Master's Thesis
Industrial Engineering

**Mobility and environment improvement of signalized networks
through Vehicle-to-Infrastructure (V2I) communications**

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ABSTRACT

Traffic signals, even though crucial for safe operations of busy intersections, are one of the leading causes of travel delays in urban settings, as well as the reason why billions of gallons of fuel are burned each year by idling engines, releasing tons of unnecessary toxic pollutants to the atmosphere. Recent advances in cellular networks and dedicated short-range communications make Vehicle-to-Infrastructure (V2I) communications a reality, as individual cars and traffic signals can now be equipped with numerous communication and computing devices. In this thesis, an initial comprehensive literature search is carried out on topics related to traffic flow models, connected vehicles, eco-driving, traffic signal timing, and the application of connected vehicle technologies in improving the operation of signalized networks. Then a car-following model and an emission model are combined to simulate the behavior of vehicles at signalized intersections and calculate traffic delays in queues, vehicle emissions and fuel consumption. Next, a strategy to provide mobility and environment improvements in signalized networks is presented. In this strategy, the control variable is the advisory speed limit, which is designed to smooth vehicles' speed profiles taking advantage of Vehicle-to-Intersection communication. Finally, the performance of the control system is studied depending on market penetration rate and traffic conditions, as well as communication, positioning and network characteristics. In particular, savings of around 15% in user delays and around 8% in fuel consumption and CO₂ emissions are demonstrated.

Keywords: Vehicle-to-Infrastructure communication, advisory speed limit, intersection efficiency, market penetration rate, communication delay

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1. INTRODUCTION

Traffic Optimization are the methods by which time stopped in road traffic (particularly, at traffic signals) is reduced. Texas Transportation Institute estimates travel delays of between 12–67 hours of delay per person per year relating to congestion on the streets [1], hence Traffic Optimization becomes a significant aspect of operations. The goal of this project is to take advantage of Vehicle-to-Infrastructure (V2I) communication capabilities to reduce stopping delays (user time), as well as to minimize the vast amount of fuel wasted by stationary vehicles [1] (energy consumption) and its environmental impact (emissions). An intelligent transportation system is developed, in which equipped vehicles are advised on a particular speed limit to avoid stops and smoothen its speed profile. This green driving strategy will be referred from now on as Advisory Speed Limit (ASL).

The project will start by modeling and optimizing the simplest case, with single signalized intersections and single-lane roads. However, in real world, a route involves driving through multiple signals. Thus, as the project advances, operation in multiple traffic signals will need to be collectively synchronized in order to be effective in a real-life situation.

First, the most relevant work found on intersection efficiency and environmental impact optimization is commented in order to better understand the ASL fundamentals explained after that.

Fig. 1: Traffic jam at an intersection [2]

1.1. Eco-Driving and Eco-Routing

Interesting research on eco-vehicle speed control at signalized intersections using V2I communication has been carried out at Virginia Polytechnic Institute and State University and at Virginia Tech Transportation Institute [3].

The conception behind this field of study is that, as researchers at the Laboratory of Energy and the Environment at the Massachusetts Institute of Technology (MIT) reported, approximately 7 percent of a vehicle's energy is lost due to braking [4]. Consequently, reducing braking was assumed a direct fuel savings strategy that gave result in driving practices known as eco-driving that assist drivers in achieving smoother speed fluctuations.

Having a smoother speed profile during driving is transformed into several research subjects pertaining to energy and emissions savings. Eco-driving and eco-routing were two types of driving system improvements found in a comprehensive literature search. Eco-driving involves driving in an eco-friendly style (avoiding abrupt speed changes in driving and maintaining a constant velocity around the fuel-optimal velocity have been associated with improved fuel economy and emission reductions by various fuel consumption models [5,6]), and eco-routing implicates selecting the route that will consume the least energy and generate minimum emission levels.

If a driver is informed of the upcoming signal status, the speed of the vehicle can be regulated accordingly to avoid hard braking or accelerating, thereby reducing energy consumption and pollutant emissions. As with Virginia Polytechnic Institute and State University and Virginia Tech Transportation Institute research on the topic, the ASL control system uses advanced notification of signal status to adjust the speed of vehicles to produce delay, fuel and emission savings.

In their research, the lowest throttle level downstream was found to be a fuel efficient technique. However, it should be noticed that lower acceleration after an intersection affects its discharge rate and thus could reduce the road's flow rate. In this thesis, following vehicles are taken into account so a compromise solution that does not adversely affect the approach capacity has to be found.

The differences between the mentioned literature and this particular research are primarily four. First of all, this thesis compares cellular networks with dedicated short-range communication (DSRC) networks, as the idea is to have this system working due to a smartphone application. The delay in cellular networks may be larger, but the distance from which the intersection is aware of the vehicle also increases. Second, another difference are the objectives, as this research does not only focus on fuel efficiency and emissions but also on stopping time and delay optimization. Third, eco-driving wants to control the speed profile and this research just controls ASL indications. And finally, as previously mentioned, vehicle-to-vehicle interaction is taken into account by using a car-following model that make the system closer to implementation, as well as more complex.

1.2. Reservation-Based Control

The idea from Kurt Dresner and Peter Stone, called reservation-based control [7,8,9], consists on computer programs (called "driver agents") controlling completely autonomous vehicles. The driver agents communicate with the intersection manager before arriving at the crossing and attempt to reserve blocks of space-time in the intersection. The reservation request may include parameters such as time and velocity of arrival, as well as vehicle characteristics like size together with acceleration and deceleration specifications.

To establish whether or not a petition can be met, the reservation manager simulates the course of the vehicle across the intersection, which it divides into a grid of square tiles. At each time step of the simulation, the system determines which tiles will need to be reserved for the arriving vehicle. If throughout the simulation no required tile is occupied by another vehicle (from previous reservations), the manager grants the reservation and books the combination of space-time tiles for this vehicle. This decision process is called the intersection control policy (which does not need to be understood by the driver agent), and determines whether or not it is safe for a vehicle to make its journey through the intersection.

If the policy considers a request to be safe, the intersection manager answers back to the driver agent pointing out that the reservation has been accepted and including any additional restrictions the driver must comply with in order to guarantee the safety of the crossing. Otherwise, if the request is not considered safe, the intersection manager sends a message indicating that the reservation request has been rejected, possibly including the reasons for the denial or responding with an alternative reservation. No vehicle is allowed to enter the intersection without a reservation, and even with a reservation, the driver agent may only lead the vehicle into the junction according to the parameters and restrictions associated with the reservation.

While the reservation-based control seems to be an effective way to maximize intersection efficiency in a future filled with fully autonomous vehicles, the focus of the current research is to obtain a more short term solution based on today's average vehicles and smartphones by advising human drivers on a particular speed limit.

1.3. Advisory Speed Limit Fundamentals

The fundamentals behind ASL ideas are easy to understand with the help of the adjoining figure. A "normal" or non-equipped vehicle would maintain a high velocity to arrive earlier at the intersection and remain idle until the traffic light turns green (see trajectory 1). Instead, equipped vehicles would slow down to a speed that would let them arrive at the intersection

when the traffic lights and the intersection capacity allow them to enter (see trajectory 2), maintaining a smoother speed profile that could lead to a series of advantages. Theoretically, this could result in less emissions released to the environment, less money spent on gas and fewer delays ($t_2 < t_1$) due to entering the downstream road at a higher speed and increasing the approach capacity.

Fig. 2: ASL fundamentals chart

In this thesis, the benefits of advising the drivers on this particular speed limit calculated by algorithms are analyzed, all within the framework of feedback control systems. In these systems, vehicles are still manually driven, the control variable is an advisory speed limit for each equipped vehicle, and the control objective is to reduce delays, air pollutant emissions and fuel consumption in stop-and-go traffic at signalized intersections.

The figure in the following page is useful to understand the work behind this thesis from an upper level, providing a global vision of the Advisory Speed Limit system.

With the data collected by the loop detectors at the start and the end of the upstream road, as well as the information provided by the traffic signals, the control algorithms are able to anticipate the expected arrival time of each vehicle at the intersection, t_{ik}^e . With this value and the position and speed of the vehicle (x_k and v_k respectively) sent over V2I communication, the 'ASL Equation' provides an individual advisory speed limit (v_k^{ASL}) for each equipped car to follow. At last, a car-following model is used to compute the acceleration of the vehicles at each time step, and therefore the position and speed too.

In this study, Gipps' model is the main car-following model used to describe vehicles' movements, and the Virginia Tech Microscopic Energy and Emission Model (VT-Micro) is used to calculate vehicle emissions and fuel consumption. With simulations, the impacts of several parameters on the performance of the explained green driving strategies are examined, namely market penetration rates (MPRs), traffic congestion levels, communication characteristics (communication delay and transmission range) and location accuracy, as well as the influence of the car-following model itself.

Fig. 3: Feedback control system of an Advisory Speed Limit strategy

The rest of the thesis is organized as follows. In the next section, the operation of the simulator is described (its variables and parameters, the car behavior and emission models used, the traffic lights and the Vehicle-to-Infrastructure communication characteristics). In section 3, ASL operation and its control algorithms are detailed. In sections 4 and 5, the obtained results in two different road configurations (isolated or open intersections, and loop or closed intersections) are shown. After that, the effects of the car-following model in the results are analyzed. Then, in section 7, the conclusions are stated and finally, in section 8, some future research topics are discussed.

2. SIMULATION TESTBED

A custom simulator has been developed using MATLAB® software. Its main properties are explained below. Both upstream and downstream roads are incorporated as fuel, emissions and delay downstream depend on the upstream behavior.

Fig. 4: Schematic representation of the simulation testbed

The following parameters and variables are used to carry out the computer simulations:

Table 1: General parameters used in the simulator

Parameter	Description	Value
v_f	free flow speed / speed limit at which vehicles wish to travel	12.5 m/s
Δt	time step between iteration computations	0.1 s
s	service rate, intersection capacity	1800 v/h
L_1	length of the upstream road (Road 1)	495 m
L_{int}	length of intersection	10 m
L_2	length of the downstream road (Road 2)	495 m
n_c	number of cars arriving at Road 1 per simulation run	100
t_{lg}	instant when the last green light turned on (it is updated every cycle)	0 s
t_{ag}	seconds after a green light that a car can enter intersection	1 s
t_{br}	seconds before a red light that a car can enter intersection	1 s

Table 2: Car and drivers' parameters used in the simulator

Parameter	Description	Value
a_{br}	absolute value of the desired maximum braking deceleration	4 m/s ²
a_{fw}	desired maximum forward acceleration	3 m/s ²
s_j	jam spacing (spacing between stopped cars)	7.1 m
τ	drivers time of reaction	1.6 s
T	car-following model sensitivity coefficient	1.2 s
j_{max}	maximum jerk	20 m/s ³

Table 3: Main variables used in the simulator

Variable	Description	Restrictions
$x_k(t)$	position of vehicle k at time t [m]	$k = 1, \dots, n_c; t \geq 0$
$v_k(t)$	speed of vehicle k at time t [m/s]	$k = 1, \dots, n_c; t \geq 0$
$a_k(t)$	acceleration of vehicle k at time t [m/s ²]	$k = 1, \dots, n_c; t \geq 0$
ta_k	arrival time of vehicle k at the upstream road [s]	$k = 1, \dots, n_c$
ti_k	arrival time of vehicle k at the intersection entrance [s]	$k = 1, \dots, n_c$
td_k	departure time of vehicle k from the system [s]	$k = 1, \dots, n_c$
tw_k	waiting time of vehicle k due to congestion [s]	$k = 1, \dots, n_c$

Given the difficulty in measuring the delays, the waiting time is defined as the extra amount of time needed to fulfill the drive compared to the time it would take to travel the roads at its speed limit, and it is obtained using the following formulation:

$$tw_k = td_k - ta_k - \frac{L_1 + L_{int} + L_2}{v_f} \quad (1)$$

2.1. Vehicle Behavior Model

Uniform acceleration equations and time-iteration correspondence equation are pertinent. To consider network properties, the speed is bounded between zero (stopped car) and v_f (speed limit).

$$x_k(t + \Delta t) = \max \left\{ x_k(t), \min \left\{ x_k(t) + v_f \cdot \Delta t, x_k(t) + v_k(t) \cdot \Delta t + \frac{a_k(t) \cdot \Delta t^2}{2} \right\} \right\} \quad (2)$$

$$v_k(t + \Delta t) = \max \{ 0, \min \{ v_f, v_k(t) + a_k(t) \cdot \Delta t \} \} \quad (3)$$

$$t = \Delta t \cdot (\text{iteration} - 1) \quad (4)$$

In order to apply these equations, $a_k(t)$ must be decided. The behavior (acceleration) of the cars is modeled depending on two different situations, explained below:

- Following car, when there are other vehicles in front (between them and the intersection entrance). This vehicles' behavior, as well as with cars on downstream roads, is simulated using Gipps' car-following model.
- Leading car on upstream road, when there are no other vehicles between this car and the intersection entrance. As there is only one lane and no overtaking, this will be the next vehicle of that road to enter the intersection. Its behavior depends on the traffic lights and other intersection parameters.

2.1.1. Gipps' Car-Following Model with Bounded Acceleration

The behavior of the following cars does not depend on the color of the traffic lights. On a single-lane road, the acceleration of these vehicles at any given time is just a function of the speed of the car in front, the speed of the follower and the distance between them. Note that no overtaking is considered.

To take into account the dynamic characteristics of the vehicles, Gipps' model with bounded acceleration is employed. In this model, the vehicle acceleration cannot be greater than a_{fw} and the deceleration cannot be inferior than $-a_{br}$.

Fig. 5: A car following scenario

The model used consists of two parts: free-flow and congested traffic.

Gipps defines the model by a set of limitations [10]. The following vehicle is limited by two constraints: that it will not exceed its driver's desired speed and its free acceleration should first increase with speed as engine torque increases then decrease to zero as the desired

speed is reached. This defines the free-flow component of the model which, by definition, cannot be greater than a_{fw} :

$$a_k^{free-flow}(t) = 2.5 \cdot a_{fw} \cdot \left(1 - \frac{v_k(t)}{v_f}\right) \cdot \sqrt{0.025 + \frac{v_k(t)}{v_f}} \quad (5)$$

This part of the model alone is useless in the current case due to the presence of signals and traffic so another constraint, braking, had to be added to the model. This second part of the model takes into account the different speeds in leading and following vehicles, and it is given by:

$$a_k^{congested}(t) = \frac{1}{T} \cdot \left[\frac{1}{\tau} \cdot \left(x_{k-1}(t) - x_k(t) - s_j + \frac{v_{k-1}(t)^2}{2 \cdot a_{br}} - \frac{v_k(t)^2}{2 \cdot a_{br}} \right) - v_k(t) \right] \quad (6)$$

Finally, the whole Gipps' model with bounded acceleration is given by:

$$a_k(t) = \max \left\{ -a_{br}, \min \{ a_k^{free-flow}(t), a_k^{congested}(t) \} \right\} \quad (7)$$

On the downstream road (Road 2), vehicles are only subject to the described car-following model, without the additional constraints related to the presence of traffic signals.

2.1.2. Leading Car Behavior

The behavior of the first car on the upstream road, the leading car, depends on the color of the traffic light (green, yellow or red) a period of time equal to the time of reaction (τ) before the current iteration. Vehicles will only enter the intersection if the service rate and the traffic lights allow them to do it safely.

If the green light was on, the vehicle will maintain the optimal acceleration so as to enter the intersection in the next possible instant (that is at least $3600/s$ seconds after the last car entered, t_{left} seconds after the current time). Acceleration is bounded between $-a_{br}$ and $a_k^{free-flow}(t)$.

(Algorithm 1)

1	$t_{left} = \max \left\{ 0^+, t_{i_{k-1}} + \frac{3600}{s} - t \right\}$
2	$a_k(t) = \max \left\{ -a_{br}, \min \left\{ a_k^{free-flow}(t), \frac{(L_1 - x_k(t) - v_k(t) \cdot t_{left}) \cdot 2}{t_{left}^2} \right\} \right\}$

If at that time the red light was on, the vehicle will stop at a specified position, which is defined as $s_j/2$ meters before the intersection entrance. Braking is imposed using the deceleration part of the car-following model imagining that the car in front is stopped, $v_{k-1}(t) = 0$, at a location $x_{k-1}(t) = L_1 + s_j/2$. An extra condition (lines 2-4) has been added in order to make sure the desired maximum braking is achieved if needed. Acceleration is bounded between $-a_{br}$ and $a_k^{free-flow}(t)$, as if the car is still far from the intersection the car-following model dictates that it will accelerate, just like it would be logical to happen in real life.

(Algorithm 2)

1	$a_k(t) = \max \left\{ -a_{br}, \min \left\{ a_k^{free-flow}(t), \frac{1}{T} \cdot \left[\frac{1}{\tau} \cdot \left(L_1 - \frac{s_j}{2} - x_k(t) - \frac{v_k(t)^2}{2 \cdot a_{br}} \right) - v_k(t) \right] \right\} \right\}$
2	if $x_k(t) + \frac{v_k(t)^2}{2 \cdot a_{br}} \geq L_1 + \frac{s_j}{2}$
3	$a_k(t) = -a_{br}$
4	end

If the yellow light was on, the driver will have to decide whether the time available until the next red light (t_{stop}) is enough to enter the intersection respecting its service rate (being t_{left} the time that the car should still remain in the upstream road to respect the intersection capacity). Decisions are made according to the following criteria:

- If, at its current speed, the vehicle is able to enter the intersection at least t_{br} seconds before the red light (and the intersection is clear), the vehicle will maintain the optimal acceleration so as to do so (same behavior as a green light).
- Else, if the vehicle is not able to enter the intersection at least t_{br} seconds before the red light or the intersection service rate does not allow more vehicles in that period of time, the car will stop $s_j/2$ meters before the intersection entrance (same behavior as a red light).

(Algorithm 3)

```

1   $t_{stop} = t_{lg} + GLP + YLP - t$ 
2   $t_{left} = \max\left\{0, t_{i_{k-1}} + \frac{3600}{s} - t\right\}$ 
3  if  $\left(L_1 - \frac{x_k(t)}{v_k(t)} < t_{stop} - t_{br}\right) \cdot (t_{stop} - t_{br} \geq t_{left})$ 
4      Algorithm 1
5  else
6      Algorithm 2
7  end

```

2.1.3. Arrival Speed

In order to avoid car crashes in the model and obtain a more realistic simulation, the arrival speed of the vehicles at the simulator is a function of the position and speed of the car in front. With the correct formulation, the cars enter the simulator at slower speeds in congested environments and at faster speeds in less saturated conditions. L_{br} is defined as the necessary distance to stop from the speed limit v_f to zero with a uniform acceleration of $-a_{br}$. Its mathematical expression is:

$$L_{br} = \frac{v_f^2}{2 \cdot a_{br}} \quad (8)$$

If, at the arrival time, the vehicle in front is within the distance needed to perform a safety complete stop, its arrival speed may be reduced by the following safety expression:

$$v_k(t) = \min\left\{v_f, \max\left\{v_{k-1}(t), v_f \cdot \frac{x_{k-1}(t) - x_k(t)}{L_{br} + s_j}\right\}\right\} \quad (9)$$

2.1.4. Jerk

With the purpose of creating a more objective simulator, the vehicles' maximum jerk (rate of change of acceleration or derivative of acceleration with respect to time) is limited. This way, the acceleration changes between two close iterations cannot be greater than a set value. Once the acceleration at a specific time step is calculated, the next statement ensures that the maximum jerk limitation is respected.

$$a_k(t) = \max\{a(k, t - \Delta t) - j_{max} \cdot \Delta t, \min\{a_k(t), a_k(t - \Delta t) + j_{max} \cdot \Delta t\}\} \quad (10)$$

2.2. Traffic Lights

A typical three-aspect traffic light system is selected (see adjacent figure). Note that an “all red” phase is also considered, as it is now a safety standard to turn the lights red in all directions, for a brief time, to clear any remaining traffic in the intersection. It is also interesting to notice how the red phase (excluding the “all red” lapse) corresponds to the time allocated to green, yellow and “all red” phases on the perpendicular approach.

Fig. 6: Traffic light cycle representation

The traffic lights simulated follow a pre-timed cycle, that is, with fixed phases' times. A fixed cycle time of 60 seconds is allocated equally to each one of the two intersection approaches, so that each approach has the following periods assigned to their phases:

Table 4: Pre-timed traffic lights parameters used in simulation

Parameter	Description	Value
GLP	Green light time per traffic light cycle	23 s
YLP	Yellow light time per traffic light cycle	5 s
RLP	Red light time per traffic light cycle (includes red and “all red” phases)	32 s

2.2.1. Dilemma Zone

Due to the network and drivers characteristics, dilemma zone must be considered when choosing the duration of the yellow light. The yellow indication is designed to warn drivers approaching an intersection that the signal is about to turn red. The length of the yellow light should be enough for the approaching drivers to either safely stop before the intersection, or continue clear through the intersection before the traffic light turns red [11].

An inadequate yellow extension will either prevent the drivers from safely stopping their vehicles before the intersection entrance or force them to enter the crossing on a red light. None of these options is admissible when designing signal timing.

The following scheme exemplifies what happens when a vehicle approaching an intersection faces a yellow light. Drivers who are in the zone marked as "Can't Go" when the traffic light turns yellow know they are too far back and will not be able to reach the intersection before the light turns red. Hence, they must stop. On the other hand, drivers who are in the "Can't Stop" zone are too close to the intersection to stop safely: they must proceed before the red light. But when the yellow time is inadequate, there is range between both zones (generally called the “dilemma zone”) where the driver can neither proceed safely, nor stop safely. The duration of a yellow light in an appropriately timed signal must be enough for drivers to avoid the impossible election presented by the dilemma zone.

Fig. 7: Dilemma zone representation

Several studies have been carried out to safely establish yellow times depending on the time needed for a 90th percentile speed vehicle to travel from its far dilemma zone boundary to the stop bar. For a 35 mph speed limit, a recommended yellow change time would be 3.9 seconds [12], being the length longer on faster roads. On the current research, with fixed reaction times and vehicle braking capabilities, the decision is much simpler. To make sure the yellow light time (*YLP*) is enough to eliminate dilemma zone given a speed limit and a desired maximum breaking deceleration on the simulation testbed, the following condition must be satisfied:

$$YLP > \tau + \frac{v_f}{a_{br}} \quad (11)$$

Considering these factors, and because of the way that vehicles' behavior is programmed, dilemma zone has been eliminated and is no longer an issue.

2.3. VT-Micro Emission Model

This study uses Virginia Tech Microscopic Energy and Emission Model (VT-Micro) due to its simplicity, accuracy, and ease of MATLAB implementation. This microscopic vehicle energy and emission model utilizes instantaneous time, position and speed as input variables and the results depend on the specified vehicle type.

The VT-Micro model was developed from experimentation with many polynomial combinations of speed and acceleration levels [13,14], which were tested using chassis dynamometer data gathered at the Oak Ridge National Laboratory in Tennessee, United States of America. The final regression model includes a combination of linear, quadratic, and cubic terms of speed and acceleration, providing the least number of terms with a relatively good fit to the experimental data (R^2 in excess of 0.92). The original data collected consisted of nine normal emitting vehicles (six light-duty automobiles and three light-duty trucks). These vehicles were selected in order to produce an average vehicle that was consistent with average vehicle sales in terms of engine, weight and vehicle type. The data collected contained between 1,300 and 1,600 individual measurements for each vehicle type, covering the entire vehicle operational regime instead of simply collecting data from a few driving cycles. Typically, vehicle acceleration values fluctuate between -1.5 and 3.7 m/s^2 at increments of 0.3 m/s^2 , and vehicle speeds ranged from 0 to 33.5 m/s (0 to 121 km/h) at increments of 0.3 m/s .

For the sake of simplicity, the type of vehicle used in the model is the same on all the simulations. Results shown in the following sections correspond to "Light-Duty Vehicle 3", which is characterized by being its model year 1995 or newer, its engine size inferior to 3.2 liters and its mileage inferior than 83,653. By always running the simulations using the same type of standard vehicle, the results are assumed to be directly comparable.

The output obtained from this energy and emission model as well as the units in which the results will be studied are:

- Average HC emission (mg/km)
- Average CO emission (mg/km)
- Average NO_x emission (mg/km)
- Average CO₂ emission (g/km)
- Average fuel economy (l/100km)

2.4. Vehicle-to-Infrastructure (V2I) Communication and Positioning Settings

Vehicles equipped with ASL technology send a series of parameters (such as position and speed) to the intersection, which processes the information and responds with an advisory speed limit indication. This kind of Vehicle-to-Infrastructure communication can be achieved over several networks, and in this thesis two of them are simulated. Cellular and dedicated short-range communications (DSRC) networks are compared to discover which one could provide greater benefits if used in Vehicle-to-Intersection green driving strategies.

A network type is characterized in the simulator by its communication delay mean (t_{com}) and its transmission range (x_{com}). It is worth repeating that the delay in cellular networks may be larger, but the distance from which the intersection is aware of the vehicle also increases. Besides its transmission range, cellular networks present some other advantages. Smartphones worldwide, the use of which has skyrocketed during the last decade [15], communicate through this network, so the system could work by simply installing a smartphone app and its market penetration could be easily widespread.

Additionally, randomness in communication delay is also considered, resulting in a different delay for each equipped vehicle in the system. Communication delay in sending the position and speed values to the intersection is hypothesized to follow an exponential distribution, bounded between half and double the communication delay mean (between $t_{com}/2$ and $2 \cdot t_{com}$).

On the other hand, equipped vehicles are also connected to the Global Positioning System (GPS) in order to be aware of its own location and communicate it to the intersection. The accuracy of this satellite system is taken into account too, as the United States government currently claims 4 meter horizontal accuracy for civilian GPS (Standard Positioning Service or SPS), with a 95% Confidence Interval of 7.8 meters [16]. For this reason, three different scenarios are simulated by introducing a fixed location error (x_{error}) which represent perfect location accuracy, over-estimation and under-estimation.

The following tables specify the values of the discussed parameters and describe the new variables used in the simulation testbed.

Table 5: V2I communication and GPS parameters used in the simulator

Parameter	Description	Communication type:	
		Cellular	DSRC
t_{com}	Communication delay mean	Values	Values
x_{com}	Transmission range	0.5 s	0.1 s
x_{error}	Error of GPS location	infinite	300 m
		-5 m, 0 m, 5 m	

Table 6: Communication variables used in the simulator

Variable	Description	Restrictions
$t_{com,k}$	Communication delay of vehicle k	$k = 1, \dots, n_c$

3. ADVISORY SPEED LIMIT (ASL) OPERATION

In the ASL control strategies that are studied in this thesis, vehicles are still manually driven. Thus, a vehicle's speed cannot be directly controlled, but instead an individual advisory speed limit is provided to each driver of the equipped vehicles. Therefore, non-equipped vehicles' movements are still described by Gipps' car-following model and the previous algorithms explained on Section 2, but for vehicles with V2I communication, the acceleration part of the model is modified by replacing the speed limit, v_f , by the advisory speed limit, $v_k^{ASL}(t)$, which is time-dependent. Consequently, the movement of vehicles that follow ASL indications and that are close enough to the intersection is described by:

$$a_k(t) = \max \left\{ -a_{br}, \min \left\{ 2.5 \cdot a_{fw} \cdot \left(1 - \frac{v_k(t)}{v_k^{ASL}(t)} \right) \cdot \sqrt{0.025 + \frac{v_k(t)}{v_k^{ASL}(t)}}, a_k^{congested}(t) \right\} \right\} \quad (12)$$

Note how V2I-equipped vehicles' movements have nothing to do with the color of the traffic light, as ASL indications already make sure that the vehicles arrive at the intersection with green or yellow lights and enough time to cross it.

But what would happen if ASL indications were incorrect, for example due to GPS inaccuracies? Human drivers are still handling the vehicles, so they are expected to brake if they feel the system is putting them in unsafe situations. Imagine a car is driving at the speed limit towards a signalized intersection with the red light on. Even though the system says it is safe to proceed at that speed because the traffic lights are soon going to turn green, the driver would be expected to gently brake to stop at a safe location if it was needed to. This kind of reaction is programmed in the simulator using a variation of algorithms 2 and 3 in equipped vehicles.

3.1. Control Algorithms

To calculate at which time instant a car is expected to enter the intersection (ti_k^e), the following algorithm is executed every time a new vehicle enters the upstream road. Basically, the control system expects the vehicles to enter the intersection at their first possible chance, taking into account three factors: the speed limit, the intersection service rate and the traffic lights.

Take the example of the next figure, where three vehicles enter a road at time instants ta_1 , ta_2 and ta_3 respectively. If the first vehicle were to travel at the speed limit (discontinuous yellow trajectory) it would arrive at the intersection during a red light. As it has no other vehicles in front, the algorithm would assign vehicle 1 an expected arrival time just after the next green light will turn on (specifically t_{ag} seconds after that). In this case, traffic lights are the bottleneck factor.

Now take a look at vehicle 2, which would have the discontinuous light green trajectory if traveling at the speed limit. In this case, the algorithm cannot assign him an expected arrival time just after the green light turns on because there is another vehicle in front.

Fig. 8: Control algorithm 4 explanation

Therefore, intersection service rate is the limiting factor and vehicle 2 would be assigned an expected arrival time $3600/s$ seconds after vehicle 1.

Finally, see how vehicle 3 is able to enter the intersection travelling at the speed limit while also respecting the intersection capacity and the traffic lights. Speed limit would be the deciding factor in this third occurrence.

This thought process has been programmed as follows:

(Algorithm 4)

```

1   $ti_k^e = \max\left\{ta_k + \frac{L_1}{v_f}, ti_{k-1}^e + \frac{3600}{s}, t_{lg} + t_{ag}\right\}$ 
2  if  $ti_k^e > t_{lg} + GLP + YLP - t_{br}$ 
3       $n = 1$ 
4      while  $ti_k^e > t_{lg} + n \cdot (GLP + YLP + RLP) + GLP + YLP - t_{br}$ 
5           $n = n + 1$ 
6      end
7       $ti_k^e = t_{lg} + n \cdot (GLP + YLP + RLP) + t_{ag}$ 
8  end

```

Note that the arrival time of all the vehicles at the upstream road, even if they do not have V2I communication capabilities, must be known in order to more accurately calculate the expected arrival times at the intersection. For this reason, inductive loops need to be set at the start of the upstream road.

Several things can happen meanwhile a vehicle is on the road that can make its expected arrival time change its value, the main reason for this being the presence of non-equipped vehicles and its less predictable behavior. When this happens, the control system needs to be prepared to update the expected arrival time values and modify the indications given to equipped vehicles.

Notice that if inductive loops are also placed at the intersection entrance it would be possible to calculate the number of cars between the intersection and any given vehicle on the upstream road. Hence, with inductive loops present at both the start and the end of the upstream road, the next confirmation algorithm will be executed before sending any advisory speed limit indication. It first ensures service rate compatibility with previously updated values, being $c_k(t)$ the number of cars between vehicle k and the intersection entrance at time t , and later verifies that the newly assigned expected arrival times are in accordance with the traffic light signals.

Basically, the function of this algorithm is to update the values of expected arrival times at the intersection (ti_k^e) whenever there is a change, until they take the real value (ti_k) when a vehicle has already entered the crossing. It can be especially useful if the traffic lights change its cycle lengths, or if the loop detectors alert the system that a vehicle is running behind schedule, potentially affecting all the following vehicles.

Imagine, for example, that a vehicle is expected to enter the intersection 5 seconds from now, but thanks to the loop detectors it is possible to know that it still has three vehicles in front. With a service rate of 1800 vehicles/hour, the first part of the algorithm (lines 1-3) update its expected arrival to $3 \cdot 3600/1800 = 6$ seconds from now, and the second part (lines 4-11) makes sure that this newly assigned expected arrival time respects the future traffic light indications, assigning the vehicle to the next green cycle if necessary.

(Algorithm 5)

```

1  for  $r = 1: c_k(t)$ 
2       $ti_k^e = \max \left\{ ti_k^e, ti_{k-r}^e + r \cdot \frac{3600}{s} \right\}$ 
3  end
4  if  $t \leq t_{lg} + GLP + YLP - t_{br}$ 
5       $ti_k^e = \max \left\{ ti_k^e, t + c_k(t) \cdot \frac{3600}{s} \right\}$ 
6      if  $ti_k^e > t_{lg} + GLP + YLP - t_{br}$ 
7           $ti_k^e = \max \{ ti_k^e, t_{lg} + GLP + YLP + RLP + t_{ag} \}$ 
8      end
9  else
10      $ti_k^e = \max \left\{ ti_k^e, t_{lg} + GLP + YLP + RLP + t_{ag} + c_k(t) \cdot \frac{3600}{s} \right\}$ 
11 end

```

Note how the system needs to gather information from both the traffic lights and the inductive loops in order to more precisely calculate the expected vehicle arrival times at the intersection. Traffic lights must share the instant when the last green light turned on as well as the length of all the phases for that particular approach. On the other hand, inductive loops will need to be placed at the start and the end of the upstream road for the system to be aware of the instants of car arrival and departures from the upstream road, therefore being possible to calculate the number of cars in front of a given vehicle (between the vehicle and the intersection entrance).

3.2. Feedback Control System

With the updated value of expected arrival time at the intersection (ti_k^e), the Advisory Speed Limit control system is able to define at which speed should the car go to enter the intersection at its expected time. This speed (v_k^{ASL}) is the necessary one to travel the distance from the last known location to the intersection entrance with the time left until the expected arrival time.

As explained, the intersection entrance is located at $x = L_1$. Moreover, the last known location is the location of the car a period of time equal to the communication delay ago, $x_k(t - t_{com,k})$; plus the location error introduced by GPS inaccuracies, x_{error} . But since within a given communication type the network delay mean is known (t_{com}), the system is able to approximate the true location multiplying this network delay mean by the last known speed, $v_k(t - t_{com,k})$.

This approximation is more accurate when the communication delay of the vehicle involved is closer to the network delay mean, when the network delay is as low as possible and when in that period of time the vehicle has not changed its speed. However, GPS-introduced location error is not known and therefore not corrected.

Finally, the time left until the expected arrival time at the intersection is defined as $td_k^e - t$, and the 'ASL Equation' is defined as:

$$v_k^{ASL}(t) = \frac{L_1 - [x_k(t - t_{com,k}) + x_{error} + v_k(t - t_{com,k}) \cdot t_{com}]}{ti_k^e - t} \quad (13)$$

This speed modifies the car behavioral model replacing the speed limit in the acceleration part of Gipps' model, as seen in Equation 12.

4. ADVISORY SPEED LIMIT (ASL) ON ISOLATED INTERSECTIONS

As already explained, the ASL control system uses advanced notification of signal status to inform drivers on an optimum speed in order to produce delay, emission and fuel savings by avoiding hard-braking and hard-acceleration maneuvers.

In this study, the influence of several parameters in the performance of ASL technology are analyzed. These parameters are: market penetration rate of the system, traffic congestion level, communication network type (which affects the communication delay and the transmission range) and GPS accuracy.

In regards to the market penetration rates (MPR's), a few values are tested, so that in each scenario a different percentage of vehicles are equipped. Theoretically, even though only a small amount of the cars followed ASL indications, all the vehicles following them would also profit from this technology as they would smoothen their speed profile too. The market penetration rates simulated are 0%, 25%, 50%, 75% and 100%, and they state the probability that a randomly generated vehicle is equipped with ASL technology or not.

Fig. 9: Schematic representation of an isolated intersection

On an isolated intersection, vehicle arrivals are random. Traffic congestion levels are characterized by their mean time between car arrivals (λ), which is hypothesized and programmed to follow an exponential distribution inferiorly bounded by h_{min} . A mean of $\lambda = 4$ seconds is used to represent dense traffic situations whereas $\lambda = 8$ seconds is used for low traffic conditions. An intermediate situation of $\lambda = 6$ seconds is also simulated to characterize a medium level of traffic congestion. Therefore, the next equation is used to determine the arrival times of the vehicles at the upstream road:

$$ta_k = ta_{k-1} + \max\{h_{min}, \text{random_exponential}(\lambda)\} \quad (14)$$

Table 7: Market penetration and congestion level parameters used in the isolated intersection simulation

Parameter	Description	Values
MPR	market penetration rate	0%, 25%, 50%, 75%, 100%
λ	mean time between vehicle arrivals	4 s, 6 s, 8 s
h_{min}	minimum arrival headway (minimum time between arrivals)	0.5 s

All the possible parameter combinations are run in the simulator on a single-lane road with only through movements permitted. Only one approach of the intersection is considered, as with the signal allocation and the network characteristics described all the approaches happen to be identical. Besides the already mentioned hypothesis, a few other are considered and are stated below:

- Roads and intersection are initially empty (no vehicles)

- All the vehicles are generated at the start of Road 1 and they exit the system at the end of Road 2 (no vehicles enter or exit the road in any other way than the stipulated, i.e. no parking or turning). Therefore, isolated intersections are open systems in the sense that vehicles get out after finishing their journey.

For each combination of market penetration rate (5 rates), mean time between arrivals (3 levels of congestion), communication network (cellular vs. DSRC) and GPS location error (3 values), 200 simulations are executed, obtaining the following average results.

4.1. Influence of the Market Penetration Rate and the Communication Network

The next graphs show the average results sorted by MPR percentage, for all the traffic congestion levels simulated and error-less GPS characteristics, depending on the communication network. The first and second row of graphs represent, respectively, the average waiting time (in seconds) and the average fuel economy (in liters/100km) of the vehicles and their 95% Confidence Intervals (CI). The third row show the average pollutant emissions.

Fig. 10: Waiting time (error-less GPS) on (a) cellular networks or (b) DSRC networks

Fig. 11: Fuel economy (error-less GPS) on (a) cellular networks or (b) DSRC networks

Fig. 12: Average emission levels (error-less GPS) on (a) cellular networks or (b) DSRC networks

In the previous figures it can be seen how as the market penetration rate increases so the benefits do, but it is not clear whether results are different depending on the network characteristics. For this reason, numerical results are presented below and will be the standard method for comparing results in this thesis from now on. The following table shows the improvements over 0% MPR on both networks (to clarify, negative values found in tables mean that a particular output has decreased):

Table 8: Improvements over 0% MPR with both cellular and DSRC networks (error-less GPS)

	Cellular networks				DSRC networks			
MPR	25%	50%	75%	100%	25%	50%	75%	100%
Average Wait	-5,1%	-8,1%	-10,2%	-14,6%	0,0%	-4,8%	-9,4%	-10,8%
Average HC	-1,5%	-1,9%	-2,1%	-2,6%	-0,5%	-0,9%	-1,1%	-1,1%
Average CO	0,0%	0,1%	0,1%	-0,3%	0,7%	0,6%	0,6%	0,7%
Average NO _x	-5,9%	-7,8%	-8,2%	-9,1%	-3,3%	-4,3%	-4,7%	-4,8%
Average CO ₂	-4,7%	-6,2%	-6,8%	-8,0%	-2,7%	-4,2%	-5,0%	-5,3%
Average Fuel Economy	-4,6%	-6,2%	-6,7%	-7,9%	-2,7%	-4,1%	-5,0%	-5,3%

Numerical results show that the implementation of the Advisory Speed Limit could report improvements of over 14% on vehicles average waiting time, almost 8% on average fuel economy and up to 9% on some pollutant emissions. Improvements are appreciably better if Vehicle-to-Infrastructure communication is carried out over cellular networks instead of DSRC.

4.2. Influence of the Location Accuracy

Previous results show that cellular networks perform better than DSRC with error-less GPS characteristics. In this section, the influence of under-estimation and over-estimation in the GPS location is analyzed, as it is of common awareness that current GPS technology may introduce location errors. The next graphs and table show the average results for all the traffic congestion levels simulated sorted by market penetration rate, for under-estimated GPS location, depending on the communication type:

Fig. 13: Waiting time (GPS under-estimation) on (a) cellular networks or (b) DSRC networks

Fig. 14: Fuel economy (GPS under-estimation) on (a) cellular networks or (b) DSRC networks

Table 9: Improvements over 0% MPR with both cellular and DSRC networks (GPS under-estimation)

MPR	Cellular networks				DSRC			
	25%	50%	75%	100%	25%	50%	75%	100%
Average Wait	-2,0%	-2,3%	-5,1%	-7,6%	-2,3%	-0,6%	-4,8%	-6,7%
Average HC	-0,9%	-0,7%	-0,6%	-0,6%	-0,7%	-0,4%	-0,6%	-0,5%
Average CO	0,8%	1,5%	1,8%	2,1%	0,5%	1,2%	1,3%	1,5%
Average NO _x	-5,4%	-6,6%	-7,0%	-7,1%	-3,4%	-4,2%	-4,5%	-4,7%
Average CO ₂	-3,4%	-3,9%	-4,2%	-4,4%	-2,5%	-2,7%	-3,2%	-3,3%
Average Fuel Economy	-3,4%	-3,8%	-4,2%	-4,4%	-2,5%	-2,7%	-3,2%	-3,3%

With the introduced GPS error (under-estimated location), results on both cellular and DSRC networks are appreciably worse than without location error, but benefits are still evident. Once again, cellular networks are preferable than DSRC networks, with improvements of nearly 8% on average waiting time and over 4% in fuel consumption. Over cellular networks, carbon monoxide emissions increased slightly with market penetration, whereas emissions of other pollutants could be decreased between 1% and 7%.

Next, results obtained with over-estimation in the GPS location are presented, both with charts and in a table format:

Fig. 15: Waiting time (GPS over-estimation) on (a) cellular networks or (b) DSRC networks

Fig. 16: Fuel economy (GPS over-estimation) on (a) cellular networks or (b) DSRC networks

Table 10: Improvements over 0% MPR with both cellular and DSRC networks (GPS over-estimation)

	Cellular networks				DSRC			
MPR	25%	50%	75%	100%	25%	50%	75%	100%
Average Wait	11,7%	28,7%	48,2%	85,1%	12,3%	27,9%	51,1%	96,1%
Average HC	-0,3%	1,1%	3,0%	6,8%	0,0%	1,1%	3,3%	7,8%
Average CO	1,4%	3,2%	5,3%	9,3%	1,2%	2,6%	5,0%	9,6%
Average NO _x	-6,5%	-8,2%	-8,7%	-7,8%	-4,2%	-5,5%	-5,6%	-4,2%
Average CO ₂	-2,9%	-1,7%	0,7%	6,0%	-2,0%	-1,0%	1,9%	8,2%
Average Fuel Economy	-2,9%	-1,6%	0,8%	6,1%	-2,0%	-0,9%	1,9%	8,2%

It is surprising how average waiting times are extremely sensitive to over-estimation in the location (increasing particularly on intense traffic levels) and how, in general, the benefits of ASL strategies are completely cancelled. Pollutant emissions, as well as fuel consumption, increased between 6% and 10%, except for NO_x emissions, which were the only to decrease in this scenario. Again, DSRC networks performed worse than cellular networks.

To understand the underlying reasons behind this results, individual simulations were observed. Under-estimating vehicles' location resulted in the system believing that drivers were further to the intersection than they really were, so higher speed indications were given. When equipped vehicles adjusted their speed to follow ASL indications, they found that they arrived earlier than expected to the intersection. The first vehicle of each platoon arrived at the intersection when the light was still red, so the driver had to start breaking before he could react to the light turning green. In consequence, all the vehicles could still enter the intersection during their expected green light cycle, but less smooth speed profiles were achieved (which is known to increase fuel consumption and emissions).

On the other hand, over-estimated locations resulted in the system thinking that vehicles were closer to the intersection than they really were, therefore sending slower ASL indications. This led to vehicles arriving late at the intersection and having to stop at red lights waiting for the next green cycle, when they could have easily passed the intersection if they had arrived a few seconds earlier. Basically, over-estimating the location resulted in a decrease of the effective green time.

In conclusion, the influence of location error cannot be neglected as the system has proven to be very sensitive to over-estimation, even though perhaps this could be compensated by purposely introducing under-estimation error in the programming.

4.3. Influence of Traffic Congestion

As expected, simulations have far different results if sorted by mean time between arrivals, being higher the delays, fuel consumption and emissions while the traffic got denser, as shown below:

Fig. 17: (a) Waiting time or (b) fuel economy sorted by mean time between arrivals on cellular networks (error-less GPS)

Finally, if the improvements over 0% MPR with the different traffic congestion levels simulated are compared, it is noticeable how ASL control can provide superior improvements in waiting time (-16%) with intermediate traffic density (regardless of the communication network). However, greater improvements in fuel consumption and emissions are possible with dense traffic (10% decrease in fuel consumption, and between 2% and 13% on pollutant emissions, much more than in low traffic conditions). The exact obtained numbers on cellular networks and error-less GPS location are:

Table 11: Improvements over 0% MPR for different traffic densities (cellular networks, error-less GPS)

(in %)	Low traffic				Intermediate traffic				Dense traffic			
MPR	25%	50%	75%	100%	25%	50%	75%	100%	25%	50%	75%	100%
Average Wait	-1,6	-5,1	-8,3	-13,1	-4,8	-7,0	-9,6	-16,3	-6,1	-9,2	-11,0	-14,5
Average HC	0,0	-0,1	-0,2	-0,5	-1,0	-1,2	-1,4	-2,0	-3,2	-4,0	-4,3	-5,0
Average CO	1,0	1,5	1,7	1,7	0,3	0,7	0,8	0,4	-1,0	-1,5	-1,9	-2,5
Average NO _x	-3,1	-4,6	-5,6	-6,2	-5,1	-6,8	-7,7	-8,4	-9,3	-11,6	-11,0	-12,3
Average CO ₂	-2,6	-4,0	-4,8	-5,7	-4,2	-5,5	-6,3	-7,5	-6,6	-8,5	-8,7	-10,1
Avg. Fuel Economy	-2,6	-3,9	-4,8	-5,6	-4,2	-5,4	-6,2	-7,4	-6,6	-8,5	-8,6	-10,0

5. ADVISORY SPEED LIMIT (ASL) ON LOOP INTERSECTIONS

To test the improvements that the Advisory Speed Limit control could provide in an intersection located inside a city's network grid, a minor modification of the previous case is programmed. To achieve this scenario, the road configuration has been changed into a loop or ring road, which is a closed system in the sense that every vehicle that leaves the downstream road finds itself another time on the upstream road leading to the same intersection. With this configuration it is possible to take into account queue spillback implications if the number of vehicles on the road is large enough. On this occasion, vehicle arrivals at the intersection are not random but instead depend on the green cycle of the previous intersection, which is also signalized.

Fig. 18: Schematic representation of a loop intersection

It is known that even with the new road configuration the simulation does not depict a real road network, as in this particular study all the intersections are exactly the same (same road lengths, no offset between green cycles, etc.) and there are no turns (no vehicles leaving or arriving), but the purpose of this study is just to provide a first approximation to the implications of non-arbitrary arrivals and see if the Advisory Speed Limit system would be able to achieve benefits.

Within this closed system, all the runway is considered “upstream road”. This means that if the transmission range is large enough, a vehicle starts receiving ASL indications for the next intersection just after leaving the current one. In the simulator, this is equivalent to:

Table 12: General parameters used in the loop intersection simulation

Parameter	Description	Value
L_1	length of the upstream road (Road 1)	990 m
L_{int}	length of intersection	10 m
L_2	length of the downstream road	0 m

As in the previous study, the ASL control system informs drivers on an optimum speed in order to produce delay, emission and fuel savings by avoiding hard-braking and hard-acceleration handling. Also, the influence of several parameters in the performance of ASL technology is analyzed. These parameters, as in the previous section, are: market penetration rate (MPR) of the technology, traffic congestion level, communication network type (which affects the communication delay and the transmission range) and GPS accuracy.

Again, several values of market penetration rates are tested, so that in each scenario a different percentage of vehicles lie equipped. The market penetration rates that are going to be simulated are the same as in the preceding section (0%, 25%, 50%, 75% and 100%), and they state the probability that a randomly generated vehicle is equipped with ASL technology or not.

A significant difference between this study and the isolated intersection study is in the way to define traffic congestion levels. In this case, instead of using the mean time between arrivals to characterize the congestion level, another indicator is employed: the number of cars on the track (COT), which is directly related to the car density. In this case, COT is equivalent to the car density expressed in vehicles/km, as the length of the loop is defined as $L_1 + L_{int} + L_2 = 1.000 \text{ m}$. A value of $COT = 24$ is utilized to represent dense traffic situations whereas $COT = 12$ is used to depict low traffic conditions. An intermediate situation of $COT = 18$ is also simulated to characterize a medium level of traffic congestion.

On a loop intersection, the position of the vehicles at the start of the simulation is random. Separation between vehicles is hypothesized and programmed to follow a normal distribution with a mean $\mu = (L_1 + L_{int} + L_2)/COT$, a standard deviation $\sigma = \sigma_x$, and inferiorly bounded by s_j . Therefore the next algorithm is used to determine the separations of vehicles (sp_k) at the beginning of the simulation:

(Algorithm 6)

```

1  for  $k = 1:COT$ 
2       $aux_k = \max \left\{ s_j, \text{random\_normal} \left( \frac{L_1 + L_{int} + L_2}{COT}, \sigma_x \right) \right\}$ 
3  end
4  for  $k = 1:COT$ 
5       $sp_k = aux_k \cdot \frac{L_1 + L_{int} + L_2}{\sum_{k=1}^{COT} aux_k}$ 
6  end

```

Table 13: Market penetration and congestion level parameters used in the loop intersection simulation

Parameter	Description	Values
MPR	market penetration rate	0%, 25%, 50%, 75%, 100%
COT	number of cars on the track ($\approx$ car density in vehicles/km)	12, 18, 24
σ_x	standard deviation of the separation between cars at simulation beginning	20 m

All the possible parameter combinations are run in the simulator on a single-lane road with only through movements permitted. Besides the already mentioned hypothesis of the simulator, a few other are considered, stated below:

- All the vehicles that leave the intersection start their journey again at the start of Road 1 with the same speed and acceleration (no vehicles enter or exit the road in any other way than the stipulated, i.e. no parking or turning)
- The first lap of each vehicle is not considered in the results

For each combination of market penetration rate (5 rates), number of cars on the system (3 levels of congestion), communication type (cellular vs. DSRC) and GPS location error (3 values), 200 simulations are executed, obtaining the following results.

5.1. Influence of the Market Penetration Rate and the Communication Network

The next graphs show the average results sorted by market penetration rate (including data from all the traffic congestion levels), error-less GPS characteristics, and depending on the communication network. Again, the first and second row of graphs represent, respectively, the average waiting time (in seconds) and the average fuel economy (in liters/100km) of the vehicles and their 95% Confidence Intervals (CI). Figure 20 shows the average emission levels.

Fig. 19: Waiting time (error-less GPS) on (a) cellular networks or (b) DSRC networks

Fig. 20: Fuel economy (error-less GPS) on (a) cellular networks or (b) DSRC networks

Fig. 21: Fuel economy (error-less GPS) on (a) cellular networks or (b) DSRC networks

In the previous figures it is seen how as the market penetration rate increases so do the improvement in results, but the numerical results presented in the following table make it easier to see the potential benefits in both mobility and environment over the 0% MPR “initial” situation (again, negative values mean that a particular output has decreased):

Table 14: Cellular vs. DSRC networks improvements over 0% MPR (error-less GPS)

MPR	Cellular networks				DSRC networks			
	25%	50%	75%	100%	25%	50%	75%	100%
Average Wait	-3,7%	-8,1%	-13,7%	-18,8%	-3,6%	-7,9%	-13,6%	-19,4%
Average HC	-0,4%	-1,1%	-1,8%	-2,5%	0,0%	-0,3%	-0,8%	-1,4%
Average CO	2,6%	2,9%	2,4%	1,8%	1,3%	1,3%	1,0%	0,5%
Average NO _x	-9,3%	-12,0%	-13,2%	-13,7%	-3,5%	-4,6%	-5,0%	-5,2%
Average CO ₂	-4,4%	-6,4%	-8,0%	-9,2%	-2,2%	-3,5%	-4,7%	-5,7%
Average Fuel Economy	-4,4%	-6,4%	-8,0%	-9,1%	-2,2%	-3,5%	-4,7%	-5,7%

With the loop configuration, simulation results show that the implementation of Advisory Speed Limit control could report improvements of around 19% on vehicles average waiting time and 9% on average fuel economy. Average carbon monoxide emissions seem to increase slightly, whereas emissions of other pollutants can be decreased between 2% and 14%. Improvements on waiting times are marginally better if V2I communication is carried out over DSRC networks, while over cellular networks it is possible to get much better fuel economy and emissions.

To further compare the advantages of using one kind of communication network over the other, the adjoining surface chart is exhibited. The graph shows the benefits of running Advisory Speed Limit communications over cellular networks instead of over DSRC networks on average fuel economy (as it is also very closely related to pollutant emissions), sorting at the same time by market penetration rate and by number of cars in the system (traffic congestion level).

Fig. 22: Fuel consumption savings using cellular networks over DSRC (error-less GPS)

The chart evidences how cellular networks can provide higher fuel consumption savings than DSRC networks, being the difference greater also when market penetration rate increases and traffic congestion level diminishes. The maximum difference in results (around 4% difference in fuel consumption) is therefore located on high MPR and low COT.

On the contrary, DSRC networks are able to provide lower waiting times than cellular networks with dense traffic and high market penetration rates (almost 5% better).

5.2. Influence of the Location Accuracy

After seeing how both networks perform with error-less GPS characteristics, the influence of under-estimating and over-estimating the GPS location is treated below. The next graphs and table show the averages for all the traffic congestion levels simulated sorted by market penetration rate, for under-estimated GPS location, depending on the communication network:

Fig. 23: Waiting time (GPS under-estimation) on (a) cellular networks or (b) DSRC networks

Fig. 24: Fuel economy (GPS under-estimation) on (a) cellular networks or (b) DSRC networks

Table 15: Cellular vs. DSRC networks improvements over 0% MPR (GPS under-estimation)

	Cellular networks				DSRC			
MPR	25%	50%	75%	100%	25%	50%	75%	100%
Average Wait	-2,3%	-4,2%	-6,3%	-8,1%	-0,1%	-0,2%	-0,2%	-0,4%
Average HC	0,0%	-0,1%	-0,2%	-0,3%	0,2%	0,4%	0,5%	0,5%
Average CO	3,1%	3,9%	4,2%	4,3%	1,6%	2,3%	2,7%	2,8%
Average NO _x	-9,2%	-11,7%	-12,6%	-13,0%	-3,6%	-4,8%	-5,3%	-5,5%
Average CO ₂	-3,7%	-4,9%	-5,5%	-6,0%	-1,1%	-1,5%	-1,6%	-1,6%
Average Fuel Economy	-3,7%	-4,8%	-5,5%	-5,9%	-1,1%	-1,5%	-1,6%	-1,6%

With the introduced GPS error (under-estimated location), results on both cellular and DSRC networks are appreciably worse than before, but in this case cellular networks clearly outperform DSRC networks on the results, with improvements of over 8% on average waiting time (vs. no improvement on DSRC networks) and almost 6% in fuel consumption. Over this network, carbon monoxide emissions increase slightly with market penetration, whereas emissions of other pollutants can be decreased by as much as 13%.

Simulation results with over-estimation in the GPS location are displayed below, both with charts and in a table format:

Fig. 25: Waiting time (GPS over-estimation) on (a) cellular networks or (b) DSRC networks

Fig. 26: Fuel economy (GPS over-estimation) on (a) cellular networks or (b) DSRC networks

Table 16: Cellular vs. DSRC networks improvements over 0% MPR (GPS over-estimation)

MPR	Cellular networks				DSRC			
	25%	50%	75%	100%	25%	50%	75%	100%
Average Wait	6,9%	18,0%	31,2%	47,1%	8,9%	21,1%	32,9%	49,3%
Average HC	0,1%	0,4%	0,8%	1,4%	0,7%	1,4%	2,4%	3,9%
Average CO	3,4%	4,7%	5,5%	6,2%	1,9%	3,2%	4,4%	6,0%
Average NO _x	-10,1%	-13,9%	-16,1%	-17,5%	-3,9%	-5,7%	-6,2%	-6,0%
Average CO ₂	-3,5%	-3,8%	-3,3%	-2,1%	-0,9%	-0,3%	1,0%	3,0%
Average Fuel Economy	-3,4%	-3,8%	-3,2%	-2,1%	-0,9%	-0,3%	1,0%	3,0%

It is noticeable how average waiting times are also very sensitive to over-estimation in the location (even though less than in isolated intersections). Again, cellular networks performed better than DSRC networks, providing over 2% improvements in fuel economy and carbon dioxide emissions, and over 17% decline in nitrogen oxides. On the other hand, hydrocarbon and carbon monoxide emissions increased between 1% and 6% with over-estimated GPS location.

The reasons for this behavior with under-estimated and over-estimated location are the same than with the previous road configuration, and are explained in Section 4.

5.3. Influence of Traffic Congestion

As expected, simulations have far different results if sorted by car density, being higher the delays, fuel consumption and emissions while the traffic got denser, as shown below:

Fig. 27: (a) Waiting time or (b) fuel economy sorted by number of cars on the track on cellular networks (error-less GPS)

Finally, if the improvements over 0% MPR for each traffic congestion level simulated are compared, it is noticeable how ASL control can provide superior improvements in waiting time (over 26% fall) with low traffic density (regardless of the communication network). However, greater improvements in fuel consumption and emissions are possible with dense traffic (almost 10% decline in fuel consumption, and between 0% and 16% on pollutant emissions). The exact obtained numbers on cellular networks and error-less GPS location are:

Table 17: Cellular network improvements over 0% MPR for different traffic congestion levels, on error-less GPS

MPR	Low traffic				Intermediate traffic				Dense traffic			
	25%	50%	75%	100%	25%	50%	75%	100%	25%	50%	75%	100%
Average Wait	-7,9	-13,1	-21,1	-26,4	-3,0	-7,0	-10,6	-15,4	-1,8	-5,9	-11,6	-16,7
Average HC	-0,4	-0,9	-1,6	-2,1	-0,1	-0,5	-1,1	-1,6	-0,8	-1,7	-2,7	-3,6
Average CO	2,1	2,3	2,0	1,6	3,1	3,8	3,6	3,2	2,6	2,5	1,7	0,8
Average NO _x	-7,3	-9,4	-10,6	-11,0	-9,0	-12,1	-13,2	-13,6	-11,5	-14,4	-15,6	-16,3
Average CO ₂	-4,6	-6,4	-8,3	-9,4	-4,2	-6,3	-7,5	-8,6	-4,5	-6,6	-8,3	-9,7
Avg. Fuel Econ.	-4,6	-6,4	-8,2	-9,3	-4,1	-6,2	-7,4	-8,5	-4,5	-6,5	-8,2	-9,6

6. INFLUENCE OF THE CAR-FOLLOWING MODEL

In previous sections, it has been proven that Advisory Speed Limit (ASL) strategies can provide benefits in a different array of situations. In this chapter, three car-following models are compared to see if the results are sensitive to the car behavioral model. Gipps' model results are compared with results of both Intelligent Driver Model (IDM) and a corrected version of Optimal Velocity Model (OVM), on an isolated intersection configuration, with ASL indications over cellular networks and error-less GPS.

First of all, the two newly mentioned models and their characteristics are discussed. Next, the obtained results are compared. The same market penetration rates and traffic congestion levels as in Section 4 are simulated with IDM and OVM, executing 200 simulations for each parameter combination.

6.1. Intelligent Driver Model (IDM) with Bounded Acceleration

Again, the behavior of the following cars does not depend on the color of the traffic lights. On a single-lane road, the acceleration of these vehicles at any given time is just a function of the speed of the vehicle immediately ahead, the speed of the follower itself and the distance between them. Note that no overtaking is considered. In this model, the vehicle acceleration cannot be greater than a_{fw} and the deceleration cannot be inferior than $-a_{br}$.

Intelligent Driver Model equations [17] read as follows:

$$a_k(t) = \max \left\{ -a_{br}, a_{fw} \cdot \left[1 - \left(\frac{v_k(t)}{v_f} \right)^\delta - \left(\frac{s_k^*(t)}{x_{k-1}(t) - x_k(t)} \right)^2 \right] \right\} \quad (15)$$

Where:

$$s_k^*(t) = s_j + \max \left\{ 0, v_k(t) \cdot T_h + \frac{v_k(t) \cdot [v_k(t) - v_{k-1}(t)]}{2 \cdot \sqrt{a_{fw} \cdot a_{br}}} \right\} \quad (16)$$

The acceleration is divided into a "desired" acceleration $a_{fw} \cdot \left[1 - (v_k(t)/v_f)^\delta \right]$ on a free road, and a braking deceleration induced by the preceding vehicle. The acceleration on a free road decreases from the initial acceleration a_{fw} to zero while the automobile's velocity approaches the specified speed limit, defined as v_f for non-equipped vehicles and as $v_k^{ASL}(t)$ for vehicles with V2I communication.

The braking term is based on a comparison between the "desired dynamical distance" s^* , and the actual gap to the front vehicle. If the actual spacing is approximately equal to s^* , then the braking deceleration part of the model essentially compensates the free acceleration part, so the resulting acceleration is nearly zero. Therefore, s^* corresponds to the gap when following other vehicles in steadily flowing traffic. In addition, s^* augments dynamically when approaching slower vehicles and decreases when the vehicle in front is advancing faster. As a consequence, the imposed braking deceleration increases with decreasing distance to the front vehicle (drivers want to maintain a certain safety distance), increasing own speed (the safety distance lengthens) or increasing speed difference to the front vehicle (when approximating the forward vehicle at a too high rate, a dangerous situation may take place).

The model parameters values used in the simulations are:

Table 18: Intelligent Driver Model (IDM) parameters used in the simulation

Parameter	Description	Value
T_h	safe time headway	1.5 s
δ	acceleration exponent	4

6.2. Corrected Optimal Velocity Model (OVM)

The concept of this microscopic traffic flow model is, as a matter of fact, quite simple: each driver tries to achieve an optimal velocity based on the distance to the preceding vehicle. This was an alternative possibility explored recently in car-following models. The formulation is based on the assumption that the desired speed depends on the distance headway with the previous vehicle, being v^{opt} the optimal velocity^{18, 19, 20}:

$$v_k^{opt}(t) = \min \left\{ v_f, \max \left\{ 0, \frac{x_{k-1}(t) - x_k(t) - s_j}{\tau} \right\} \right\} \quad (17)$$

Therefore the acceleration for the Optimal Velocity Model with bounded acceleration is given by:

$$a_k(t) = \max \left\{ -a_{br}, \min \left\{ a_{fw}, \left(\frac{1}{T} \right) \cdot (v_k^{opt}(t) - v_k(t)) \right\} \right\} \quad (18)$$

Nevertheless, the presence of traffic lights and stopped traffic suppose that the previous equations are not enough to ensure that the vehicles brake properly, resulting in car crashes or vehicles skipping red lights. A correction to the model is added to guarantee that the appropriate safety distance is respected, even though the desired maximum braking deceleration can sometimes be surpassed:

$$x_k(t + \Delta t) \leq x_{k-1}(t) - s_j - \frac{1}{2} \cdot a_{br} \cdot \left(\Delta t - \sqrt{\frac{2 \cdot [x_{k-1}(t) - s_j - x_k(t)]}{a_{br}}} \right) \quad (19)$$

6.3. Results Comparison

The first row of graphs show the average waiting time and its 95% Confidence Interval (CI), the second row the average fuel economy and its 95% CI, and the third row contains the average emission levels (average data for all the traffic congestion levels simulated). On the left part of each row there are the results utilizing Gipps' car-following model (previously shown in Section 4), while on the center and the right part there are the results obtained utilizing IDM and OVM car-following models, respectively.

Fig. 28: Waiting time with (a) Gipps, (b) IDM or (c) OVM car-following models

Fig. 29: Fuel economy with (a) Gipps, (b) IDM or (c) OVM car-following models

Fig. 30: Emissions with (a) Gipps, (b) IDM or (c) OVM car-following models

Although the previous figures show that results are far different depending on the car-following model used (for example, with the Intelligent Driver Model waiting times can be over 80% higher, while fuel and emissions can be over 10% higher than with Gipps' model), there are also some similarities. The next table shows the improvements over 0% MPR with all three models:

Table 19: Improvements over 0% MPR using Gipps, IDM or OVM car-following models on cellular networks and error-less GPS

(in %)	Gipps				IDM				OVM			
MPR	25%	50%	75%	100%	25%	50%	75%	100%	25%	50%	75%	100%
Average Wait	-5,1	-8,1	-10,2	-14,6	-6,4	-12,5	-16,4	-20,7	-2,8	-6,2	-10,0	-13,4
Average HC	-1,5	-1,9	-2,1	-2,6	-2,6	-3,7	-4,2	-4,9	-5,9	-6,8	-7,2	-7,6
Average CO	0,0	0,1	0,1	-0,3	-0,3	-0,7	-1,0	-1,6	-4,7	-5,3	-5,7	-6,1
Average NO _x	-5,9	-7,8	-8,2	-9,1	-6,2	-7,7	-8,0	-8,2	-10,1	-12,1	-12,9	-13,4
Average CO ₂	-4,7	-6,2	-6,8	-8,0	-4,8	-6,6	-7,5	-8,6	-8,6	-10,9	-12,3	-13,3
Avg. Fuel Econ.	-4,6	-6,2	-6,7	-7,9	-4,7	-6,5	-7,4	-8,5	-8,5	-10,8	-12,2	-13,2

Even though the absolute results are highly distinct, the benefits that the presented green driving strategies can provide share some resemblance. With all the former car-following models, ASL technology is able to achieve significant improvements in both mobility and environment as the market penetration rate increases. Improvements on waiting time are more remarkable with Intelligent Driver Model (almost 21% decrease in waiting time vs. 15% with Gipps' model and 13% with OVM). On the other hand, ASL strategies are able to reduce fuel consumption and emissions the most with Optimal Velocity Model (over 13% drop in fuel economy vs. around 8% in the other models). Nitrogen oxides emissions are the ones which relatively can be reduced the most, and other emissions have shown falls of up to 13% depending on the model and the pollutant.

At last, if the improvements over 0% MPR are sorted by the different traffic congestion levels simulated, it is noticeable how ASL control can provide superior improvements in emissions and fuel consumption with dense traffic in all three models (incredible 20% drop in fuel consumption and some pollutant emissions with OVM). Also, both Gipps' model and IDM were able to achieve greater improvements in waiting time (over 30% drop with IDM) with intermediate traffic density, whereas with OVM the higher reductions in waiting time were accomplished with dense traffic levels. The exact improvements over 0% MPR obtained with IDM and OVM car-following models are:

Table 20: IDM improvements over 0% MPR for different traffic congestion levels, on V2I communication through cellular networks and error-less GPS

(in %)	Low traffic				Intermediate traffic				Dense traffic			
MPR	25%	50%	75%	100%	25%	50%	75%	100%	25%	50%	75%	100%
Average Wait	-3,8	-9,0	-11,1	-14,8	-10,8	-15,2	-21,9	-30,6	-5,2	-12,3	-15,4	-18,1
Average HC	-0,5	-0,7	-0,7	-0,8	-2,7	-3,4	-4,2	-5,3	-4,2	-6,1	-6,9	-7,7
Average CO	0,9	1,2	1,6	1,7	-0,6	-0,5	-1,1	-2,3	-0,9	-2,4	-2,9	-3,5
Average NO _x	-2,7	-3,6	-3,8	-3,8	-5,9	-7,2	-7,5	-7,4	-9,5	-11,5	-12,2	-12,6
Average CO ₂	-2,0	-3,2	-3,5	-4,0	-4,8	-6,0	-7,3	-9,1	-6,7	-9,4	-10,4	-11,2
Avg. Fuel Econ.	-2,0	-3,1	-3,4	-3,9	-4,7	-5,9	-7,2	-9,0	-6,6	-9,3	-10,2	-11,1

Table 21: Corrected OVM improvements over 0% MPR for different traffic congestion levels, on V2I communication through cellular networks and error-less GPS

(in %)	Low traffic				Intermediate traffic				Dense traffic			
MPR	25%	50%	75%	100%	25%	50%	75%	100%	25%	50%	75%	100%
Average Wait	-2,7	-6,6	-11,5	-12,1	-0,5	-5,0	-9,3	-12,3	-3,5	-6,5	-10,0	-14,0
Average HC	-0,3	-0,5	-0,7	-0,8	-2,3	-2,9	-3,2	-3,5	-12,6	-14,2	-14,9	-15,6
Average CO	0,7	0,8	0,7	0,8	-1,1	-1,3	-1,6	-1,9	-11,2	-12,7	-13,3	-14,0
Average NO _x	-3,4	-5,0	-5,8	-6,4	-6,7	-8,5	-9,3	-9,6	-18,4	-20,8	-21,5	-22,0
Average CO ₂	-2,6	-4,5	-6,0	-6,9	-4,7	-6,9	-8,4	-9,5	-15,1	-17,7	-19,0	-20,0
Avg. Fuel Econ.	-2,6	-4,5	-6,0	-6,8	-4,7	-6,9	-8,3	-9,4	-15,0	-17,6	-18,9	-19,9

7. CONCLUSIONS

In this thesis, the Advisory Speed Limit (ASL) control strategies based on Vehicle-to-Infrastructure communication were studied to smooth vehicle trajectories in stop-and-go traffic. The problem was formulated with the feedback control theory, in which improvements in delays, fuel economy and emissions were first studied in an isolated intersection and then in a loop intersection. Control algorithms for the calculus of ASL indications were proposed, and the effects of several parameters in the results were analyzed, namely market penetration rate, traffic congestion level, communication network and location accuracy, as well as the car-following model itself.

Through simulations, the effectiveness of this control strategy was demonstrated in multiple scenarios, concluding that high market penetration rates will make possible to achieve remarkable improvements in average delay, fuel economy and emissions, and that this is certainly an encouraging alternative for individuals in the near future. In particular, it was found that the system would perform better over cellular networks than over DSRC networks (therefore being more important a higher transmission range than a lower delay), with the added benefit of the system being able to work thanks to a smartphone application solely, without implying general modifications in the vehicle.

Also, it was seen how average waiting times are very sensitive to location over-estimation with the designed strategy, and that this perhaps could be resolved by purposely introducing a fixed under-estimation error in the vehicles' location, even though sacrificing greater improvements in fuel economy and pollutant emissions. At last, it was observed that improvements can be obtained either on isolated or non-isolated intersections, and using diverse car-following models.

8. FUTURE DIRECTIONS

After discussing the influence of each of the studied parameters on ASL control strategies, it would be interesting to extend the current study in several other directions. A list of proposed future work is:

- Field-test the effectiveness of ASL strategies in real life to verify the results
- Results have been encouraging enough to at least consider this kind of strategies in the future, therefore being important to know the improvements at even lower market penetration rates (probably between 1% and 10%) to observe short term benefits
- Even though the implementation of ASL technology could provide benefits, would it be possible to obtain the goals of this project (reduce vehicle stopping time, fuel consumption and emissions) by just changing the state of the traffic lights and the duration of its phases (Signal Timing Change –STC- control)?
- Consider large networks (see figure below), adding the possibility to perform right and left turns, or even multi-lane roads

Fig. 31: Network grid

- Placing initial inductive loops on each road would help to know how many vehicles are on the road and therefore improve ASL indications, but it would require a lot of infrastructural change and resources. It would be interesting to know how would the system perform without knowing the exact number of vehicles on the road (non-equipped vehicles would appear “invisible” to the system). A simple modification of some of the ASL operation algorithms could provide an answer to this discussion, which will probably be studied in the future
- Vehicle-to-Infrastructure (V2I) communication has proven successful in managing intersection traffic by reducing delays, emissions and fuel consumption. Would Vehicle-to-Vehicle (V2V) communication be able to outperform or complement V2I communication on the scenarios studied in this thesis?
- The benefits of ASL control in intersections with a cycle length of 60 seconds has been studied, but most certainly the cycle length could impact the results. Future study could consider the effects of different cycle lengths or even non pre-timed (actuated) traffic lights
- Study similar strategies for autonomous vehicles (smaller reaction times)
- Discuss GPS delay implications (take into account that the position of the GPS updates every 1s approximately)

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