Treball de Fi de Grau

Enginyeria en Tecnologies Industrials

Analytical design of a Synchronous Reluctance motor (SRM)

ANNEX

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ANNEX A

A.1. LUA scripts

Here is shown the script designed to analyse the geometry of the SRM every 5° rotated by the rotor for a complete 360° turn. In the example below an intensity of 1 A has been established to flow through the phases.

As already mentioned, if a more accurate analysis were to be run then the angle of rotation should be established as 1° in the sixth line of the code when defining the *for* loop. Moreover, in order to turn off the switcher of the i-th phase in the real maximum inductance position (rotor and stator poles totally overlapped), a full analysis of the solution should be inserted inside every *if* statement before the *mi_modifycircprop()*, *mo_showdensityplot()* and *mo_savebitmap()* functions. This analysis would take a lot of time and has been neglected since the beginning of the project.

```
showconsole()
open("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Arxius Femm i Dxf\\experimento7.FEM")
mi saveas("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Arxius Femm i Dxf\\temp carr sinus freq 19.FEM")
mi_seteditmode("group")
for angle = 0,360,5 do
         if angle == 0 then
                  \label{local-prop} $$mo_showdensityplot(0,0,2,0,"bmag")$$mo_savebitmap("C:\Users\Lluís\Desktop\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot0.bmp")$$
         if angle == 15 then
                 mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,I)
                  mo showdensityplot(0,0,2,0,"bmag")
                  mo_savebitmap("C:\\Users\\Lluis\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot1.bmp")
                  mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,0)
                  mi_modifycircprop("D",1,I)
         if angle == 45 then
                  mi_modifycircprop("A",1,I)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,0)
                  mi_modifycircprop("D",1,0)
         if angle == 50 then
                  mo showdensityplot(0,0,2,0,"bmag")
```

```
mo savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot3.bmp")
  if angle == 60 then
                      mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,I)
mi_modifycircprop("C",1,0)
                       mi_modifycircprop("D",1,0)
  if angle == 65 then
                      mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot4.bmp")
  if angle == 75 then
                      mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,I)
mi_modifycircprop("D",1,0)
   end
   if angle == 80 then
                      mo_showdensityplot(0,0,2,0,"bmag")
mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot5.bmp")
  if angle == 90 then
                      mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,0)
mi_modifycircprop("C",1,1)
   end
   if angle == 95 then
                      mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot6.bmp")
   if angle == 105 then
                      mi_modifycircprop("A",1,I)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,0)
mi_modifycircprop("D",1,0)
   end
   if angle == 110 then
                      mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot7.bmp")
if angle == 120 then
                    e == 120 then
mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,I)
mi_modifycircprop("C",1,0)
mi_modifycircprop("D",1,0)
if angle == 125 then
                     mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot8.bmp")
if angle == 135 then
                     mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,I)
                      mi_modifycircprop("D",1,0)
if angle == 140 then
                     : == 140 then
mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot9.bmp")
if angle == 150 then
                    mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,0)
mi_modifycircprop("D",1,I)
end
if angle == 155 then
                     \label{localize} $$mo\_showdensityplot(0,0,2,0,"bmag")$$mo\_savebitmap("C:\Users\Lluís\Desktop\ETSEIB\4t curs - 1r quatrimestre\TFG\Fotos\sim2.2\screenshot10.bmp")$$
if angle == 165 then
                     mi_modifycircprop("A",1,I)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,0)
                     mi_modifycircprop("D",1,0)
if angle == 170 then
                     mo_showdensityplot(0,0,2,0,"bmag")
                     \label{local-prop} $$mo_save bitmap("C::\Users\lluis\park) $$ possible $$mo_save bitmap("C::\Users\lluis\park) $$ possible $$possible $$possi
if angle == 180 then
                     mi_modifycircprop("A",1,0)
```

```
mi_modifycircprop("B",1,I)
mi_modifycircprop("C",1,0)
mi_modifycircprop("D",1,0)
if angle == 185 then
             e -- 105 (||e||
mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot12.bmp")
if angle == 195 then
             e == 195 then
mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,I)
mi_modifycircprop("D",1,0)
end
if angle == 200 then
             \label{local-constraint} $$mo\_showdensityplot(0,0,2,0,"bmag")$$mo\_savebitmap("C:\Users\Lluı´s\Desktop\ETSEIB\4t curs - 1r quatrimestre\TFG\Fotos\sim2.2\screenshot13.bmp")$$
if angle == 210 then
             mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,0)
mi_modifycircprop("C",1,1)
if angle == 215 then
             e -- 13 clied
mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot14.bmp")
if angle == 225 then
             mi_modifycircprop("A",1,I)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,0)
mi_modifycircprop("D",1,0)
end
if angle == 230 then
             \label{local-constraint} $$mo\_showdensityplot(0,0,2,0,"bmag")$$mo\_savebitmap("C:\Users\Lluı́s\Desktop\ETSEIB\4t curs - 1r quatrimestre\TFG\Fotos\sim2.2\screenshot15.bmp")$$
if angle == 240 then
             mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,I)
mi_modifycircprop("C",1,0)
             mi_modifycircprop("D",1,0)
if angle == 245 then
             \label{local_mo_showdensity} $$mo\_savebitmap("C:\Users\Lluís\Desktop\ETSEIB\4t curs - 1r quatrimestre\TFG\Fotos\sim2.2\screenshot16.bmp")$
end
if angle == 255 then
             mi_modifycircprop("A",1,0)
             mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,I)
mi_modifycircprop("D",1,0)
if angle == 260 then
             mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot17.bmp")
if angle == 270 then
             mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,0)
mi_modifycircprop("D",1,I)
if angle == 275 then
             = -- 27 cliein
mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot18.bmp")
if angle == 285 then
             e == 285 then
mi_modifycircprop("A",1,I)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,0)
mi_modifycircprop("D",1,0)
if angle == 290 then
             \label{local-prop} $$mo\_showdensityplot(0,0,2,0,"bmag")$$mo\_savebitmap("C:\Users\Lluı´s\Desktop\ETSEIB\4t curs - 1r quatrimestre\TFG\Fotos\sim2.2\screenshot19.bmp")$$
end
if angle == 300 then
mi_modifycircprop("A",1,0)
             mi_modifycircprop("B",1,I)
mi_modifycircprop("C",1,0)
             mi_modifycircprop("D",1,0)
```

```
if angle == 305 then
                               mo_showdensityplot(0,0,2,0,"bmag")
mo_stowdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot20.bmp")
              if angle == 315 then
                              e == 315 then
mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,I)
mi_modifycircprop("D",1,0)
              if angle == 320 then
                               mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot21.bmp")
            end
if angle == 330 then
mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,0)
mi_modifycircprop("D",1,I)
              if angle == 335 then
                               : -- 35 them
mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot22.bmp")
              end
if angle == 345 then
                               a == 345 Then
mi_modifycircprop("A",1,I)
mi_modifycircprop("B",1,0)
mi_modifycircprop("C",1,0)
mi_modifycircprop("D",1,0)
              if angle == 350 then
                               mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluís\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot23.bmp")
              end
              if angle == 360 then
                              e == 360 then
mi_modifycircprop("A",1,0)
mi_modifycircprop("B",1,I)
mi_modifycircprop("C",1,0)
mi_modifycircprop("D",1,0)
              mi_analyze()
                mi_loadsolution()
                mo_groupselectblock(1)
Parell_tensor=mo_blockintegral(22)
mo_clearblock()
mo_groupselectblock(1)
                mo_groupselectblock(2)
mo_groupselectblock(3)
mo_groupselectblock(4)
mo_groupselectblock(5)
                mo_groupselectblock(6)
mo_groupselectblock(7)
Magnetic_field_energy=mo_blockintegral(2)
mo_clearblock()
               mo_clearblock() currentA,voltsA,fluxA=mo_getcircuitproperties("A")
currentB,voltsB,fluxB=mo_getcircuitproperties("B")
currentD,voltsB,fluxB=mo_getcircuitproperties("C")
currentD,voltsD,fluxC=mo_getcircuitproperties("C")
currentD,voltsD,fluxD=mo_getcircuitproperties("C")
arxiu=openfile("intens_flux_22.txt","a")
write(arxiu,angle," ",Parell_tensor," ",Magnetic_field_energy," ",currentB," ",currentB," ",currentD," ",fluxA," ",fluxB," ",fluxC," ",fluxD," ","\n")
closefile(arxiu)
mi_selectgroup(1)
mi_selectgroup(1)
mi_selectgroup(3)
                mi_selectgroup(3)
mi_moverotate(0,0,5)
end
mi_moverotate(0,0,-5)
mo_showdensityplot(0,0,2,0,"bmag")
mo_savebitmap("C:\\Users\\Lluis\\Desktop\\ETSEIB\\4t curs - 1r quatrimestre\\TFG\\Fotos\\sim2.2\\screenshot24.bmp")
mo_close()
```

Fig A.1: LUA script

ANNEX B

B.1. Improvement of the geometry

B.1.1. First Geometry

The current geometry of the SRM is such that the density flux generated in some parts of the stator is very high and can cause the temperature to increase and even a loss of properties from the stator's material (see *Fig 18.1* and Fig *18.2*) can eventually occur, reducing the reluctance output torque and subsequently reducing the overall performance of the motor. In order to know the intensity of the magnetic field in the critical points of the geometry the FEMM post-processor allows to draw a red line (called contour line from now onwards) along which the program calculates the total intensity of the magnetic field for every point of the line. Thus, the program gives a graph of the density of the magnetic field as a function of the distance of the contour line starting always from its left end.

The nominal current has been set up for all the geometries.

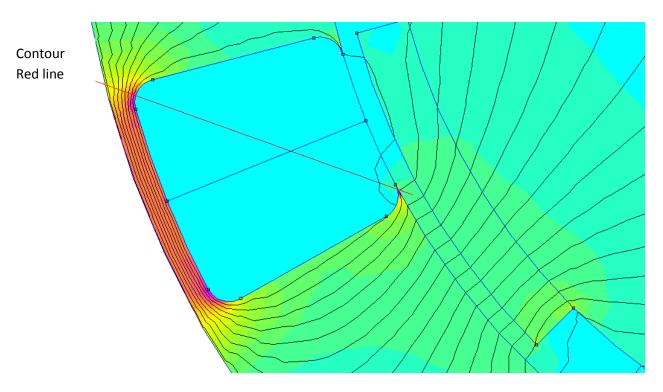


Fig B.1: The flux density lines are very saturated

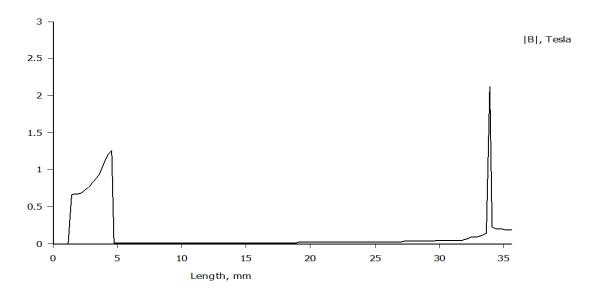


Fig B.2: Graph of the flux density that crosses the contour line drawn in the **Fig B.1**. The x-axis length goes from left to the right, following the path of the contour red line.

Since we obtain that values over 2 T are being generated in the stator and the hysteresis curve (see *Fig B.3* and *Fig B.4*) from Vanadium Permedur shows that for values over 2,2 T the material is working under saturated conditions, then it is cautious to re-design the stator geometry in order to reach lesser values of flux density in the model because with time materials can easily lose their magnetic properties and the increase the magnetic losses of energy. The sharp edges of the stator are useful in order to keep the copper wire confined within the stator slots. However, the density of the magnetic field is very high in those sharp ends. Future work regarding the smoothing of those edges could be carried out.

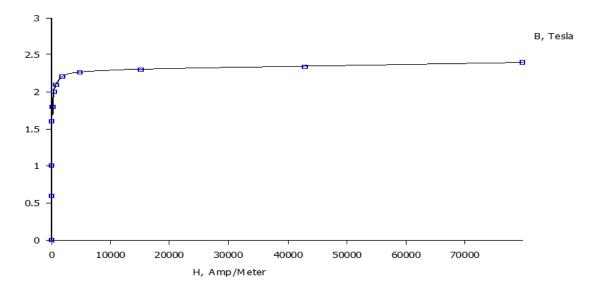


Fig B.3: Vanadium Permedur B-H curve

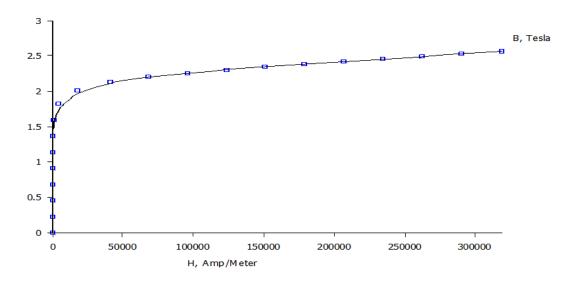


Fig B.4: Pure Iron B-H curve

B.1.2. Second Geometry

The saturated space between the slot and the outer diameter of the stator has been modified; now it has 10mm (see **Fig B.5**). The number of turns of copper wire is the same, although the occupational factor of the slot has changed to $F_o = 0.44$.

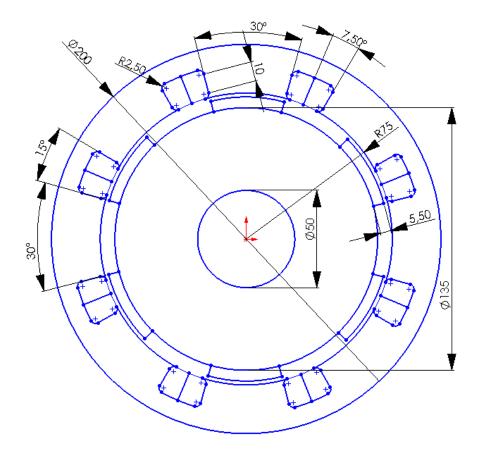


Fig B.5: Second geometry proposed for the 8/6 SRM

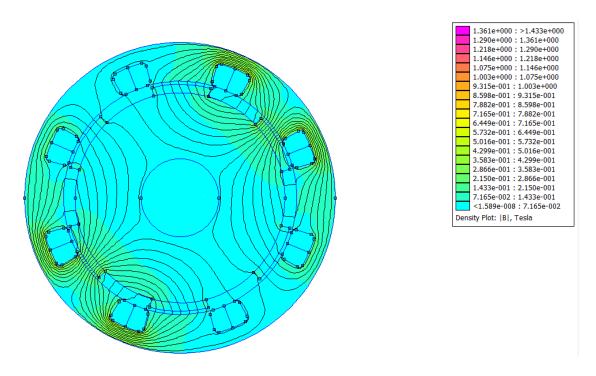


Fig B.6: Flux density lines as soon as phase B is energized with the nominal current, and legend

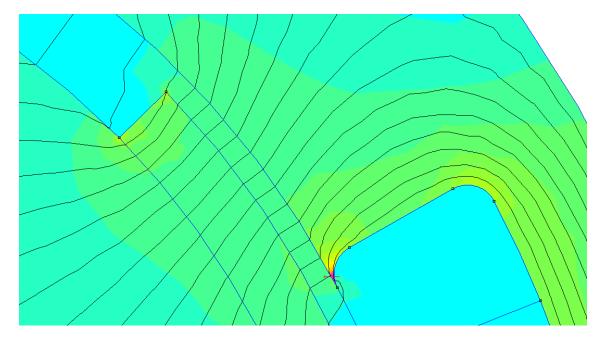


Fig B.7: Flux density lines as soon as phase B is energized and contour red line

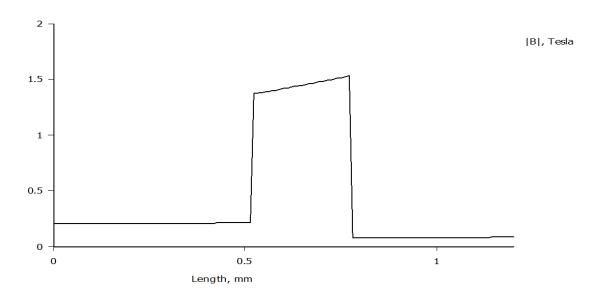


Fig B.8: Graph of the flux density that crosses the contour line drawn in the Fig B.7

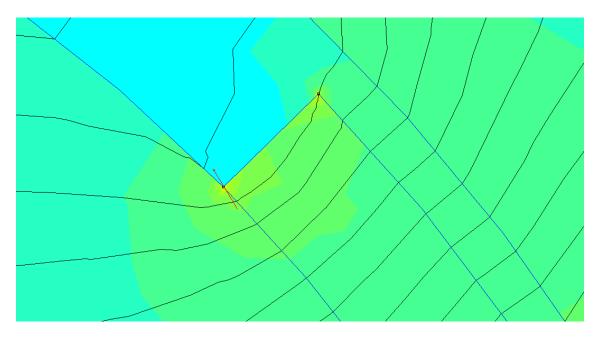


Fig B.9: Flux density lines as soon as phase B is energized and contour red line

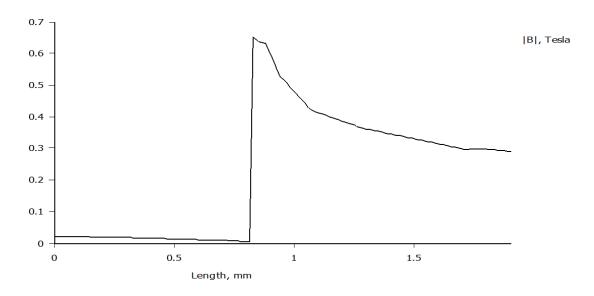


Fig B.10: Graph of the flux density that crosses the contour line drawn in the Fig B.9

From the graphs of the FEMM software can be seen that the maximum value of intensity of magnetic flux is around 1,5 T and is given as soon as the i-th phase is energized. The sharp edges of the stator poles work very saturated. However, this value is contained in the linear part of the hysteresis diagram for both stator and rotor's material, and this part of the geometry has remained unchanged because it is useful in order to maintain the copper wire inside the stator slot.

When the rotor pole is totally overlapped with the stator pole the highest values for the magnetic flux intensity are around 0,55 T, but the motor materials are still working in linear conditions (see *Fig B.11* and *Fig B.12*).

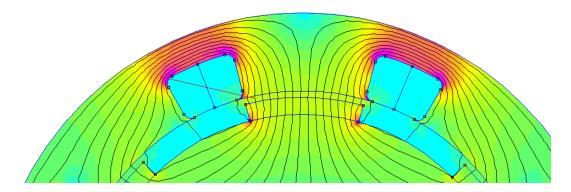


Fig B.11: Flux density lines when phase A is energized and the rotor pole is totally overlapped with the stator pole, and contour red line

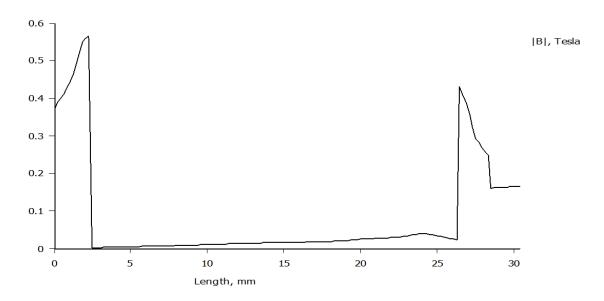


Fig B.12: Flux density lines crossing the contour line drawn in the Fig B.11

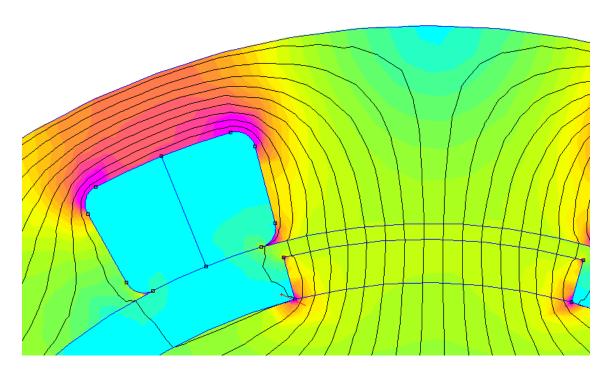


Fig B.13: Flux density lines when the rotor pole is totally overlapped with the stator pole and phase A is energized, and contour red line

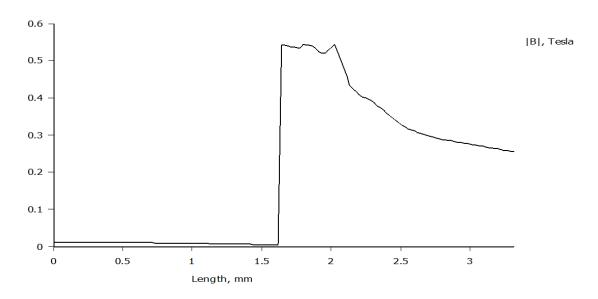


Fig B.14: Flux density lines crossing the contour line drawn in the Fig B.13

B.1.3. Third geometry

In order to increase the saliency ratio, four flux guides per rotor pole have been implemented with the same measures as in the fourth geometry. The air gap has been doubled to 4 mm (shown in *Fig B.15*). The flux barriers help to guide the flux density lines and concentrate them in a smaller region the space, that is to say, increments the density of the magnetic flux thus triggering a higher output torque. The U-shape of the flux barriers have been chosen according to the ease of the rotor manufacturing and the high performance over other type of flux barrier shapes [1]. The is 2 mm left from the outer flux barrier to the outer diameter of the rotor in order to avoid non-feasible rotors from a constructive point of view.

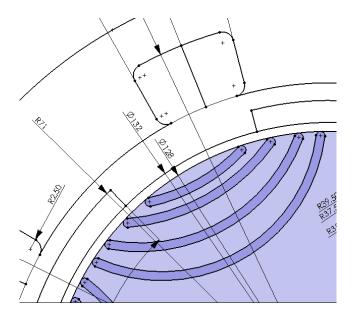


Fig B.15: Third geometry proposed with four flux barriers per rotor pole

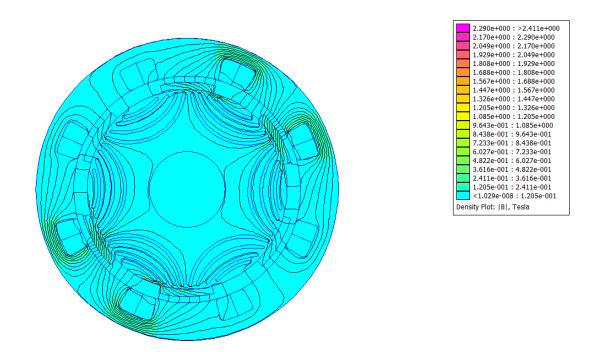


Fig B.16: Flux density lines for the third geometry as soon as phase B is energized, and legend

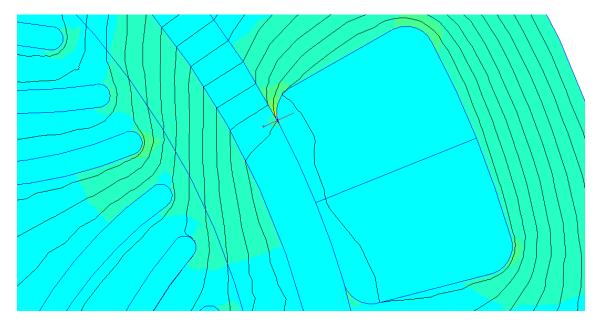


Fig B.17: Flux density lines as soon as phase B is energized and contour red line

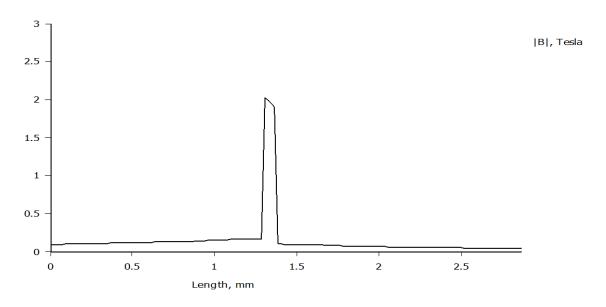


Fig B.18: Flux density lines crossing the contour line drawn in the Fig B.17

It can be seen that the only part that works saturated is the sharp edge of the stator. This geometry is not useful since the output torque and the saliency ratio are very low. In order to increase them, the air gap should be smaller. Incrementing the air gap has been detrimental to the output reluctance torque.

B.1.4. Fourth geometry

A fourth geometry has been designed in order to increase the saliency ratio. The air gap has been reduced to 2 mm (see *Fig B.19*) and the rotor's overall volume has been slightly increased by enlarging the rotor's outer diameter by 3 mm. In addition the length from the outer flux barrier to the outer diameter of the rotor has been diminished by 1 mm.

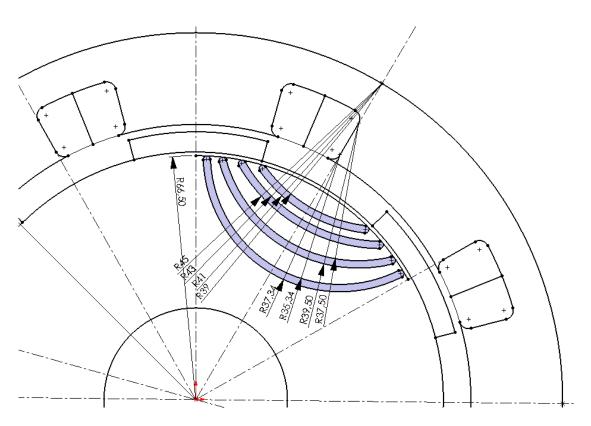


Fig B.19: Fourth geometry proposed with an air gap of 2 mm and the flux barrier's measures

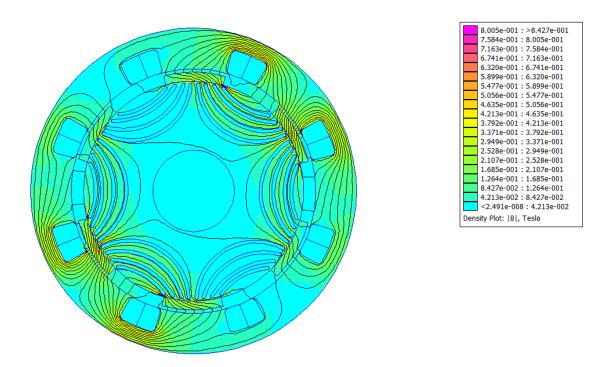


Fig B.20: Flux density lines as soon as phase B is energized with the nominal current, and legend

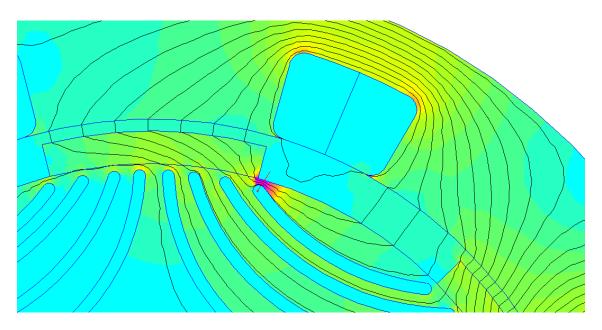


Fig B.21: Flux density lines as soon as phase B is energized and contour red line

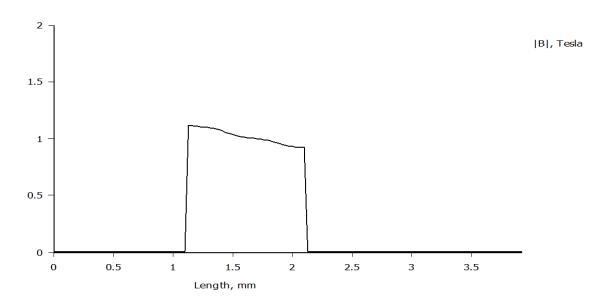


Fig B.22: Graph of the flux density that crosses the contour line drawn in the Fig B.21

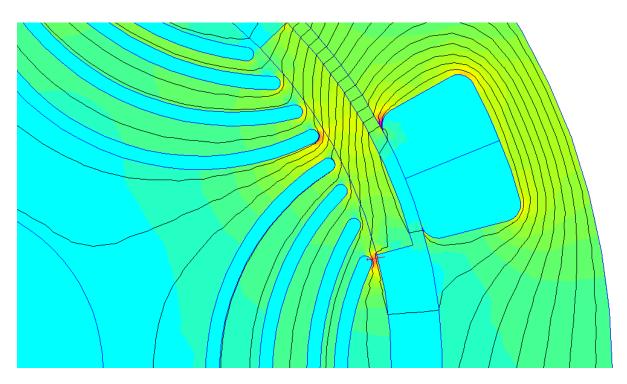


Fig B.23: Flux density lines as soon as phase B is energized and contour red line

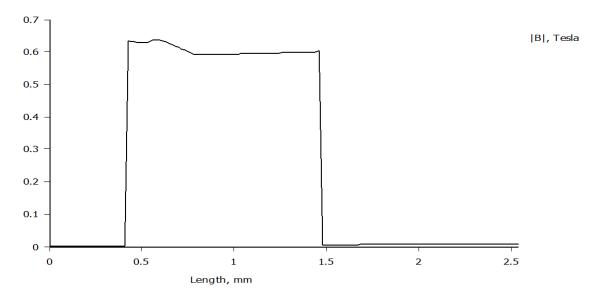


Fig B.24: Graph of the flux density that crosses the contour line drawn in the Fig B.23

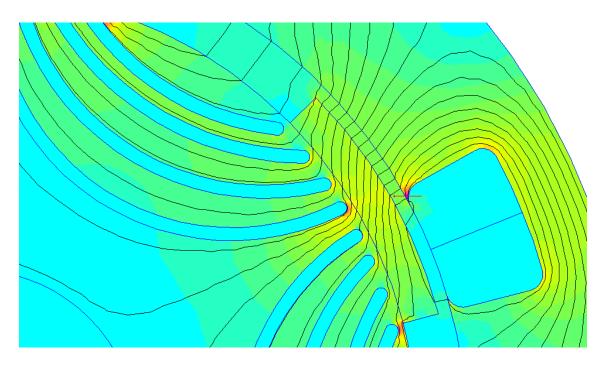


Fig B.25: Flux density lines as soon as phase B is energized and contour red line

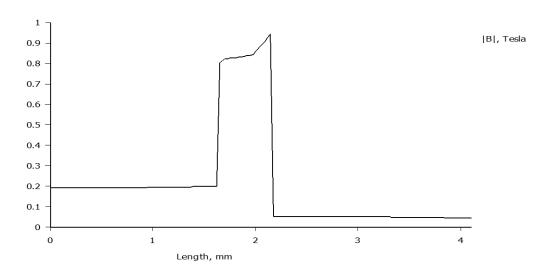


Fig B.26: Graph of the flux density that crosses the contour line drawn in the Fig B.25

The highest values for the intensity of the magnetic field are around 1,1 T, which means that the materials of the motor are working under linear conditions. The torque in the instant where phase B is energized is a little bit higher than that obtained by the first and the second geometry in the same instant.

B.1.5. Fifth geometry

Finally, a fifth geometry has been designed in order to increase the saliency ratio. The air gap has been reduced to 0,2 mm (see *Fig B.27* and *Fig B.28*) and the rotor's overall volume has been slightly increased by enlarging the rotor poles. Now their length are 8,8 mm, 3,8 mm larger than in the previous geometries.

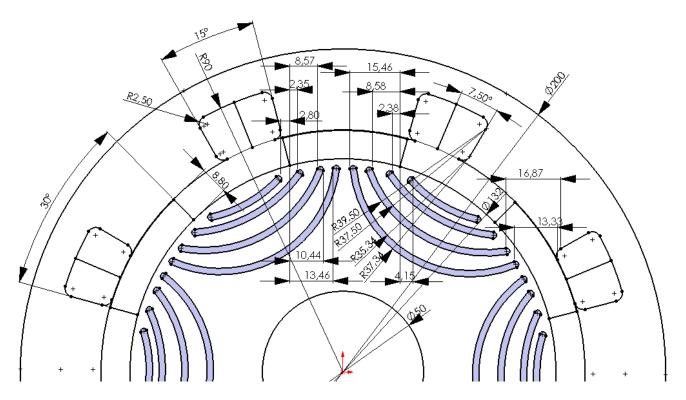


Fig B.27: Fifth geometry

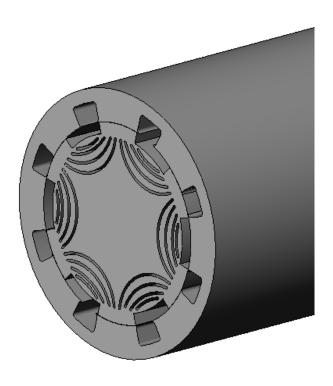


Fig B.28: 3D view of the fifth geometry without the non-magnetic shaft

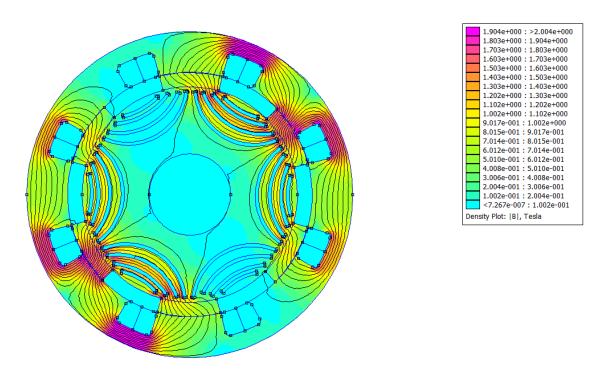


Fig B.29: Flux density lines as soon as phase B is energized and legend

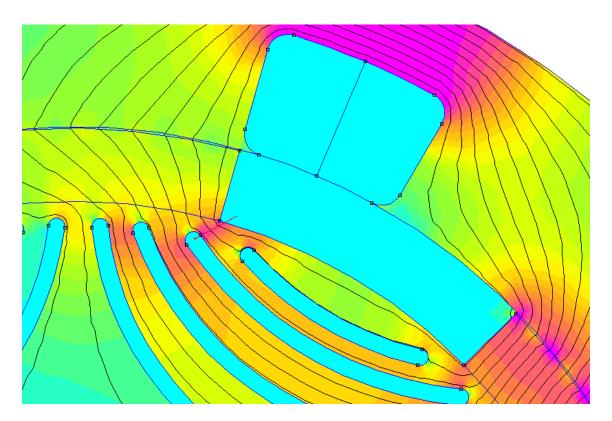


Fig B.30: Flux density lines as soon as phase B is energized and contour red line

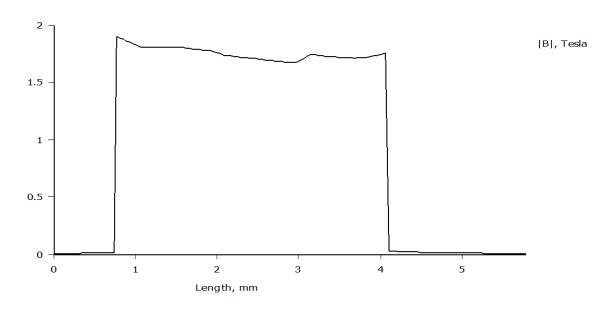


Fig B.31: Flux density lines crossing the contour line drawn in the Fig B.29

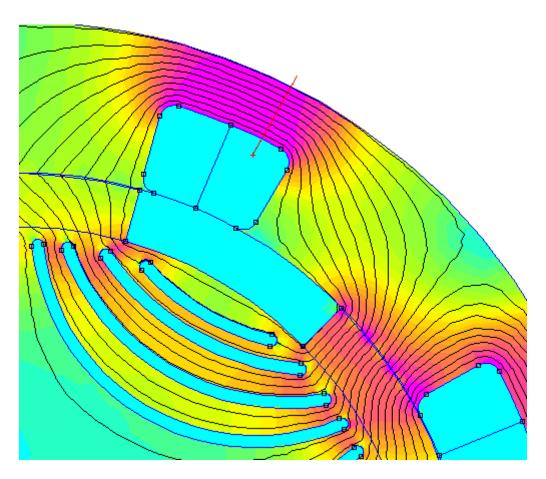


Fig B.32: Flux density lines as soon as phase B is energized and contour red line

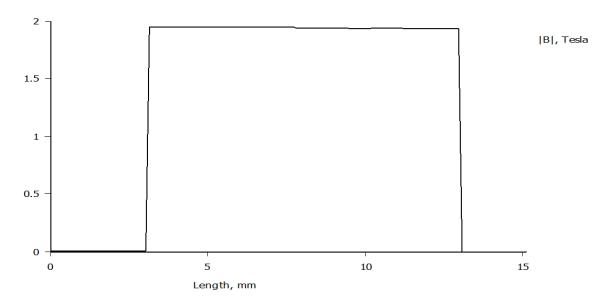


Fig B.33: Flux density lines crossing the contour line drawn in the Fig B.31

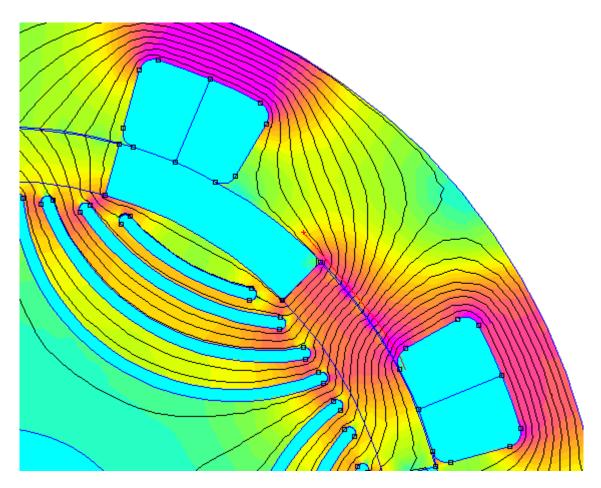


Fig B.34: Flux density lines as soon as phase B is energized and contour red line

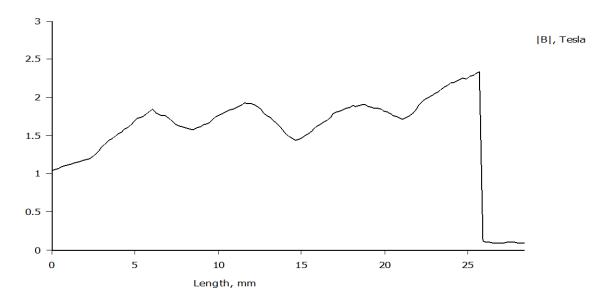


Fig B.35: Flux density lines crossing the contour line drawn in the Fig B.33

The highest values of density of the magnetic field are between 2 and 2,5 T. This geometry is working quite saturated with the nominal current. However, this motor design shows the

highest performance among the five geometries. Further study regarding the smoothing of the most saturated areas could be carried out.

B.2. Calculation of the number of turns, resistance of the magnetic copper wire, and phase inductance of the coil

The number of turns per stator pole has been calculated in order to achieve a coherent occupational factor F_o . Since the number of turns of the first SRM proposed geometry had to be the same as the number of turns of the second and final geometry for calculation comparisons, the number of turns have been limited by the slot surface of the second geometry, which is smaller than the first proposed ($S_1 = 0.251229 \cdot 10^{-3} \ m^2 > S_2 = 0.159232 \cdot 10^{-3} \ m^2$).

$$F_o = \frac{S_{occ}}{S_{slot}} = \frac{N \cdot S_{1 \, wire}}{S_{slot}} = \frac{N \cdot 0,667 \, mm^2 \cdot \frac{1 \, m^2}{1000000 \, mm^2}}{0,159232 \cdot 10^{-3} \, m^2} \approx 0,4 \rightarrow N = 100 \, turns$$

The occupational factor of the first geometry therefore is a bit lower ($F_0 = 0.265$) although in a reasonable range.

B.3. Variation of the components of the density of the magnetic field with the number of finite elements

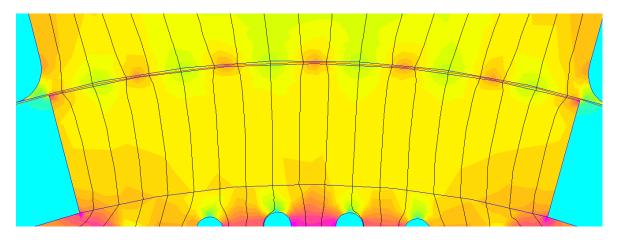


Fig B.36: Contour red line in the air gap of the fifth geometry for the position of maximum inductance when the nominal current is energised

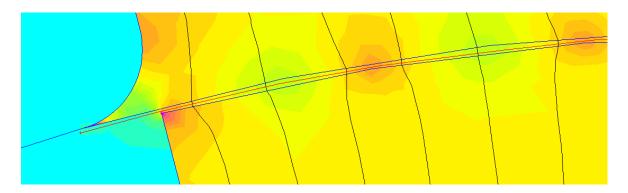


Fig B.37: Contour red line in the air gap of the fifth geometry for the position of maximum inductance when the nominal current is energised

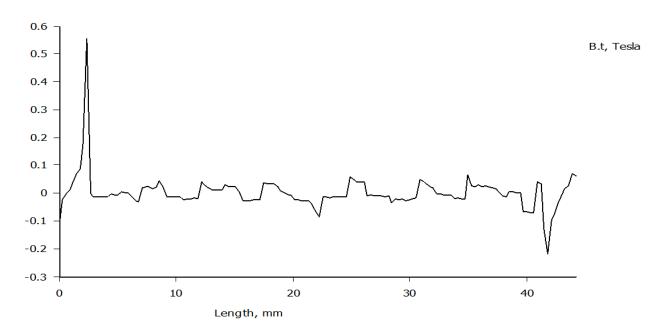


Fig B.38: Tangent component of the density of the magnetic field in the air gap in the position of maximum inductance. The number of nodes for the finite elements is 13.861 nodes.

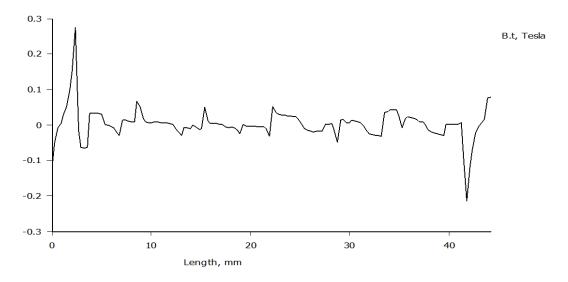


Fig B.39: Tangent component of the density of the magnetic field in the air gap in the position of maximum inductance. The number of nodes for the finite elements is 15.120 nodes.

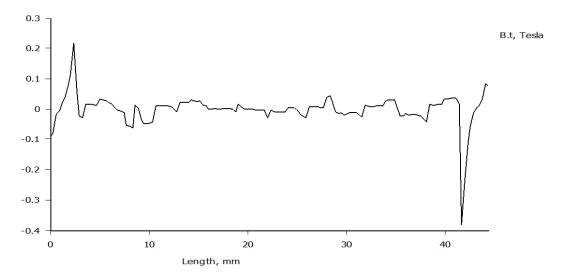


Fig B.40: Tangent component of the density of the magnetic field in the air gap in the position of maximum inductance. The number of nodes for the finite elements is 15.804 nodes.

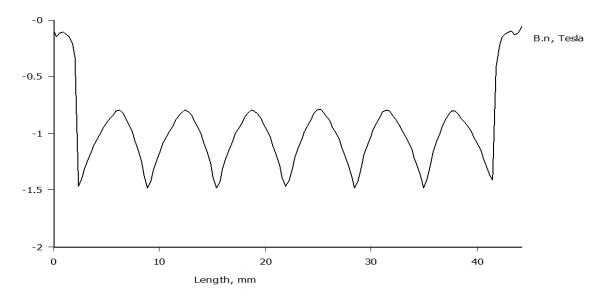


Fig B.41: Normal component of the density of the magnetic field in the air gap in the position of maximum inductance. The number of nodes for the finite elements is 13.861 nodes.

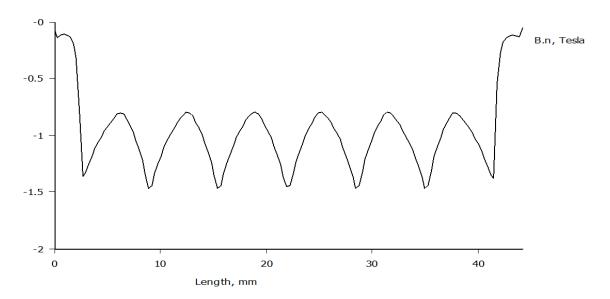


Fig B.42: Normal component of the density of the magnetic field in the air gap in the position of maximum inductance. The number of nodes for the finite elements is 15.120 nodes.

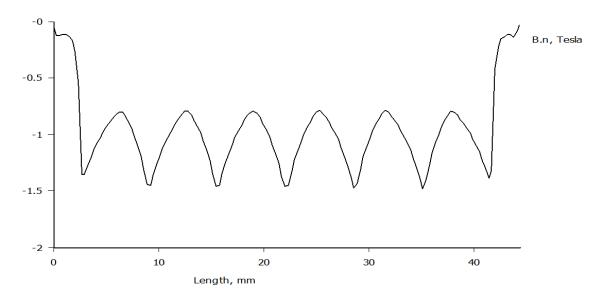


Fig B.43: Normal component of the density of the magnetic field in the air gap in the position of maximum inductance. The number of nodes for the finite elements is 15.804 nodes.

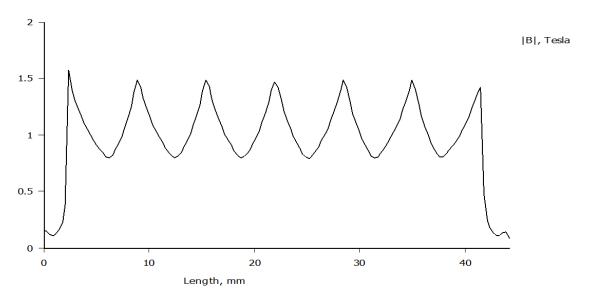


Fig B.44: Total density of the magnetic field in the air gap in the position of maximum inductance. The number of nodes for the finite elements is 13.861 nodes.

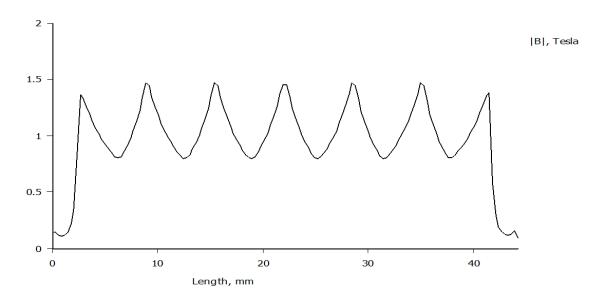


Fig B.45: Total density of the magnetic field in the air gap in the position of maximum inductance. The number of nodes for the finite elements is 15.120 nodes.

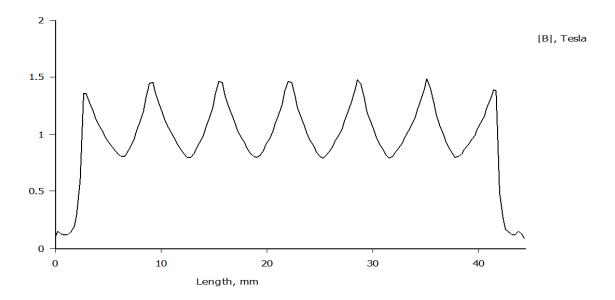


Fig B.46: Total density of the magnetic field in the air gap in the position of maximum inductance. The number of nodes for the finite elements is 15.804 nodes.

B.4. Calculation of the hysteresis and eddy current losses

Due to irreversible processes of magnetization a loss of heat occurs in the magnetic material. These losses are proportional to the area confined in the cycle of hysteresis of that material. The softer a magnetic material is, the smaller its area of hysteresis cycle and therefore the lower the losses due to alternate magnetization of the material.

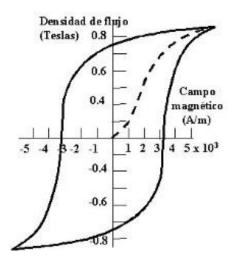


Fig B.47: Hysteresis cycle of a ferromagnetic material

The quantification of the losses due to the hysteresis cycle of the material can be approximated by the Steinmetz formula:

$$P_{h} = \frac{K_{H} \cdot f \cdot B_{max}^{n}}{\gamma \cdot 10^{4}} \frac{W}{kg}; n \begin{cases} 1.6 \text{ if } B_{max} < 1 \text{ T} \\ 2 \text{ if } B_{max} > 1 \text{ T} \end{cases}$$

 K_H is the hysteresis coefficient that depends on the material characteristics and other parameters, the frequency equals 75 Hz (phase commutation frequency), γ is the specific weight of iron of the rotor and B_{max} accounts for the highest value of density of the magnetic field in the magnetization cycle considered.

The quantification of the losses due to the eddy currents can also be approximated by the following formula from Steinmetz:

$$P_{ed} = \frac{\sigma_E \cdot f^2 \cdot B_{max}^2}{\gamma \cdot 10^4} \frac{W}{kg}$$

 σ_{E} is the eddy current coefficient that depends on the material characteristics.