

## Appendix A

% Defining known parameters

```
lamb=0.001027; % laser wavelength(mm)
radi_ExPup=8.5; % aperture radius (mm)
w_ini=7.075; % beam width (mm)
Ein=3*10^-6; % laser pulse energy (J)
Fllin=2500; % titanium fluence threshold (J/m^2)
temps=450*10^-15; % laser pulse duration (s)
cn=0.00265; % speed of light multiplied by the electrical permittivity of vacuum (F/s^2)
Z_ini=-13; % focalization distance (mm)
tilt_deg=0.7; % lens tilt angle (with respect to the xy plane) (degrees)
angle1=26; % angle of rotation with respect to the x axis (degrees)
A=1; % electric field amplitude (V/m)
desp_openx=1.02; % pupil displacement in the x axis (mm) (real value*2.83)
desp_openy=-0.50; % pupil displacement in the y axis (mm) (real value*2.83)
```

% Gaussian beam parameters calculation

```
k=2*pi/lamb; % wave vector (rad/mm)
w0=w_ini/(sqrt(1+(pi*w_ini^2/lamb/z_ini)^2)); % beam waist width (mm)
LRayl=pi*w0^2/lamb; % Rayleigh range (mm)
R_ini=z_ini*(1+(LRayl/z_ini)^2); % curvature radius at the initial plane(mm)
gouy_ini=atan(z_ini/LRayl); % Gouy phase
```

% Defining the matrix dimensions and matrix positions

```
N=2048; iN=-N/2:(N/2-1); % number of points of the matrix
L_ini=20.9*radi_ExPup; % length of the matrix (mm)
T_ini=L_ini/N; % digitalization interval (mm)
[x,y]=meshgrid(iN*T_ini,iN*T_ini); % generating the matrix positions
x2= x.*cosd(angle1)-y.*sind(angle1); % changing the coordinates
y2= x.*sind(angle1)+y.*cosd(angle1);
```

% Calculating the electric values at the output of the objective

```
f_ini = A * exp(1i*(k*z_ini-gouy_ini)) * exp((1i*k/2/R_ini-
1/w_ini^2)*((x2*cosd(tilt_deg)).^2+y2.^2)); % the cosine implements the objective tilt
% The real distribution is implemented here
```

% Taking into account the optical path with tilt in x2 direction

```
tilt_x2 = exp(1i*k.*x2.* sind(tilt_deg)/ cosd(tilt_deg));
f_ini = f_ini.* tilt_x2;
```

% The beam is cut by the pupil

```
pupil=sqrt((x-desp_openx).^2+(y-desp_openy).^2)< radi_ExPup;
f_ini=f_ini.*pupil;
```

% The electric field values are recalculated to match the laser pulse energy

```
E= sum(sum(abs(f_ini).*abs(f_ini)*T_ini*T_ini*10^-6*cn/2))*temps;
f_ini=f_ini*sqrt(Ein/E);
```

% Plot of the intensity distribution at the output of the objective

```
zoom=-400:399;
figure(1), imshow(abs(f_ini(zoom+N/2+1,zoom+N/2+1)).^2,[],),colormap(jet);
```

% Using the propagator to propagate to a certain distance

```

d=12.971;
[Uf Tf]=propaga_d(lamb,N,f_ini,T_ini,d);

% Plot of the intensity distribution at certain position
figure(2), imshow(abs(Uf(zoom+N/2+1,zoom+N/2+1)).^2,[],colormap(jet);
% Plot of the threshold image at certain position
figure(3),imshow((abs(Uf(zoom+N/2+1,zoom+N/2+1)).^2)<Fllin*2/(cn*temps),[]);
% Calculation of the beam width at certain position
beamwidth=sqrt(sum(sum((abs(Uf).^2)>(max(max(abs(Uf).^2))/exp(2))))*Tf*Tf/pi());

```

## Appendix B

```

% read the real intensity distribution matrix before the objective
% first column= x position, second column= y position, third column = value
M=csvread('real_intensity_distribution.txt');
p=size(M);
NN=zeros(240,320);
M(p(1),2)
for r=1:p(1)
    NN(M(r,1)+1,M(r,2)+1)=M(r,3);
end
% normalize the matrix
NN=NN/max(max(NN));
% substitute the simulated values for the real ones
zoomy=-119:118;
zoomx=-157:155;
f_ini(zoomy+N/2+1,zoomx+N/2+1)=sqrt(NN(1:238,8:320)).*exp(1i*angle(f_ini(zoomy+N/2+1,
zoomx+N/2+1)));

```

## Appendix C

```

% propagator based on the Fresnel diffraction equations [5]
% return electric values and the digitalization value
% the function acts using wavelength, number of matrix points, electric field, digitalization value
and propagation distance
function [Uf Tf]=propaga_d(lamb,N,Ui,Ti,d)
    iN=-N/2:(N/2-1);
    if d==0,      Uf=Ui; Tf=Ti; % it allows to not do propagation
    else
        k=2*pi/lamb;
        [x,y]=meshgrid(iN*Ti,iN*Ti);
        fase_i=exp(1i*k/2/d*(x.^2+y.^2));
        lamb*d/2/(N/2*Ti); % digitalization limit value
        integ=fftshift(fft2(fftshift(Ui.*fase_i))*Ti*Ti);
        Tf=lamb*d/N/Ti; % new digitalization values
        x=x*Tf/Ti; y=y*Tf/Ti; % before...[x,y]=meshgrid(iN*Tf,iN*Tf);
        fase_f=exp(1i*k*d)/(1i*lamb*d)*exp(1i*k/2/d*(x.^2+y.^2));
        Uf=fase_f.*integ; % electric field values at position d
    end

```