Aerodynamic study on the design and optimization of flatback airfoils for wind turbine applications

REPORT

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Chapter 1

Introduction

1.1 Aim

The aim of this project is to study the flatback profiles that are used for wind turbine applications, this kind of profiles replace the usual thick profiles used at the root of the blade of the wind turbines. More precisely, the target of the project is to continue the aerodynamic optimization of the flatback profiles started in a previous project.

1.2 Scope

The target of this project is to optimise a flatback profile. This goal is achieved by using intermediate steps, which help to carry out an ordinate and coherent project.

At first, a research of information will be done, in order to understand how wind turbines work and to know all their components. It is also necessary to pay attention on the interaction that appears between the blade and the air. All these topics are really important in order to know which are the parameters that have to be changed in order to improve the aerodynamic performance of the blade of the wind turbine.

Knowing the parameters that need to be changed, new geometries will be created. They are supposed to be better than the original one and will be proved during the project.

The aerodynamic characteristics of each geometry will be computed. Considering the complexity of the calculations a 2D and steady study will be developed instead of a unsteady and 3D one. All the calculations will be done by using ANSYS software.

So, a mesh that fits the geometry needs to be created and it is also important to know the boundary conditions of the object in order to get reasonable and real values.
Finally, a comparison of the results for each profile will be done and the conclusions will be extracted.

All these activities could be summed up and distributed in different groups as follow:

- Research of information and documentation
  - State of the art and information of flatback profiles
  - Research of related information
- Creation of a new geometry
- Software tasks
  - Ansys software learning
  - Creation of an appropriate mesh for each profile
  - Simulation of each profile
  - Post-process of the simulation
- Results evaluation
- Writing of the TFG
- Revision

The documents that will be delivered to achieve the goals are:

- Project charter
- Follow up reports
- TFG draft
- Quality report
- Final delivery

1.3 Requirements

- The new flatback profile must have better aerodynamic properties than the profiles used in the inner zones of a blade in a wind turbine. In general, this better aerodynamic properties are higher $C_L$ and higher $E = \frac{C_L}{C_D}$.
- The new flatback profile must have better aerodynamic properties than the profile designed in the previous project.
1.4 Justification

Nowadays there is a very high consumption of electricity. It is increasingly important to use renewable energy with the aim of avoiding pollution and because fossil fuels are running out.

One of the most used renewable energy is wind energy, and this project will be focused on it. In recent years, due to the increasing demand of electricity, wind turbines have changed, becoming larger and more profitable. The near tip region, which gives most part of the energy, has been optimized to the maximum in the last decades. Nowadays, new methods that are used to improve performance are focused on the near root region. It is for this reason that this project will be focused on changing the thick profiles that are used at the root of turbine blades for flatback profiles.

The lack of information and documentation about this type of profiles make necessary their analysis. The final target of this project is to improve the aerodynamic performance of flatback profiles by means of an optimization in order to capture more energy from the wind or, what is the same, increase the $C_p$.

This project optimization will not consist in a modification of a thick profile, but will continue the optimization of a flatback profile already started on another project.
Chapter 2

Development

2.1 State of the art

Windmills have been used for at least 3000 years, their main function were grinding grain or dumping water, while in mailing ships the wind has been an essential source of power for even longer [11]. Exactly, windmills are used to grinding grain whereas wind turbines are the modern turbines used to generate electricity.

In 1973, after the world energetic crisis, there was a growth in global interest in the development and use of alternative energy sources like solar, wind, geothermic, etc.

Focusing on wind energy, wind turbines have experienced a long and gradual improvement in performance, reducing capital cost per installed megawatt, improving capacity factor and reducing operations and maintenance costs.

In 2004, a suddenly jump in cost of the products, produced a sudden increase in capital cost. From this moment, technology has experienced gradual and steady improvement.

The most important areas of investigation are; turbine blade structural design (size considerations), blade flow and load control devices and blade profile design (for increase power and efficiency). However these areas are not independent, there are several interconnected parameters that have to be taken into account during this process. These parameters and their relationship are shown at figure 2.1.

Nowadays wind energy is one of the greatest growing technologies in the energy sector and it is expected to supply 12% of the world’s electricity consumption by 2020 [13].

The most visible change is the continuous increase in the rotor diameter from around 30 m to more than 100 m. This increase in size occurs despite the unexpected and
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Figure 2.1: Wind turbine design [1]

undesirable square-cube law. This law says that the output power is proportional to the square of the rotor diameter, whereas rotor mass is proportional to the cube of the rotor diameter. So, a doubling of the rotor diameter leads to a four-times increase in power output and an eight-times increase in mass [11]. The evolution in size and power of the wind turbines is shown at figure 2.2.

Figure 2.2: Esqueme of the evolution of wind turbines in size and power, [2]

It is easy to understand that to improve energy capture without increasing capital cost requires that rotors sweep a greater area without increasing gravitational and aerodynamic system loads. So, some changes in wind turbines have to be done.

Profile shapes are important to wind turbines because their geometry affects directly the thrust and the torque force. At the same time, thrust and torque force affect the energy generated by the wind turbine.

In the last decades, several airfoil families have been created to modify these geometries in order to accomplish the intrinsic requirements in terms of design point, off-design capabilities, and structural properties. Among these families, the most famous are FX from the University of Stuttgart (Germany), DU designed at the Delft University of
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Technology (Netherlands) and NACA 64 [16]. Actually, NACA profiles are not designed to be used specifically in wind turbines but they perform better than expected at the tip of the blade.

Flatback profile is one of the new designs of the geometry, it consist in a blunt trailing edge, this geometry generates a larger moment of inertia and have manufacture facilities, moreover it has an aerodynamic performance a little bit better than the common profiles.

This type of profiles can be created using two main methods:

- Truncation: this method consists in cutting-off the edge part of the profile.
- Adding thickness: this method consists in adding thickness symmetrically to either sides of the camber line.

Their main characteristics, advantages and disadvantages will be explained after, at section 2.3.2 Flatback creation.

A comparison between a classical representation of blades (CX-100) and an example of flatback profiles incorporated in a blade has been showed in the follow graphs. Figure 2.3 shows the plan forms of these blades, figure 2.4 provides a view of the two different blade geometries as seen from the trailing edge and finally, figure 2.5 shows the profiles geometries and the relative sizes at the root of the blades [3].

![Figure 2.3: Plan forms of blades [3]](figure)

![Figure 2.4: Trailing edge blades [3]](figure)
2.2 Wind turbine

Wind turbine is a machine that transforms the mechanical energy contained in the wind into electricity. Wind turbines can be divided in two groups:

- Vertical Axis Wind Turbines (VAWT)
- Horizontal Axis Wind Turbines (HAWT)

Both, VAWT and HAWT, have a subdivision that consists in high velocity turbines with few blades and low velocity ones that have a lot of blades. A balanced solution between efficiency and cost has been found. This solution is used for almost all the manufacturers and consists in an horizontal axis with three blades with an upwind orientation so, the rotor is always faced to the wind.

This project is centred in horizontal axis wind turbines, which method to extract wind energy is based in the sustentation that the blades have.

The main components of a typical wind turbine are [4]:

- The tower: it is mostly cylindrical and from 80 to 140 metres in height.
- Rotor blades: can be from one to three rotor blades. They are usually between 80 and 140 meters in diameter.
- The yaw mechanism: it turns the turbine to face the wind
- Direction monitor: Tower head is turned to line up with the wind, using the sensors that are used to monitor wind direction.
- The gearbox
Figure 2.6: Main components of a wind turbine [4]

An esqueme of the wind turbine components is shown at figure 2.6.

The wind turbine blade can be divided in three different parts: root, middle and tip, where the root part is mainly determined from structural considerations. In contrast, for the tip part the aerodynamic requirements have a higher priority compared to the structural ones.

This project is focused on the root part of the blade. This region of the wind turbine contribute a relatively small portion of the overall torque generated by the total blade because of the relatively small moment arm, the low dynamic pressure compared with the tip region and the use of thick profiles that have low aerodynamic performance [14] [15]. Moreover some structural restrictions have to be considered, taking into account the square-cube law.

It is for this reason that it is common to use thick profiles or circular section geometries at the inner part of the blade. The main problem is that these profiles have low aerodynamic performance or, in some cases, a negative contribution to the torque of the wind turbine. Consequently the flatback airfoils are developed to increase this aerodynamic performance without penalizing the structural characteristics. In fact, these type of profiles can also increase the structural properties of the blade.
2.2.1 Wind turbine operation

The final target of wind turbine aerodynamics is to produce as much torque as possible to generate power, trying at the same time to minimize the thrust loads in order to reduce out-of-plane bending and structural concerns.

The main angles and forces considered during the calculations are shown at figure 2.7

![Diagram showing forces orientations and pertinent angles at a given radial station](image)

Figure 2.7: Forces orientations and pertinent angles at a given radial station [5]

The forces that are important in a wind turbine are torque, which is parallel to the plane of rotation, and thrust, which is perpendicular to the plane of rotation. So, for a given radial station, lift and drag coefficients have to be converted into torque force, $C_Q$, and Thrust, $C_T$ coefficients using the following relations [5]:

\[
\phi = \alpha + \beta \\
C_Q = C_L \sin\phi - C_D \cos\phi \\
C_T = C_L \cos\phi + C_D \sin\phi
\]

Looking at the torque-force coefficient equation it is easy to see that the twist angle ($\beta$) at a given radial station plays a significant role. It is important particularly in the root region of the blade where twist angles are the greatest.

The output power, $P$, from a wind turbine is given by the expression:

\[
P = \frac{1}{2} C_P \rho A U^3
\]
where $\rho$ is the density of the air (at sea level is 1.225 kg/m$^3$), $A$ is the rotor swept area [m$^2$], $U$ is the wind speed [m/s] and $C_P$ is the power coefficient. The power coefficient describes that fraction of the power in the wind that may be converted by the turbine into mechanical work. There is a theoretical maximum value of 0.593 (Betz limit) and rather lower values are achieved in practice [11].

### 2.3 Flatback profile

Flatback is one of the new profile designs created to improve the properties of a wind turbine blade. It is based in a common thick profile that is modified to create a thick profile with a blunt trailing edge.

#### 2.3.1 Advantages and disadvantages

There are many studies that have investigated this type of profiles and show that blunt trailing edge profiles enhance the structural and aerodynamic properties of the blade.

They are helpful to guarantee the needed structural strength and stiffness, increasing the sectional area and the sectional moment of inertia for a given airfoil maximum thickness [14]. This is one of the reasons why flatback profiles are used in the root zone. It has to be taken into account that the structural requirements are more important at the inner part of the blade than for the sections at the outer part. There are also more structural advantages from flatback profiles; they can have more resistance to panel bucking than a common profiles and they have also a simpler structural design that is easier to be build, resulting in a blade that is easier to be transported. All these simplifications result in a reduction of the final cost.

The main aerodynamic advantage of the flatback profile is the reduction of the sensitivity of the lift characteristics of thick profiles to surface soiling, caused by the increase of the sectional maximum lift coefficient and lift curve slope [14].

The angle of attack for the inner part of the blades can be quite high, in normal operating conditions. So, it is important to have good values of $C_{l_{max}}$ and good stall characteristics in order to have good aerodynamic performance. It is proved that lift performance of thick airfoils may be significantly improved over that obtained with a sharp trailing edge, increasing the trailing edge thickness while holding the airfoil’s maximum thickness and camber constant. This modification allows that part of the pressure recovery to occur in the wake of the airfoil, reducing the adverse pressure gradient on the suction surface,
thereby delaying turbulent separation and simultaneously improving lift performance [14] [5].

However, the use of blunt trailing edge comes with penalties: as there may be issues and concerns associated with aeroacoustics, excess base drag caused by the pressure distribution in the trailing edge and produce possible vortex shedding, which are undesirable.

2.3.2 Flatback creation

There are two main methods to create flatback profiles.

• Truncation

The first method consists in cutting off a segment from the rear portion of the baseline profile. The main problems are that the modified geometry has a higher thickness and a change in the camber.

The resulting changes in the lift characteristics make it difficult to isolate the favourable effect of the blunt trailing edge from the often negative effects associated with increased thickness and loss in camber. Therefore making it difficult to consistently compare the aerodynamic performance characteristics of the resulting profiles.

The method of truncation used to create flatback profiles is shown at figure 2.8.

![Figure 2.8: Truncation method [5]](image)

• Adding thickness

The new geometry is created opening the trailing edge thickness at the same percentage towards both intrados and extrados. In other words, consists in symmetrically adding thickness to either sides of the camber line starting from a point \( \epsilon \), which is at the point of maximum thickness of the profile or behind it.

The advantage of the use of this method is the preservation of important geometric aspects of the profile like profile thickness, camber line distribution and chord line orientation. So, using this method there isn’t lift curve displacement and the effect of the blunt trailing edge becomes isolate. Moreover, varying the thickness without
a chord length change allows for a better solution for both the structural designer and the manufacturer.

At figure 2.9 are shown three profiles with the same maximum thickness but with different trailing edge-thickness-to-chord-ratio.

![Figure 2.9: Addition of symmetric thickness method [5]](image)

It is also possible to add thickness asymmetrically, this method is a little bit more difficult but is has a higher improve in the aerodynamic performance.

The adding thickness method proved to have better lift enhancement than the cutting off method because it does not reduce the mean camber and does not increase the airfoil thickness [14]. Taking into account also, that using the second method some geometric aspects do not change, the adding thickness method will be used in this project.

### 2.4 Fluid mechanics

In this section, a review of the most important concepts of fluid dynamics used during this study will be done.

#### 2.4.1 Mechanic fluid properties

The two main properties of the fluids that will be used during this project are:

- Density and specific volume:

  \[ \rho = \frac{m}{V} ; \text{[kg/m}^3\text{]} \]

  \[ v = \frac{V}{m} ; \text{[m}^3\text{/kg]} \]

- Viscosity: if a fluid flows in x direction orderly, layered and increasing the velocity in z direction, a change of the momentum between the layers tends to stop the
quick layers and tends to accelerate the slow ones. A shear stress is created. An scheme of this movement is shown at figure 2.10.

A lot of times, this stress is proportional with the velocity gradient. The proportionality constant is known as dynamic viscosity, \( \mu \):

\[
\tau = \mu \frac{\partial u}{\partial z} \quad [\text{Pa} \cdot \text{s}]
\]

Kinematic viscosity is defined as:

\[
\nu = \frac{\mu}{\rho} \quad [\text{m}^2 \text{s}^{-1}]
\]

2.4.2 Navier-Stokes equations

Turbulence is the three-dimensional unsteady random motion observed in fluids at moderate to high Reynolds numbers. As technical flows are typically based on fluids of low viscosity, almost all technical flows are turbulent. Turbulence is normally described by the Navier-Stokes equation.

This equation can be obtained from differential momentum conservation equation.

\[
\vec{f}_T = \rho \frac{\partial \vec{v}}{\partial t} + \rho (\vec{v} \nabla) \vec{v} \quad (2.1)
\]

Where \( \vec{f}_T \) is the amount of all the forces on the fluid. There are two main types of forces that affect the fluid:

- Superficial forces: this type of forces are applied at the boundary of the volume of fluid. They create normal stress (\( \theta \)) and shear stress (\( \tau \)). The stresses created from the superficial forces in a differential of volume are shown at figure 2.11.

The \( x \) component of the force due to the stresses is:
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Figure 2.11: Stress at a differential of volume of fluid created by superficial forces [7]

\[ dF_x = \frac{\partial \theta_x}{\partial x} dxdydz + \frac{\partial \tau_{yx}}{\partial x} dxdydz + \frac{\partial \tau_{zx}}{\partial x} dxdydz \]

The other components of the force follow the same structure. Now, it is possible to compute the force per unit of volume:

\[ \vec{f} = \frac{d\vec{F}}{dV} = \left( \frac{\partial \theta_x}{\partial x} + \frac{\partial \tau_{yx}}{\partial y} + \frac{\partial \tau_{zx}}{\partial z} \right) \hat{i} + \left( \frac{\partial \tau_{yx}}{\partial x} + \frac{\partial \theta_y}{\partial y} + \frac{\partial \tau_{zy}}{\partial z} \right) \hat{j} + \left( \frac{\partial \tau_{zx}}{\partial x} + \frac{\partial \tau_{yz}}{\partial y} + \frac{\partial \theta_z}{\partial z} \right) \hat{k} \]

The previous equation can be abbreviated as:

\[ \vec{f}_S = \nabla \vec{\tau} \]

Where \( \vec{\tau} \) is the stress tensor:

\[ \vec{\tau} = \begin{pmatrix} \theta_x & \tau_{xy} & \tau_{xz} \\ \tau_{yx} & \theta_y & \tau_{yz} \\ \tau_{zx} & \tau_{zy} & \theta_z \end{pmatrix} \]

- Body forces: they are produced by force fields (gravitational, electromagnetic...).

The most common body force is the gravitational one, and this is the force that will be considered in this project:

\[ \vec{f}_g = \rho \vec{g} \]

To sum up, the amount of the forces on the fluid, \( \vec{f}_T \) is the addition of gravitational forces and friction forces:
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\[ \vec{f}_T = \rho \vec{g} + \vec{\nabla} \vec{\tau} \]

Finally, the differential momentum conservation equation 2.1, yields:

\[ \rho \vec{g} + \vec{\nabla} \vec{\tau} = \rho \frac{\partial \vec{v}}{\partial t} + \rho (\vec{v} \vec{\nabla}) \vec{v} \]

However, the stress tensor could be divided in two components; the isotopic part and the anisotropic part, respectively:

\[ \vec{\tau} = -pI + \vec{\tau}' \]

The last term of this equation, for newtonian flows, is related with the symmetric part of the velocity divergence, as showed at 2.2.

\[ \vec{\tau}' = 2\mu[\vec{\nabla} v^S - \frac{1}{3}(\vec{\nabla} v)I] \quad (2.2) \]

Substituting in the momentum conservation equation, the Navier-Stokes equation is obtained [19]:

\[ \rho \frac{\partial \vec{v}}{\partial t} + \rho (\vec{v} \vec{\nabla}) \vec{v} = \rho \vec{g} - \vec{\nabla} p + \vec{\nabla}\{2\mu[\vec{\nabla} v^S - \frac{1}{3}(\vec{\nabla} v)I]\} \]

For a incompressible flow with constant viscosity, Navier-Stokes equation can be simplified as:

\[ \rho \frac{\partial \vec{v}}{\partial t} + \rho (\vec{v} \vec{\nabla}) \vec{v} = \rho \vec{g} - \vec{\nabla} p + \mu \vec{\nabla}^2 \vec{v} \]

This equation has four unknown variables; the pressure and the 3 components of the velocity vector. So, another equation is needed in order to have four equations and four unknown variables, so that the system can be solved. The used equation is continuity equation, also known as conservation of mass, which for a single phase problem is:

\[ \frac{\partial \rho}{\partial t} + \nabla (\rho \vec{v}) = 0 \quad (2.3) \]
2.4.3 Reynolds number

The measure of the non-linearity of Navier-Stokes equation is given by the Reynolds number, which is defined as:

\[ Re = \frac{\rho UD}{\mu} = \frac{UD}{\nu} \]

Where \( \rho \) is the density \([\text{kg}/\text{m}^3]\), \( U \) the characteristic velocity of the flow \([\text{m}/\text{s}]\), \( D \) the characteristic length of the problem \([\text{m}]\), \( \mu \) the dynamic viscosity of the flow \([\text{kg}/\text{m} \cdot \text{s}]\) and \( \nu \) the kinematic viscosity of the flow \([\text{m}^2/\text{s}]\).

It is a non-dimensional number that estimates the relative weight between the convective terms \( ((\vec{v} \cdot \nabla) \vec{v}) \) and the viscous terms \( (\nu \Delta u) \) of the Navier-Stokes equations. It is an indicator of the transition between laminar and turbulent flow, which occurs when \( Re \) reaches a critical value.

Reynolds number is used to compare two different experiments with different characteristic parameters during the numerical simulation of a problem. On the first place, it is important to validate the results of the simulation in order to verify that all the parameters of the simulation are correct. The validation is performed by comparing the numerical results with experimental data. The most significant parameter in this kind of flow is the Reynolds number, if the Reynolds number is the same both results can be compared. The experiment was performed in such conditions that the Reynolds number was \( 3 \cdot 10^6 \). So, the Reynolds number of the simulations needs to be the same. Then considering that the Reynolds number is \( Re = \frac{\rho UD}{\mu} = 3 \cdot 10^6 \): \( U=1 \text{ m/s}, D=1 \text{ m}, \rho = 1 \text{ kg/m}^3 \) and \( \mu = 3.333 \cdot 10^{-7} \text{kg/m} \cdot \text{s} \). The values of \( U, D \) and \( \rho \) are 1 for simplicity reasons and the dynamic viscosity is then fixed. Even though those values do not correspond to real values of air properties they are correct given that the important parameter is the Reynolds number as said before.

2.4.4 RANS models

While turbulence is, in principle, described by the Navier-Stokes equations, it is not feasible in most situations to resolve the wide range of scales in time and space by Direct Numerical Simulation (DNS) as the CPU requirements would by far exceed the available computing power for any foreseeable future. For this reason, averaging procedures have to be applied to the Navier-Stokes equations to filter out all, or at least, parts of the turbulent spectrum. The most widely applied averaging procedure is Reynolds-averaging (which, for all practical purposes is time-averaging) of the equations, resulting in
the Reynolds- Averaged Navier-Stokes (RANS) equations. By this process, all turbulent structures are eliminated from the flow and a smooth variation of the averaged velocity and pressure fields can be obtained.

The fundamental idea is that each magnitude is divided in mean magnitude and fluctuations of the magnitude, for a magnitude $\phi$: $\phi = \bar{\phi} + \phi'$.

Using this fundamental idea at Navier-Stokes equations the new averaged equation is (for simplicity purposes only x component is showed) [8]:

$$\rho \left[ \frac{\partial \bar{v}_x}{\partial t} + \bar{v}_x \frac{\partial \bar{v}_x}{\partial x} + \bar{v}_y \frac{\partial \bar{v}_x}{\partial y} + \bar{v}_z \frac{\partial \bar{v}_x}{\partial z} \right] = -\frac{\partial \bar{p}}{\partial x} + \frac{\partial}{\partial x} \left( \tau_{xx} - \rho \bar{v}_x' \bar{v}_x' \right) + \frac{\partial}{\partial y} \left( \tau_{xy} - \rho \bar{v}_y \bar{v}_x' \right) + \frac{\partial}{\partial z} \left( \tau_{xz} - \rho \bar{v}_z \bar{v}_x' \right)$$

The Navier-Stokes equations are the same except for the terms $-\rho \bar{v}_i' \bar{v}_j'$. These terms are responsible for the dissipation caused by fluctuations and form the turbulent stress tensor or Reynolds tensor:

$$\tau_{ij} = -\rho \bar{v}_i' \bar{v}_j'$$

The value of this tensor is not known but, Prandtl developed the concept of turbulent viscosity, $\mu_t$:

$$\tau_{ij} \approx \mu_t \frac{\partial \bar{v}_i}{\partial x_j}$$

But $\mu_t$ is still unknown. He also defines this variable with the model known as mixing length model.

$$\mu_t \approx \rho \ell^2 \frac{\partial \bar{v}_i}{\partial x_j}$$

The mixing length, $\ell$, depends on the problem that is being solved.

### 2.4.5 Turbulence model

Reynolds- Averaged Navier-Stokes (RANS) equations are very useful, eliminating turbulent structures from the flow and obtaining average values of the important parameters like pressure and velocity. However, the averaging process introduces additional unknown terms into the transport equations (Reynolds Stresses and Fluxes) that need to be provided by suitable turbulence models (turbulence closures).
Chapter 2. Development

The choice of turbulence model will depend on considerations such as the physics of the flow, the established practice for a specific class of problem, the level of accuracy required, the available computational resources, and the amount of time available for the simulation.

Shear stress transport (SST) k-ω model has been chosen to do the simulation of this project.

K-ω models are typically better in predicting adverse pressure gradient boundary layer flows and separation. The drawback of the standard k-ω equation is a relatively strong sensitivity of the solution depending on the freestream values of k and ω outside the shear layer.

It is for this reason that a SST k-ω model has been chosen, this model has been designed to avoid the freestream sensitivity of the standard k-ω model, by combining elements of the ω-equation and the ε-equation. In addition, the SST model has been calibrated to accurately compute flow separation from smooth surfaces.

The constants that this model need are k and ω, they are defined as follows:

Turbulent kinetic energy: \( k = 1.5(UI)^2 = 1.5 \cdot 10^{-6} \) [\( m^2/s^2 \)]

Specific dissipation rate: \( \omega = \rho k \left( \frac{\mu_t}{\mu} \right)^{-1} = 0.45 \) [\( 1/s \)]

Where, U is the mean flow velocity (1 m/s), I is the turbulence intensity, a reasonable value of this parameter is 0.1%, considering the problem in study. Focusing on Specific dissipation rate, \( \rho \) is the density on the air (1 kg/m³), k is the turbulent kinetic energy previously calculated, \( \mu \) is the dynamic viscosity (3.333 \( \cdot 10^{-7} \) kg/ms) and the fraction \( \mu_t/\mu \) is known as turbulent viscosity ratio and its value could be approximated as 10 [18].

### 2.4.6 Wall law and turbulent boundary layer

Turbulence problems are very difficult to solve, a case relatively easier is the study of the turbulence near of the wall. In this area the velocity of the flow tends softly to the velocity of the solid, it is known as boundary layer. The boundary layer thickness is defined as the distance from the wall at which the velocity is 0.99U, considering U the velocity of the flow far from the wall. This distance is defined as \( \delta \) at figure 2.12.

It is also possible to see in figure 2.12 the tangential stress in the wall (\( \tau_p \)). The expression \( v_z^+ = F(y^+) \) is known as the wall law, it is defined by two dimensionless groups [8]:

\[
\begin{align*}
 v_z^+ &= \frac{v_z}{v^+} \\
 y^+ &= \frac{\rho v^+ y}{\mu}
\end{align*}
\]
where, \( v^* \) is known as friction velocity but, even though it has velocity units it is not a real velocity. It is defined as:

\[
    v^* = \frac{\tau}{\rho}
\]

Focusing in the numerical study, \( y^+ \) is a non-dimensional distance from the wall to the first mesh node. It is important to ensure that this first node is not outside of the boundary layer region. If it happens the mesh of our problem do not have enough quality to compute the boundary layer behaviour, so the results may be incorrect.

\( y^+ \) can reach different values, and depending on them the numerical simulation will be done using different methods. These procedures will be explained at section 4.3 Simulation, where all the parameters of the simulation will be determined.
Chapter 3

Original profile and transformation

3.1 Reference Aerodynamic Profile

The reference profile that has been chosen to do the aerodynamic optimisation is a representation of the common profiles used at the inner part of the blades. This flatback profile is used, exactly, at the first 20% of the length of the blade as seen at 2.3 and 2.4 and it has a maximum thickness ratio about 40% (t/c = 0.4).

As have been said before, this project consists on an optimisation that starts from another study of another project [9]. This project was made for Efrain Sotelo Ferry, at 2014 and the director is the same than in this project. It is for this reason that this project continues with the previous work but, taking into account another parameters and trying to improve a little bit more the aerodynamic performance of the profiles chosen.

The initial common profile, from which starts the optimisation of the first work, belongs to one of the most famous families of study, Delft University of Technology, its main characteristics are explained at table 3.1 and an scheme of its shape is shown at figure 3.1.

<table>
<thead>
<tr>
<th>Airfoil</th>
<th>Designer</th>
<th>Maximum thickness ratio (t/c)</th>
</tr>
</thead>
<tbody>
<tr>
<td>DU00-W2-401</td>
<td>Delft University</td>
<td>0.4</td>
</tr>
</tbody>
</table>

**Table 3.1:** Initial profile’s characteristics.

As a continuation of the aerodynamic optimisation of the previous study [9], this one has input data that are the final results form the other project.
Exactly, from the conclusions is extracted that torque-force coefficient has been improved about 21% transforming the original profile DU00-W2-401 to a flatback profile with a thickness at the trailing edge of TE=14%. So, the reference profile of this project is a flatback profile from DU00-W2-401 with a trailing edge thickness of TE=14%. An example of these reference profile is shown at 3.2.

3.2 Profile Transformations

3.2.1 Changes on the trailing edge opening

The method used to transform the original profile to flatback consists in adding thickness symmetrically to either sides of the camber line. As has been said before this method is more useful to compare some profiles and it is also proved that this method has a better lift enhancement than the cutting off one.

The equation used to transform the profile is the same used at the previous project [9] in order to continue the same optimisation. This equation satisfies some general rules that are used to create flatback profiles; the addition of thickness has to be done after the point of maximum thickness in order to make sure that the thickness ratio does not change, it is also important to add the thickness symmetrically to achieve that the
Chapter 3. *Original profile and transformation*

camber line does not change and the distribution of thickness should be soft in order to avoid adverse effects on the boundary layer.

This equation is defined as:

\[
\bar{y}_{fb} = \bar{y}_{or} \pm \frac{TE/100}{2} a(\bar{x})
\]

where:

\(\bar{y}_{fb}\) = y coordinate of flatback profile (non-dimensional)

\(\bar{y}_{or}\) = y coordinate of original profile (non-dimensional)

TE = Trailing edge thickness with respect to the chord (%)

\(a(\bar{x})\) = Distribution factor (non-dimensional)

The equation that governs the distribution factor is also the same than in the previous project:

\[
a(\bar{x}) = A(\bar{x} - B)^n + C
\]

The distribution factor is characterised by three constants (A, B, and C) that have to be computed using the boundary conditions, which enable to accomplish the general rules creating a soft thickness distribution. Other parameters that have to be considered are; the point where the addition of thickness starts and the thickness at the trailing edge. Actually, these are the boundary conditions that have to be considered to compute the constants.

The main difference between the two projects remains in the boundary conditions. Whereas the soft transition remains constant, the point where the addition of thickness starts is changed. The previous study considered that the point where the addition of thickness starts was the point of maximum thickness. This study will consider different variations of the same profile, by changing the point where the addition of thickness starts (point \(\epsilon\)) and the resulting aerodynamic performances of each case will be compared. This variations are chosen because there is not much information about the changes that this parameter causes at the aerodynamic performance.

Specifically, four different variations of each profile will be created. The start thickness point will be located at: the point of maximum thickness, 0.4c, 0.5c and 0.6c.

Considering all the boundary conditions it is possible to write these equations:
Chapter 3. *Original profile and transformation*

\[
\bar{x} = \epsilon \rightarrow a = 0 \\
\bar{x} = 1 \rightarrow a = 1 \\
\left. \frac{da}{d\bar{x}} \right|_\epsilon = An(\bar{x} - B)^{(n-1)} + C = 0
\]

It is also important to define the exponent’s value, \( n \). It has been proved that the value that produce the softest variation on the thickness is \( n=0.5 \) [9].

Finally, the constants are computed as:

\[
A = \frac{1}{(1-B)^{n-1} - n(\epsilon-B)^{n-1}} \\
B = \epsilon(1 - n) \\
C = 1 - A(1 - B)^n
\]

To sum up, the value of the constants for each variation on the profile is outlined at table 3.2. A sketch of the 4 variations for the profile is also shown at figure 3.3 (DU00-W2-401).

<table>
<thead>
<tr>
<th>( \epsilon )</th>
<th>A</th>
<th>B</th>
<th>C</th>
</tr>
</thead>
<tbody>
<tr>
<td>max.thickness</td>
<td>-2.71</td>
<td>0.15</td>
<td>3.498</td>
</tr>
<tr>
<td>0.4</td>
<td>-4.47</td>
<td>0.20</td>
<td>5.000</td>
</tr>
<tr>
<td>0.5</td>
<td>-7.46</td>
<td>0.25</td>
<td>7.460</td>
</tr>
<tr>
<td>0.6</td>
<td>-13.12</td>
<td>0.30</td>
<td>11.978</td>
</tr>
</tbody>
</table>

*Table 3.2: Constant values for each variation.*

*Figure 3.3: Variations of the point of addition of thickness for DU00-W2-401.*
3.2.2 Changes on the curvature

The other changes done at the profile are variations on the curvature. This changes have been done with the aim to improve the aerodynamic performance: it is known that if the profile has more curvature the lift coefficient increases in general in the linear part. On the other hand, exists the risk that a high curvature causes an earlier separation damaging lift and drag curves. So, the changes will increase the positive curvature of the profile in order to increase the lift coefficient but trying to remain constant the drag coefficient, obtaining an increase of efficiency and torque coefficient.

The curvature of the initial profile is shown at figure 3.4.a. It can be observed that there are three different parts; at the front and at the rear part positive curvature whereas at the middle part negative one. At first, the profile will be transformed to another one with zero curvature but maintaining the thickness at each point of the chord. This transformation is shown at figure 3.4.b.

Exactly, two variations have been done to understand the behaviour of the profile with different types of curvature and trying to improve the aerodynamic performance of the initial profile. They are explained below:

- Positive curvature for all the profile: this profiles has a positive curvature with the point of maximum curvature at 50% of the chord and with a maximum value of 0.02c. At figure 6.7 a superposition between the profile with zero curvature (red) and the new profile with positive curvature (blue) is shown.

- Accentuation on the positive curvature of the profile: this profile has the same scheme on the curvature than the reference profile but with a change in the parts of positive curvature. Exactly, the maximum value of the positive curvature has been incremented, producing a larger positive curvature. The superposition between the profile with zero curvature (red) and the profile with accentuated positive curvature (blue) is shown at figure 6.8.
Figure 3.5: Superposition between zero curvature profile (red) and all positive curvature profile (blue)

Figure 3.6: Superposition between zero curvature profile (red) and accentuated positive curvature profile (blue)
Chapter 4

Computational study

4.1 Design

The flatback profile that has been studied in this project is created using the method of adding thickness to original common profiles. The original common profile used is DU00-W2-401.

The software that has been chosen to compute the design of the flatback profiles is Excel. Taking into account that the aeronautic profiles are defined by a set of coordinates, two different columns have been done: one for the coordinates of the upper surface and another one for the coordinates of the lower surface.

Then, the transformation of the profile could be done. Actually, the changes done in the profile are at $y$ coordinates, using the equation with the plus sign, 4.1, in the column of the upper surface and the equation with the minus sign, 4.2, in the column of the lower surface.

\[
\bar{y}^{fb} = \bar{y}^{or} + \frac{TE}{100} \frac{2}{a(\bar{x})}
\]  

\[
\bar{y}^{fb} = \bar{y}^{or} - \frac{TE}{100} \frac{2}{a(\bar{x})}
\]

The values of the constants of the equations depend on the point where starts the addition of thickness and on the thickness at the trailing edge. They are explained and computed at section 3.2 Profile transformation.

Finally, the coordinates of the new flatback profiles need to be saved as a Text document, specifying three columns for the three coordinates that define each point of the profile: $x$, $\bar{y}^{or}$, and $\bar{y}^{fb}$. 

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y and z. In fact, z coordinates will be all zero, taking into account that a 2D configuration is studied.

### 4.2 Meshing

The mesh is maybe the most important part of the project. A lot of different parameters need to be taken into account to have a good mesh like the precision of the results, the computing power available, the areas of the design that need more precision, etc.

At first, it is important to know what a mesh is, in order to know its most important parameters. The computational fluid dynamics is based on distretization of the physical domain into extremely small volumes where the equations that govern the problem are locally solved. These small volumes are known as cells and the amount of all of these cells is the mesh. Knowing that, it is easy to see that the quality of the mesh is directly related with the result of the problem, so it is very important to have a high quality mesh in order to get good results.

The properties of each cell are assumed constant inside it. So, it is easy to understand that the bigger the cell is, the less precision there is. For this reason the high quality meshes have very small cells. Despite of this fact, it is important to considerate the time used to do the simulation. If the mesh is very fine, a lot of equations will be solved and this needs time and has computing costs. So, a balance between the precision and the time and costs will be done in this project in order to have precision enough but do not spend too time doing the simulations.

There are three main types of meshes:

- **Structured meshes**: they have regular cells, there is always the same number of cells at the vertexes and each cell has a fix number of sides.

- **Unstructured meshes**: they are connected arbitrarily, the cells do not have the same number of sides. This requires an additional storage cost, considering that the programme needs to know the configuration of each cell during all the process.

- **Hybrid meshes**: they are the combination of the two previous types.

A hybrid mesh will be used in this project because the unstructured mesh fits better with the angulate zone of the trailing edge of the profile and the structured mesh is useful at the boundary layer.

The programme used to do the mesh is Meshing, from ANSYS.
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At first, the area around the profile will be divided in different zones in order to define the different types of mesh and its quality. Then, the characteristics of each region will be defined and the mesh will be created. It is important to prove that this mesh accomplishes all the requirements and fits with the profile. Finally, the zones where the boundary conditions will be introduced have to be defined. All this procedure is explained in more detail in the following sections.

### 4.2.1 Zones division

The area around the profile is divided into 15 different zones in order to define in more detail the parameters of the mesh, especially at the sensible zones around the profile, like the boundary layer of the turbulent wake. A scheme of these zones is shown at figure 4.1.

![Figure 4.1: Zones distribution around the profile](image)

There are six regions around the profile located at the part of the boundary layer. In fact, these regions need to be larger than the real boundary layer in order to let its expansion without any restriction. Three more zones can be observed after the trailing edge of the profile, they are located at the turbulent wake.

These nine areas are maybe the most interesting ones due to the fact that these are the zones where the profile in study interacts with the fluid around it. For this reason, it is very important to create a mesh with a high density in these zones, in order to be able to compute the boundary layer’s behaviour and the turbulences created at the wake.

However, the computational domain is about 120 times the chord length of the profile (L=1m). At the real world the domain around the profile is the atmosphere, but shape and size need to be determined in order to simulate the profile using CFD. In this study,
the shape chosen is a circumference because it is used to study the profiles fitting well with them, and the size is 120m to ensure BL is not affected by farfield.

Another circumference is created at the surface. This circumference has 6m of diameter and defines the unstructured zone of the mesh. This zone extends from the boundary layer to 3m of radius around the profile in order to avoid obliquity problems in the mesh.

4.2.2 Final mesh

As mentioned above, Meshing has been the software used for the mesh design. This programme allows defining the parameters of the mesh at each region.

The mesh around the profile is divided in two types:

- Structured mesh: comprising boundary layer, turbulent wake and the outer part of the mesh (from radius 3m to 60m). It has quadrilateral cells that are very efficient in terms of memory space and they also have better convergence than triangles.

- Unstructured mesh: which extends from the boundary layer to the circumference of 3m of radius. These cells have triangular shape and the main function of this zone is to avoid obliquity problems.

These two types of mesh could be observed at figure 4.2.

![Figure 4.2: Mesh around the profile](image)

At figure 4.3 a detail of the mesh at the inner part is shown. At the boundary layer there is a mesh with a major density of cells at the contact part between the flow at the profile, and with larger cells at the extreme of the boundary layer.
A structured mesh is recommended in the perpendicular direction of the profile’s perimeter [18]. It is needed that the mesh extends always all around the boundary layer. Moreover, more than 15 cells need to be inside the boundary layer in order to guarantee better results with the advanced models of turbulence like k-ω SST than with other common methods. A brief explanation of this methods will be done at section 4.3 Simulation.

The mesh is divided in 1500 edges all over the tangential direction of the profile, 750 divisions for the upper surface and 750 more for the lower surface. Focusing of the radial direction, the boundary layer has 50 divisions with smaller cells at the inner part and larger ones at the outer part. This principle is also applied at the turbulent wake, having smaller cells at the zone behind the trailing edge and a growth to the extremes.

Finally, figure 4.4 shows a total view of the mesh done.

The final mesh has approximately 420000 cells, with small variations depending on each profile. In this project the study of the sensibility of the mesh have not been done, but considering that the mesh is created with the same parameters than the previous
project [9], the same study of sensibility can be used. In the thesis by Sotelo [9] the number of cells of the mesh chosen at the study of sensibility is lower than the cells of this project. It is for this reason that can be affirmed that the mesh is good enough to give good results. However, this mesh could be improved reducing a little bit the number of cells, in order to reduce the computing cost.

### 4.2.2.1 Important parameters of the mesh

The quality of the mesh plays a significant role in the accuracy and stability of the numerical computation, it is for this reason that some indicators are needed to check the quality of the mesh used.

One of the most important indicators that ANSYS Fluent allows to check is the orthogonal quality. This parameter measures the distortion of the cell, in other words, it considers if the cells have orthogonal angles or not. Therefore, the worst cells will have an orthogonal quality closer to 0 and the best cells will have an orthogonal quality closer to 1. The minimum orthogonal quality for all types of cells should be more than 0.01, with an average value that is significantly higher [18]. This parameter reaches a value about 0.19 at the meshes used.

Another important indicator is the aspect ratio. It is a measure of the stretching of a cell. Generally, it is best to avoid sudden and large changes in cell aspect ratios in areas where the flow field exhibit large changes or strong gradients. This indicator must be less than 100, considering that the program warns you if this happens. The aspect ratio of the meshes used is about 24.03, this value is very far from the limit of 100.

It is also important to consider the skewness inside the cell quality. This parameter is defined as the difference between the shape of the cell and the shape of an equilateral cell of equivalent volume. Highly skewed cells can decrease accuracy and destabilize the solution. A general rule is that the maximum skewness for a triangular/tetrahedral mesh (which is the case of the mesh of this project) should be kept below 0.95, with an average value that is significantly lower [18].

### 4.2.3 Zones to determine the boundary conditions

It is important to define different parts of the geometry for the boundary conditions that must be set later, in Fluent.

The external edges of the regions around the profile are used to define the boundary conditions. These edges create a circumference with a 120 chords of diameter. Exactly,
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the external part of the biggest circle is divided in two parts: the inlet zone is defined as a half of the circumference and a little bit more and the rest of the circumference is defined as the outlet area.

It is also needed to define the edge of the profile because is the part where the fluid interacts with the solid. A scheme of these parts is shown at figure 4.5.

![Figure 4.5: Zones where the boundary conditions are defined](image)

### 4.3 Simulation

The numerical simulation has been performed with ANSYS Fluent software. This program computes the flow properties by solving a set of equations on each mesh node. The equations solved by Fluent are conservation of mass (2.3) and momentum conservation (2.1) while energy equation is not used in this study because it computes parameters that are not relevant. Transport equations are also used for a turbulent flow.

As in the previous project [9], this study is bidimensional (planar). There are two main types of numerical solver; pressure-based and density-based. Density-based solver uses the continuity equation to obtain the density and the equation of state to obtain the pressure field. In contrast, pressure-based compute the pressure field using pressure equation or a combination of continuity and momentum equations. The chosen solver is *Pressure-Based*, given that this solver is conceived for low-speed incompressible flows, and this is the behavior of wind turbines.

Apart from that, time dependence of the problem must be considered. The Reynolds that characterise the problem is $3 \cdot 10^6$, for this reason it could be considered a turbulent problem. At first, a steady state study was considered. However, another method had
been used regarding the slow convergence rate obtained due to the fact that a steady state study is not the best method to solve a turbulent problem. The first step is solving the problem using steady state study. If it converges the solution is computed, if the residuals keep oscillating without converge an unsteady study is started. The initial values of the unsteady study are obtained from the steady state, this fact lets obtain the solution more quickly and taking advantage of the results computed at the previous state.

In the unsteady simulation the variables change over time. The time is discretized into time steps, and the solutions of the equations are computed for each time step. It is important to set a correct order of magnitude of the time step for the simulation in order to get good convergence rates.

The indicators of the convergence are the residuals; the problem is converged when they are smaller than a value defined by the user. After an iteration of the numerical process the difference of the values of the equations is compared between the result found and the previous result. This difference is called residual and it is what has to be smaller than a fixed value in order to make sure that the solution is correct.

The turbulence model that fits better with the simulations of the project is SST K-ω because it is good predicting adverse pressure gradient boundary layers flows and separation and the solution is not sensible at free stream values. The fluid around the profiles is air, which has constant properties that depend on Reynolds number. The Reynolds number must be the same than in the experimental study (Re =3·10^6) in order to characterize the real conditions, so fixing chord (c = 1m), density (ρ = 1Kg/m^3) and flow velocity (U = 1 m/s) the dynamic viscosity is computed as $\mu = \frac{\rho U c}{Re} = 3,333 \cdot 10^{-7}$ kg/m · s .

Two different procedures can be followed depending on the value of the $y^+$. If $y^+$ is approximately 1, low Reynolds corrections must be selected in the section of the viscous turbulent model whereas wall functions are not used. However, if the value of $y^+$ is near to 50 wall functions must be used instead of low Reynolds corrections. In this project, $y^+$ is of the order of 1, slightly changing depending on the mesh. So, low Reynolds corrections are selected.

To characterize the problem, the boundary conditions must be fixed. The airfoil is defined as a viscous wall, choosing the condition no slip. The inlet surface is defined using the velocity of the flow, which has a module of 1m/s and the direction changes depending on the angle of attack. The outlet surface is defined with the pressure. This surface is located at a distance of 60 times the chord of the profile, for this reason it is assumed that the pressure at this area is not affected by the profile, so it is the ambient
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pressure. In this step the characteristic constants of the model of turbulence are defined. Their values are computed at section 2.4.5 Turbulence model.

The method used to find the solution is *Coupled*. This coupled algorithm solves the momentum and pressure-based continuity equations together. The coupled scheme uses a robust and single phase implementation for steady-state flows, with better performance than the segregated solution schemes. The steps of this algorithm are illustrated at figure 4.6. It is also important to activate *High Order Term Relaxation*, this option improves the stability and the convergence of the solution.

![Figure 4.6: Scheme of the pressure-based coupled algorithm [10]](image)

The main parameters of the simulation are summarized at table 4.1.

<table>
<thead>
<tr>
<th>Solver type</th>
<th>Pressure-Based</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time</td>
<td>Steady-Transient</td>
</tr>
<tr>
<td>Dimension</td>
<td>2D</td>
</tr>
<tr>
<td>Turbulence model</td>
<td>Viscous SST $k$-$\omega$</td>
</tr>
<tr>
<td>Material</td>
<td>Air</td>
</tr>
<tr>
<td>Boundary conditions</td>
<td>Inlet Velocity-Inlet (Flow velocity) 1 m/s</td>
</tr>
<tr>
<td></td>
<td>Outlet Pressure-Outlet (gauge Pressure) 0 Pa</td>
</tr>
<tr>
<td>Solution Method</td>
<td>Coupled</td>
</tr>
<tr>
<td>Spatial Discretisation</td>
<td>First Order Upwind</td>
</tr>
<tr>
<td>Monitors</td>
<td>Residuals 0.0001</td>
</tr>
<tr>
<td>Time Step</td>
<td>Size 0.01 s</td>
</tr>
<tr>
<td></td>
<td>Max iterations/time step 20</td>
</tr>
</tbody>
</table>

*Table 4.1: Main parameters of the simulation.*
Chapter 5

Profiles validation

At this point, the mesh is done and the parameters that characterize the fluid and the method of resolution are defined at Fluent ANSYS. Now, it is important to verify that the hypothesis assumed to define Fluent parameters are correct. It is also needed to make sure that the mesh has reasonable quality; enough quality to compute turbulence and separation of the boundary layer but, at the same time, considering that the finer the mesh is, higher is the time needed to perform the numerical analysis. If any of the previous requirements is not accomplished some parameters need to be changed.

The verification consists in compare the results obtained by means of the simulation with the values obtained in an experimental study. Exactly, the dates that are compared in this chapter are the variation of the $C_d$ and $C_l$ respect to the angle of attack, and the relation between $C_l$ and $C_d$, also known as polar curve. These dates are used because they are the known values from the experimental study. In order to be able to compare both values, experimental and simulated ones, the Reynolds number in both analyses needs to be the same. The experimental studies were done with a Reynolds number $Re=3\cdot10^6$, so this value is imposed at the numerical analysis. Two different profiles will be validated; NACA0012 and DU00-W2-401.

5.1 Validation of NACA 0012

At first, a thin and well documented profile was proved. The aim of this first validation is to prove that the mesh has good quality, it is for this reason that a thin profile is chosen; to make sure that there is no separation of the boundary layer for small angles of attack, thus avoid the problems caused by this turbulent flow. The profile validated is NACA0012, which is shown at figure 5.1.
This is a very common profile, there are a lot of studies and documents about it and this is a good point because there are a lot of resources where the results can be validated. Moreover this profile is a good choice because it is symmetric, so the $C_l$ must be zero for an angle of attack $\alpha = 0 rad$. The comparison between the experimental values and the results of the simulation is shown at figures 5.2 and 5.3.
Chapter 5. Profiles validation

As for the polar curve, an important difference can be observed. The simulation results are higher than the experimental values and in this case this difference cannot be neglected. This difference is caused by the hypothesis assumed in the Fluent parameters. In the experimental analysis the flow is laminar during most part of the profile, while in Fluent a turbulent boundary layer is considered for the whole length of the profile. This are the reason that causes the increase of the $C_d$. It is important to take into account that the parameters have been chosen to fit with thick profiles, that are the profiles in study.

5.2 Validation of DU00-W2-401

The other profile validated is DU00-W2-401. It is the initial reference profile, used to create the flatback profiles. The target of this validation is to prove that the mesh and the Fluent parameters are also acceptable for thick profiles and that they also enable the solver to correctly compute turbulence and the separation of the boundary layer. A draft of the profile shape is shown at figure 5.4.

![Figure 5.4: Draft of the thick profile validated. DU00-W2-401](image)

Two different tests have been done to validate the parameters used. The first one is shown at figures 5.5 and 5.7 with a red curve whereas the second one has blue color.

Focusing on the relation between $C_l$ and angle of attack, figure 5.5, $C_l$ of the first test is very similar in the two first points of the graphic, 0 and 5 degrees, creating an almost horizontal line between both points. From the second point the graphic has a good behaviour, with a slope similar to the experimental one. However, all the curve is moved to the right with respect to the experimental curve.

The slope of the second test is almost constant and with the same tendency than the experimental curve. Up to ten degrees the points are aligned but the curve is also moved
Chapter 5. Profiles validation

Figure 5.5: Comparison between experimental values and simulation results, for a DU00-W2-401. Cl vs. angle of attack

to the right. However, the difference with respect to the experimental data is not as big as in the first test.

This difference in the lineal zone could be caused by the separation that appears at the lower surface for small angles of attack. The profile DU00-W2-401 was created to be used in wind turbines that operate with angles of attack between 8 and 16 degrees. It is for this reason that the profile has good efficiency at high angles of attack and that the flow is separated at low angles. This separation causes poor precision at the lineal zone.

Figure 5.6 shows the velocity distribution around the profile. A blue zone can be observed at the lower surface of the profile, this zone is the separated one.

Figure 5.6: Draft of the velocity distribution around the profile for an angle of attack of 0 degrees.

The validation of the $C_d$ with respect the angle of attack has better results than the graphic that relates $C_l$ with angle of attack. For the first test the $C_d$ at 20° do not reach the experimental value, having a maximum value of 0.17 whereas the experimental one is 0.27. This big difference evidence that a change on the properties or in the mesh was needed.
Chapter 5. Profiles validation

Figure 5.7: Comparison between experimental values and simulation results, for a DU00-W2-401. Cd vs. angle of attack

The changes done between test one and two are the follows:

- Reduction on the size of the cells near the profile, reducing the value of $y^+$ to a value near to 1.
- Selection of Low Re corrections at viscous turbulent model.
- Change on the computation of the specific dissipation rate, changing it to $\omega = 0.45$ (This change can be done because the turbulent viscosity ratio varies between 1 and 10, this values depends on the problem solved).

The simulations for all the flatback profiles are performed using the second test configuration, so all the procedure explained during the project is referred to the configuration of the parameters of the second test.
Chapter 6

Results

In this section the results of the numerical simulation are presented. At first, a brief review of the used profiles is done. Then, the results are schemed using graphs and tables.

6.1 Study of the changes at the point where the addition of thickness starts

6.1.1 Geometry

The geometries of the profiles studied in this section are flatback profiles created from profile DU00-W2-401. A draft of their shape is shown at figure 6.1. The difference between the profiles is low, it is for this reason that they are shown at the same figure, to be able to observe the difference between them.

Figure 6.1: Shapes of the profiles simulated.
Chapter 6. Results

The parameter that changes between the profiles is the point where the addition of thickness that creates the flatback profile starts. For simplicity and clarity purposes, each profile is called as follows and has a characteristic colour:

- Closed: reference profile DU00-W2-401. Before to create the flatback profile and studied using Fluent. Colour: grey
- Experimental: reference profile DU00-W2-401. Before to create the flatback profile and experimentally studied. Colour: green
- MAX: profile where the addition of thickness starts at the point of maximum thickness (approximately at 30% of the chord). Colour: blue
- 0.4c: profile where the addition of thickness starts at the 40% of the chord. Colour: red
- 0.5c: profile where the addition of thickness starts at the 50% of the chord. Colour: purple
- 0.6c: profile where the addition of thickness starts at the 60% of the chord. Colour: light blue

6.1.2 Results

For wind turbine applications, there are important parameters to consider when comparing the performance of different profiles. The most important one is the coefficient of torque, that produces the movement of the blade, it is also important the efficiency of the profile that relates lift and drag coefficients. They are also important in order to see the behaviour of the different profiles. Exactly, a high value on the lift coefficient is really important at the root zone, where flatback profiles are used, in order to create a high torque without any penalisation at the bending moment generated at the inner part of the blade. Comparing the results of flatback profiles with the numerical and experimental values of the closed profile, different behaviours can be observed.

Starting with the relation between lift coefficient and angle of attack, figure 6.2. Flatback profiles have higher values of $C_l$ during all the performance. The maximum value of the $C_l$ is reached later than for the experimental closed profile; this last profile reaches the maximum $C_l$ at about 8 degrees while the flatback profiles have the maximum later, at about 15 degrees. This behaviour could be caused by the software, considering that the simulated closed profile also has a higher stall angle of attack than the experimental closed profile.
Chapter 6. Results

Figure 6.2: Comparison between experimental values and simulation results, for a DU00-W2-401. Cl vs. angle of attack.

It is important to notice also that for the experimental closed profile, the $C_l$ remains almost constant from 10 to 20 degrees whereas for flatback profiles, the $C_l$ increases to the maximum value and then decreases. The maximum $C_l$ for flatback profiles is reached at 15 degrees and has a value about two times higher than the closed profile.

Figure 6.3: Comparison between experimental values and simulation results, for a DU00-W2-401. Cd vs. angle of attack.

Focusing on the relation between drag coefficient and angle of attack, figure 6.3, the tendency of all the profiles is very similar, having an almost horizontal part from 0 to 10 degrees and a growth from 10 to 20 degrees. It is important to pay attention that there
is not a relevant change between the behaviour of closed profiles and flatback profiles, in terms of $C_d$. Despite of this similitude, there are two main differences: the maximum $C_d$ is higher for flatback profiles than for the simulated closed profile and the $C_{d0}$ of the simulated profiles is higher than for the experimental one. This increase on the $C_d$ for zero angle of attack could be caused by the fact that the program considers that there is turbulence at all the profile whereas, in reality, the flow remains attached at the first part of the profile.

This increase on the $C_d$ for flatback profiles is an expected change. Flatback’s geometry, with the open trailing edge, creates the separation of the boundary layer and a turbulent wake behind the profile. Exactly, the open trailing edge produce a very low pressure behind the profile and for this reason a high pressure drag is created.

The efficiency is an important parameter that characterise the profiles, it is defined as the division between lift coefficient and drag coefficient and it determines the quality of the profile. The higher is the efficiency, the better is the profile. The relation between the efficiency and the angle of attack is shown at figures 6.4 and 6.5.

![Figure 6.4: Comparison between experimental values and simulation results, for closed DU00-W2-401. E vs. angle of attack](image)

Focusing on the experimental results for the closed profile (Experimental) the maximum efficiency is reached at about 5 degrees with a value of 54. The numerical results of the simulation for the closed profile (Closed) have the same behaviour, having its maximum at 5 degrees, but the value of the maximum efficiency is quite small, approximately a half of the experimental efficiency. The comparison between the results from the closed profile is shown at figure 6.4.
Chapter 6. Results

Comparing flatback profiles with closed profile, flatback profiles have more efficiency than the closed profile using numerical simulation, but less than the experimental closed profile. The point where the maximum efficiency is reached also changes for each flatback profile. The closed profile has its maximum efficiency at 5 degrees because in this profile the separation of the boundary layer starts for an angle of attack about 8 degrees, so from this angle a high increase on the drag coefficient will appear and a high decrease of the efficiency is produced, as could be observed at figure 6.5.

![Figure 6.5: Comparison between experimental values and simulation results, for a DU00-W2-401. E vs. angle of attack](image)

However, the behaviour of the efficiency changes for the flatback profiles, this change could rely on the changes on the geometry. Flatback profiles are created from closed profiles, adding thickness symmetrically at both sides of the profile. This increment of thickness generates a profile with less slope, it is for this reason that the boundary layer remains attached to the profile longer, delaying the creation of pressure drag caused by the separation of the boundary layer and producing the increment of drag later. Then, the efficiency increases during more angles of attack without separation, delaying the point of maximum efficiency. This delay on the efficiency is good considering that the range of operation of the wind turbine profiles is about 8 to 16 degrees of angle of attack [5]. So, the point of maximum efficiency is located at this range for flatback profiles and improve the performance of the profile.

Actually, the most important parameter that measures the effectiveness of the blade of wind turbines is $C_q$, which is a non-dimensional parameter that measures the force done in the direction of the rotating plane. This force is defined at section 2.2.1 Wind turbine operation and it depends on two angles, the angle of attack and the twist angle and on
two coefficients; $C_l$ and $C_d$. The simulation has been done changing the angle of attack, so for simplicity reasons twist angle will be considered constant.

Typical twist angles for the 15%–30% radial stations range from roughly 10 to 20 degrees [5], so the twist angle used in this project is the mean value $\beta = 15$ degrees. Then, the torque coefficient can be computed as:

$$C_q = C_l \sin(15 + \alpha) - C_d \cos(15 + \alpha)$$

The torque coefficient values obtained for all the angles of attack and for all the profiles are showed at table 6.1. They are also schemed at figure 6.6.

<table>
<thead>
<tr>
<th>Angle of attack</th>
<th>$C_q$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Closed</td>
<td>-0.008</td>
</tr>
<tr>
<td>0</td>
<td>0.115</td>
</tr>
<tr>
<td>5</td>
<td>0.185</td>
</tr>
<tr>
<td>10</td>
<td>0.157</td>
</tr>
<tr>
<td>15</td>
<td>0.099</td>
</tr>
</tbody>
</table>

Table 6.1: Torque coefficient for all the profiles depending of the angle of attack.

The maximum torque coefficient is located at 15 degrees of angle of attack for most of the profiles. It can also be observed at figure 6.6 that the highest $C_q$ is obtained for the profile that starts the addition of thickness at the point of maximum thickness (MAX). Actually, it is really interesting to observe that at $C_l$ vs. angle of attack graphic there is no clear tendency depending on the point where the addition of thickness starts on
flatback profiles. This means that moving this point forward does not imply that the $C_l$ is increased or decreased and the same for moving it backwards. It seems to change randomly for each profile, and the same happens for drag coefficient. However, $C_q$ indeed shows a decreasing tendency as the point is moved aft of the profile. In fact, the maximum $C_q$ is obtained by the MAX profile and it decreases for 0.4c, 0.5c and it is minimum at 0.6c.

6.2 Study of the changes on the curvature of the profile

6.2.1 Geometry

The reference profile of this section is the profile that gives best aerodynamic performance at the previous section; flatback profile where the addition of thickness starts at the point of maximum thickness (approximately at 30% of the chord).

The variations done in this section consist in change the curvature of the profile; increasing the positive curvature in order to increase the $C_{l0}$, but maintaining constant the thickness at each point of the chord. Exactly, this changes consist in a positive curvature all over the chord and an increment of the positive curvature of the reference profile, they are better explained at section 3.2 Profile Transformations. A draft of this variations respect to the profiles with zero curvature are shown at figures 6.7 and 6.8.

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{figure6_7.png}
\caption{Superposition between zero curvature profile (red) and all positive curvature profile (blue)}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{figure6_8.png}
\caption{Superposition between zero curvature profile (red) and accentuated positive curvature profile (blue)}
\end{figure}
6.2.2 Results

The aim of this variations is to improve lift performance with a minimum drag penalization, in order to improve the torque coefficient and consequently improve the performance of the blade of the wind turbine. It is known that the lift coefficient for an angle of attack of zero degrees increases when the curvature become more positive. So, the $C_{l0}$ should increase for the two variations of the profile. Table 6.2 shows the values of the $C_{l0}$ for the initial profile (MAX) and for the two variations.

<table>
<thead>
<tr>
<th>Profile</th>
<th>MAX</th>
<th>All positive</th>
<th>Accent. positive</th>
</tr>
</thead>
<tbody>
<tr>
<td>$C_{l0}$</td>
<td>0.306</td>
<td>0.359</td>
<td>0.345</td>
</tr>
</tbody>
</table>

Table 6.2: Comparison of lift coefficients at zero degrees of angle of attack.

The maximum value of $C_{l0}$ is reached for the profile that has all the curvature positive whereas the initial profile (MAX) has the minimum value. These results are consistent with the predictions done before; having the maximum $C_{l0}$ the profile with more positive curvature and decreasing the values of the initial lift coefficient as the positive curvature decreases.

Considering the lift coefficient for all the angles of attack, it can be observed at figure 6.9 that this behaviour does not remain during all the performance. Despite of the fact that the $C_{l0}$ is increased, the increase on the positive curvature creates a higher adverse pressure gradient, that promotes an earlier separation of the boundary layer. So, a decrement of the lift coefficient is produced for some angles of attack.

Focusing on drag coefficient, it can be observed at figure 6.10 that the $C_d$ is higher at almost all angles of attack. It is important to pay attention on the range of operative angles of attack, where the drag coefficient for the two variations studied is higher than the $C_d$ of the MAX flatback profile. This increment on the drag is caused by the fact...
that if the separation of the boundary layer is produced before, the point where the pressure drag importantly increase is also advanced, creating a higher drag in this zone.

**Figure 6.10:** Comparison between experimental values and simulation results, for a DU00-W2-401. Cd vs. angle of attack

A comparison between velocity fields at 15 degrees for MAX and "All positive" profiles is shown at 6.11, it can be observed that the profile with more curvature has separation of the boundary layer at the upper surface whereas the initial profile, without changes on the curvature, does not have appreciable separation. These velocity fields agree with the expected behaviour of the different profiles.

**Figure 6.11:** Comparison between velocity fields of a.) profile with all the curvature positive and b.) MAX profile
The efficiency for the three profiles is very similar, having its maximum efficiency around 10 degrees, angle compressed in the range of operative angles of attack. The maximum efficiency is located at this zone because at this angle of attack lift and drag coefficients are not penalized in a noticeable way by the separation of the boundary layer. The best efficiency is reached by the MAX profile although the profile with all the curvature positive has a very similar efficiency. The performance of the different efficiencies is showed at figure 6.12. While studying the behaviour of the efficiency, the parameter maximum lift coefficient, $C_{l_{max}}$, is more important at the root of the blade considering that it is directly related with the torque coefficient.

![Figure 6.12: Comparison between experimental values and simulation results, for a DU00-W2-401. E vs. angle of attack](image)

Finally, the most important parameter for blades of wind turbines, the torque coefficient is shown at figure 6.13. It can be observed that the two proposed variations produce more torque than the reference MAX profile. Despite of the fact that the behaviour of the three profiles is the same, reaching its maximum value at 15 degrees of angle of attack, the maximum value for the profile with all the curvature positive is 1.04 whereas the maximum values for the other two profiles are around 0.8. It is interesting to observe that the increase of $C_q$ is lower for the profile where the positive curvature is accentuated than for the profile with all the curvature positive. This behaviour shows that the changes on the curvature are very important because the curvature is directly related with the lift coefficient.

The computation of the increment of $C_q$ at 15 degrees of angle of attack of the profiles that reaches better performance, profile with all the curvature positive, with respect to the reference profile, MAX, is shown at table 6.3. It can be observed that the maximum increment that produces the variation on the curvature of the profile is about 30%.
Chapter 6. Results

Figure 6.13: Comparison between experimental values and simulation results, for a DU00-W2-401. delta Cq vs. angle of attack

<table>
<thead>
<tr>
<th>Angle of attack [°]</th>
<th>$C_q$ MAX</th>
<th>$C_q$ All positive</th>
<th>$\Delta C_q$</th>
<th>$\Delta C_q$ %</th>
</tr>
</thead>
<tbody>
<tr>
<td>15</td>
<td>0.809</td>
<td>1.045</td>
<td>0.236</td>
<td>29.138</td>
</tr>
</tbody>
</table>

Table 6.3: Increase of torque coefficient at 15 degrees of angle of attack.
Chapter 7

Budget

The budget of this project considers the main expenses effectuated during all the process, including numerical calculations and writing of the study. Considering that this project consist basically in a numerical simulation that is effectuated with a computer, there are not expenses for material. The two main expenses of the project are human resources and computational resources.

For human resources it is important to consider the spent hours of work and multiply them by the cost per hour of an engineer. Considering that this project has been done in 390 hours and that the cost per hours of an engineer is about 15 €/hour, the final cost of human resources is 5850 €.

As have been said before the computational expenses only include the price of the licence of the software used. In this project the software used is ANSYS Fluent 15.0. A licence is necessary to use this program, this licence is about 24903.36 €[21]. Considering that this licence is annually and that this project has been done during 3 month, the cost of this software for this time is 6225.84 €.

The costs of the project can be computed as the addition between the human resources time and the computational costs. The final cost of the project appears at the following table, 7.1.

<table>
<thead>
<tr>
<th></th>
<th>Cost [€]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Human resources</td>
<td>5850</td>
</tr>
<tr>
<td>Computational resources</td>
<td>6225.84</td>
</tr>
<tr>
<td>Total</td>
<td>12075.84</td>
</tr>
</tbody>
</table>

Table 7.1: Final cost of the project
Chapter 8

Environmental analysis

In this chapter an environmental analysis will be done. There are two main aspects to focus on: the environmental effect of the elaboration of this project, and the environmental effect of the implementation of the changes proposed in this study.

On the one hand, the realised study and the comparison of the obtained results do not have any relevant repercussion on the environment. The only parameter that could be taken into account is the power consumption produced by the laptop and the computer used to do the study.

On the other hand, the theme of this project is strongly related with the creation of a better environment, using renewable resources instead of fossil fuels.

Current electricity generation relies mainly on burning fossil fuels, this procedure generate carbon dioxide and moreover, waste much of their primary input energy. So, a complete transformation of the way we produce, consume and distribute energy is required, while maintaining economic growth.

Wind turbines have a lot of good environmental effects. This technology enables to reduce consume of fossil fuels, which produce carbon dioxide that generates the climatic change. Data from the wind industries show that it is possible to maintain a growth rate of about 30% in the renewable energy sector [17]. As have been said before, wind turbine generators tend to be larger in order to produce more power. These turbines and their evolution could create some negative environmental effects like acoustic problems because the motion of the blades creates noise that could affect the ecosystem of the wind farm. The birds ecosystem is also affected because they can impact with the blades of the turbine. Moreover, wind farms create also a visual contamination, considering their large volume.
Chapter 8. *Environmental analysis*

Focusing on this project, its aim is to improve the aerodynamic performance of the flat-back profiles, which enables to increase the power generated for the wind turbine. This optimisation reduces the bad effects of the wind turbine, creating smaller wind farms with the same power generated. It also helps on the transformation on the production of the energy, changing fossil fuels for renewable resources.
Chapter 9

Conclusions

9.1 Conclusions

On the one hand, knowledge about numerical analysis and problems resolution by means of computational fluid dynamics has been acquired. On the other hand, this project has been useful as an introduction at wind turbines and their blades, specially at the inner part of the blade.

Nowadays, a lot of studies are focused in designing better thick profiles. This necessity comes from the fact that at the inner part of the blade, thick profiles are used for structural purposes and also because they are a transition between the common profiles of the blade and the cylindrical axis that links blade and gearbox. This type of profiles have a maximum thickness higher than the 30% of the chord ($\frac{t}{c} > 0.3$) so, there is a big slope at the rear part of the profiles, creating a strong pressure gradient which causes the separation of the boundary layer. This separation creates a dramatic increment on the drag and a decrement of the lift.

Flatback profiles are a good alternative to design a more energetic root for a wind turbine blade. They are created adding thickness at the rear part of the thick common profiles creating a blunt trailing edge. This increment of thickness reduces the slope of the profile, delaying the separation of the boundary layer and increasing the lift performance of the profile. It is true that the drag also increase but the growth of lift is higher, so the total performances of the profile improves.

Focusing on this project, the profiles proved are common DU00-W2-401 closed profile and flatback profiles created from this closed profile. The change between them is the point where the addition of thickness starts.
The main changes observed between closed and flatback profiles are the increase of lift and the increase also of drag. The results of this project, section 6.1.2 Results, show that an important increase on lift force appears using flatback profiles. This increase appears for high angles of attack, caused by the delay of the boundary layer separation. The results of the simulation show that the maximum lift coefficient for flatback profiles are two times the maximum lift coefficient for the closed profile. The drag coefficient for flatback profiles also increases with respect to the $C_d$ of the simulated closed profile, however this increment is smaller than the lift one.

The differences between flatback profiles are not easy to see. On drag vs. angle of attack graphic it can be observed that as the point where the addition of thickness starts is moved aft of the profile, the drag coefficient increases. The most important parameter that must be considered in wind turbine applications is the torque coefficient, $C_q$, it represents the amount of force at rotational plane direction. This parameter reaches its maximum value for flatback MAX (flatback profile where the addition of thickness starts at the point of maximum thickness). $C_q$ decreases as the point where the addition of thickness starts is moved aft of the profile. It is for this reason that can be affirmed that the most aerodynamically optimal profile is the flatback with the start of addition of thickness at the point of maximum thickness. This result agrees with the results of similar studies done in parallel of this one.

Considering the changes done on the curvature of the profile, it has been proved that both, the accentuation of the positive curvature and the change to get a profile with positive curvature, improve the aerodynamic performance of the profile. Reaching the best values of torque performance for the profile with positive curvature for all the chord of the profile. Despite of the fact that more curvature promotes a higher adverse pressure gradient that produces an earlier separation of the boundary layer and this separation creates more drag, the increment of lift is higher than the increment of drag, obtaining higher values of torque coefficient for the profiles with more curvature than for the initial profile, MAX. Exactly, the maximum increment is reached at angle of attack 15 degrees for the profile with all the curvature positive, this maximum value is 30% higher than the torque coefficient for the initial profile. As a result, it can be concluded that the best studied profile is a flatback profile created from DU00-W2-401 with TE of 14%, the addition of thickness starts at the point of maximum thickness and all the curvature of the profile is positive with a maximum of 0.02c at the 50% of the chord. However, this profile is not optimised with respect to the curvature, only two configurations have been tried in order to improve its performance.

Finally, it has been proved that the usage of flatback profiles could improve a lot the performance of the inner part of the blade of wind turbines, incrementing the coefficient
of torque and lift coefficient all over the work range. So, this type of profiles have a big potential to improve the wind turbine blades.

9.2 Proposed future work

This project consists in an aerodynamic optimisation of the profiles done in 2D and using mostly steady computations. Taking into account that the objects in study are thick profiles, turbulence need to be considered and the best method to compute the turbulence is by means of a unsteady study in stead of a steady one. Is is also important to compute the turbulence using a 3D geometry, considering that the turbulence is a three-dimensional unsteady random motion. This type of studies requires a basic knowledge about flatback profiles and their aerodynamic behaviour, moreover they are more computationally expensive. Now, they can be performed considering that there is a previous background established by this work and by Sotelo [9]. The following list contains the proposed future work:

- 3D analysis of a segment of the inner part of the blade.
- Unsteady analysis of flatback profiles.
- Unsteady analysis of a 3D segment of the inner part of the blade.
- Analysis of flatback profiles changing parameters that have not been changed yet.
Chapter 10

Planning of the future work

The proposal of future work that is planned in this chapter is the aerodynamic optimisation of the inner part of the blade. In this case the study will be in 3D instead of 2D. Despite of the addition of one dimension at the problem, the activities that have to be developed are really similar to the ones done in this project. It is for this reason that the Gantt diagram and the other elements used for the planning of the study, will be very similar to the ones that appear in the project charter of this project.

A correct planning of the project is very important in order to achieve its goal using efficiently the time and the resources. Taking into account that the entire project could be done by the same person, almost all the activities will done in series except the writing, which has been done in parallel as the evolution of the other activities.

The body of the project are the simulations of the flatback profiles that are done using CFD. So, the activities that have been longer are the activities related with the software. At first a good mesh that fits the geometry needs to be created, and then it is necessary to know the boundary conditions used to define the problem. It is necessary to spend a lot of time during the simulations. And the port-process and the analysis of the results is very important, so it is necessary to do this part step by step and this takes time.

A brief explanation of the main activities of the project is showed:

- Research of information and documentation
  - State of the art and information of flatback profiles
    To know the evolution of the flatback profiles and understand the necessary to create this type of profiles in order to do the best optimisation. It is important also to study the implementation of this profile at the inner part of the blade.
Chapter 10. Planning of the future work

– Research of related information

To find important information related with the flatback profiles and wind turbine blades that is necessary for the project.

• Creation of a new geometry

The new geometry of the profile can be created from an original profile and the optimised profile created in this project. In the 3D project it is also important to focus on the shape of the whole blade in order to create a geometry that not only optimises aerodynamically the profile, but optimise aerodynamically the whole blade of the wind turbine. In order to do this 3D optimisation two main parameters need to be considered: the chords distribution and the twist angle distribution.

• Software tasks

– Ansys software learning

Learn how to insert a geometry, mesh the geometry and post-process the results.

– Creation of an appropriate mesh for each geometry

Create a good mesh for each 3D geometry that fits with the different geometries and gets convergence.

– Simulation of each geometry

Simulate each mesh considering boundary conditions.

– Post-process of the simulation

Extract significant values of the results of the simulation.

• Results evaluation

Ensure that the obtained results are consistent and draw conclusions. In this section the geometry that best adapts to the root blade characteristics of a wind turbine will be found. This characteristics combine high $C_L$ and high $E$. The best geometry will be that one that gives the highest torque value which is giving the electrical energy generation.

• Writing of the TFG

Writing of all the deliverables of the TFG; report, annexes and budget.

• Revision

Make sure that the work that has been done is correct.
Chapter 10. *Planning of the future work*

<table>
<thead>
<tr>
<th>Code of task</th>
<th>Task identification</th>
<th>Preceding task(s)</th>
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*Table 10.1: Relationship between activities.*

<table>
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<th>Time (hours)</th>
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*Table 10.2: Hours spent for each task.*

The following tables show the relation between the activities described before 10.1, and the spent time for each activity 10.2.

At table 10.2 an important increase of hours of work could be observed comparing with the spent hours in this project. The reason of this increment lies in the fact that the study of a 3D geometry is quite more complicated than a 2D study. For instance, the creation of the new geometry needs to consider the evolution of the flatback profiles along the blade. So, the interaction between the profiles have to be considered during the aerodynamic optimisation. The mesh will be also more complicated, having nodes in three directions. It has to fit not only with one profile, but in a part of the blade. This 3D mesh has more nodes than a 2D mesh, is for this reason that the simulation of each geometry will be longer and heavier.

Adding all the hours predicted at table 10.2 the time needed to do this project is about 610 hours. As said before, this is a larger project that can be done in more time or with the same time but spending more daily hours, considering that is an academic project it could be a focused on GrEVA.
At last, a possible planning of the main activities could be the Gantt diagram shown at figure 10.1. Actually, this is the Gantt used in the project charter of this project but, considering the similarities of the procedure the only change needed is to multiply per two the hours spent each day.

**Figure 10.1: Gantt diagram of the project**

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<th>Fecha de final</th>
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