Different Accretion Heating of the Neutron Star Crust during Multiple Outbursts in MAXI J0556-332

Abstract

The transient neutron star (NS) low-mass X-ray binary MAXI J0556–332 provides a rare opportunity to study NS crust heating and subsequent cooling for multiple outbursts of the same source. We examine *MAXI*, *Swift*, *Chandra*, and *XMM-Newton* data of MAXI J0556–332 obtained during and after three accretion outbursts of different durations and brightnesses. We report on new data obtained after outburst III. The source has been tracked up to \sim 1800 days after the end of outburst I. Outburst I heated the crust strongly, but no significant reheating was observed during outburst II. Cooling from \sim 333 eV to \sim 146 eV was observed during the first \sim 1200 days. Outburst III reheated the crust up to \sim 167 eV, after which the crust cooled again to \sim 131 eV in \sim 350 days. We model the thermal evolution of the crust and find that this source required a different strength and depth of shallow heating during each of the three outbursts. The shallow heating released during outburst I was \sim 17 MeV nucleon and outburst III required \sim 0.3 MeV nucleon 1. These cooling observations could not be explained without shallow heating. The shallow heating for outburst II was not well constrained and could vary from \sim 0 to 2.2 MeV nucleon 1, i.e., this outburst could in principle be explained without invoking shallow heating. We discuss the nature of the shallow heating and why it may occur at different strengths and depths during different outbursts.

Key words: accretion, accretion disks - stars: neutron - X-rays: binaries - X-rays: individual (MAXI J0556-332)

1. Introduction

Transient neutron stars (NSs) in low-mass X-ray binaries (LMXBs) are excellent laboratories to study dense matter physics. These systems experience accretion outbursts separated by periods of quiescence. During outbursts, the accreted matter compresses the NS surface, inducing heat-releasing nuclear reactions deep in the crust (Haensel & Zdunik 1990, 2008; Steiner 2012) that disrupt the crust-core thermal equilibrium. Once the source transitions into quiescence the crust cools to restore equilibrium with the core. Tracking this crustal cooling and fitting theoretical models to study its evolution allows us to infer NS crust properties (e.g., Brown & Cumming 2009). So far, eight NS LMXBs that show crustal cooling have been studied (see Wijnands et al. 2017 for a review). In addition to the standard deep crustal heating $(\rho \sim 10^{12} - 10^{13} \,\mathrm{g \, cm^{-3}})$, a shallow heat source $(\rho \sim 10^8 - 10^{10})$ g cm⁻³) is required to explain the observed cooling curve of many of these sources. The origin of this shallow heat source is unknown and is important to resolve because the cooling curve can be used to constrain a number of different aspects of crust physics (such as conductivity of the crust and pasta, and the core specific heat; Brown & Cumming 2009; Horowitz et al. 2015; Cumming et al. 2017). Most systems need $\sim 1-2 \,\mathrm{MeV}$ nucleon⁻¹ of shallow heating to explain their

cooling curves (e.g., Degenaar et al. 2014; Parikh et al. 2017; Wijnands et al. 2017).

The transient NS LMXB MAXI J0556-332 (hereafter J0556) was discovered on 2011 January 11 (Matsumura et al. 2011) and exhibited a \sim 16 month outburst. The source showed a second outburst in 2012 that lasted \sim 2 months (Sugizaki et al. 2012) and a third \sim 3 month outburst in 2016 (Negoro et al. 2016). In Figure 1 (top panel), we show the MAXI light curve with all three outbursts. Sugizaki et al. (2013) examined the spectral data obtained using the MAXI, Swift, and RXTE when the source was in outburst, and constrained the source distance to be >17 kpc. Homan et al. (2014, hereafter Ho14) studied the Swift, Chandra, and XMM-Newton spectra of the source after its outbursts and found a distance of \sim 45 kpc. Such a large distance was further supported by the 46 ± 15 kpc distance the same authors obtained when comparing the X-ray color-color and hardness-intensity diagram of J0556 with those observed for other, similarly bright (~Eddington limited) NS LMXBs (i.e., the so-called Z

Ho14 studied J0556 in quiescence after outburst I and II and found it to have a very hot NS crust. They showed that outburst II did not seem to reheat the NS crust. Deibel et al. (2015) showed that J0556 released a very large amount of shallow

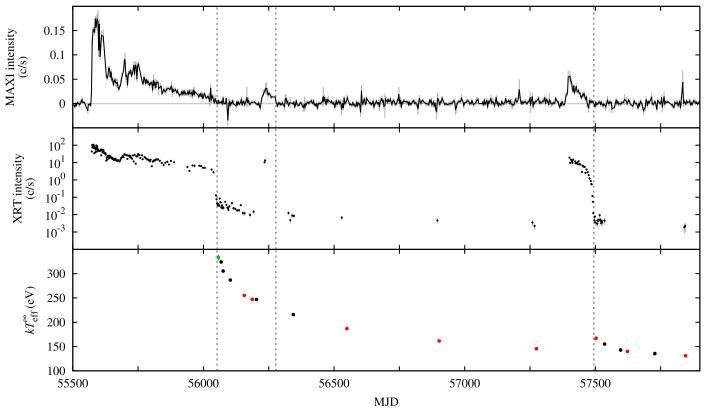


Figure 1. Long-term light curves of J0556 from MAXI/GSC (top panel; 2–4 keV) and Swift/XRT (middle panel; 0.5–10 keV). In the bottom panel, we show the temperature evolution of the source during its quiescent periods (the green, black, and red points indicate the Swift/XRT, Chandra, and XMM-Newton data, respectively). The dotted gray lines indicate the time of transition to quiescence after each outburst.

heating during outburst I of $\sim \! 10 \, \text{MeV}$ nucleon $^{-1}$ to explain its crust cooling evolution, the largest required by any NS LMXB source studied so far. During outburst II, the shallow heating mechanism was inactive or at a much reduced level compared to outburst I. Here, we present cooling observations of J0556 after outburst III demonstrating that the source was reheated during this outburst, requiring a small but significant amount of shallow heating. Therefore, the shallow heating mechanism is not just active or inactive but can indeed be active at different strengths.

2. Observations, Data Analysis, and Results

J0556 has been observed in quiescence by the *Swift*, *Chandra*, and *XMM-Newton* observatories. We use *MAXI* and the X-ray Telescope (XRT; Burrows et al. 2005) on board *Swift* to track the variability of the source during its outbursts. We report on eight new *Chandra* and *XMM-Newton* observations of this source. For uniformity, we also reanalyze all observations reported by Ho14. Table 1 shows the log of quiescent observations.

2.1. MAXI

The outburst evolution of J0556 was observed using the *MAXI*/Gas Slit Camera (GSC; Mihara et al. 2011). We downloaded the light curve from the *MAXI* archive¹³ for the 2–4 keV range as Ho14 suggest that this energy range results in the highest signal-to-noise ratio. Similar to their analysis, we

remove data that have error bars larger than 0.025 counts s⁻¹ and apply a three-day rebinning.

2.2. Swift/XRT

Swift/XRT was also used to monitor the evolution of J0556. The raw data were processed with HEASOFT (version 6.17) using xrtpipeline. The light curve and spectra were extracted using XSelect (version 2.4c). A circular source extraction region with a radius of 40" was used. For the background extraction region we used an annulus of inner and outer radii 50" and 80", respectively.

Four observations after outburst I were combined into one interval to obtain constraints on the earliest crust cooling phase (observation ID [obsID]: 00032452004–00032452007; from 2012 May 7 to 2012 May 11). The Photon Counting mode data from these observations were stacked into a single event file, and the spectrum was extracted using the same source and background regions as those used for the light curve. The ancillary response file was generated using xrtmkarf, and the appropriate response matrix file "swxpc0to12s6_20110101v014.rmf" was used. The 0.3–10 keV spectrum was binned to have a minimum of 5 counts per bin using grppha.

2.3. Chandra

J0556 was observed 10 times with the Chandra/ACIS-S (Garmire et al. 2003) in the FAINT mode using the 1/8 subarray. Two observations (ObsID: 14429 and 14227; see Table 1 of Ho14) took place during episodes of temporary increases in accretion rate during the first ~ 100 days after the

¹³ http://maxi.riken.jp/top/slist.html

Table 1
Log of the Quiescent Observations^a

	Instrument	ObsID	Days since End of Outburst I	Exposure Time ^b (ks)	$kT_{\mathrm{eff}}^{\infty}$ (eV)	$F_{\rm X}$ (×10 ⁻¹⁴ erg cm ⁻² s ⁻¹)	$L_{\rm X} \ (\times 10^{33} { m erg s}^{-1})$
				After Outburst I			
1	Swift	Interval 1 ^c	5.4	10.1	333.1 ± 5.5	109.7 ± 6.6	249.5 ± 15.1
2	Chandra	14225	16.0	9.2	324.1 ± 2.5	106.3 ± 3.6	241.9 ± 8.3
3	Chandra	14226	23.3	9.1	305.4 ± 2.5	79.7 ± 2.8	181.2 ± 6.3
4	Chandra	14433	51.0	18.2	286.9 ± 1.9	62.4 ± 1.8	142.0 ± 4.0
5	XMM-Newton	0700380901	104.3	28.2, 27.6, 21.5	255.2 ± 0.9	37.9 ± 0.6	86.2 ± 1.3
6	XMM-Newton	0700381201	134.9	24.4, 23.7, 17.5	247.1 ± 1.0	32.6 ± 0.7	74.1 ± 1.4
7	Chandra	14434	150.8	18.2	246.8 ± 2.1	33.5 ± 1.3	76.2 ± 2.8
				After Outburst II			
8	Chandra	14228	291.7	22.7	215.8 ± 2.2	19.1 ± 0.8	43.5 ± 1.9
9	XMM-Newton	0725220201	496.8	44.3, 42.3, 34.9	186.8 ± 1.0	10.2 ± 0.2	23.2 ± 0.6
10	XMM-Newton	0744870201	850.1	77.3, 78.6, 59.9	161.5 ± 0.8	5.5 ± 0.1	12.6 ± 0.3
11	XMM-Newton	0762750201	1222.6	83.9, 72.3, 57.5	145.4 ± 1.0	3.5 ± 0.1	7.9 ± 0.3
				After Outburst III			
12	XMM-Newton	0784390301	1450.7	20.4, 18.6, 18.6	166.9 ± 1.8	6.9 ± 0.5	15.7 ± 1.1
13	Chandra	18335	1483.2	27.3	155.1 ± 2.8	4.8 ± 0.4	10.9 ± 1.0
14	Chandra	18336	1544.3	27.1	142.9 ± 3.3	3.4 ± 0.5	7.8 ± 1.0
15	XMM-Newton	0784390401	1570.6	45.9, 41.3, 39.5	139.9 ± 1.4	3.0 ± 0.1	6.7 ± 0.3
16	Chandra	18337	1675.5	27.3	135.6 ± 3.5	2.6 ± 0.3	6.0 ± 0.7
17	XMM-Newton	0782670201	1793.1	61.0, 58.3, 36.7	130.9 ± 1.5	2.3 ± 0.1	5.1 ± 0.3

Notes.

end of outburst I. Since we are only interested in the crust cooling behavior we do not discuss these data (see Ho14 for more information about these observations). CIAO (version 4.9) was used to process the raw data of the remaining eight observations. We examined the source light curves for possible episodes of background flaring, but none were found. We used circular source extraction regions with a radius of 2"-3" (depending on source brightness). The background extraction region used was an annulus with inner and outer radii 10" and 20", respectively. The spectra were extracted using specextract. The point-source aperture-corrected arf files, as generated by specextract, were used. The 0.3-10 keV spectra were grouped using dmgroup to have a signal-to-noise ratio of 4.5.

2.4. XMM-Newton

XMM-Newton (Strüder et al. 2001) was used to observe J0556 eight times using all three European Photo Imaging Cameras (EPIC)—MOS1, MOS2, and pn. The raw data were reduced using the Science Analysis System (SAS; version 16.0) and processed using emproc and epproc for the MOS and pn detectors, respectively. The observations were checked for background flaring by examining the light curves for the >10 keV range for the MOS detectors and 10–12 keV range for the pn detector. Depending on the average source brightness during an observation, we removed data of >0.08–0.16 counts s^{-1} and data of >0.32-0.4 counts s^{-1} for the MOS and pn detectors, respectively. Circular source and background extraction regions were used for the spectral extraction. The optimal source region to be used was determined with eregionanalyse. Depending on the source brightness, regions of radii 19"-45" were used for the MOS detectors and regions of radii 19"-37" were used for the pn detector. A

background region of radius 50" was used for each observation, placed on the same CCD that the source was located on. The position of the background region as suggested by the ebkgreg tool was used. The redistribution matrix file and ancillary response function were generated using rmfgen and arfgen. The 0.3–10 keV spectra were binned using specgroup, with the signal-to-noise ratio set to 4.5.

2.5. Spectral Fitting

All Chandra and XMM-Newton 0.3–10 keV spectra were fit simultaneously in XSpec (version 12.9; Arnaud 1996) using χ^2 statistics. We used the NS atmosphere model nsa (Zavlin et al. 1996). The nsatmos model cannot be used as the source was very hot at the start of the cooling phase (see Ho14 for details). The temperature was left free for each individual XMM-Newton and Chandra observation. However, this parameter was tied between the MOS and pn cameras for a given XMM-Newton observation. All of the temperatures were converted into the effective temperature measured by an observer at infinity. The mass and radius of the NS were fixed to $1.4\,M_\odot$ and 10 km (since in the nsa model the surface gravity has only been calculated for this combination and does not give accurate results for other mass and radius values; Zavlin et al. 1996; Heinke et al. 2006). The magnetic field parameter was set to zero (indicating a non-magnetized star). The normalization $(1/D^2; D)$ is the distance and the N_H were free parameters but were tied between all observations. The $N_{\rm H}$ was modeled using tbnew_feo¹⁴ with WILM abundances (Wilms et al. 2000) and VERN cross-sections (Verner

^a All errors are 1σ . The distance and $N_{\rm H}$ were fixed to 43.6 kpc and 3.2×10^{20} cm⁻². The unabsorbed fluxes and luminosities are quoted for 0.5–10 keV.

^b The XMM-Newton effective exposure times have been displayed as "MOS1, MOS2, pn."

^c See Section 2.2.

¹⁴ http://pulsar.sternwarte.uni-erlangen.de/wilms/research/tbabs/

et al. 1996). The oxygen and iron abundances for tbnew_feo were fixed to 1.

We use the pileup component to model the pileup in the Chandra data. We set the maximum number of photons considered for pileup in a single frame to 3, the grade correction for single photon detection to 1, the PSF fraction is fixed to 0.95, and the number of regions and the FRACEXPO keyword are both set to 1. We find that the fits are not very sensitive to the alpha parameter (see also Ho14), and we fix this value to 0.6. The frame time, an input parameter for pileup, was set to 0.4 s for the *Chandra* observations. To prevent the pileup model from affecting the XMM-Newton data, we set the frame time for these observations to a very small value $(10^{-6} \,\mathrm{s})$. We also use the multiplicative model constant to allow for normalization offsets between the Chandra and XMM-Newton observatories. For the Chandra data we used a constant of 1 and for the various XMM-Newton detectors— MOS1, MOS2, and pn the constants were calculated from Table 5 of Plucinsky et al. (2017; $C_{MOS1} = 0.983$, $C_{MOS2} = 1$, $C_{\rm pn} = 0.904$).

The simultaneous fit of all the *Chandra* and *XMM-Newton* data resulted in a column density of $N_{\rm H}=(3.2\pm0.5)\times10^{20}$ cm⁻² and a distance of $43.6^{+0.9}_{-1.6}$ kpc. While calculating the error on the temperature, we fixed the best-fit $N_{\rm H}$ and distance values as they are not expected to vary between observations (see also, e.g., Wijnands et al. 2004, Ho14). The parameters from the obtained fit $(\chi^2_{\nu}/{\rm d.o.f.}=1.02/715)$ are shown in Table 1. Changing the mass, radius, $N_{\rm H}$, and distance will change the absolute $kT_{\rm eff}^{\infty}$, but the trend, which helps us understand crust physics, will not change significantly (e.g., Cackett et al. 2008). The brightest *Chandra* observations had a pileup fraction of $\sim 2\%$.

Due to the small number of counts per bin in the Swift/XRT spectra (0.3–10 keV), they were fit separately with W-statistics (background-subtracted Cash statistics) using the same N_H and distance as used for the *Chandra* and *XMM-Newton* spectral fitting. We allow for a normalization offset of $C_{XRT} = 0.872$ (Plucinsky et al. 2017).

Figure 1 shows the *MAXI* (top panel) and *Swift/XRT* (middle panel) light curves of J0556. The bottom panel of Figure 1 shows the cooling evolution of J0556, suggesting a strong decrease in the $kT_{\rm eff}^{\infty}$ after the end of outburst I. Outburst II did not reheat the crust significantly, and the cooling appeared to continue along its previous trend (see also Ho14). Overall, the crust cooled from ~333 eV to ~146 eV, after outbursts I and II. Outburst III caused the crust to be reheated significantly (to ~167 eV) and was followed by subsequent cooling (to ~131 eV approximately 350 days after the end of this recent outburst).

2.6. Modeling the Quiescent Thermal Evolution

We model the outbursts and quiescence of J0556 using the crustal heating/cooling code NSCool (Page & Reddy 2013; Page 2016). We account for the accretion rate variability during the outbursts and model all three outbursts collectively (using the methods of Ootes et al. 2016, 2017). The transition to quiescence after outburst I occurred on MJD 56052.1 (see Ho14). We use the methodology described by Fridriksson et al. (2010) to calculate the time of transition to quiescence by

fitting an exponential to the rapidly decaying trend at the end of the outburst and a straight line to the quiescent points soon after the end of the outburst. We used the *MAXI* and *Swift/XRT* light curve, respectively, for this calculation after outbursts I and II and determined the transition time to be MJD 56277.4 and MJD 57494.2.

We account for accretion rate variability during the outbursts by tracking the daily average rate, which is determined from the daily averaged MAXI and Swift/XRT count rates. If data from both instruments are available on the same day, the Swift/ XRT data are used. Sugizaki et al. (2013) report the bolometric flux (F_{bol}) from J0556 at six different instances during the first outburst (no such reports are available for the other two outbursts). We use these values to calculate a count rate to the $F_{\rm bol}$ conversion constant for the MAXI and Swift/XRT data using count rates from the same days as the six reported F_{bol} values. This constant was calculated for each of the six observations for both instruments, and the final constant used for each instrument was the averaged value. The obtained constants are $C_{MAXI} = 2.353 \times 10^{-8} \, \mathrm{erg \, cm^{-2}} \, \mathrm{count^{-1}}$ and $C_{Swift} = 4.957 \times 10^{-11} \, \mathrm{erg \, cm^{-2}} \, \mathrm{count^{-1}}$. The individual count rates to F_{bol} conversion constants differ at most by a factor of \sim 2 from each other. We tested our NSCool model results by using these minimum or maximum calculated individual conversion constant values (instead of the averaged ones) for all three outbursts as well as by using different values for different outbursts. We find that this only inconsequentially changes our inferred NS parameters without affecting our main conclusions. The F_{bol} was used to calculate the daily average accretion rate using

$$\dot{M} = \frac{F_{\text{bol}} 4\pi D^2}{\eta \ c^2},$$

where η (=0.2) indicated the efficiency factor and c is the speed of light. Using this we obtained the fluences of the three outbursts to be \sim 4.3 \times 10⁻² erg cm⁻², \sim 2.1 \times 10⁻³ erg cm⁻², and \sim 4.4 \times 10⁻³ erg cm⁻², respectively.

The NS mass and radius used for the NSCool models are the same as those used for the spectral fits. The distance used is that calculated from the best fit to the spectra (Section 2.5). The NSCool adjustable parameters are the impurity factor in the crust $(Q_{\rm imp})$, the column depth of light elements in the envelope $(y_{\rm light})$, the core temperature prior to the first outburst (T_0) , and the strength $(Q_{\rm sh})$ and depth $(\rho_{\rm sh})$ of the shallow heating. We model the shallow heating with different parameters during each outburst. Furthermore, we also allow the envelope composition of the crust to vary for each outburst (Ootes et al. 2017). The best fit is found using a χ^2 -minimization algorithm, and all errors are calculated for the 1σ confidence range.

Our modeling shows that heating only by deep crustal reactions (in combination with changes in the envelope composition) cannot explain the observations of J0556. A significant amount of shallow heating is necessary to explain the data. $Q_{\rm sh} \sim 17 \, {\rm MeV} \, {\rm nucleon}^{-1}$ is needed to explain the high temperatures after outburst I. The best-fit model $(\chi^2_{\nu}/{\rm d.o.f.} = 2.8/9)$ is shown by the solid black line in Figure 2, and the parameters are listed in Table 2. Outbursts II and III cannot be explained with the same shallow heating as required for outburst I, not even if the envelope composition is allowed to change (Brown et al. 2002). The dotted gray line in

¹⁵ We use values suggested by the *Chandra* pileup guide: http://cxc.harvard.edu/ciao/download/doc/pileup_abc.pdf.

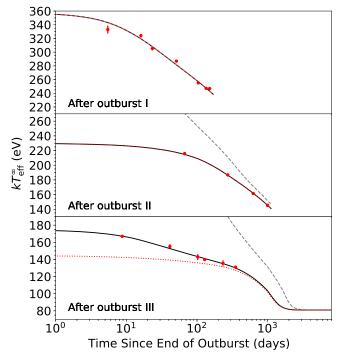


Figure 2. The $kT_{\rm eff}^{\infty}$ evolution of J0556 in quiescence with the cooling curves calculated using NSCool. The solid black line shows the best-fit model with all three outbursts having different shallow heating parameters. The dashed gray line shows the outcome if the same shallow heating parameters as inferred for outburst I were used for all three outbursts. The dotted red line shows the model when no shallow heating was assumed to be active during outbursts II and III

Table 2
Shallow Heating Parameters from NSCool

Outburst	$Q_{ m sh}$ (MeV nucleon $^{-1}$)	$(\times 10^9 {\rm g}^{\rho_{\rm sh}} {\rm cm}^{-3})$
I	$17.0^{+2.2}_{-0.7}$	$5.3^{+0.2}_{-0.5}$
II^a	0	•••
	2.2 ± 0.7	33.5 ± 0.8
III	0.33 ± 0.03	1.6 ± 1.3

Note.

Figure 2 shows a model that assumes that during all three outbursts the shallow heating mechanism $Q_{\rm sh} \sim 17 \, {\rm MeV \ nucleon^{-1}}$, clearly showing that this would result in much hotter crusts than what we have observed. Outburst III could be modeled with $Q_{\rm sh} \sim 0.3 \, {\rm MeV \ nucleon}^{-1}$ at shallower depths than that required for outburst I. Outburst III could not be modeled without shallow heating. This is shown by the dotted red line in Figure 2, which indicates a model for which we assumed that the shallow heating mechanism was not active during outbursts II and III. This model shows that outburst II can be explained without shallow heating. However, the uncertainties on the shallow heating parameters after outburst II are large, ranging from (a) no shallow heating $(Q_{\rm sh} \sim 0 \, {\rm MeV \, nucleon}^{-1})$ when this heating source is at relatively shallow depths (i.e., the $\rho_{\rm sh}$ corresponding to outburst I or outburst III) as well as (b) a large $Q_{\rm sh}\sim 2.2~{\rm MeV}$ nucleon⁻¹ very deep in the crust (at $ho_{
m sh} \sim 33.5 imes 10^9 \, {
m g \ cm}^{-3}$). This is because $Q_{
m sh}$ and $ho_{
m sh}$ are

correlated and the modeled curve from these two possibilities have a very similar shape.

In addition to constraining the shallow heating parameters, we found a core temperature of $T_0 = (5.5 \pm 0.4) \times 10^7 \, \mathrm{K}$. Assuming a $Q_{\mathrm{imp}} = 1$ throughout the crust fit the data well. Increasing the Q_{imp} to $\sim\!20$ as suggested by Horowitz et al. (2015), in the pasta layer (which extends from $\rho \sim 10^{13} \, \mathrm{g \ cm^{-3}}$ to the crust–core boundary), reduced the fit quality, indicating that the crust of this source has a high thermal conductivity throughout.

Our best-fit model indicates that a relatively light envelope is necessary after outburst I ($y_{\rm light} \sim 3.1 \times 10^9 \, {\rm g \, cm}^{-2}$). The data after outburst I cannot be adequately fit using a heavy element envelope as the light elements are necessary to raise the effective temperature to that which we observe. The envelope composition systematically raises or drops the observed trend, whereas a change in the shallow heating changes the slope of the trend itself; therefore, they are only partially degenerate in determining the cooling trend. The best fit indicates that a similar envelope composition ([2.1–3.1] \times 10⁹ g cm⁻²) is present after all three outbursts. Further extensive investigation into the NSCool parameters is not the aim of this Letter.

3. Discussion

We studied the NS LMXB J0556 in quiescence. Since the NS mass, radius, and distance remain the same between outbursts, studying the source after multiple outbursts allows us to investigate which parameters affecting the heating and cooling behavior of the crust may change. As reported by Ho14, we found a strongly heated crust after outburst I. The amount of shallow heating during outburst I was very large at $Q_{\rm sh} \sim 17 \, {\rm MeV \ nucleon^{-1}}$. During outburst II the shallow heating mechanism may have been inactive (see also Deibel et al. 2015 for similar results of outbursts I and II). However, it should be noted that the first pointing was obtained long after the end of outburst II (\sim 70 days) and $Q_{\rm sh}$ could not be constrained well. Up to \sim 2.2 MeV nucleon⁻¹ was still allowed during this outburst if the heating occurred at much larger depths. We present new quiescent observations after the end of outburst III. Shallow heating (at $\sim 0.3 \,\mathrm{MeV}$ nucleon⁻¹) needs to have been active during outburst III to explain the reheating we observed after the end of the outburst since the deep crustal reactions alone cannot account for this reheating. Based on the well-constrained shallow heating parameters found after outbursts I and III we find that this heating mechanism may release different amounts of heat per accreted nucleon during different outbursts and may not be simply active or inactive (as could still be the case after the study by Deibel et al. 2015).

The origin of shallow heating remains unknown and thus also why its strength varies during different outbursts. One possibility (as suggested by Inogamov & Sunyaev 2010) is that the shallow heating originates from the dissipation of the accretion-generated g-modes in the ocean (i.e., the melted crust). Based on $kT_{\rm eff}^{\infty}$, we find that the ocean is deeper during outburst II than outburst III. If the shallow heat source is placed at this ocean–solid crust interface then our models indicate that more shallow heat is required during outburst III than outburst II, suggesting that the strength of heat deposition is unlikely to vary with the depth of the ocean (as suggested by Deibel 2016).

It is interesting to note that the strength of the shallow heating seems to correlate with the outburst fluences ($Q_{\rm sh}$ decreases from $\sim 17~{\rm MeV~nucleon}^{-1}$ to $\sim 0.3~{\rm MeV~nucleon}^{-1}$

^a The parameters for outburst II are given for a range of values.

when the fluence decreases from $\sim 4.3 \times 10^{-2} \, \mathrm{erg \, cm^{-2}}$ to $\sim 4.4 \times 10^{-3} \, \mathrm{erg \, cm^{-2}}$). However, even if true for J0556, this cannot be extrapolated to other sources. Another NS LMXB, XTE J1701–462, experienced an outburst in 2006/2007 with a similar fluence to outburst I of J0556 (Fridriksson et al. 2010, 2011; see Ho14 for details), but J0556 needs $Q_{\rm sh} \sim 17 \, \mathrm{MeV}$ nucleon⁻¹ to explain its cooling data, whereas XTE J1701–462 needs only $Q_{\rm sh} \sim 0.1 \, \mathrm{MeV}$ nucleon⁻¹ (Page & Reddy 2013). Therefore, across sources there is another, unknown parameter that sets the strength of the shallow heating.

Using our NSCool models we attempted to discern if the observed crust cooling currently follows the cooling trend defined by outburst I or if the reheating from outburst III still influences the crust temperature. We find that a model that only includes heating from outburst I slightly undershoots our most recently obtained data point, suggesting that the crust might not have yet returned to the original cooling trend. However, due to uncertainties in the data and the modeling we cannot conclusively say if this is indeed the case. Future *Chandra* observations will clarify this as well as probe the pasta layer present deeper in the crust.

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