)−(f) on white and black backgrounds.

Figure 2. Color tuning through UTMF dewetting. We illustrate this concept with three representative samples produced upon dewetting of silver UTMFs. (a−c) Sample SEM images for different initial silver UTMF thicknesses (i.e., before dewetting; see top labels and also Table 1). (d−f) Measured (solid curves) and calculated (broken curves) normal-incidence transmission (blue curves) and reflection (red curves) spectra for the samples shown in (a)−(c). (g) Photographs for the three samples with measured spectra corresponding to (d)−(f) on white and black backgrounds.
the method can be generally applied to other combinations of metal film and dielectric substrate. We gain further flexibility in color range and spectral absorbance by creating interfering structures with the addition of another properly spaced UTMF.

## RESULTS AND DISCUSSION

The power of changing the contact angle of nanocaps and of a straightforward dewetting process for structural coloring is clearly illustrated by Figure 1, which shows simulated reflection spectra of uniform and dewetted silver UTMFs embedded in silica for typical geometrical parameters similar to those of the actual samples (see below). The UTMF thickness is increased in the \( t = 3\)–10 nm range, the reflectance gradually grows at long wavelengths. This effect has a minor influence on reflection structural colors, which are mostly faded red (see Figure 1, in which different curves are given the RGB color computed from the spectra that they represent; see Materials and Methods for more details). However, a radical change in color is observed when moving from continuous UTMFs to dewetted nanocaps with different sizes and shapes (contact angle). As we show below, the average base diameter \( D \) and contact angle \( \beta \) can be controlled by the dewetting temperature, the duration of the thermal treatment used to induce dewetting, and the initial UTMF thickness; so these parameters allow us to generate on-demand bright structural colors, which are in all cases associated with the excitation of LSPRs in the nanocaps.

In particular, we observe an excursion along a red-green-blue hue when the contact angle is varied in the \( \beta = 60\)–135° range, driven by a change in plasmon resonance position. Generally, colors become lighter as the nanocap base diameter increases, due to LSPR broadening produced by radiative losses of the individual particles. For illustration, all reflection spectra of Figure 1 are calculated for triangular lattices of spacing \( 8t \), with nanocap size determined by the condition that the metal volume is maintained as in the initial film of thickness \( t \), which results in the values of the base diameter \( D \) indicated by labels.

Reflection spectra for spheres are also provided as a reference. Incidentally, we observe similar trends when examining arrays of particles with fixed base diameter but varying contact angle, in which the spacing is adjusted in order to maintain total metal volume as a constant (see Figure S1 in the Supporting Information (SI) for calculations of the transmittance as a function of light wavelength and incidence angle, indicating that LSPR-based coloring is robust against changes of incidence angle). In contrast to previous work, which focused on changing particle size (diameter), our proposed tuning scheme, relying on changing the contact angle, is much wider. Additionally, previous work has also shown that periodic structures can be used to achieve structural coloring, tuning the plasmonic response by changing the period. However, such approaches suffer from either broad resonance features or strong angular dependence of the obtained color.

We corroborate the potential of UTMF dewetting for coloring by preparing and optically characterizing samples consisting of silver on silica with different metal thicknesses (see Materials and Methods for fabrication details). A nearly index-matching 150 nm thick layer of poly(methyl methacrylate) (PMMA) is deposited on top (2% difference with the refractive index of the silica substrate; similar results are obtained with silica embedding; see Figure S2 in the SI). The results are summarized in Figure 2. In particular, Figure 2a–c shows SEM images of three samples, which produce the

<table>
<thead>
<tr>
<th>Initial film thickness (nm)</th>
<th>Particle density (μm⁻²)</th>
<th>Average base diameter (nm)</th>
<th>Average diameter std (nm)</th>
<th>Average height (nm)</th>
<th>Estimated contact angle (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
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<td>20</td>
<td>9</td>
<td>16</td>
<td>116</td>
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<td>7</td>
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</tr>
<tr>
<td>10</td>
<td>35</td>
<td>82</td>
<td>30</td>
<td>71</td>
<td>120</td>
</tr>
</tbody>
</table>

*See Figure 2a–c. The contact angle is estimated from the height and base diameter assuming spherical nanocap profiles.*

As a rule, a larger initial metal thickness gives rise to lower particle density and larger particle size (Figure 2a–c). This increase in size switches on retardation, which in turn produces plasmon broadenings and red-shifts (Figure 2d–f). Similar conclusions can be extracted from samples of nanocaps exposed to air (see Figure S2 in the SI), but now the LSPRs are blue-shifted with respect to those covered with PMMA. The dielectric protection also prevents silver oxidation: we have verified their stable optical properties over a period of several months.

Figure 2g displays photographs taken from these three samples (Figure 2d–f). A large contrast in structural colors depending on whether the samples are on white or black background is evident.

We seek further understanding of our measurements (Figure 2d–f, solid curves) by formulating an analytical theoretical model (broken curves), which is in excellent agreement with experiment in the details of the reflection/transmission spectra (Figure 2d–f). The model uses as input the geometrical parameters retrieved upon inspection of the sample SEM images (Figure 2a–c), which are summarized in Table 1. We describe the particles as spherical nanocaps similar to those of Figure 1 and assume a fixed value of the silver-on-silica contact angle \( \beta = 120° \). The optical response of the nanocaps is reduced to their average anisotropic polarizability (for axial and transversal directions), which we combine with the dynamical interaction between them, taking into account their random distribution, to produce reflection and transmission coefficients (see Materials and Methods for more details). This model produces satisfactory results compared with experiment (Figure 2d–f), except for the discrepancy in plasmon width of the thinner sample (Figure 2d), where the particle details are at the limit of the SEM spatial resolution, which probably affects the determination of statistic geometrical parameters.

The optical response of our samples emerges from the properties of the individual nanocaps and their LSPRs, which we investigate in more detail in Figure 3. In particular, the dependence on contact angle \( \beta \) is summarized in Figure 3a–c for small nanocaps (base diameter \( D = 10 \) nm), for which retardation can be neglected. The response in the spectral range under consideration is dominated by the lowest order axial and transversal dipolar plasmons, whose spectral position and weight are fully captured by two parameters in the electrostatic limit, which we extract from boundary-element method electromagnetic simulations (BEM; see methods): the value of the metal permittivity at which the plasmon shows up (Figure 3a) and the dipolar transition strength (Figure 3b). The
189 latter is expressed in terms of a fractional volume associated with the resonance, and it amounts to the fraction that it contributes to the integral of the extinction cross-section over frequency. These two parameters are all the input that we need to analytically describe the polarizability of the particles (see Materials and Methods), from which we calculate the cross-section represented in Figure 3c (broken curves). Despite the simplicity of this method, we find a remarkable agreement of the spectra with BEM simulations (broken curves). Notice that under light incidence along the particle axis the transversal plasmon dominates the response. Near-field plots associated with this mode reveal light confinement and enhancement near the edge of the particle base (see insets to Figure 3c). Unlike the axial plasmon, the transversal one has a strong dependence on contact angle (Figure 3a), whereas its spectral weight remains at a high level of $\sim 0.8$ (Figure 3b). This explains the weak dependence of the optical properties of our samples on incidence angle. Nevertheless, the axial plasmon can also be excited in our nanostructures at larger incidence angle, emerging as a feature at shorter wavelength (see Figure S1 in the SI).

190 When the particle size increases, retardation effects become important, leading to plasmon red-shifting and broadening. Both of these effects can be easily accounted for in a modified analytical polarizability that we present in Materials and Methods. The results are in excellent agreement with electromagnetic BEM simulations, as illustrated in Figure 3d for nanocaps of shape and sizes similar to those involved in the measured samples of Figure 2. Additionally, the dominant plasmon feature in the spectra is expected to blue-shift with increasing contact angle (see Figure 3c), as the particle aspect ratio is reduced. This result is fully corroborated by measurements on additional samples in which a treatment of the surface can produce a change in contact angle (see Figure S3 in the SI). Further comparisons between numerical and theoretical results for nanocaps with other contact angles are offered in Figure S4 of the SI.

Optical interference can also produce structural colors, adding an extra knob to further tune the chromatic suite achieved through metal dewetting. We test this principle by adding an extra nickel layer of thickness varied from $d = 3$ nm (transparent) to 40 nm (opaque). In particular, we show in Figure 4a results for samples produced by this procedure starting with a dewetted 7 nm silver film, covered with 150 nm of PMMA. A clear asymmetric plasmonic coloring effect is observed in measurements from the two sides of the sample (front and back, see scheme in Figure 4a). Transmittance from both sides is identical in virtue of reciprocity, as corroborated in both measurements and simulations (see Figure 4b and also Figure S5 in the SI), and it eventually evolves toward negligible values as the nickel eventually becomes optically thick. In contrast, there are clear differences in absorbance from both sides: front-side absorption increases with nickel thickness $d$ in the 300–550 nm wavelength range, reaching values above 85%, essentially as a result of a Salisbury screen effect; however, back-side absorption decreases with increasing $d$, attenuating the effect of the dewetted silver layer and eventually saturating at the bulk nickel surface absorption level. The chromatic variation produced upon nickel deposition is illustrated by photographs in Figure 4c. We note that both in the spectra and...
in the resulting colors our simple theory compares reasonably well with experiment, including in this case the effect of multiple reflections at the different interfaces of the sample.

**CONCLUSION**

In summary, we have demonstrated that arrays of metal nanocaps created via a low-cost, lithography-free dewetting process display intense colors as a result of the excitation of localized surface plasmons in the particles. A wide chromatic range is accessible through careful control of the initial metal thickness and the dewetting conditions (temperature and duration), which ultimately defines the size, density, and contact angle of the resulting nanoparticles. Colors can be actually customized over a sizable range of the visible spectrum for a wide range of incidence angles, as shown in Figure 5, where we represent the colors associated with our obtained experimental spectra superimposed on the Commission Internationale de l’Eclairage (CIE) 1931 color map. For example, we observe structures that go from reflective (scattered) red to green and blue, suggesting the potential for large-scale manufacturing of structurally colored glass windows, optical filters, and display panels. The addition of an extra ultrathin metal film produces interference with the dewetted film, leading to further control over the chromatic properties. The combination of continuous and dewetted metal layers thus holds great potential to achieve full control over the visible spectral properties of thin films, which are accessible through industrially scalable, economic fabrication processes. Our

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**Figure 4.** Additional color tuning through interference. (a) A nickel UTMF is deposited on a 150 nm PMMA spacer embedding the silver nanocaps that are previously obtained upon dewetting a 7 nm silver film. (b) Measured and calculated transmission and absorption spectra for normal-incidence illumination from the back and front sides of the structure (see (a)). We consider different nickel thicknesses in the $d = 3 - 40$ nm range. (c) Photographs of the samples whose measured absorption (reflection) spectra are shown in (b), taken on white and black backgrounds.

**Figure 5.** Position of the colors in our samples on the CIE 1931 map. We show the colors associated with our experimental spectra (see labels), as obtained for a D65 illumination light source.
results can be readily extrapolated to other spectral regimes through a choice of appropriate materials (e.g., aluminum for the UV).

## MATERIALS AND METHODS

### Ultrathin Metal Film Deposition and Dewetting

Ultrathin films are deposited on the silica substrate using a magnetron sputtering system (ATC Orion 8, Aja International, Inc. or KDF 903i). The coated substrates are then subjected to rapid thermal annealing in a Tsunami RTP-600S at a temperature of 750 °C for about 90 s under a nitrogen flow of 1 atm. In this way the ultrathin silver films are dewetted into nanocaps. The PMMA overlayer is deposited through spin-coating.

### Sample Characterization

Optical transmittance and reflectance are measured using a UV–vis–NIR spectrophotometer (PerkinElmer Lambda 950). The morphology of the nanocaps is examined with a field-emission scanning electron microscope (FEG-SEM, Inspect F, FEI Systems). The optical transmittance and reflectance are measured using a UV–vis–NIR spectrophotometer (PerkinElmer Lambda 950). The morphology of the nanocaps is examined with a field-emission scanning electron microscope (FEG-SEM, Inspect F, FEI Systems).

### Simulation of Individual Nanocaps

The optical response of individual nanocaps is simulated using BEM. The metal dielectric function is taken from tabulated data, whereas a homogeneous surrounding medium is assumed with constant permittivity $\epsilon_\infty = 2.13$ similar to that of silica and PMMA in the spectral region under consideration. The particle geometry is determined by its base diameter $D$ and contact angle with the substrate $\beta$, where the edges are smoothed with a rounded radius of 0.5 nm. These simulations yield the particle extinction cross-section and its scattering matrix used to simulate arrays.

### Average Polarizability of Nanocaps in the Actual Samples

For a given sample, the contact angle is roughly constant, and in particular, it takes the value $\beta = 120^\circ$ for silver on silica. In practice, we retain only the lowest order dipolar mode for polarization directions either parallel to the nanocap base (transverse) or along its rotation axis (axial).

### Simulation of Periodic Nanocap Arrays

We use the layer-KKR method to simulate the response of periodic arrays (see Figure S1 in the SI). A rigorous solution of Maxwell’s equations is then obtained by describing the particles through their scattering matrix (i.e., their multipolar response), as described above.

### Analytical Model for Disordered Nanocap Arrays

We formulate an analytical model of the response of the samples by describing the nanocaps through the average polarization $\vec{A}_\parallel$ (see above), following similar methods to those reported elsewhere. In particular, the reflection and transmission coefficients for p-polarized light with angle of incidence $\theta$ reduce to

$$r = \frac{i2\pi\rho}{\cos \theta} \left( \frac{-\cos^2 \theta}{\alpha_\parallel^{-1} - G_{\parallel}} + \frac{\sin^2 \theta}{\alpha_\perp^{-1} - G_{\perp}} \right)$$

where $\rho$ is the particle density, whereas $G_{\parallel,\perp}$ are the dipole–dipole interaction lattice sums. The latter allows the expression

$$G_{\parallel,\perp} = \frac{1}{(2\pi)^3} \int \left[ \frac{1}{\rho} S(Q - k_{\parallel}) - 1 \right] \vec{Q}$$

in terms of the momentum representation of the dipole–dipole interaction components

$$G_{\parallel}(Q) = 2\pi k_{\parallel} Q_{z}^2 / Q^2 + 2\pi i k_{\parallel} k_{z} (1 - Q_{z}^2 / Q^2)$$

and

$$G_{\parallel}(Q) = 2\pi i Q^2 / k_{z}^2$$

where $k_z = \sqrt{k^2 - Q^2}$, as extracted for both interacting dipoles oriented either perpendicular or parallel to the surface normal, respectively. The lattice sums also depend on the particle density and contribute to the surface projection of the incident light wave. The sum runs over particle positions. More precisely, we have

$$G_{\parallel}(Q) = \frac{1}{(2\pi)^3} \int \left[ \frac{1}{\rho} S(Q - k_{\parallel}) - 1 \right] \vec{Q}$$

where $\epsilon(\omega)$ and $\epsilon_s$ are the permittivities of the metal in the particle and the dielectric host, respectively. Here, the sum extends over the electrostatic eigenmodes of the system, which are identified by eigenvalues $\epsilon_j$ and contribute to the polarizability with a partial volume $V_j$ (the sum of $V_j$'s is equal to the particle volume). The metal dielectric function is taken from tabulated data, whereas a homogeneous surrounding medium is assumed with constant permittivity $\epsilon_\infty = 2.13$ similar to that of silica and PMMA in the spectral region under consideration. The particle geometry is determined by its base diameter $D$ and contact angle with the substrate $\beta$, where the edges are smoothed with a rounded radius of 0.5 nm. These simulations yield the particle extinction cross-section and its scattering matrix used to simulate arrays.

The optical transmittance and reflectance are measured using a UV–vis–NIR spectrophotometer (PerkinElmer Lambda 950). The morphology of the nanocaps is examined with a field-emission scanning electron microscope (FEG-SEM, Inspect F, FEI Systems). The metal dielectric function is taken from tabulated data, whereas a homogeneous surrounding medium is assumed with constant permittivity $\epsilon_\infty = 2.13$ similar to that of silica and PMMA in the spectral region under consideration. The particle geometry is determined by its base diameter $D$ and contact angle with the substrate $\beta$, where the edges are smoothed with a rounded radius of 0.5 nm. These simulations yield the particle extinction cross-section and its scattering matrix used to simulate arrays.

The average polarizability of nanocaps in the actual samples is then obtained by describing the particles through their scattering matrix (i.e., their multipolar response), as described above.

### Analytical Model for Individual Nanocaps

We use the layer-KKR method to simulate the response of periodic arrays (see Figure S1 in the SI). A rigorous solution of Maxwell’s equations is then obtained by describing the particles through their scattering matrix (i.e., their multipolar response), as described above.

We formulate an analytical model of the response of the samples by describing the nanocaps through the average polarization $\vec{A}_\parallel$ (see above), following similar methods to those reported elsewhere. In particular, the reflection and transmission coefficients for p-polarized light with angle of incidence $\theta$ reduce to

$$r = \frac{i2\pi\rho}{\cos \theta} \left( \frac{-\cos^2 \theta}{\alpha_\parallel^{-1} - G_{\parallel}} + \frac{\sin^2 \theta}{\alpha_\perp^{-1} - G_{\perp}} \right)$$

where $\rho$ is the particle density, whereas $G_{\parallel,\perp}$ are the dipole–dipole interaction lattice sums. The latter allows the expression

$$G_{\parallel,\perp} = \frac{1}{(2\pi)^3} \int \left[ \frac{1}{\rho} S(Q - k_{\parallel}) - 1 \right] \vec{Q}$$

in terms of the momentum representation of the dipole–dipole interaction components

$$G_{\parallel}(Q) = 2\pi k_{\parallel} Q_{z}^2 / Q^2 + 2\pi i k_{\parallel} k_{z} (1 - Q_{z}^2 / Q^2)$$

and

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where $k_z = \sqrt{k^2 - Q^2}$, as extracted for both interacting dipoles oriented either perpendicular or parallel to the surface normal, respectively. The lattice sums also depend on the particle density and contribute to the surface projection of the incident light wave. The sum runs over particle positions. More precisely, we have

$$G_{\parallel}(Q) = \frac{1}{(2\pi)^3} \int \left[ \frac{1}{\rho} S(Q - k_{\parallel}) - 1 \right] \vec{Q}$$

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for a completely disordered array and $S(Q) = (2\pi \rho)^2 \sum_\mathbf{g} \delta(Q - \mathbf{g})$ for a periodic one, where $\mathbf{g}$ runs over reciprocal lattice vectors. Theory curves in Figures 2 and 4 are obtained assuming random particle distributions.

**RGB Color.** We show RGB colors in several figures, as extracted from measured and calculated spectra, assuming a flat-spectrum illumination. RGB parameters are obtained simply by projection on the spectra of the three pigments that define this color scheme.

### ASSOCIATED CONTENT

#### Supporting Information
The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsphoto-0009.

Further simulations and experiments and, in particular, calculations of the transmittance of ordered and disordered planar particle arrays for fixed particle size and different contact angles (Figure S1); measured reflection and transmission spectra for silver nanocaps with different surrounding media (Figure S2) and contact angles (Figure S3 and Table S1); an extension of Figure 3d to cover more contact angles (Figure S4); the reflectance spectra corresponding to the samples of Figure 4b (Figure S5); and measured spectra for gold and copper on silica (Figure S6) and silver on sapphire (Figure 5) (PDF)

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The authors declare no competing financial interest.

### ACKNOWLEDGMENTS
This work has been supported in part by Spanish MINECO (MAT2014-59096-P and SEV2015-0522), Fundació Privada Cellex, the European Commission (Graphene Flagship CNECT-ICT-604391 and FP7-ICT-2013-613024-GRASP), AGAUR (2014 SGR 1400 and 1623), and the Fondo Europeo de Desarrollo Regional (FEDER, TEC2013-46168-R).

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