

1 **BOND-SLIP RESPONSE OF STEEL FIBERS AFTER EXPOSURE TO ELEVATED**
2 **TEMPERATURES: EXPERIMENTAL PROGRAM AND DESIGN-ORIENTED**
3 **CONSTITUTIVE EQUATION**

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14 **Keywords:** pullout; bond-slip response; hooked-end steel fibers; elevated temperatures; numerical simulation

15
16 **ABSTRACT**

17 This study aimed to evaluate the effect of elevated temperatures on the bond-slip behavior of
18 hooked-end steel fibers. A total of 180 pullout specimens were tested in post-cooling conditions
19 using a double-sided pullout test with multiple embedded fibers for target temperatures between
20 25 and 750 °C. Results proved that the bond strength significantly increases for temperatures
21 up to 450 °C, and drastically decreases for temperatures of 600 and 750 °C. The contribution
22 of hooks reduced with temperature and is negligible for temperatures higher than 600 °C, while
23 the fiber-matrix frictional interaction seems to improve for all temperatures evaluated. A

24 temperature-sensitive constitutive equation that allows simulating the bond-slip behavior of
25 hooked-end steel fibers is proposed and its suitability confirmed through a numerical model.

26 1 Introduction

27 The fundamental principle of steel fiber reinforced concrete (SFRC) is based on the interaction
28 between fibers and the cementitious matrix to provide plain concrete a pseudo-ductile behavior
29 and enhance post-crack mechanical properties. The steel fibers bridge the cracks through the
30 matrix and enhance the post-crack tensile strength of the composite, which is a key feature for
31 structural applications [1,2]. Three main components that must be characterized to analyze these
32 composites after temperature exposure are the cementitious matrix, the fibers, and the fiber-
33 matrix interface. In this regard, the bond-slip response between the fiber and the cementitious
34 matrix is a key parameter to model the SFRC mechanical behavior [3] and is known to strongly
35 influence the post-crack behavior of the composite [4,5]. The bond-slip response of hooked-end
36 steel fibers in the cementitious matrix can be parameterized by pullout test results and can be
37 divided into five main stages [6], which are schematically shown in Figure 1.

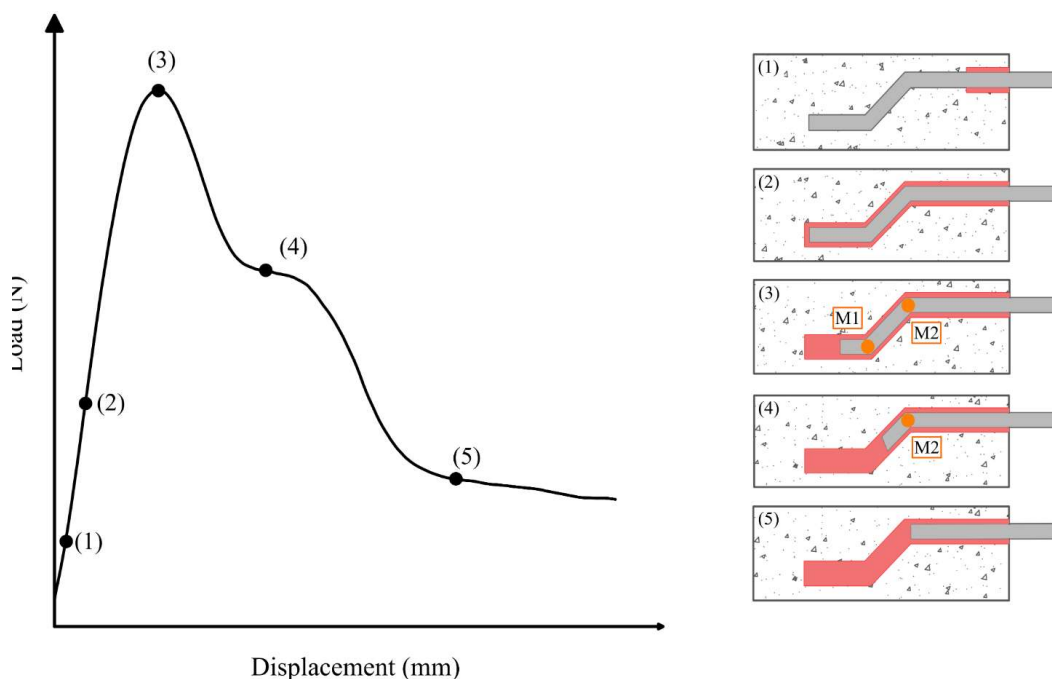


Figure 1 – Schematic diagram of the pullout mechanism for hooked-end steel fibers

40 Stage 1 and 2 are defined as the partial and full debonding between fiber and matrix,
41 respectively. Once the full debonding takes place, the dynamic frictional interaction between
42 fiber and matrix begins. At this stage, the fibers must undergo a considerable plastic
43 deformation due to the straightening of the hooks before the dynamic frictional interaction
44 occurs [6], which defines Stages 3 and 4. The mechanical interlocking caused by the plastic
45 deformation of the hooks at M1 and M2 increases the maximum pullout load value at Stage 3.

46 As soon as the tip of the fiber goes beyond M1, the pullout load substantially decreases and the
47 mechanical interlocking is caused only by the plastic deformation of the hook at M2. It is
48 important to remind that the matrix cracks as the pullout occurs [5] and that the energy required
49 to yield the hooks is intrinsically bound to the bending stiffness and the hook geometry of the
50 steel fiber, as well as the interfacial bond properties [7,8]. After the hook is completely
51 straightened, the dynamic frictional interaction between fiber and matrix takes place in Stage 5.
52 This last phase results in a rapid drop in the pullout load values and prevails until the whole
53 fiber is removed from the matrix pathway [6].

54 Pullout tests are conducted in a wide variety of setups in the literature. The difference between
55 methodologies adopted is usually related to the number of fibers embedded (single or multiple
56 fibers) and the method of applying the tensile force (single- or double-sided). The pullout tests
57 are commonly performed employing single-sided tests on a single fiber, owing to the simplicity
58 of the methodology during the preparation of specimens and during the test [6]. However, a
59 major drawback of this methodology is that the test setup needs to be capable of precision
60 measurements due to the intrinsically low pullout forces. More than that, difficulties
61 encountered in single-sided tests are mainly associated with the interaction between the grip
62 and the fiber. Also, high variability is common in single-sided tests on a single fiber, which
63 requires a considerable number of specimens to guarantee the reliability of the results [9].

64 The drawbacks of using single-sided tests with a single fiber are further aggravated for pullout
65 specimens that are exposed to elevated temperatures. This occurs because the pullout forces are
66 expected to reduce and the steel fiber mechanical properties to be negatively affected after high-
67 temperature exposure. Several studies have investigated the bond-slip properties of hooked-end
68 steel fibers at room temperature conditions in the last decades [9–12]. However, the studies
69 regarding the bond-slip behavior of steel fibers after elevated temperatures are very scarce in
70 the literature. In this sense, there is a need for identifying constitutive equations and analytical
71 formulations to the designers' community so that the effect of fire on SFRC structures can be
72 properly assessed.

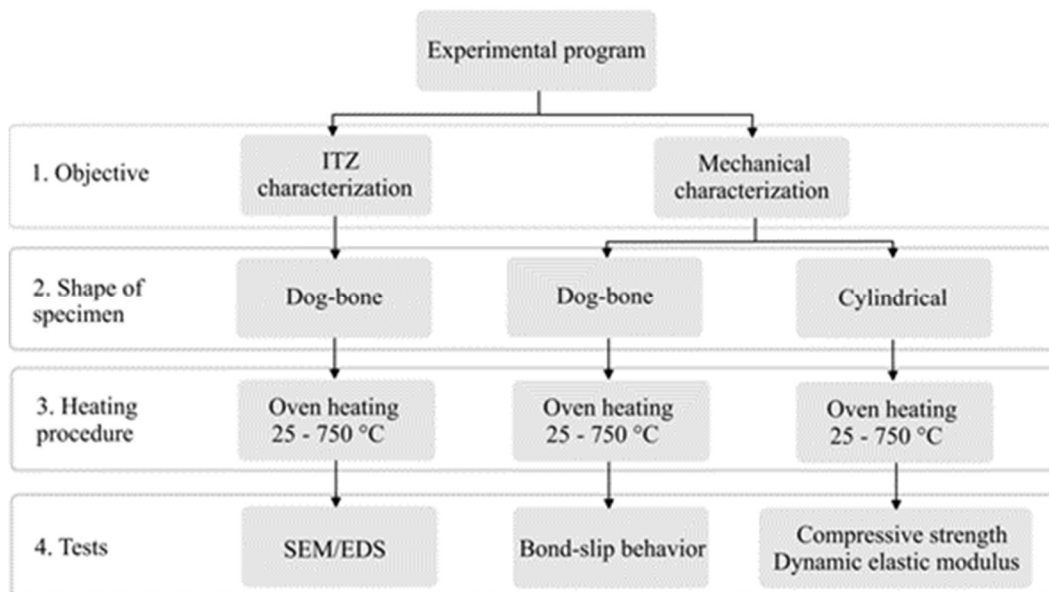
73 Results obtained by recent studies show that the pullout load values were comparable up to
74 ~400 °C and significantly reduced for higher temperatures [13–16]. However, the non-
75 significant effect of temperature up to 400 °C may be a side effect of the intrinsic dispersion of
76 single-sided tests with a single fiber, since the standard deviation values were omitted.
77 Moreover, numerical models focusing on the explicit and discrete representation of the steel
78 fibers in SFRC have been developed recently and require an accurate description of the steel
79 fiber bond-slip behavior as input [17,18]. So far, the results published in the literature have not
80 provided a microstructural based explanation for the changes in the bond-slip behavior or
81 proposed a constitutive equation for design purposes, which denotes that the topic still needs to
82 be deeply investigated.

83 The present study aims to evaluate the bond-slip behavior of hooked-end steel fibers after
84 exposure to elevated temperatures employing a double-sided pullout test using multiple fibers.
85 This test methodology aims at increasing the stability of the test and avoiding the drawbacks
86 associated with single-sided and single fiber pullout tests. The interfacial transition zone of the
87 steel fibers was characterized to assess the effect of temperature on the vicinity of the fiber and
88 relate the microstructural results with the mechanical behavior. Additionally, an analytical

89 model was proposed and the pullout tests were validated through numerical simulations using
90 a discrete and explicit representation of steel fibers inside the pullout specimens.

91 2 Materials and methods

92 Figure 2 shows a schematic drawing of the experimental program conducted in this study. The
93 investigation herein conducted took place within the framework of a Ph.D. research project
94 regarding the study of the effect of temperature on the properties of fiber-reinforced composites.
95 In this sense, all the characterizations were conducted using a mortar that followed the SFRC
96 mix design based on the work of Serafini et al. [19] and a detailed description and
97 characterization of the materials employed can be found in the referenced study. Even with
98 those considerations, a brief description is presented in this section.



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Figure 2 – Scheme adopted for the experimental program of this study

101 The bond-slip response of the hooked-end steel fibers was evaluated after exposure to high
102 temperatures. Based on the experimental results, an analytical equation that computes the effect
103 of temperature on the bond-slip behavior of steel fibers is proposed. This equation is used as
104 input for a refined numerical model that is capable of representing the steel fibers discretely and
105 explicitly inside the plain concrete [18]. As supplementary investigations, the characterization

106 of the interfacial transition zone (ITZ) is performed and aims to verify the effect of temperature
 107 on the vicinity of the fiber, which can be correlated with the bond-slip response. Additionally,
 108 the effect of temperature on the compressive strength and dynamic elastic modulus of the mortar
 109 were evaluated and serve as input for the numerical simulation conducted in this study.

110 **2.1 Materials**

111 The cementitious materials used in this study were a Type I Portland cement (CEM I 52.5R)
 112 and silica fume type Elkem 920-U. The particle packing was increased by using river and
 113 artificial sand as fine aggregates and two coarse granite aggregates. A polycarboxylate-based
 114 superplasticizer, GCP ADVA Cast 525, was used to provide consistency to the mix. A cold-
 115 drawn, hooked-end steel fiber, Dramix 3D 80/60-BG, was employed. This steel fiber was
 116 chosen since it is commonly used in structural applications. The explosive spalling phenomenon
 117 was mitigated by the addition of Neomatex FireX polypropylene microfibers. Table 1 shows
 118 fiber manufacturer data for both fiber types.

119 Table 1 – Fiber manufacturer data for both fiber types

Characteristics	Hooked-end steel fiber	Micro-synthetic fiber
Length (mm)	60	12
Diameter (mm)	0.75	0.03
Aspect ratio (l/d)	80	400
Specific weight (kg/m ³)	7850	910
Specific surface area (m ² /kg)	3.45	147
Melting point (°C)	~1370	165
Tensile strength (MPa)	1225	Not provided
Young modulus (GPa)	210	Not provided

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121 **2.2 Composition and preparation of mortar**

122 The composition of the mortar was based on the mix design of the precast segments used in
 123 tunnel linings of Subway Line 6 of São Paulo [19], which is described in Table 2. Silica fume

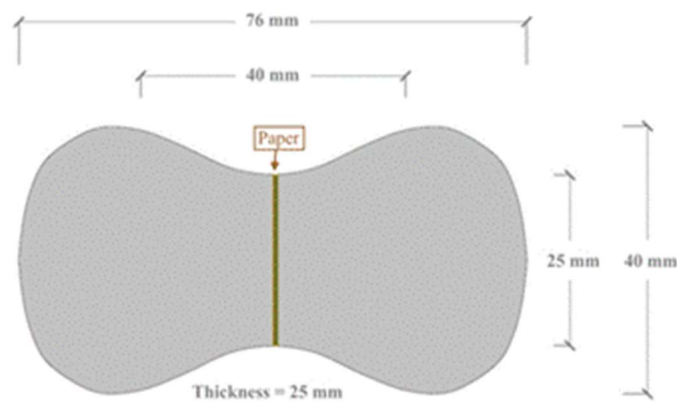
124 was used as supplementary cementitious material at a content of 5.5% of the cement mass, and
125 the w/cm ratio was kept constant at 0.39. All aggregates were oven-dried at 100 °C for 14 h
126 before mortar production. Synthetic micro-fibers were added in a content of 0.15% of the total
127 volume, or 1.4 kg/m³, according to project specifications, to avoid damage of the mortar due to
128 explosive spalling.

129 Table 2 – Dosage of materials to produce 1 m³ of mortar

Materials	Dosage (kg/m ³)
Portland cement	700
Silica fume	39
Water	289
Siliceous river sand	705
Artificial granite sand	471
Superplasticizer	5.25
Synthetic micro-fiber	1.4

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131 The mortar mixing was conducted by using a planetary Hobart N50 mixer with a total capacity
132 of 5 L in a room at (25 ± 1) °C. The following procedure was adopted: microfibers were added
133 to the bowl and dispersed with water for 90 seconds. This period was divided into 30-30-30
134 seconds in, respectively, low-high-low speed. Then, the fine aggregates, cement, and silica
135 fume were added during 60 seconds with the equipment turned off and 30 seconds were given
136 for particle wetting. At last, water and dry powder were mixed for 90 seconds, following the
137 same 30-30-30 seconds in low-high-low speed. The aforementioned mixing procedure was
138 adopted since it results in better homogenization of materials and microfibers according to
139 Dantas et al. [20]. A total of 30 cylindrical specimens with a diameter of 50 mm and a height
140 of 100 mm were produced to assess the compressive strength and the dynamic elastic modulus
141 of the material.

142 Pullout specimens in the shape of dog-bones were produced to assess the bond-slip behavior of
143 the hooked-end steel fibers. Figure 3 shows the dimensions of the pullout specimens produced.
144 The pullout specimens were manufactured using four steel fibers instead of the usual single
145 fiber, which had as objective to increase the stability of the test. This was adopted by the authors
146 as a countermeasure to the intrinsic low pullout load values of single-fiber pullout tests, which
147 are made even more severe by the exposure to elevated temperatures [13,14,16]. A total of 180
148 pullout specimens were produced and tested in this study.

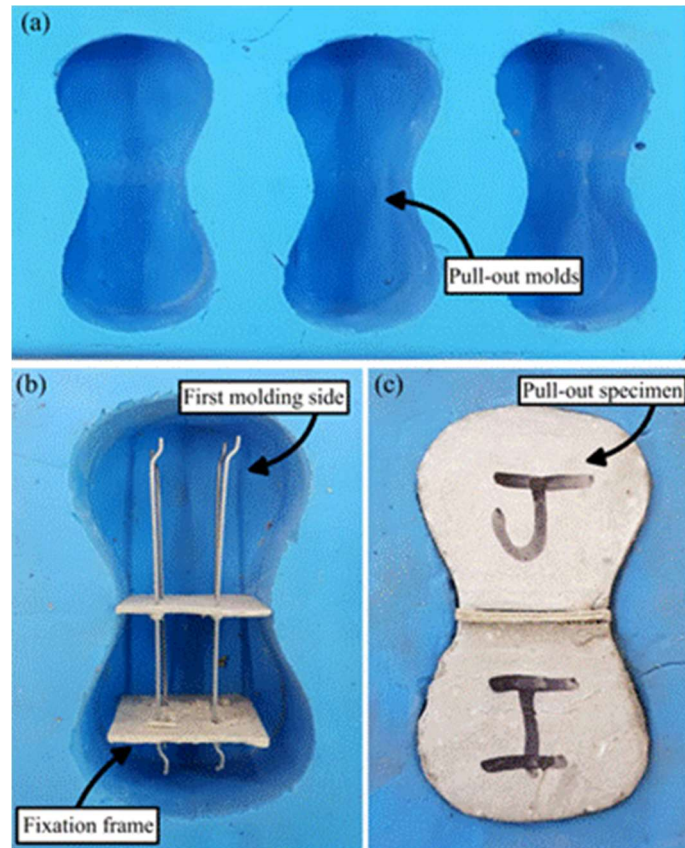


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Figure 3 – Dimensions of the pullout specimen produced

151 Figure 4 illustrates the molding procedure, the fixation frame, and the pullout specimen
152 produced. The four steel fibers were positioned in the middle of the molds with a measured
153 embedded length of 30 mm at each side and separated by a distance of 10 mm between the
154 fibers. Since the embedded lengths are the same on both sides, the pullout may occur from either
155 side without any detrimental effect on the results. In cases where different embedded lengths
156 are adopted, the methodology must ensure that the four fibers are pulled out from the same side
157 of the specimen to ensure the reliability of the results.



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Figure 4 – Molding procedure: (a) the pullout molds (b) fixation frame (c) pullout specimen

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Two papers of 250 g/m^2 were used to fix the steel fibers inside the mold. This procedure had the objective of preventing the steel fibers from moving or rotating inside the pullout specimens.

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After that, the mortar was poured inside one half of the mold. The embedded length was double-

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checked on the empty side of the mold and, after 4 hours, the fixation frame was removed, and

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the other half of the mold was filled with mortar. After the molding procedure, the pullout molds

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were sealed with a protective plastic film during 12 h until the specimens could be removed

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from the mold. After demolding, the pullout specimens were cured in a humid chamber for 72

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h and then stored at room temperature of $(25 \pm 1) \text{ }^\circ\text{C}$ until the age of 150 days to better simulate

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in situ humidity and curing conditions.

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2.3 Heating procedure

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The cylindrical and pullout specimens were heated using an EDG FC series electric oven, model

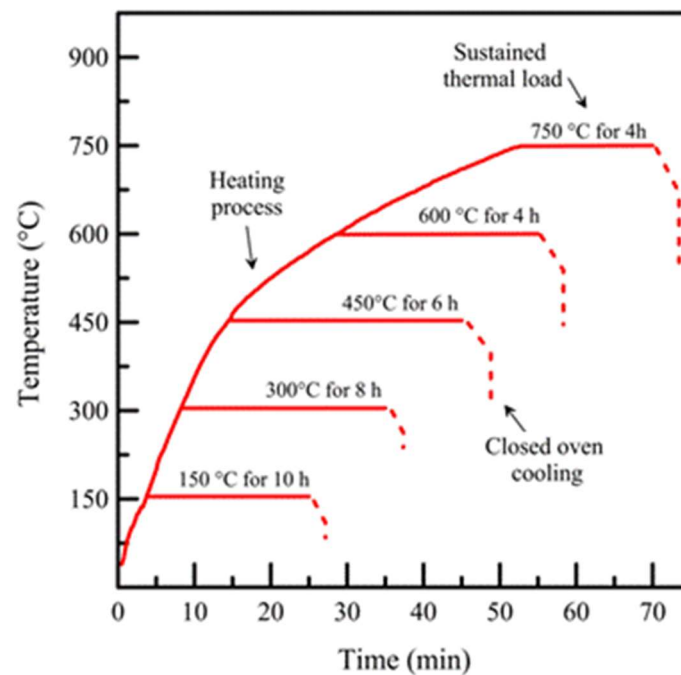
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EDG10P-S, at a heating rate of $(20 \pm 3) \text{ }^\circ\text{C}/\text{min}$ at the age of 150 days. The period at target

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temperature adopted was determined by numerical simulation to ensure the thermal stability of

173 the specimens based on the work of Carpio et al. [21]. Therefore, the pullout specimens were
174 kept at target temperatures during 10, 8, 6, 4, and 4 h for the respective temperatures of 150,
175 300, 450, 600, and 750 °C. After the heat exposure was over, the chamber was kept closed and
176 cooling until the room temperature was achieved for 24 h. The cooling rate was not controlled.
177 After cooling, both the cylindrical and pullout specimens were taken for mechanical testing.
178 Figure 5 shows the heating procedure adopted for the cylindrical and pullout specimens.



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Figure 5 – Heating procedure adopted for cylindrical and pullout specimens

181 2.4 Test method

182 2.4.1 Compressive strength test

183 The compressive strength tests were conducted on a Shimadzu Universal Testing Machine,
184 model UH-F1000kN, with a computer-controlled hydraulic servo system, and a maximum load
185 capacity of 1,000 kN. The test was load-controlled at a rate of 0.5 MPa/s and piston
186 displacement data was used to calculate the strain values during the test. A total of 30 specimens
187 were tested, 5 for each target temperature: 25, 150, 300, 450, 600, and 750 °C.

188 2.4.2 Ultrasonic pulse velocity test

189 The ultrasonic (US) propagation test was conducted by using a Portable Ultrasonic Non-
190 destructive Digital Indicating Tester (PUNDIT) equipment using 200 kHz transducers and a
191 circular cross-section with a 20 mm diameter. The US propagation velocity was determined in
192 the same specimens before and after temperature exposure and used to determine the dynamic
193 elastic modulus (E_c) of the mortar before and after temperature exposure, calculated as:

$$E_c = \frac{\rho \cdot V^2 \cdot (1 + \nu) \cdot (1 - 2\nu)}{1 - \nu} \quad \text{Eq. (1)}$$

194 where ρ is the density of the mortar (in kg/m^3); V is the propagation pulse velocity (in km/s);
195 ν is the Poisson's ratio). The density of the material was recalculated for each target temperature
196 based on the mass and volume of the specimens. Although data about the effect of temperature
197 on Poisson's ratio are relatively scarce and tend to be inconsistent, the results found in the
198 literature show that this property does not change significantly for small stress values [22].
199 Therefore, the Poisson's ratio was assumed to be constant at 0.2 for all target temperatures.

200 **2.4.3 Fiber-matrix interface**

201 The effect of elevated temperatures on the fiber-matrix interface was evaluated through
202 Scanning Electron Microscopy (SEM) with Energy Dispersive Spectroscopy (EDS) for a more
203 in-depth analysis of the results. Line scanning EDS analyses were conducted to obtain the
204 surface chemical profile concerning the radial distance from the fiber, represented by the red
205 line in the example presented in Figure 6.

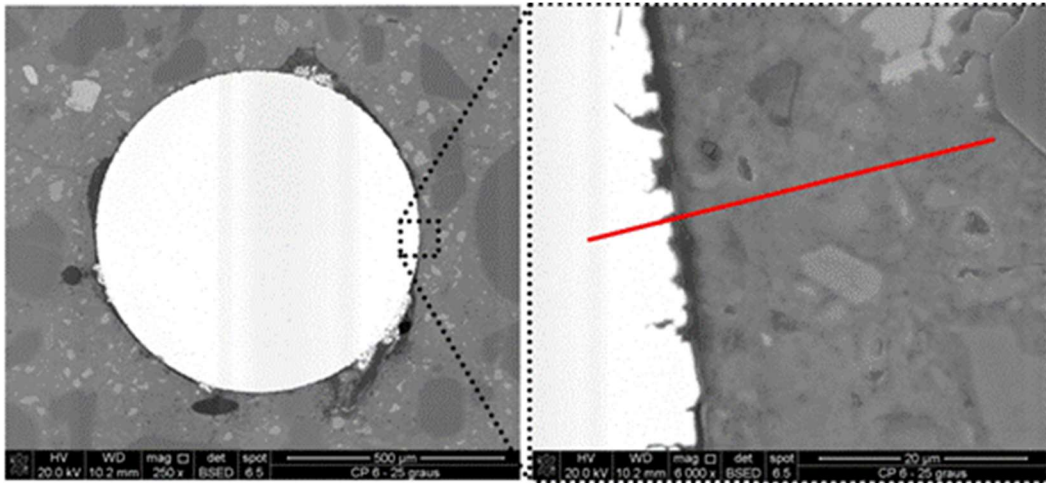


Figure 6 – EDS analysis conducted to obtain the surface chemical profile in the vicinity of the fiber

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Samples were prepared by using the dog-bone shaped pullout specimens after the heat procedure and mechanical testing was conducted. The pullout specimens were sliced with a precision saw and the region around the fiber was analyzed in samples measuring 25 x 25 x 25 mm. The samples were embedded in resin and plane ground employing 150 μm grained sandpaper and fine ground employing 9 μm grained sandpaper for 10 minutes at the 1000 and 150 rpm, respectively. After grinding, the samples were dry-polished using a 2 μm diamond polishing cloth specific for metallographic purposes. Samples were then taken for SEM/EDS analysis in the Center for Metallurgical and Materials Technologies (CTMM) at the Institute for Technological Research (IPT). SEM/EDS tests were conducted using a Quanta 3D FEG instrument, equipment at the voltage of 20 kV, working distance of 10 mm, using XT microscope control FEI software to obtain backscattered electron imagery.

The calcium (Ca) and silicon (Si) contents were determined by EDS and can be used as an indirect method to assess the composition of the cementitious matrix utilizing the Si/Ca ratio [23]. Additionally, the contents of iron (Fe), oxygen (O), and carbon (C) were determined and served as a means to assess the changes in steel and the location of fracture surfaces.

2.4.4 Pullout test

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Figure 7 illustrates the pullout test setup conducted in this study. The pullout tests were conducted using an electromechanical universal testing machine in an open-loop configuration,

226 EMIC DL 10000, with a load-cell with a maximum load capacity of 10 kN and precision of 1
227 N. The test was displacement-controlled at a rate of 0.5 mm/min. The load cell was placed on
228 the top of the machine crosshead to read the fiber pullout force while the slip between the fiber
229 and matrix was determined by piston displacement readings. The initial accommodation was
230 minimized by slowly applying the load to the specimens until some load was recorded by the
231 load cell before initiating the test.



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Figure 7 – Pullout test setup conducted in this study

234 The pullout test was stopped before the complete pullout of the fiber from the specimen
235 occurred. This was adopted because the failure criteria established into the design guidelines
236 (i.e. maximum crack width of 2.5 mm according to the *fib* Model Code 2010 [24]) is achieved
237 before the full embedded length (30 mm) is pulled out of the matrix. Therefore, the pullout tests
238 of this study were conducted until a displacement of 10 mm was achieved, since any result

239 obtained for greater displacement values would have no useful application from the engineering
240 standpoint. In this sense, 30 pullout tests were performed for each target temperature of 25, 150,
241 300, 450, 600, and 750 °C, representing a total of 180 specimens.

242 Furthermore, the pullout curves obtained from the pullout tests were normalized to be
243 representative of a single fiber pullout. This was achieved by dividing the pullout curves by the
244 amount of resisting fibers in each section of the test. This normalization was required to make
245 a valid comparison with the literature results. Additionally, the rupture of some fibers occurred
246 in specimens exposed to elevated temperatures, thus, this normalization was strictly necessary
247 to guarantee the validity of the comparison.

248 **2.4.5 Statistical analysis**

249 The compressive strength and dynamic elastic modulus of the mortar, as well as the results of
250 bond-slip results obtained in this study, were statistically analyzed through analysis of variances
251 (ANOVA) and Tukey tests [25]. The relationship between the sample size and the admissible
252 error was determined only for the variables associated with the bond-slip response of the
253 hooked-end steel fibers since this topic is the main contribution of this study. In this sense, the
254 relationship between the sample size and the admissible error was determined based on concepts
255 of inferential statistics [26], as follows:

$$n = \frac{s^2 \cdot z_\gamma^2}{\varepsilon^2} \quad \text{Eq. (2)}$$

256 where n is the required sample size; s is the standard deviation obtained by the pilot sample (in
257 MPa); z_γ is the Student's t-distribution value; ε is the admissible error for the test. The average
258 and standard deviation values were determined based on the experimental campaign conducted,
259 while a t-distribution value was adopted considering a confidence interval of 95% and $(n - 1)$
260 degrees of freedom.

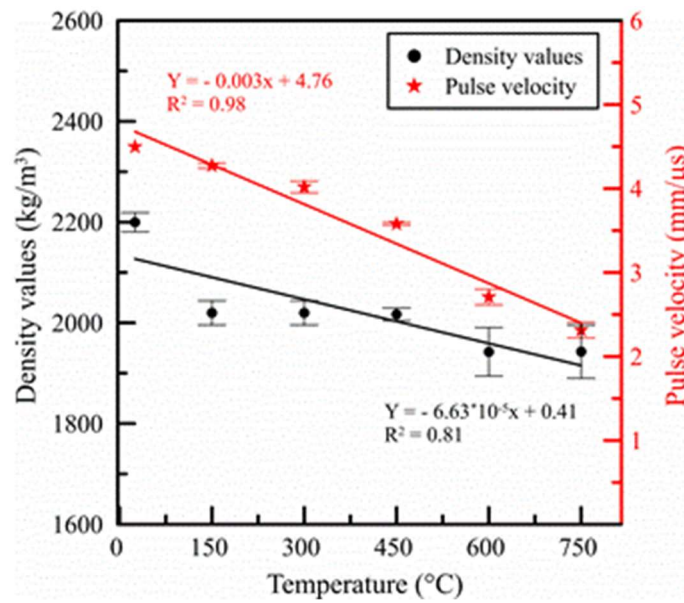
261 **3 Results and discussion**

262 **3.1 Compressive strength and elastic modulus**

263 Figure 8 illustrates the density values and pulse velocity changes as a function of temperature.

264 Table 3 shows the average results for the density and pulse velocity of mortar before and after

265 temperature exposure.



266

267 Figure 8 – Average density values and pulse velocity changes as a function of temperature

268 Table 3 – Average results for the density and US propagation velocity of the mortar

Temperature (°C)	Before temperature exposure		After temperature exposure	
	Density (kg/m ³)	Pulse velocity (mm/μs)	Density (kg/m ³)	Pulse velocity (mm/μs)
25	2200 (± 19)	4.50 (± 0.06)	Not applicable	Not applicable
150	2186 (± 23)	4.52 (± 0.04)	2020 (± 24)	4.27 (± 0.03)
300	2192 (± 16)	4.52 (± 0.06)	2020 (± 24)	4.02 (± 0.07)
450	2212 (± 9)	4.52 (± 0.11)	2017 (± 13)	3.58 (± 0.02)
600	2202 (± 25)	4.53 (± 0.08)	1942 (± 48)	2.71 (± 0.09)
750	2186 (± 23)	4.50 (± 0.11)	1943 (± 53)	2.31 (± 0.09)

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270 The reductions in density values were of 7.6%, 7.9%, 8.8%, 11.8%, and 11.1% for the respective

271 temperatures of 150, 300, 450, 600, and 750 °C. Reductions were also observed in terms of the

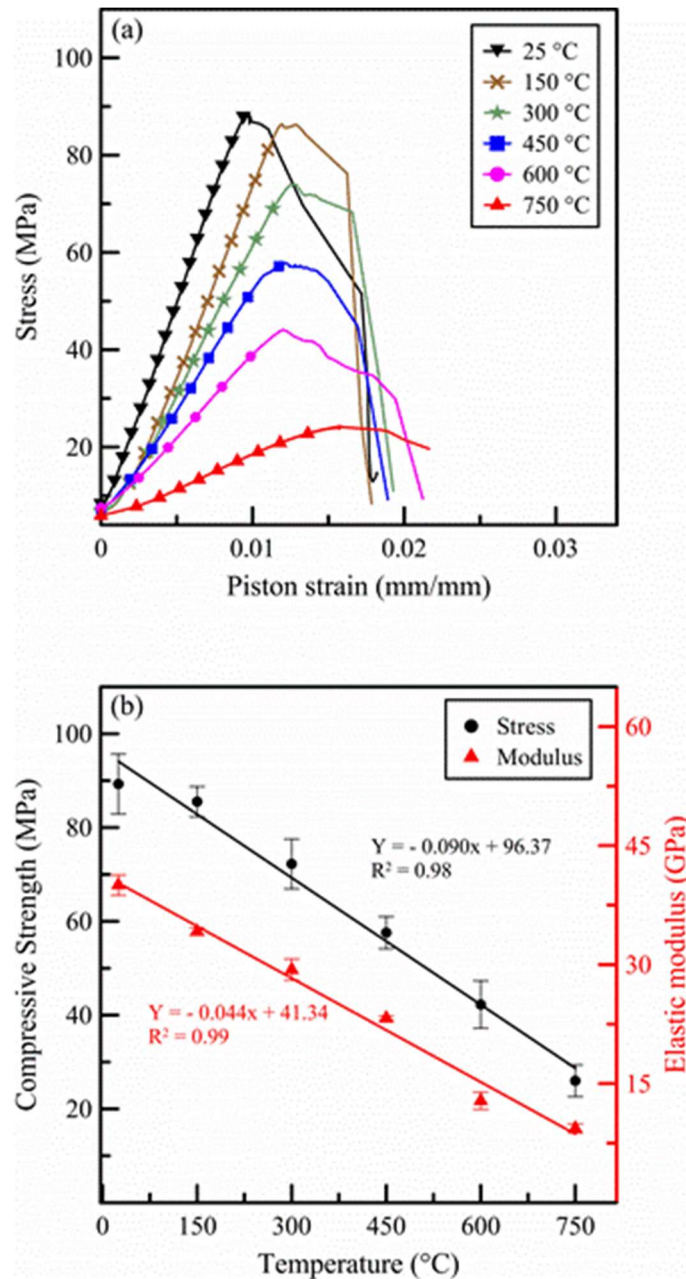
272 ultrasonic pulse velocity, which were 5.4%, 11.1%, 20.9%, 40.3%, and 48.5% for the same
 273 respective temperatures. As temperature increases, the release of free water and the dehydration
 274 of hydrated products of the cement paste occurs [19,27]. This dehydration is responsible for the
 275 reduction in the specific surface area of the hydrates and the coarsening of the pore structure,
 276 which increases the porosity of the cement paste [27,28], the increase in capillarity pore size,
 277 and the generation of cracks [29]. The aforementioned changes significantly contribute to the
 278 reductions in terms of density values and ultrasonic pulse velocity evidenced in this study.

279 Figure 9 shows the stress-strain curves and the residual values of compressive strength (f_c) and
 280 dynamic elastic modulus (E_c) as a function of temperature for the mortar used in this study. The
 281 average results can be found in Table 4. Specimens tested at room temperature presented an
 282 average compressive strength of 89.3 MPa and an average elastic modulus of 40.0 GPa.

283 Table 4 – Average results in terms of mechanical properties for each target temperature

Target temperature (°C)	f_c (MPa)	E_c (GPa)
25	89.3 (\pm 6.4)	40.0 (\pm 1.3)
150	85.5 (\pm 3.2)	34.2 (\pm 0.5)
300	72.3 (\pm 5.3)	29.4 (\pm 1.3)
450	57.6 (\pm 3.4)	23.2 (\pm 0.3)
600	42.3 (\pm 5.0)	12.8 (\pm 1.1)
750	26.0 (\pm 3.4)	9.4 (\pm 0.6)

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286 Figure 9 – (a) Stress-strain curves and (b) residual values of compressive strength and dynamic elastic modulus

287 as a function of temperature

288 The residual compressive strength values after temperature exposure of 150, 300, 450, 600, and

289 750 °C were, respectively, 4.2%, 19.1%, 35.5%, 52.7%, and 70.9% lower than the value reached

290 at room temperature (89.3 MPa). The changes in terms of elastic modulus may be qualitatively

291 observed by analyzing the slope of the stress-strain curves shown in Fig. 9a. The dynamic elastic

292 modulus results denote a reduction trend of 14.9%, 27.1%, 43.0%, 68.5%, and 76.5% for the

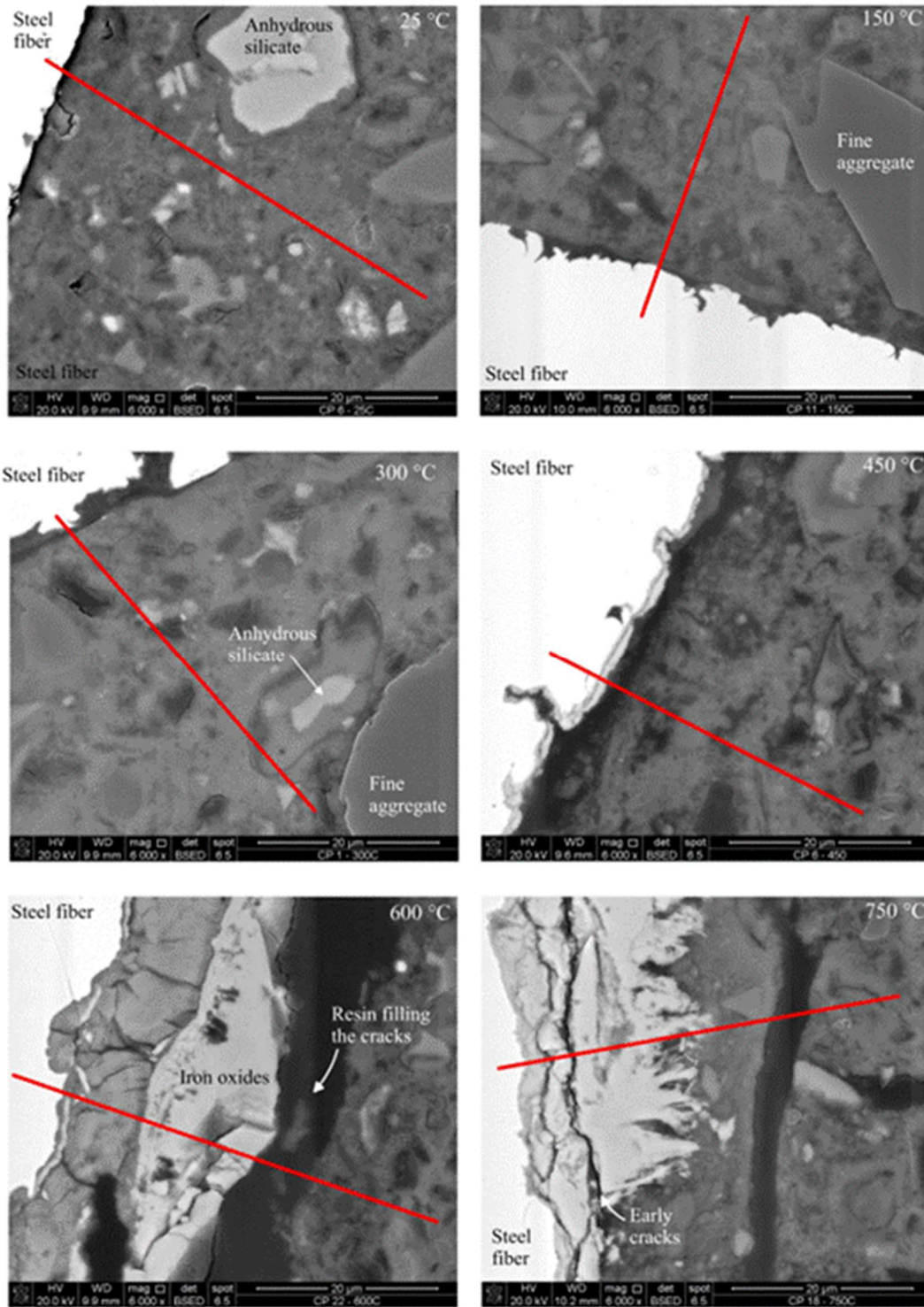
293 respective target temperatures of 150, 300, 450, 600, and 750 °C when compared to room

294 temperature (40 GPa). It is possible to observe that the properties of compressive strength and

295 elastic modulus linearly reduce with temperature increase. The elastic properties of the
296 composite are significantly affected by the changes in the cement paste pore structure caused
297 by the dehydration of hydrated products [19]. The reduction trend observed for the compressive
298 strength and elastic modulus of the mortar is in line with the results found in the literature
299 conducted in comparable conditions [30,31].

300 **3.2 Interfacial transition zone properties**

301 Figure 10 shows the fiber-matrix interface obtained by SEM analysis as a function of
302 temperature. The region analyzed with EDS is indicated by the red line. Figure 11 illustrates
303 the line scanning EDS results in the fiber-matrix interface as a function of temperature.

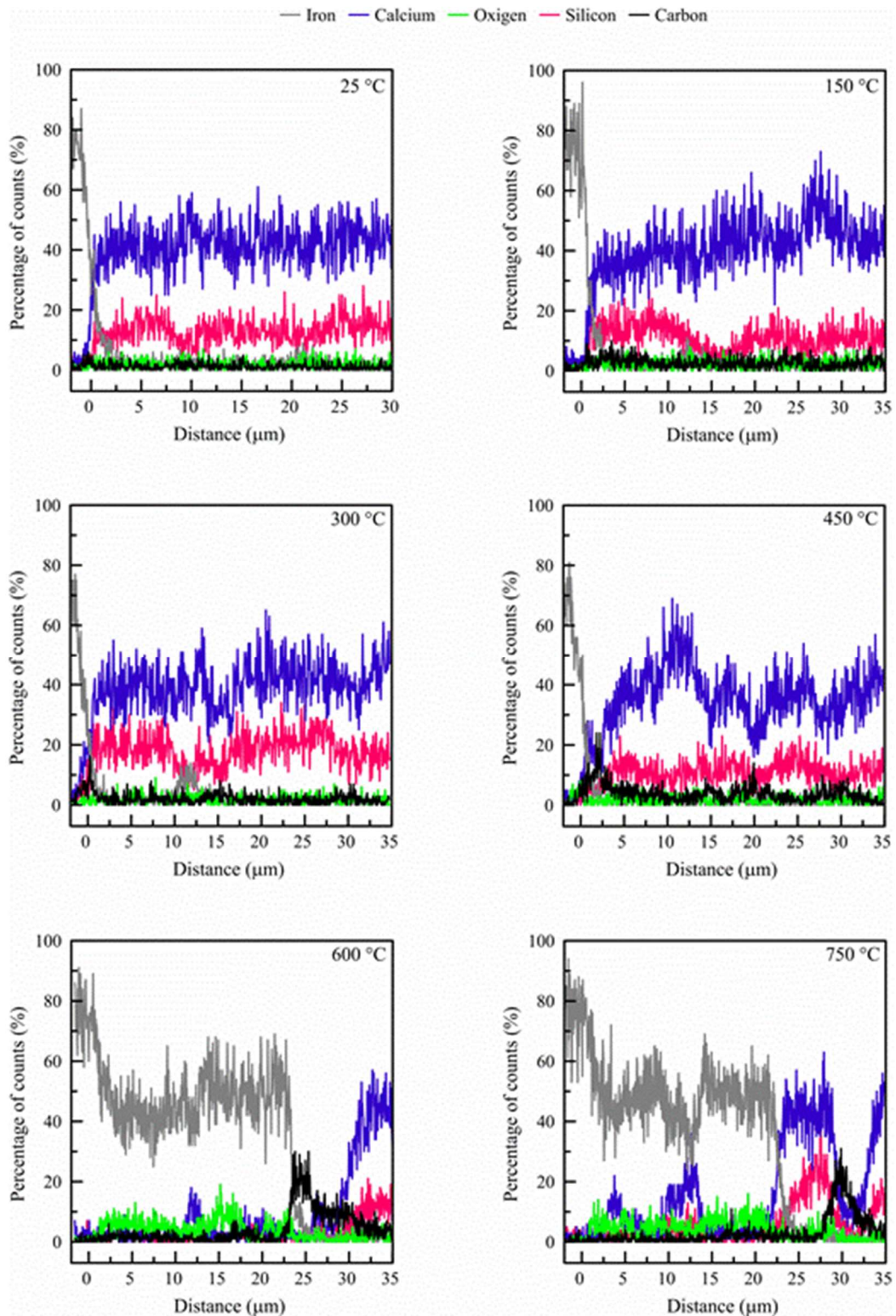


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Figure 10 – Fiber-matrix interface obtained by SEM analysis as a function of temperature



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308 Figure 11 – Line scanning EDS results in the fiber-matrix interface as a function of maximum temperature

309 The qualitative evaluation of SEM images provided in Fig. 10 shows that the oxidation of the
 310 steel fibers begins at ~450 °C and increases significantly for temperatures of 600 and 750 °C.

311 Literature results show that this oxide phase is a three-layered scaled structure composed of
 312 wüstite (FeO), hematite (Fe₂O₃), and magnetite (Fe₃O₄) and that this oxide product has higher

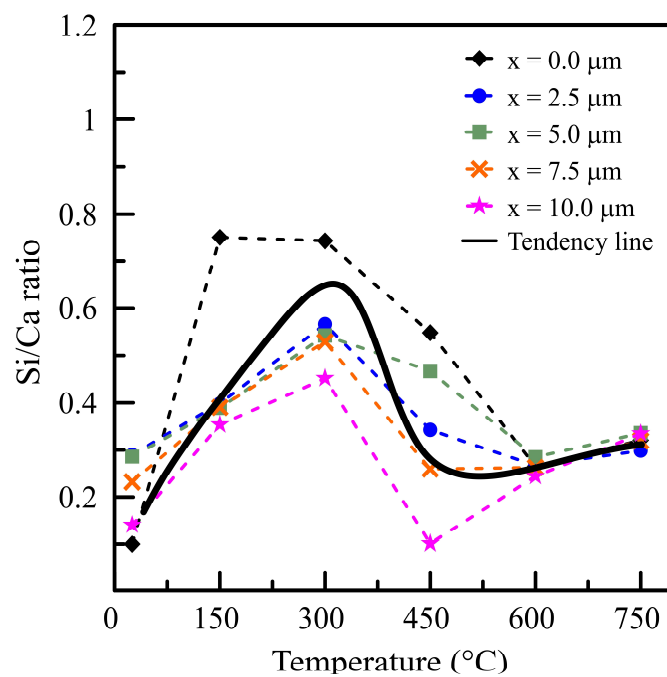
313 mass and lower density than the original steel structure, which results in the significant increase
314 in terms of the external diameter of the steel fibers. Results in the literature point out to an
315 increase of 3.8% in total diameter (steel + oxide) after exposure to 750 °C [32]. Also, the iron
316 oxide may expand into the interfacial transition zone porosity for temperatures of 600 °C and
317 above, which is denoted by the overlap of Si, Ca, Fe, and O peaks in the EDS results (see Fig.
318 11).

319 Cracks were formed in the vicinity of the fiber can be verified by analyzing the cracks filled
320 with resin (see Fig. 10), as well as by the peak of carbon determined by EDS (see Fig. 11). This
321 crack formation can be attributed to the detachment of fibers from the cementitious matrix and
322 the passive thrust generated by the expansive oxidation process suffered by steel fibers. The
323 debonding of fibers during the pullout test seems to occur in the region between the steel fiber
324 and the interfacial transition zone for temperatures up to 450 °C. For temperatures of 600 °C
325 and above the debonding of fibers seems to occur in the interface between the iron oxide formed
326 and the interfacial transition zone. This rupture pattern change may result in changes in the
327 fracture energy associated with the debonding of steel fibers and the energy dissipated during
328 the slip portion of the test since the oxide formation increases the total diameter of the fiber
329 [33,34].

330 It is worth highlighting that the cracks filled with resin are the only cracks that may be evaluated
331 in SEM imagery since they were generated before the resin was applied. A few “early cracks”
332 that are not filled with resin can be also noticed in Fig. 11, however, those must not be
333 interpreted as a result of the pullout test or temperature exposure since they are likely to be
334 generated by the vacuum applied during preparation and testing of samples, or even due to the
335 influence of the beam of electrons during the SEM test.

336 Figure 12 shows the Si/Ca ratio as a function of temperature and distance from the fractured
337 surface. For room temperature conditions, values of Si/Ca ratio lower than 0.3 represent systems
338 with a high content of portlandite crystals and reduced amount of C-S-H, while Si/Ca ratios

339 greater than 0.3 indicate systems rich in C-S-H [35]. Some studies conducted also show that
 340 systems formed mainly by C-S-H show a Si/Ca ratio of 0.5 or more in the form of α -C-S-H (1
 341 $\leq \text{Si/Ca} < 1.5$), β -C-S-H ($0.66 < \text{Si/Ca} < 1$), and γ -C-S-H ($0.5 < \text{Si/Ca} < 0.66$) [36]. The results
 342 obtained for specimens tested at room temperature (25 °C) present a Si/Ca ratio between 0.1
 343 and 0.3 for the first 10 μm from the fracture surface, which denotes that portlandite tends to
 344 precipitate around the steel fiber and a low amount of C-S-H is present in this interface, which
 345 is in agreement with classical literature [5].



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Figure 12 – Si/Ca ratio as a function of temperature and distance from fractured surface

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At the temperature range between 150 and 300 °C, the Si/Ca ratio exhibits an increasing tendency. Considering that very limited data is available in the literature regarding the effect of temperature on the Si/Ca ratio of hydrated products, the origin of this behavior cannot be precisely determined based on SEM/EDS results alone. This investigation requires specific studies that aim to investigate the chemical and mineralogical changes in the vicinity of the fiber, which is a methodological challenge given the significantly reduced size of this region. Even though this specific experimental investigation is out of the scope of this paper, a few possible scenarios may be discussed.

356 The first hypothesis is that the thermal energy provided may work as a catalyst for the
357 topochemical reaction of anhydrous silicates (i.e. C_3S and C_2S) that are deposited on the
358 interfacial transition zone. This reaction may occur with silicates that are either partially
359 hydrated or non-hydrated, which have been found in the interfacial transition zone in SEM
360 imagery (see Fig. 11). Additionally, recently published studies pointed out that the temperature
361 range between 100 and 400 °C is favorable for the formation of new hydration products capable
362 of filling the pores of concrete [37,38]. This hypothetical hydration process could lead to the
363 densification of the interfacial transition zone due to the formation of hydrated products and
364 affect the bond-slip behavior of the hooked-end steel fibers.

365 The second hypothesis is based on the fact that the vicinity of the fiber has a considerable
366 amount of portlandite in room temperature conditions (see Fig. 12). In this sense, the increase
367 in temperature acts as a catalyst to the pozzolanic reaction between the $Ca(OH)_2$ rich interfacial
368 transition zone and the SiO_2 present in the concrete mix. Literature results show that the increase
369 in temperature has been responsible for the significant increase in the compressive strength for
370 lime-pozzolan mortars [39,40], which may be another factor that indicates the plausibility of
371 the hypothesis proposed. According to recent studies, the presence of SiO_2 in the ITZ is so
372 significant that the coating of steel and carbon fibers with nano-silica significantly reduced the
373 ITZ porosity around the fiber matrix and improved the interfacial adhesion [41,42].

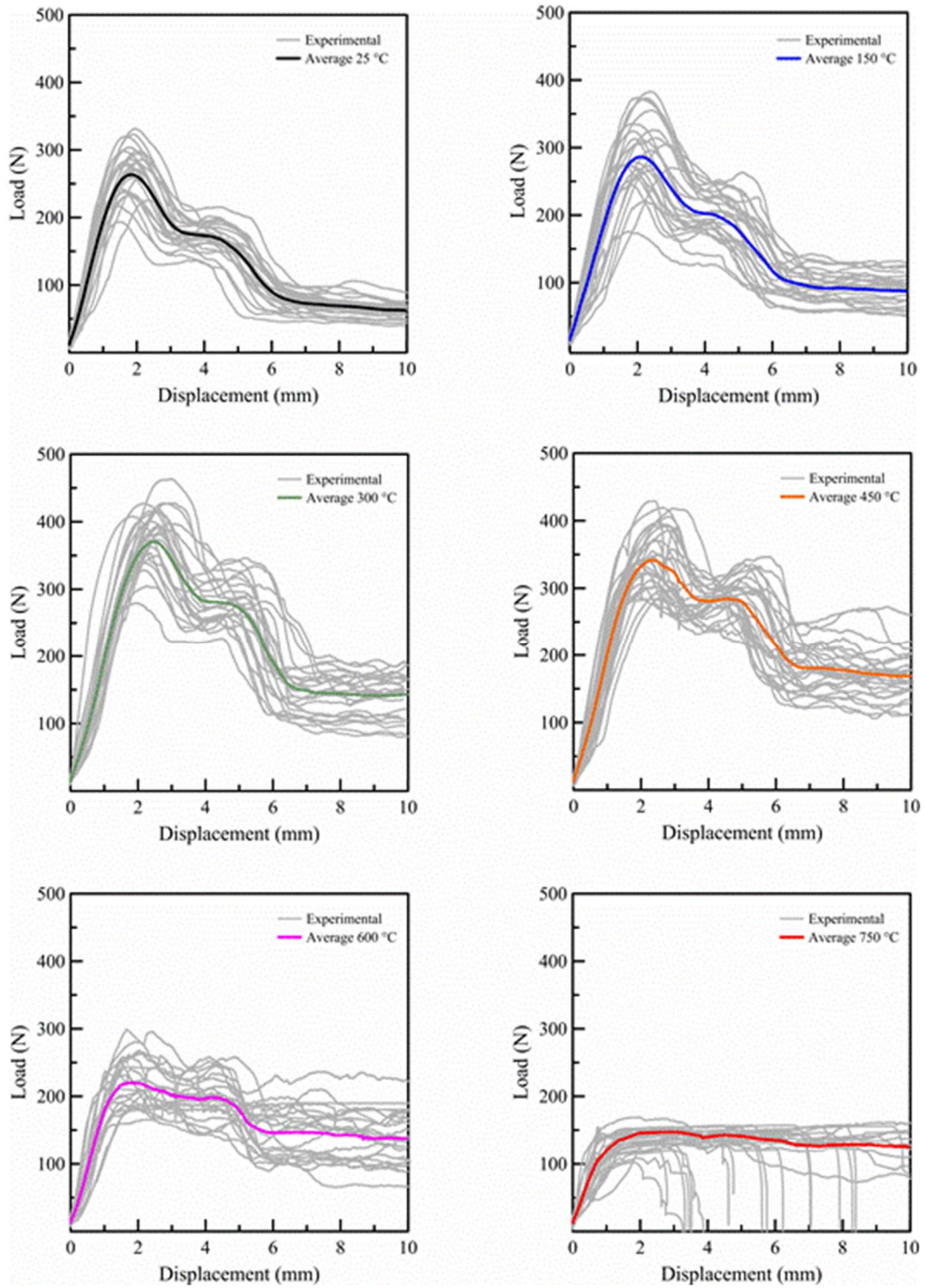
374 What is particularly concerning about the two hypotheses proposed is that both require water
375 for the chemical reaction to occur. In this sense, the steam generated by the evaporation of free,
376 adsorbed, and interlayer water results in the increase of the internal pressure in the mortar and
377 induces an internal autoclaving condition [43]. Therefore, the water required could be trapped
378 inside the specimen in the form of steam and superheated water, associated with the gas-liquid-
379 solid triple point of a substance. Superheated water occurs between the usual boiling
380 temperature (~100 °C at 1 atm) and the critical temperature of 374 °C in pressured
381 environments. This pressured environment could be provided by the low porosity and limited

382 permeability of the mortar used in this study, which has a compressive strength of ~90 MPa
383 (see Section 3.1).

384 In this context, the fiber-matrix interface is composed of three main phases at room temperature:
385 the steel fiber, an interfacial transition zone (mostly portlandite), and the cementitious matrix.
386 The increase in temperature within the range between 25 and 450 °C leads to changes in the
387 Si/Ca ratio of the interfacial transition zone and the debonding of fibers seems to occur between
388 the steel fiber and the interfacial transition zone. For temperatures equal or higher than 450 °C
389 the oxidation process of steel fibers becomes relevant, which means that a new phase is present
390 in the fiber-matrix interface. Therefore, the fiber-matrix interface can be described as having
391 four phases: the steel fiber, the oxide layered structure, the interfacial transition zone, and the
392 cementitious matrix. This oxide formation leads to an increase in the confinement forces applied
393 in the steel fiber and change the location where the fracture occurs from fiber-matrix to oxide-
394 matrix, which are both factors that affect the bond-slip mechanism.

395 **3.3 Bond-slip behavior**

396 Figure 13 shows both the individual and averaged load-displacement curves obtained
397 experimentally for each target temperature. The maximum pullout load (P_{L1}) accounts for the
398 energy required to yield the hooks at two points, while the lower peak (P_{L2}) is associated with
399 the force required to straighten the fiber. The load values at a displacement of 10 mm (P_{L3}) were
400 used to evaluate the changes in the dynamic frictional interaction between fiber and matrix.
401 Table 5 shows the load values of P_{L1} , P_{L2} , P_{L3} , and the observations made during the pullout
402 tests, as well as the standard deviation values. The results presented show that the temperature
403 exposure tends to increase the dispersion of the experimental curves even in a double-sided
404 pullout test using multiple fibers; however, this dispersion increase is not as significant as in
405 single-fiber pullout tests found in the literature [16].



406

407

Figure 13 – Experimental and average load-displacement curves obtained for each target temperature

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Table 5 – Load values of P_{L1} , P_{L2} , P_{L3} and the observations that were made during the pullout tests

Temperature (°C)	P_{L1} (N)	P_{L2} (N)	P_{L3} (N)	P_{L1}/P_{L2}	Observation
25	269.0 (± 34.9)	177.3 (± 21.0)	61.2 (± 11.3)	1.52	NFR in 30 specimens
150	297.1 (± 50.2)	203.4 (± 33.5)	85.3 (± 22.4)	1.46	NFR in 30 specimens
300	378.3 (± 45.9)	285.4 (± 32.0)	134.5 (± 34.5)	1.33	NFR in 30 specimens
450	350.1 (± 46.1)	295.5 (± 27.3)	157.0 (± 28.7)	1.18	NFR in 30 specimens
600	227.1 (± 36.3)	209.6 (± 34.9)	121.3 (± 42.7)	1.08	3 FR in 03 specimens
					2 FR in 04 specimens
					1 FR in 08 specimens
750	140.8 (± 16.1)	139.6 (± 12.9)	114.3 (± 23.9)	1.01	NFR: 15 specimens
					4 FR in 15 specimens
					3 FR in 05 specimens 2 FR in 03 specimens NFR: 07 specimens

413

NFR – no fiber rupture; FR – fiber rupture

414 For specimens exposed to temperatures of 600 °C, it is possible to observe the occurrence of

415 pullout and rupture of steel fibers (see Table 5). This suggests that for temperatures of 600 °C

416 and above the tensile strength of fibers is exceeded before the shear strength of the fiber-matrix

417 interaction. Considering that the peaks P_{L1} and P_{L2} are directly associated with the yielding of418 the hooks, the changes in the P_{L1}/P_{L2} ratio can be used as a qualitative indirect method to verify

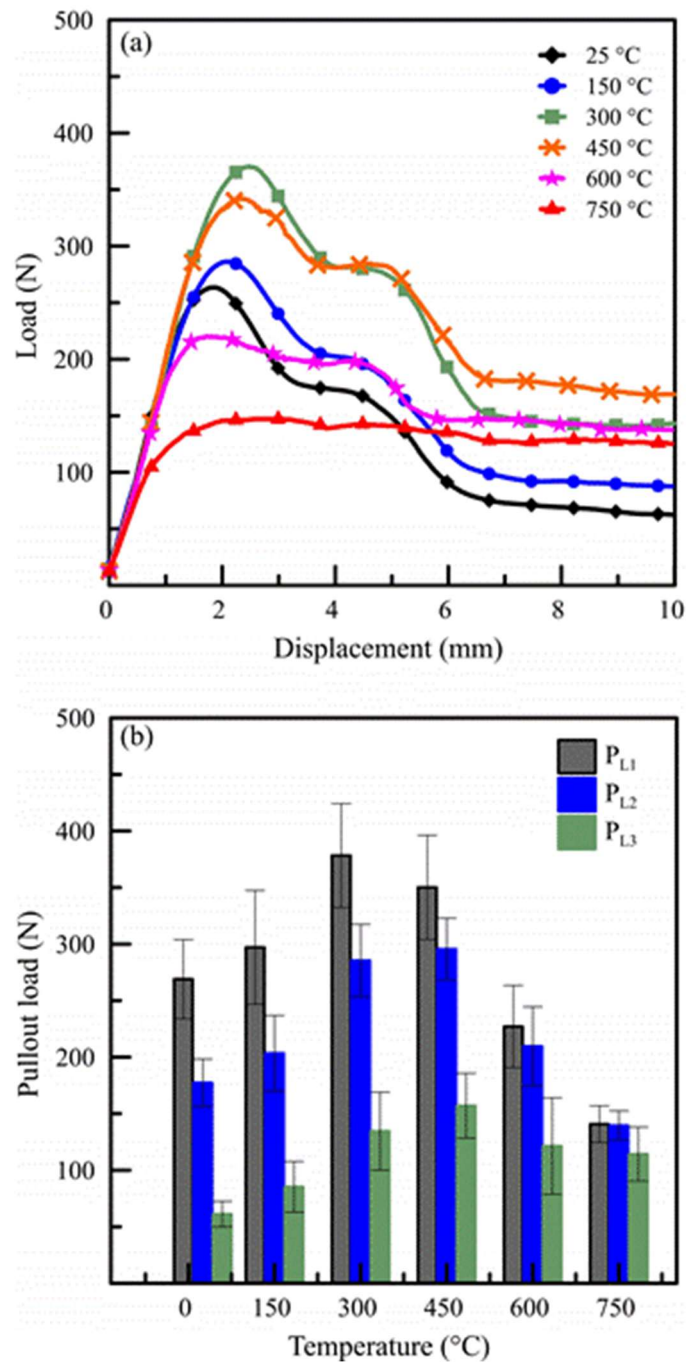
419 the tendency changes in the mechanical interlocking caused by the fibers. Since elevated

420 temperatures affect the microstructure of the cement paste and the ITZ as a whole, the reduction
421 of the P_{L1}/P_{L2} ratio may be attributed mainly to changes in the properties of steel fibers.

422 Results obtained are presented in Table 5, confirming that the P_{L1}/P_{L2} values significantly
423 reduce as temperature increases. This reduction may be evidence that the bending stiffness of
424 the steel fibers substantially reduces after temperature exposure, and could suggest that the
425 mechanical interlock provided by the hooks is negligible for temperatures of 600 °C and above.
426 This would also confirm that the dynamic frictional interaction between fiber and matrix is the
427 preponderant factor in this temperature range. Furthermore, the reduction in bending stiffness
428 is associated with the effects of elevated temperatures on the physical, mechanical, and
429 microstructural properties of hooked-end steel fibers, mainly due to the oxidation and
430 recrystallization processes. These temperature-related processes have shown to significantly
431 increase the grain-size structure of the fiber for temperatures of 600 °C and above [32].

432 Figure 14 illustrates the effect of temperature on the average load-displacement curves and the
433 maximum values of P_{L1} , P_{L2} , and P_{L3} . The maximum pullout load (P_{L1}) values have shown an
434 increasing trend up to 450 °C. In this sense, the P_{L1} values increased by 10.5%, 40.6%, 30.2%
435 for the respective target temperatures of 150, 300, and 450 °C when compared to room
436 temperature results. This increasing tendency may be associated with the Si/Ca ratio changes
437 that may occur in the interfacial transition zone (see Section 3.2), which may result in increased
438 interfacial chemical adhesion and enhances the dynamic frictional interaction between fiber and
439 matrix due to the densification of the ITZ. Since the bond-slip response is sensitive to normal
440 stresses, the changes in the Poisson's ratio of the materials [5] and the shrinkage behavior of
441 the cementitious matrix up to ~300 °C [29] may influence the results obtained.

442



443

444 Figure 14 – Effect of temperature on (a) the average load-displacement curves and (b) the maximum values of

445

P_{L1} , P_{L2} , and P_{L3}

446

Although an increasing trend is verified in this study, literature results show that the values of

447

P_{L1} remain relatively constant up to ~ 400 °C [13–16]. This negligible effects of temperature on

448

P_{L1} values may be associated with two main factors. The first factor is that literature results

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were obtained using less stable test methods than the one proposed in this study, which increases

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the dispersion and may result in the non-significance of results. The second is that the ITZ

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remains relatively unchanged when compared to the cement paste up to the dehydration

452 temperature of portlandite (~ 450 °C [44]) since the region in the vicinity of the fiber contains a
453 considerable volume of CaOH_2 crystals (see Section 3.2).

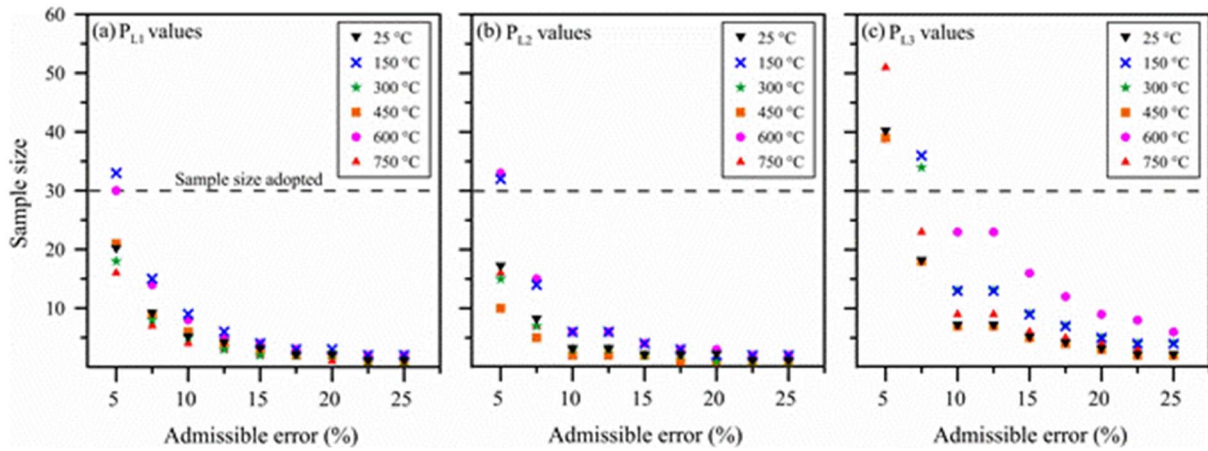
454 After exposure to temperatures of 600 and 750 °C, a reduction trend was observed in the P_{L1}
455 values with the respective reductions of 15.6% and 47.6% when compared to room temperature
456 results. This reduction is mainly associated with the drastic reductions in the bending stiffness
457 of steel fibers, as previously determined by the analysis of the P_{L1}/P_{L2} ratio, and the dehydration
458 of hydrated products in the ITZ. Even with those considerations, additional factors that
459 significantly influence the evidenced behavior can be cited, such as the coarsening of the ITZ
460 pore structure, the significant cracking caused by the thermal gradients, and the reversible
461 transformation of quartz from α -trigonal to β -hexagonal at 573 °C [29].

462 The values of P_{L3} significantly increase by 39.4%, 119.8%, 156.6%, 98.2%, and 86.7% for the
463 respective temperatures of 150, 300, 450, 600, and 750 °C when compared to room temperature
464 results. It is also important to notice that the maximum increase is detected at 450 °C, which
465 may be associated with the changes in the Si/Ca ratio in the interfacial transition zone and the
466 initial oxidation of steel fibers. Even for temperatures of 600 °C and above a significant increase
467 is verified in terms of P_{L3} when compared to room temperature results. This increase may be
468 attributed to the increase in the confining forces and the changes in the fracture mechanism
469 from fiber-matrix to oxide-matrix, discussed in Section 3.2. Another relevant aspect is that the
470 increase in the confining forces may be associated with the shrinkage suffered by the cement
471 paste for temperatures above 300 °C, which can easily overcome 1.6% [29,45].

472 **3.4 Admissible error and sample size determination**

473 Figure 15 shows the sample size required as a function of the admissible error for the peak load
474 values P_{L1} , P_{L2} , and P_{L3} . The analysis conducted using inferential statistics and a 95%
475 confidence interval shows that the sample size increases with the reduction of the admissible
476 error for the pullout test. This increase in sample size is particularly greater for the P_{L3} values
477 both in room conditions and after exposure to elevated temperatures, which can be justified by

478 the reduced stability during the dynamic portion of the test and the consequent increase in the
479 variability of results.



480
481 Figure 15 – Sample size required as a function of the admissible error for the (a) P_{L1} values, (b) P_{L2} values, and
482 (c) P_{L3} values

483 It is possible to observe that the sample size of 30 pullout specimens adopted in this study was
484 enough to ensure an admissible error of $\sim 11\%$. Moreover, a total of 16 pullout specimens ensure
485 a maximum admissible error of $\sim 15\%$ and 9 pullout specimens a maximum admissible error of
486 $\sim 20\%$ for all the peak loads evaluated. In this sense, the results obtained using double-sided and
487 with multiple fibers have shown an acceptable error for the purpose. This suggests that the
488 adoption of a double-sided pullout test using multiple fibers may be a stable and adequate test
489 method to improve the reliability of the pullout results obtained, both in room conditions and
490 after exposure to elevated temperatures.

491 Even with those considerations, the results regarding the admissible error of the pullout test
492 proposed in this paper (double-sided, multiple fibers) could not be compared with the tests
493 found in current literature (single-sided, single fiber). The comparison was not possible because
494 the standard deviation values are not provided in studies found in the literature [13–16].
495 Therefore, the experimental data reported in this work serves as a reference for comparison for
496 future works that aim to study the effect of temperature on the bond-slip of steel fibers.

497 4. Numerical simulation

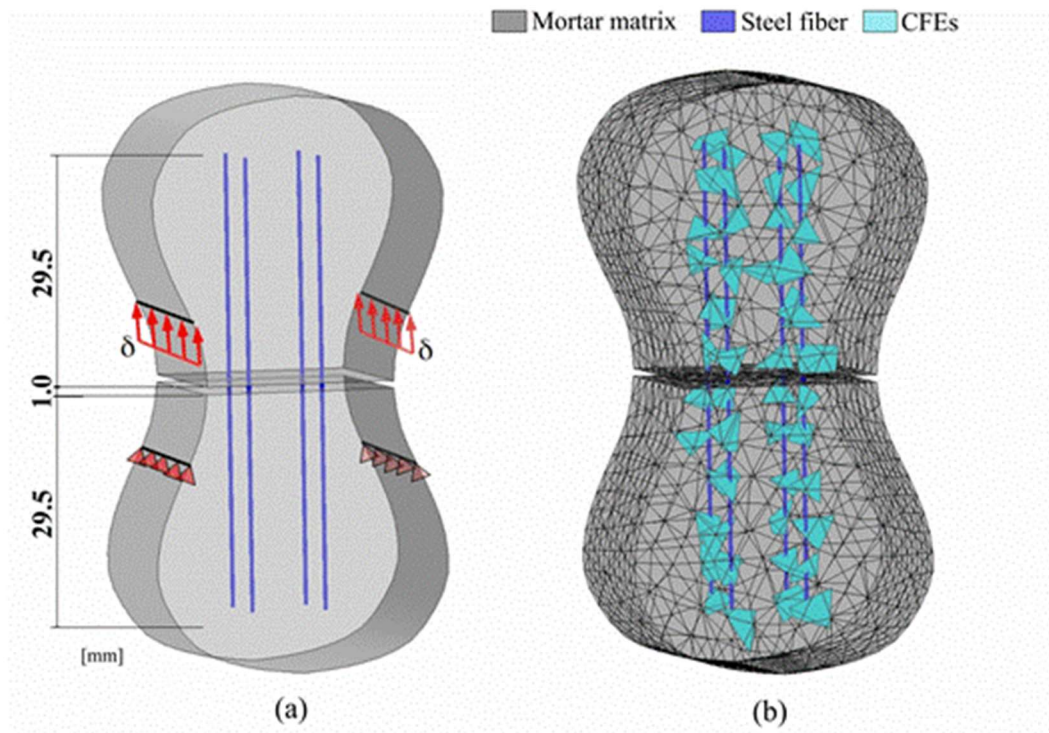
498 In this section, the numerical approach proposed by Bitencourt et al. [18] for modeling steel
499 fiber reinforced concrete (SFRC) is employed. This is one of the most appropriate approaches
500 available in literature for the numerical simulation of pullout tests since the model allows
501 representing the fiber/matrix interaction separately.

502 Figure 16 illustrates the 3D model constructed for the numerical simulations of the pullout tests.
503 As can be seen in this figure, the fibers are represented discretely and explicitly and a crack is
504 predefined at the central part of the specimen, as considered in the laboratory tests. Therefore,
505 the interaction between the top and bottom parts is given by the fiber/matrix interface. The
506 bottom part of the specimen is fixed, while a vertical displacement of 10 mm with a
507 displacement rate of 0.5 mm/min is imposed at the top part, as depicted in the Figure 16a.

508 Initially, fibers and mortar matrix are discretized in finite elements in a totally independent way
509 (non-conforming meshes) using two-noded truss finite elements and four-noded tetrahedral
510 finite elements, respectively. Then, five-noded tetrahedral coupling finite elements (CFEs) are
511 inserted (see light blue elements in Figure 16b) to describe the fiber-matrix interaction [46].

512 In this work, the behavior of the fibers is described by a one-dimensional elastoplastic material
513 model, while the mortar matrix is idealized with a linear elastic behavior. The fiber/matrix
514 interaction is described by the non-rigid version of the CFEs, and a continuum damage model,
515 by adjusting the parameters obtained in the laboratory tests. Details about the fiber/matrix
516 interaction and a comparison with an analytical model can be found in Bitencourt et al. [18].

517 It is important to mention that the effect of the hooks is distributed along the length of a straight
518 fiber in the numerical model. This simplification has proven to be a feasible manner to represent
519 hooked-end steel fibers in the model since the effect of the hooked-end is considered in the
520 bond-slip law adopted. Recently, this numerical strategy was successfully employed for
521 modeling three-point bending tests (3-PBT) to predict the post-cracking parameters of SFRC
522 [47] and the behavior of beams with combined reinforcement of steel fibers and rebars [48].



523

524 Figure 16 –3D model for the numerical simulation of the pullout tests: (a) geometry of the specimen, boundary
 525 conditions and imposed displacement, and (b) discretization in finite elements

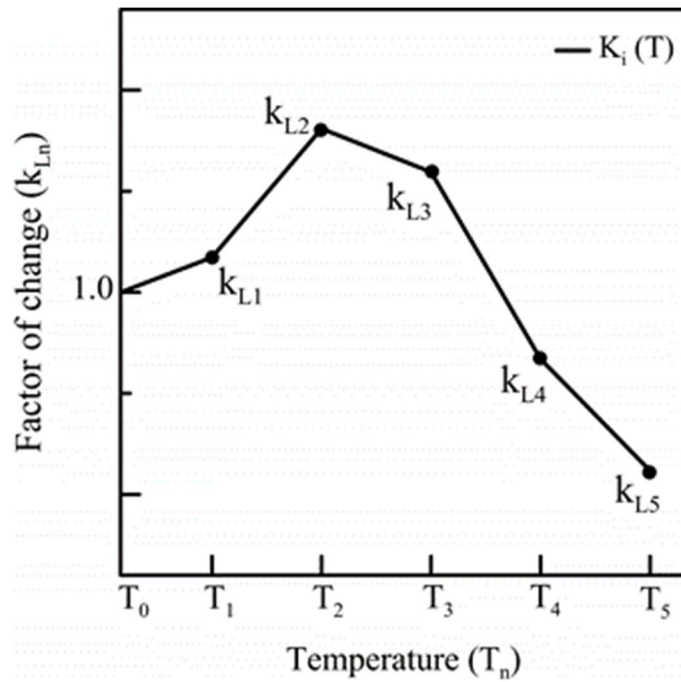
526 In the numerical analyses performed, the mortar matrix was discretized by 8,165 four-noded
 527 tetrahedral finite elements, whereas 11 two-noded truss finite elements were used for each steel
 528 fiber. To couple the initially independent meshes of the mortar matrix and steel fibers, 48 five-
 529 noded tetrahedral CFEs were added.

530 The behavior of the CFEs, given by a continuum damage model is adjusted to describe the
 531 response of the pullout test at room temperature. Therefore, a bond-slip model defined by the
 532 relationship between the shear stress (adherence stress) and relative sliding is initially
 533 constructed for the temperature of 25° according to the response presented in Fig. 14a. An
 534 appropriate damage coefficient is introduced in the constitutive equation based on the
 535 experimental responses to capture the responses for other temperatures. In the following
 536 sections, the definition of the damage coefficient, and the bond-slip model are presented as the
 537 main constitutive parameters for the definition of the fiber-matrix interaction.

538 **4.1 Fiber-matrix interaction**

539 **4.1.1 Damage coefficient**

540 In this section, the damage coefficient (K_i) and the factors of change (k_{Ln}) that are applied in
 541 the constitutive model as the effect of temperature on the bond-slip behavior of the hooked-end
 542 steel fibers are presented. Figure 17 illustrates the analytical model for the damage coefficient
 543 as a function of temperature. One damage coefficient (K_i) is generated for each major peak of
 544 the bond-slip model, therefore K_1 , K_2 , and K_3 for the respective peak loads of P_{L1} , P_{L2} , and P_{L3} .



545
 546 Figure 17 – The analytical model for the damage coefficient as a function of temperature

547 The factors of change (k_{Ln}) are determined based on the value of one of the peak loads (P_{Li})
 548 after exposure to a given temperature (T_n) related to room temperature (T_0) results, which is
 549 calculated as:

$$k_{Ln} = \frac{P_{Li}(T_n)}{P_{Li}(T_0)} \quad \text{Eq. (3)}$$

550 The damage coefficient (K_i) is a multilinear equation that interpolates the factor of change for
 551 other temperatures than the temperatures evaluated. Therefore, the analytical equation for K_i
 552 can be defined as a function of temperature, as follows:

$$K_i = \begin{cases} 1 + (k_{L1} - 1) \frac{(T - T_0)}{(T_1 - T_0)} & \text{if } T_0 \leq T \leq T_1 \\ k_{L1} + (k_{L2} - k_{L1}) \frac{(T - T_1)}{(T_2 - T_1)} & \text{if } T_1 \leq T \leq T_2 \\ \vdots \\ k_{L(n-1)} + (k_{Ln} - k_{L(n-1)}) \frac{(T - T_{(n-1)})}{(T_n - T_{(n-1)})} & \text{if } T_{(n-1)} \leq T \leq T_n \end{cases} \quad \text{Eq. (4)}$$

553 4.1.2 Bond-slip

554 A constitutive model for the bond-slip behavior of hooked-end steel fibers after exposure to
 555 elevated temperatures is proposed. The shear stresses associated with P_{L1} , P_{L2} , and P_{L3} used as
 556 input in the model may be calculated by the simplified assumption that the shear stress is
 557 constant, and the effect of the hook is distributed along the length of the fiber, as follows:

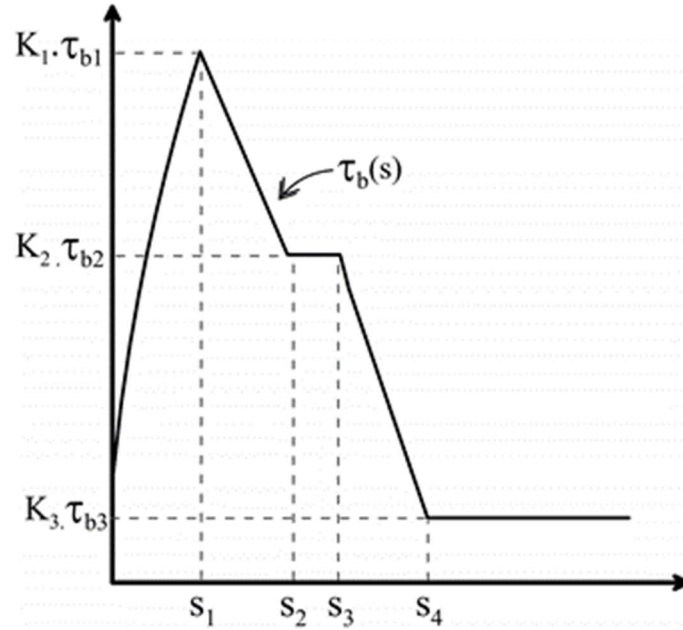
$$\tau_{bn} = \frac{P_{Ln}}{\pi * d * l_e} \quad \text{Eq. (5)}$$

558 where τ_{bn} is the average shear stress for a given peak load; P_{Ln} is the respective load value for
 559 P_{L1} , P_{L2} , or P_{L3} ; d is the diameter of the steel fiber; l_e is the embedded length of the fiber in the
 560 cementitious matrix. In this sense, the bond stresses (τ_b) between the substrate and the hooked-
 561 end steel fiber for pullout and splitting failure are given as a function of the slip (s) along the
 562 axis of the fiber, as follows:

$$\tau_b(s) = \begin{cases} K_1 \cdot \tau_{b1} \left(\frac{s}{s_1}\right)^a & \text{if } 0 \leq s \leq s_1 \\ K_1 \cdot \tau_{b1} - (K_1 \cdot \tau_{b1} - K_2 \cdot \tau_{b2}) \left(\frac{s - s_1}{s_2 - s_1}\right) & \text{if } s_1 \leq s \leq s_2 \\ K_2 \cdot \tau_{b2} & \text{if } s_2 \leq s \leq s_3 \\ K_2 \cdot \tau_{b2} - (K_2 \cdot \tau_{b2} - K_3 \cdot \tau_{b3}) \left(\frac{s - s_3}{s_4 - s_3}\right) & \text{if } s_3 \leq s \leq s_4 \\ K_3 \cdot \tau_{b3} & \text{if } s \geq s_4 \end{cases} \quad \text{Eq. (6)}$$

563 where K_1 , K_2 , and K_3 are the analytical equations that relate the factors of change for the peaks
 564 of P_{L1} , P_{L2} , and P_{L3} , respectively. The shear stresses τ_{b1} , τ_{b2} , and τ_{b3} account respectively for
 565 the shear generated by P_{L1} , P_{L2} , and P_{L3} for the steel fibers at room temperature (see Eq. 5),

566 while the variable s is the slip of fibers in the cementitious matrix. Figure 18 shows the curve
 567 defined by the Eq. 6.



568

569 Figure 18 – Bond-slip constitutive model for the hooked-end steel fibers after elevated temperatures

570 By assuming that the function $q(r)$ represents the hardening/softening law of the continuum
 571 damage model assumed to describe the fiber-matrix interaction, the Eq. 6 can be rewritten in
 572 terms of these stress (q) and strain (r) like internal variables by considering the relationship

573 $q(r) = \tau_b\left(\frac{r}{k}\right)$, as follows:

$$q(r) = \begin{cases} K_1 \cdot \tau_{b1} \left(\frac{r/k}{s_1}\right)^a & \text{if } 0 \leq r/k \leq s_1 \\ K_1 \cdot \tau_{b1} - (K_1 \cdot \tau_{b1} - K_2 \cdot \tau_{b2}) \left(\frac{r/k - s_1}{s_2 - s_1}\right) & \text{if } s_1 \leq r/k \leq s_2 \\ K_2 \cdot \tau_{b2} & \text{if } s_2 \leq r/k \leq s_3 \\ K_2 \cdot \tau_{b2} - (K_2 \cdot \tau_{b2} - K_3 \cdot \tau_{b3}) \left(\frac{r/k - s_3}{s_4 - s_3}\right) & \text{if } s_3 \leq r/k \leq s_4 \\ K_3 \cdot \tau_{b3} & \text{if } r/k \geq s_4 \end{cases} \quad \text{Eq. (7)}$$

574 where k is the coupling parameter in the direction normal to the fiber, varying from 10^6 to 10^9
 575 (MPa/mm) according to the recommendation of Bitencourt et al. [46]. More details about the
 576 numerical model for SFRC may be found in the work of Bitencourt et al. [18].

577 The mortar matrix is assumed as a linear elastic material with Poisson's ratio of $\nu = 0.2$ and the
578 elastic modulus (E_c) determined based on the experimental characterization conducted for each
579 target temperature. The behavior of the steel fibers is given by an elastic perfectly plastic model,
580 with an elastic modulus of $E_f = 210$ GPa for all target temperatures, since the initial interatomic
581 distance of the metallic ions is not changed after the steel fibers are exposed to the heat-cooling
582 process [49,50]. The yield stress (σ_y) of the steel fibers as a function of temperature was
583 estimated based on the rate of change obtained in the experimental work conducted by Abdallah
584 et al [13] applied to the tensile strength of the steel fiber used in this study. The damage
585 coefficient values were calculated based on the peak load values (P_{L1} , P_{L2} , and P_{L3}) presented
586 in Table 5 of Section 3.3. Table 6 shows a summary of the parameters adopted in the numerical
587 simulations.

Table 6 – Summary of the parameters adopted in the numerical simulations

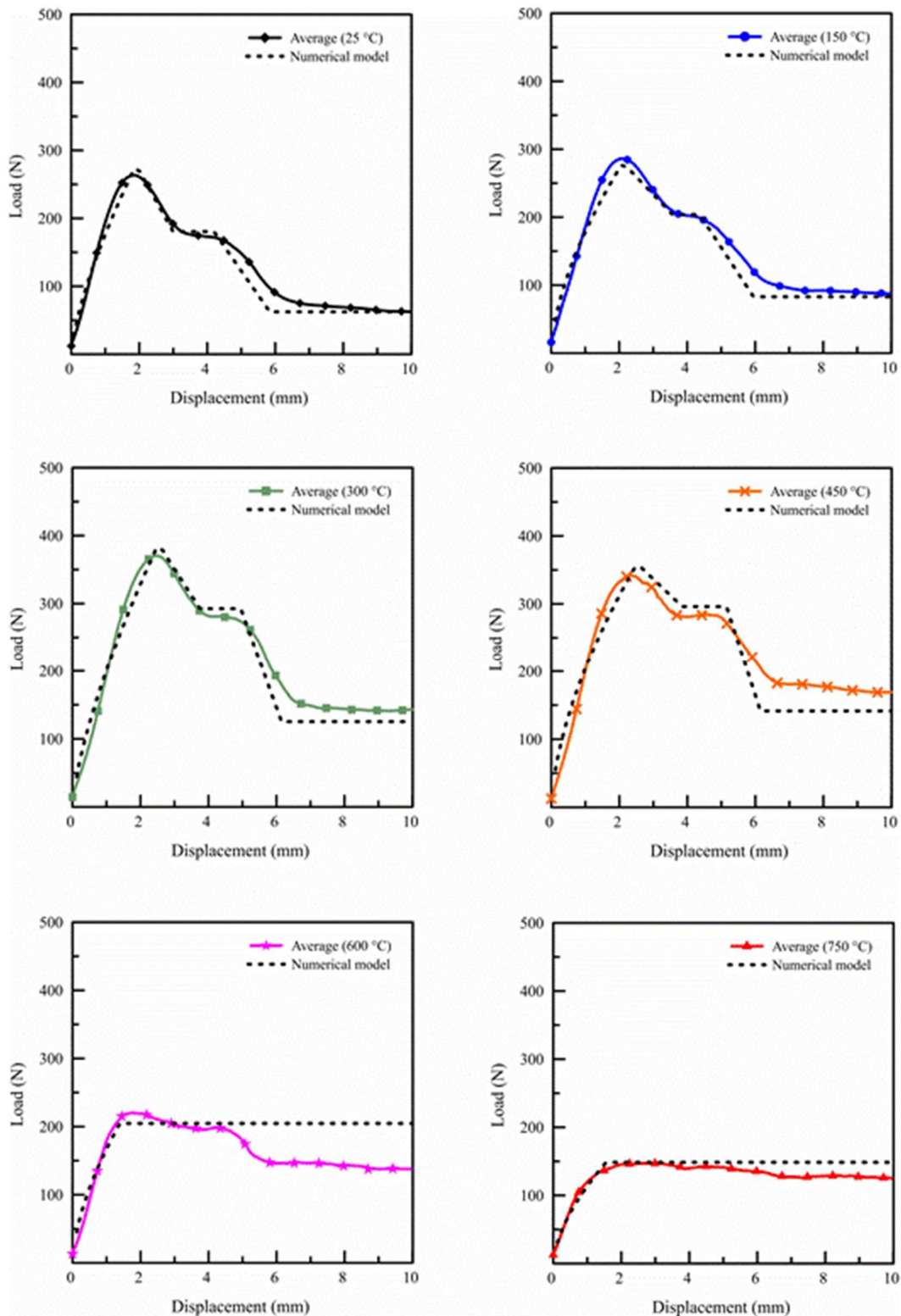
Target	Bond-slip parameters								Mortar properties			Steel fiber properties			
temperature (°C)	τ_{b1} (MPa)	τ_{b2} (MPa)	τ_{b3} (MPa)	s_1 (mm)	s_2 (mm)	s_3 (mm)	s_4 (mm)	a	K_1	K_2	K_3	f_c (MPa)	E_c (GPa)	σ_y (MPa)	E_f (GPa)
25	3.9	2.6	0.9	0.9	2.3	3.5	5.6	0.7	1.0	1.0	1.0	89.3	40.0	1240	210
150	3.9	2.6	0.9	1.0	2.7	3.5	5.6	0.6	1.1	1.1	1.3	85.5	34.2	1226	210
300	3.9	2.6	0.9	1.2	2.7	3.9	5.7	0.7	1.4	1.6	2.0	72.3	29.4	1199	210
450	3.9	2.6	0.9	1.2	2.7	4.0	5.6	0.6	1.3	1.6	2.3	57.6	23.2	1032	210
600	3.9	2.6	0.9	0.8	2.3	3.5	4.8	0.6	0.8	1.1	2.0	42.3	12.8	463	210
750	3.9	2.6	0.9	0.8	2.3	3.5	4.8	0.6	0.6	0.8	1.7	26.0	9.4	336	210

590 **4.2. Numerical results**

591 Figure 19 shows the average experimental curves compared to the numerical simulation
592 conducted in this study. It is confirmed that the numerical curves are capable of describing the
593 bond-slip behavior of fibers as a function of temperature. In this sense, a good agreement
594 between the experimental and numerical results is observed.

595 The value adopted for the slip parameter s_1 in the numerical simulation is the half of that
596 obtained in the experimental results. Moreover, the other slip parameters (i.e. s_2 , s_3 , and s_4) are
597 defined as the experimental slip value subtracted by the half of the slip parameter s_1 . The
598 difference in terms of slip values can be explained by the slip mechanism that occurs in double-
599 sided pullout specimens.

600 For slip values up to the peak load P_{LI} , both sides of the pullout specimen are experiencing the
601 mechanical anchorage of the hooks and fiber slipping. In general lines, half of the total slip can
602 be attributed to each side of the pullout specimen. Once the hook is straightened in one of the
603 sides, the slip mechanism is similar to the single-sided pullout tests. Therefore, the difference
604 between experimental and numerical values of slip occurs since the Eq. 5 was developed
605 considering the pullout test of a single fiber embedded on one side, while the fibers are
606 embedded on both sides in the pullout tests performed in this research. This difference in terms
607 of slip values was also reported by other researchers in the literature. According to Lee et al.
608 [51], the slip s_1 for fiber embedded on both sides is about twice that obtained with fiber
609 embedded on one side and this difference between responses decreases as smaller is the fiber
610 embedded length.



611

612

Figure 19 – Average experimental load curves compared to the numerical simulation

613

Figure 20 shows the fiber stress at the crack compared to the tensile strength of steel fibers, and

614

the stress distribution for temperatures of 25 and 750 °C. Comparing the results, it can be

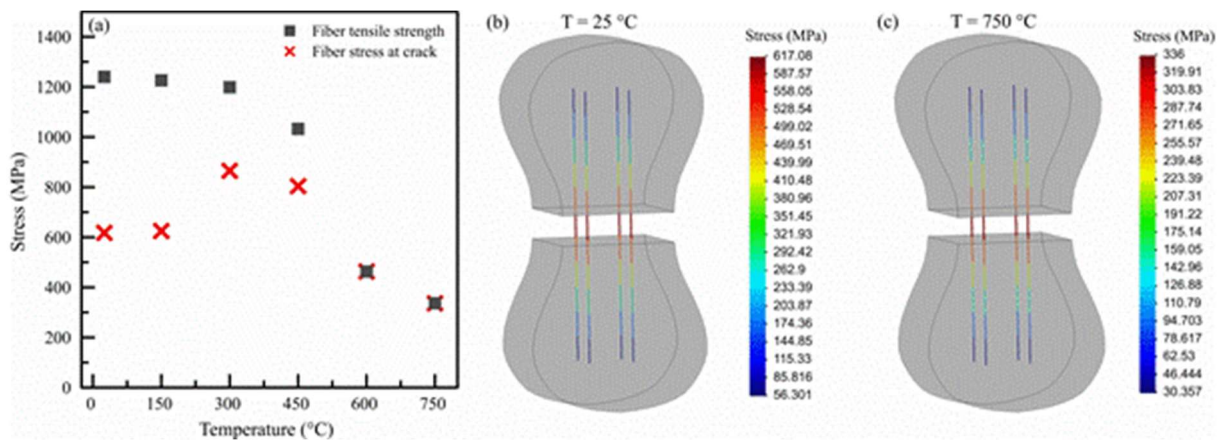
615

observed that in the temperature range of 25 and 450 °C the governing mechanism can be

616

attributed to the shear interaction between the steel fibers and the cementitious matrix since the

617 tensile stresses generated on the steel fibers are not sufficient to cause fiber rupture. For
 618 specimens exposed to temperatures of 600 and 750 °C, the tensile strength of the steel fibers is
 619 reached, therefore fiber rupture occurs. This can also be noticed in the numerical simulations in
 620 Fig. 19. Additionally, the difference between the experimental and numerical results for T =
 621 600 °C may be attributed to the fact that the numerical model does not account for partial
 622 yielding of the steel fibers as occurred for the experimental results (see Table 5, column
 623 “Observations”), and instead considers that all steel fibers reach the yield strength at the same
 624 time.



625
 626 Figure 20 – Effect of temperature on (a) the fiber stress at the crack, and the stress distribution for (b) T = 25 °C
 627 and (c) T = 750 °C

628 This suggests that for temperatures of 600 °C and above the tensile strength of fibers is exceeded
 629 before the shear strength of the fiber-matrix interaction (see Fig. 20a). This behavior is in line
 630 with the experimental results presented in Table 5 and Figure 14 of this study. The significant
 631 reduction of the tensile strength of steel fibers can be attributed to the reduction of grain
 632 boundary surface due to the grain-growth process induced by temperature [32]. In summary,
 633 the governing mechanism changes from bond-slip behavior to the tensile strength capacity of
 634 fibers for temperatures of 600 °C and above.

635 5 Conclusions

636 The following conclusions can be drawn from the present study:

- 637 - The compressive strength and elastic properties of the mortar reduced linearly with
638 temperature increase. The compressive strength was reduced by 4.2% (150 °C) to 70.9%
639 (750 °C) and the dynamic elastic modulus was reduced by 14.9% (150 °C) to 76.5%
640 (750 °C), both related to room temperature results. These changes were attributed to the
641 severe dehydration of hydrated products and were comparable with the results found in
642 the literature.
- 643 - The iron oxide began to form ~450 °C and expanded into the ITZ porosity for
644 temperatures of 600 °C and above. This process resulted in changes in the rupture
645 pattern and the debonding of fibers, which occurred in the interface between the oxide
646 and the matrix. Additionally, the Si/Ca ratio in the region surrounding the steel fibers
647 increased considerably up to 300 °C, denoting changes in the mineralogical properties
648 in the vicinity of the fiber.
- 649 - The maximum pullout load values increased up to ~30% in the range of $150\text{ °C} \leq T \leq$
650 450 °C and decreased up to ~48% for $600\text{ °C} \leq T \leq 750\text{ °C}$. Additionally, the dynamic
651 frictional interaction between fiber and matrix increases for all temperatures evaluated.
652 These changes were attributed to the changes in the Si/Ca ratio in the vicinity of the
653 fiber, the oxide formation, and the increase in the confining forces applied to the fibers.
654 Additionally, the bending stiffness of the steel fibers reduced with the increase in
655 temperature and reached a negligible contribution at ~600 °C.
- 656 - The numerical model can describe the bond-slip behavior of fibers as a function of
657 temperature with a good agreement between the experimental and numerical results. For
658 $25\text{ °C} \leq T \leq 450\text{ °C}$, the governing mechanism is the shear interaction between the fibers
659 and the cementitious matrix. For $T \geq 600\text{ °C}$, the tensile strength of steel fibers is
660 achieved before the bond-slip can take place. The aforementioned governing
661 mechanisms were confirmed by experimental results and the numerical simulation
662 conducted.

663 Finally, it must be highlighted that the experimental campaign conducted, and the numerical
664 model developed in this study may serve as a reference for the simulation of mesoscale tests
665 and assessing the behavior of structural elements built with steel fiber reinforced concrete under
666 high temperatures.

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673 **Data availability:** The raw/processed data required to reproduce these findings cannot be
674 shared at this time as the data also forms part of an ongoing study. The raw/processed data may
675 be provided by the corresponding author upon request.

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