Robust Repetitive Control of Power Inverters for Standalone Operation in DG Systems

Germán A. Ramos, Ricardo Isaza Ruget and Ramon Costa-Castelló

Abstract—Standalone operation of an inverted-based distributed generation unit is performed in voltage control mode. In this mode, it is important that the controller provides tracking and rejection of periodic signals. Strategies like Repetitive Control (RC) are well suited in the voltage control of power inverters. However, the robustness of repetitive controllers is importantly affected by the connected loads. The reason is that the load modifies the dynamics of the system where the design of the RC relies on. Having a low bandwidth action can reduce the problem but with the cost of degrading the voltage waveform and transient response. As an alternative, an H_∞ design is proposed for the RC of voltage source inverters. In this proposal the load is directly treated as an unstructured uncertainty. With this approach, the design procedure directly maximizes the robust stability margin of the system against load variations/uncertainty. Additionally, the analysis provides some insight about the design of the inverter LC filter. Experimental results show that a remarkable Total Harmonic Distortion and good transient response are obtained for a large variety of loads.

Index Terms—AC-DC power conversion, voltage control, H_∞ control, robustness, repetitive control, robust control, power inverters.

I. INTRODUCTION

In standalone operation, the Voltage Source Inverter (VSI) of the main Distributed Generation (DG) unit operates in voltage control mode [1], [2], [3]. In this mode, the main task of the VSI is to guarantee an output voltage with good regulation and low harmonic distortion in face to various types of loads [4], [5], [3]. Additionally, the control of the VSI is intended to provide compensation to dynamic variations of the current, regulate active/reactive power and improve the dynamic response [4].

Repetitive Control (RC) is a useful strategy for tracking/rejecting periodic signals [6], [7]. That given characteristic, makes RC well suited for the control of VSIs [8], [9], [10]. In this case, the intended goal is to produce a sinusoidal voltage with low Total Harmonic Distortion (THD) and good enough transient response. Obtaining low THD entails the rejection of distortions and harmonics that comes mainly from the connected loads. Other phenomena, like non-uniform

switching and Pulse-width Modulation (PWM) dead time also can affect the voltage waveform.

RC practical implementations use concrete controller architectures [11] which explicitly depend on the plant model. In these architectures, it is not difficult to establish closed-loop stability and robustness. However, using this nominal plant model constitutes an important drawback when using RC in a VSI for DG applications. The reason is that connected loads, which in general are not known, produce a big change in the plant system dynamics. As a consequence, some loads, as the non-linear ones for example, can cause severe loss of system robustness yielding to undesired oscillations and high THD in the produced voltage waveform [12].

The design of controllers for uncertain systems is possible thanks to the robust control theory. A widely used approach is the H_∞ design [13], [14], [2]. In this technique, the controller design can be expressed as an optimization problem that takes into account the plant uncertainties. These uncertainties are bounded by a frequency dependent weighting function which describes how much the plant might differ from the nominal model. Additionally, performance can be specified using extra weighting functions. However, the controllers obtained using this methodology are known to be high order, in fact the resulting controller order equals the plant plus weighting functions order [15].

An approach which permits the application of H_∞ methodologies in RC design to obtain lower order controllers is based on removing the high order part of the internal model from the generalized plant used in the optimization [16]. Following this scheme RC controllers have been successfully designed using H_∞ methods in VSI [17], [18]. However, in these approaches no plant/load uncertainty was taken into account.

A similar approach is employed in [19] using μ -synthesis to design an RC for a three-phase inverter. Structured uncertainty is used to describe the converter parameter variations in the LC filter. Resistive and non-linear loads were considered obtaining a THD for nonlinear loads of 1.52 %. In [20] a robust RC is designed using the state space formalism, converter parameter variations are modeled using a time-varying structured uncertainty. It is claimed that non-linear and linear loads can be modeled using that definition. The reported TDH for nonlinear loads is 5.3 %.

In this paper, a methodology to design a robust RC for VSI inverters in DG systems is proposed following the H_∞ norm based optimization procedure. The proposal takes into account the uncertain loads using a weighting function that directly represents how the loads affects the VSI operation. Additional weighting functions for performance improvement are used,

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Fig. 1. VSI circuit diagram.

thus configuring a mixed sensitivity problem. The presented analysis also offers very interesting hints that provide additional criteria to choose the inverter components (LC filter) in order to improve the robustness against uncertain loads.

Furthermore, as it is well-known, linear systems are subject to intrinsic constraints like the waterbed effect[15]. In RC based control systems, this phenomena implies inter-harmonic amplification [21] and the appearance of a resonance peak in the output impedance of the VSI. Proposed methodology allows us to reduce this peak, thus reducing the appearance of undesired oscillations and resonances.

Experimental validation shows that proposed VSI RC provides remarkable performance for a wider range of loads in comparison with conventional RC design methodologies. A THD of 0.6 % is achieved for nonlinear loads which represents an improvement regarding the performance of related robust RC strategies in VSI applications.

This article is organized as follows: Section II describes the architecture of the proposed controller and control goals, Section III explains the RC internal model, Section IV presents the proposed H_∞ design, Section V describes the platform and the experimental results, finally conclusions and remarks are posed in Section VI.

II. APPLICATION DESCRIPTION

The VSI depicted in Figure 1 is a single phase inverter. It is composed of a dc bus voltage, V_{dc} , four switching devices (IGBT), and an LC filter. The dynamical model of the VSI is obtained using the average of the switching function and applying the Kirchhoff's laws. The following model is then obtained:

$$\begin{bmatrix} \dot{i}_f \\ \dot{v}_o \end{bmatrix} = \mathbf{A}_c \begin{bmatrix} i_f \\ v_o \end{bmatrix} + \mathbf{B}_{c,1} v_f + \mathbf{B}_{c,2} i_l \quad (1)$$

$$v_o = \mathbf{C}_c \begin{bmatrix} i_f \\ v_o \end{bmatrix} \quad (2)$$

$$\text{where, } \mathbf{A}_c = \begin{bmatrix} -\frac{R_f}{L_f} & -\frac{1}{L_f} \\ \frac{1}{C} & -\frac{1}{R_c C} \end{bmatrix}, \mathbf{B}_{c,1} = \begin{bmatrix} \frac{1}{L_f} \\ 0 \end{bmatrix}, \mathbf{B}_{c,2} = \begin{bmatrix} 0 \\ -\frac{1}{C} \end{bmatrix}, \mathbf{C}_c = \begin{bmatrix} 0 & 1 \end{bmatrix}.$$

The system states are i_f and v_o which corresponds to the inductor current and capacitor voltage, respectively, v_f is the input voltage, L_f is the filter inductor, C_f is the filter capacitor,

R_f and R_c are the parasitic resistance of inductor and capacitor, respectively. The average of switching function, d_c , is defined in the interval $[0,1]$. Additionally, $v_f = (2d_c - 1)v_{dc}$, where v_{dc} is the dc bus voltage. Therefore, it is important to note that the controller measures the DC bus voltage and adapts the PWM duty cycle to it. This, ideally, decouples the DC bus from the inverter side and introduces robustness against the oscillations of the DC bus voltage. Clearly, the DC bus voltage must always be over the boost value, otherwise the inverter could not operate.

From (1)-(2), two transfer functions can be obtained: $G_p(s) = V_o(s)/V_f(s)$ which is the plant and $G_d(s) = V_o(s)/I_l(s)$ that represents the effect caused by the load in the system. It is important to note that $Z_l(s) = V_o(s)/I_l(s)$, where $Z_l(s)$ is the load impedance.

A. Discrete-time model

Controller design and implementation will be carried out in discrete time domain. Thus, model (1)-(2) is discretized to obtain:

$$\mathbf{x}_p(k+1) = \mathbf{A}_p \mathbf{x}_p(k) + \mathbf{B}_{p,1} v_f(k) + \mathbf{B}_{p,2} i_l(k) \quad (3)$$

$$v_o(k) = \mathbf{C}_p \mathbf{x}_p(k) \quad (4)$$

with $\mathbf{x}_p(k) = [i_f(k) \ v_o(k)]^T$, $\mathbf{A}_p = e^{\mathbf{A}_c T_s}$, $\mathbf{B}_{p,1} = \int_0^{T_s} e^{\mathbf{A}_c \tau} d\tau \mathbf{B}_{c,1}$, $\mathbf{B}_{p,2} = \int_0^{T_s} e^{\mathbf{A}_c \tau} d\tau \mathbf{B}_{c,2}$, $\mathbf{C}_p = \mathbf{C}_c$, and T_s the sampling period.

B. Control goals

The control objective is to provide a sinusoidal voltage output v_o with low distortion. THD values less than 5 % are commonly accepted in actual power quality regulations like IEEE Std-519 and Std-1547. This goal should be achieved despite the load placed at the output of the VSI. Based on model (1)-(2), the load affects the system in two ways: 1) modifies system dynamics 2) in case of nonlinear loads like rectifiers or triggered drives, injects harmonic signals. Since the load is not known a priori, the controller design needs to take into account these operating conditions. From the former, it is necessary to provide the controller with enough robustness to deal with model system variation/uncertainty. From the later, it is needed to reject periodic disturbances.

In the following sections an H_∞ based methodology to design the RC system will be described.

III. REPETITIVE CONTROL STRUCTURE

Fig. 2. Proposed Repetitive Control structure.

Figure 2 shows the RC proposed structure. It consist of an internal model capable of dealing with periodic signals with

only odd harmonics components (see [7] for other internal models used in RC):

$$G_{im}(z) = \frac{-z^{-N/2+l+d}H(z)}{1+z^{-N/2+l}H(z)} \quad (5)$$

where $N = T_p/T_s$ is the number of samples per period of the periodic signal, with T_p the period of the signal and T_s the sampling time. Filter $H(z)$ is a low-pass filter introduced for robustness purposes [22] with the following causal form:

$$H(z) = z^{-l} \left[q_0 + \sum_{k=1}^l q_k (z^{-k} + z^k) \right], \quad (6)$$

where $l < N/2$ must hold in order to preserve the causality of the internal model.

In RC, the controller is usually required to have a lead phase characteristic in order to achieve stability [23], [8], [24]. Non causal controllers can deal easily with this task. Therefore, since the H_∞ design will not seek for non-causal solutions, we can provide a lead phase behavior from the internal model. For that reason, d in (5) is introduced to provide the phase lead.

In this work, a two-degree-of-freedom controller $K(z) = [K_1(z) \ K_2(z)]$ is used, i.e. a compensator with two-input and one-output, as shown in Figure 2. The idea behind using this structure is to add flexibility to the H_∞ design that will be described later in Section IV.

IV. PROPOSED H_∞ BASED DESIGN

Fig. 3. Proposed H_∞ structure design for Repetitive control.

The H_∞ design seeks to find a controller $K(z)$ that makes the closed-loop system stable and achieves enough robustness against load uncertainty. Proposed design is based on the system structure presented in Figure 3, which results from modifying the RC scheme shown in Figure 2.

The following are the criteria for setting up the H_∞ design in concordance with Figure 3:

- 1) Delay element in the internal model, $z^{-N/2+l+d}$, is usually a high order function since it employs a large number N . Due to this, following the developments in [16] and noting that $\|z^{-N/2+l+d}\|_\infty = 1$, the delay is removed from the system. This allows us to obtain lower order controllers. As a result, a fictitious uncertainty is set as Δ_d , where $n\|\Delta_d\|_\infty = \|z^{-N/2+l+d}\|_\infty = 1$. Additionally, weight $n > 1$ provides some extra flexibility during design [17], [18].
- 2) To shape the sensitivity transfer function frequency response and to achieve an appropriate closed-loop transient behavior, the weighting function, $W_e(z)$ is introduced.

- 3) To avoid a control action with high gain in the high frequency range a weighting function, $W_u(z)$, is used.
- 4) The load is taken directly as an uncertain element. This uncertainty is decomposed into a frequency dependent weighting function $W_l(z)$ and a normalized uncertainty Δ_l , where $\|\Delta_l\|_\infty \leq 1$. Therefore, $W_l(z)$ is used to bound the load uncertainty and will take the shape of the highest allowable admittance. Also, this function add flexibility in the minimization of the system norm viewed from u_1 to y_1 . Therefore, it is expected that $W_l(z)$ will add robustness in face to linear and non-linear loads.

In this manner, a mixed sensitivity H_∞ problem is stated [15]. Figure 4 shows the generalized plant scheme of the H_∞ design. The generalized plant is a system expression by means of which the designer can take into account outputs for performance $v = [y_1 \ y_u \ y_e \ y_2]^T$, and feedback $y = [y_3 \ y_4]^T$, reference and disturbances inputs $w = [u_1 \ r \ u_2]^T$, as well as actuator inputs $u = u_3$. In this manner, we seek a stabilizing controller $K(z)$, with input y and output u , that minimizes the H_∞ norm from w to v and satisfies:

$$\left\| \begin{bmatrix} W_l(z)G_{vi}(z) \\ G_{zrc}(z) \\ W_e(z)G_{er}(z) \\ W_u(z)G_{ur}(z) \end{bmatrix} \right\|_\infty < 1 \quad (7)$$

Where $G_{vi}(z)$ is the system from load current to output voltage, $G_{zrc}(z)$ is the function viewed from the delay term, $G_{er}(z)$ is the sensitivity function (from reference to error), and $G_{ur}(z)$ is the function from reference to control action. As it can be derived from (7), the first two terms define the system robust stability and the last two are performance indexes. Therefore, for robust stability, controller $K(z)$ must achieve an H_∞ norm less than one viewed from the delay function $-z^{-N/2+l+d}$ (function $G_{zrc}(z)$) and at the same time from the admittance function $Y_l(z)$ ($W_l(z)G_{vi}(z)$). Precisely, the last characteristic can be interpreted as minimizing the output impedance of the inverter, since its output impedance is $Z_o(z) = V_o(z)/I_l(z) = G_{vi}(z)$. Finally, the performance indexes are used to shape the sensitivity function $G_{er}(z)$ and control action response $G_{ur}(z)$.

Fig. 4. Linear Fractional Transformation model used in the H_∞ design.

Based on the small gain theory, the accomplishment of (7) together with $\|\Delta_d\|_\infty = 1$ and $\Delta_l \leq 1$ will guaranty the robust stability of the system.

In order to obtain the state-space form of the system, the expressions of the system elements have to be defined. Thus, the filter $H(z)$ is realized as:

$$H = \left[\begin{array}{c|c} \mathbf{A}_h & \mathbf{B}_h \\ \hline \mathbf{C}_h & \mathbf{D}_h \end{array} \right].$$

Weight functions $W_l(z)$, $W_u(z)$, $W_e(z)$, and delay $W_z = z^{-d}$ have the expressions:

$$W_l = \left[\begin{array}{c|c} \mathbf{A}_l & \mathbf{B}_l \\ \hline \mathbf{C}_l & \mathbf{D}_l \end{array} \right], \quad W_u = \left[\begin{array}{c|c} \mathbf{A}_u & \mathbf{B}_u \\ \hline \mathbf{C}_u & \mathbf{D}_u \end{array} \right],$$

$$W_e = \left[\begin{array}{c|c} \mathbf{A}_e & \mathbf{B}_e \\ \hline \mathbf{C}_e & \mathbf{D}_e \end{array} \right], \quad W_z = \left[\begin{array}{c|c} \mathbf{A}_z & \mathbf{B}_z \\ \hline \mathbf{C}_z & \mathbf{D}_z \end{array} \right].$$

With the previous definitions, the extended plant $\mathbf{P}$ results:

$$\begin{bmatrix} v \\ y \end{bmatrix} = \mathbf{P} \begin{bmatrix} w \\ u \end{bmatrix} \quad (8)$$

where:

$$\mathbf{P} = \left[\begin{array}{c|c|c} \mathbf{A} & \mathbf{B}_1 & \mathbf{B}_2 \\ \hline \mathbf{C}_1 & \mathbf{D}_{11} & \mathbf{D}_{12} \\ \hline \mathbf{C}_2 & \mathbf{D}_{21} & \mathbf{D}_{22} \end{array} \right]$$

with:

$$\mathbf{A} = \begin{bmatrix} \mathbf{A}_p & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \mathbf{B}_l \mathbf{C}_p & \mathbf{A}_l & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{A}_u & \mathbf{0} & \mathbf{0} & \mathbf{0} \\ -\mathbf{B}_e \mathbf{C}_p & \mathbf{0} & \mathbf{0} & \mathbf{A}_e & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{A}_z & \mathbf{0} \\ -\mathbf{B}_h \mathbf{C}_p & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{B}_h \mathbf{C}_z & \mathbf{A}_h \end{bmatrix},$$

$$\mathbf{B}_1 = \begin{bmatrix} \mathbf{B}_{p,1} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{B}_e & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{B}_z \\ \mathbf{0} & \mathbf{B}_h & \mathbf{B}_h \mathbf{D}_z \end{bmatrix}, \quad \mathbf{B}_2 = \begin{bmatrix} \mathbf{B}_{p,2} \\ \mathbf{0} \\ \mathbf{B}_u \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \end{bmatrix},$$

$$\mathbf{C}_1 = \begin{bmatrix} \mathbf{D}_l \mathbf{C}_p & \mathbf{C}_l & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{C}_u & \mathbf{0} & \mathbf{0} & \mathbf{0} \\ -\mathbf{D}_e \mathbf{C}_p & \mathbf{0} & \mathbf{0} & \mathbf{C}_e & \mathbf{0} & \mathbf{0} \\ -\mathbf{D}_h \mathbf{C}_p & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{D}_h \mathbf{C}_z & \mathbf{C}_h \end{bmatrix},$$

$$\mathbf{C}_2 = \begin{bmatrix} \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} \\ -\mathbf{C}_p & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} \end{bmatrix},$$

$$\mathbf{D}_{11} = \begin{bmatrix} \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{D}_e & \mathbf{0} \\ \mathbf{0} & \mathbf{D}_h & \mathbf{D}_h \mathbf{D}_z \end{bmatrix}, \quad \mathbf{D}_{12} = \begin{bmatrix} \mathbf{0} \\ \mathbf{D}_u \\ \mathbf{0} \\ \mathbf{0} \end{bmatrix},$$

$$\mathbf{D}_{21} = \begin{bmatrix} \mathbf{0} & \mathbf{0} & \mathbf{1} \\ \mathbf{0} & \mathbf{1} & \mathbf{0} \end{bmatrix}, \quad \mathbf{D}_{22} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \end{bmatrix}.$$

V. EXPERIMENTAL VALIDATION

This section presents the numerical design and experimental validation of the proposed robust RC strategy.

A. Design

The parameters of the single phase VSI shown in Figure 1 are: $L_f = 900 \mu\text{H}$, $C_f = 40 \mu\text{F}$, $R_f = 1.5 \Omega$, $R_c = 8200 \Omega$, $v_{dc} = 300 \text{ V}$, $v_o = 110 \text{ V}_{\text{rms}}$. With this, the proposed H_∞ design will be presented including a comparison with a conventional plug-in RC. Both designs use an odd-harmonic internal model with $N = 240$ resulting of tracking/rejecting a 60 Hz periodic signal with a sampling period of $T_s = 14400 \mu\text{s}$.

Fig. 5. Repetitive control in plug-in structure.

1) *Plug-in RC*: For comparison purposes, a plug-in RC configuration has also been designed and its scheme is shown in Figure 5. The structure is equivalent to the one shown in Figure 2 using $K(z) = [G_x(z)G_c(z) \ G_c(z)]$, where $G_x(z)$ is a stabilizing filter and $G_c(z)$ is a baseline compensator. It is important to note that the plug-in RC controller was designed aimed at obtaining a balance between: performance for linear loads, performance for non-linear loads, and small transient time.

The stability condition of the plug-in RC is defined by $\|z^{-N/2}H(z)[1 - G_x(z)G_o(z)]\|_\infty < 1$ [7], [25]. Where $G_o(z)$ is the closed loop of the baseline controller $G_c(z)$ without the RC, i.e. $G_o(z) = G_c(z)G_p(z)/(1 + G_c(z)G_p(z))$. Usually $G_x(z)$ can be defined as $G_x(z) = k_r/G_o(z)$, with k_r a design parameter. Therefore, the system robustness will depend on achieving a good inversion of $G_o(z)$, which in turn depends on the plant transfer function. As a consequence, the change in plant dynamics caused by the connected loads affects the plug-in RC system robustness. It is important to note that, with an exact inversion of $G_o(z)$, the constant $k_r \in (0, 2)$ for stability.

By means of the stability condition, a relation between $H(z)$ and k_r can be inferred. Since $G_x(z)$ does not perform a perfect inversion of $G_o(z)$, specially at high frequencies, the bandwidth of the low pass filter $H(z)$ should not be too large and k_r should take small values. As a result, a small bandwidth in $H(z)$ will allow larger values in k_r but a larger bandwidth will limit the value of k_r that can be used.

The following characteristics were found to be critical:

- 1) The bandwidth of filter $H(z)$ defines the among of harmonics the system can reject effectively [22], [26]. In that way, good THD performance can be achieved by means of using a large bandwidth in $H(z)$. However, as stated before, the system robustness might be reduced.
- 2) Parameter k_r affects the transient convergence of the system [27], [28]. The larger the value of k_r is, the faster the system response will be, but the robustness will be reduced.
- 3) These two parameters, $H(z)$ bandwidth and k_r , interact in such a way that using a larger bandwidth limits the

values of k_r we can use. Therefore, a balance between performance in THD and system transient needs to be made.

- 4) Baseline controller $G_c(z)$ must be designed for the rejection of low frequency and non-periodic disturbances. Also, its design should provide enough robustness margins. Simple controllers as Proportional (P), Proportional-Integral (PI) or lead and lag networks are usually employed.

As a result, bandwidth of filter $H(z)$ and value of k_r were selected to obtain acceptable performance for all loads with good harmonic compensation and small transient time. The final setup is as follows: the controller was defined as $G_c(z) = 0.002$ and $G_x(z) = k_r/G_o(z)$, with $k_r = 0.3$ and $G_o(z) = G_c(z)G_p(z)/(1 + G_c(z)G_p(z))$, also $H(z) = (-0.002495z^{12} - 0.009018z^{11} - 0.0145z^{10} + 0.01771z^9 + 0.1166z^8 + 0.2417z^7 + 0.3001z^6 + 0.2417z^5 + 0.1166z^4 + 0.01771z^3 - 0.0145z^2 - 0.009018z - 0.002495)/z^{12}$ with bandwidth $BW_{rc} = 1670$ Hz was used (filter $H(z)$ computation is based on Matlab algorithm *fir1* which calculates FIR filter parameters based on least-squared approximation).

2) H_∞ design: The H_∞ design described in Section IV starts with the definition of filter $H(z)$. Thus, filter $H(z)$ is obtained as a balance between harmonic rejection performance and robustness. In this case, a filter with bandwidth of $BW_{hinf} = 2740$ Hz achieves the balance (the order of the filter is selected to provide enough stopband attenuation):

$$H(z) = (0.003419z^{12} + 0.006348z^{11} - 0.01444z^{10} - 0.05083z^9 + 0.03771z^8 + 0.2938z^7 + 0.4481z^6 + 0.2938z^5 + 0.03771z^4 - 0.05083z^3 - 0.01444z^2 + 0.006348z + 0.003419)/z^{12}.$$

It is important to note that the maximum obtained bandwidth of filter $H(z)$ in case of the plug-in RC was $BW_{rc} = 1670$ Hz which is significantly lower than the one obtained for the proposed robust design $BW_{hinf} = 2740$.

The design of the weighting functions is done as follows:

1) Weighting function $W_e(z)$ shapes the system sensitivity function $G_{er}(z)$. Therefore, $W_e(z)$ acts to obtain small error response at low frequencies, allows enough action at the fundamental and harmonic frequencies and penalizes the amplification at the high end. Firstly, attenuation of low frequency non-periodic errors was defined to be less than 20% below 0.1 Hz. Secondly, due to the water-bed effect, it is expected that the RC makes $G_{er}(z)$ larger in the harmonic rejection zone, therefore $W_e(z)$ will allow larger values in the interval from 6 Hz to 600 Hz. With this definition the Nyquist plot will get closer to the $(-1, 0)$ point, however this approximation remains valid since we expect less system uncertainty in this frequency interval. Furthermore, penalizing in excess this region yields larger transient response. A maximum of 14 dB was allowed for this interval. Finally and in concordance with the design of $H(z)$, at frequencies beyond 2500 Hz, where more uncertainty is common and no harmonic rejection is required ($H(z)$ bandwidth is 2740 Hz), $W_e(z)$ is defined to obtain less than 4.5 dB in $G_{er}(z)$. Figure 6 shows the frequency response of $1/W_e(z)$.

2) Weighting function $W_u(z)$ is defined to limit the action of the control signal at high frequencies. Although a specific frequency response can be defined, for sake of simplicity a constant value of 0.5 was found to be sufficient for this goal.

3) The weighting function $W_l(z)$ has the shape of the given load admittance uncertainty. At the same time, $W_l(z)$ helps to minimize the VSI output impedance. For those reasons, $W_l(z)$ should be as large as possible for all frequencies. Due to the strong connection between $G_{il,v}(z)$ and $G_{er}(z)$ defined by $G_{il,v}(z) = G_d(z)G_{er}(z)$ (with $G_d(z) = V_o(z)/I_l(z)$), it is important to note that we expect large values in $G_{il,v}(z)$ for the harmonic rejection region (above 6 Hz). Following these reasoning, at low frequencies, below 0.5 Hz, a conductance of maximum 1.1 S was expected, and at frequencies above 5 Hz, the allowable admittance was lower with 0.124 S. Figure 7 depicts the frequency responses of $1/W_l(z)$.

4) The delay function $W_z = z^{-d}$ was found to affect the gain of the obtained controller $K(z)$. Fixing the other weighting functions and varying d , it is found that for larger values of d the controller achieves lower gain at very high frequencies and higher gain below them. This is a good characteristic since it allows obtaining lower high frequency amplification and faster transient response. However, this characteristic is lost as d is increased, showing little effect after $d = 7$. For that reason $W_z = z^{-7}$ was selected. On the other hand, the value $n = 100$ was found to work well during the procedure of adjustment of all other weights.

The designed weighting functions are:

$$W_l = \left[\begin{array}{cc|c} 0.9998 & 0.01562 & \\ \hline 0.01475 & 0.1241 & \end{array} \right], W_u = 0.5,$$

$$W_e = \left[\begin{array}{cc|c} 0.0.9998 & -0.02931 & 0.08927 \\ 0 & 0.7475 & 0.5 \\ \hline 0.024 & -0.1796 & 0.547 \end{array} \right], W_z = z^{-7}, n = 100.$$

With this setup, the solution of the proposed H_∞ problem can be realized by means of the LMI (linear matrix inequality) option of the Matlab algorithm *hinfsyn* [29]. Resulting controller has the same order of $\mathbf{P}$ which is 26. However, a controller with reduced order can be calculated using the transformation to the balanced form and truncating [30], taking care of obtaining the same frequency response. This reduction order method is available through the *balancmr* command in Matlab. Therefore, after a state reduction, we obtain the controller $K(z)$:

$$K(z) = \left[\begin{array}{c|c} \frac{N_{k,1}(z)}{D_k(z)} & \frac{N_{k,2}(z)}{D_k(z)} \end{array} \right]$$

with:

$$N_{k,1}(z) = 0.2296z^6 - 0.2266z^5 - 0.08976z^4 + 0.1849z^3 - 0.192z^2 + 0.04177z + 0.0521,$$

$$N_{k,2}(z) = -0.06293z^6 - 0.3568z^5 + 0.6323z^4 + 0.00574z^3 - 0.4793z^2 + 0.3514z - 0.09,$$

$$D_k(z) = z^6 - 2.195z^5 + 1.914z^4 - 0.8831z^3 + 0.1336z^2 + 0.05221z - 0.02161.$$

Fig. 6. Frequency response of $G_{er}(z)$ and $1/W_e(z)$.

Since the robust design is done without the delay term, a variation over the obtained functions is expected when this is finally added to the system. Figure 6 shows the frequency response of $1/W_e(z)$ and the obtained $G_{er}(z)$ with and without the delay term. It can be seen that once the delay function is added, the modified sensitivity function exceeds the bound but the obtained performance index is still good. Figure 7

Fig. 7. Frequency response of $G_{vl}(z)$, $1/W_l(z)$, and $1/W_e(z)$.

depicts the frequency responses of $1/W_l(z)$ and the obtained $G_{il,v}(z)$ with and without the delay function. It is observed, that although the response of $G_{il,v}(z)$ with repetitive control is larger, the obtained bound is still satisfactory. Additionally, since strong influence of $W_e(z)$ can be expected over $G_{il,v}(z)$, it can be seen that the low frequency definition of $W_e(z)$ bounds $G_{il,v}(z)$ while the higher frequencies are limited by $W_l(z)$.

3) *Robust stability analysis:* Since the delay function has been taken apart and treated as a fictitious uncertainty with infinite norm 1, we can verify the robustness of the system viewed from this delay, i.e. function $G_{zrc}(z)$. In order to do that we use a resistive load. Figure 8 shows the H_∞ norm $\|G_{zrc}(z)\|_\infty$ against different values of a resistive load. It can be observed that $\|G_{zrc}(z)\|_\infty$ tends to 1 whenever R_L tends to 0, and tends to 0.9638 when R_L tends to infinity. Therefore, viewed from the delay function, the control system always

Fig. 8. $\|G_{zrc}(z)\|_\infty$ as a function of a resistive load. Fig. 9. Frequency response of $G_{vl}(z)$ for plug-in and proposed RC schemes.

preserves robust stability. Furthermore, this characteristic does not depend on the value of the delay.

The robustness against load uncertainty is analyzed introducing the delay function in the system. In this way, the achieved H_∞ norm of $G_{vl}(z)$, with the delay function $-z^{-N/2+l+d}$ in place, is 8.48, which means that a load with H_∞ norm less than $1/8.48$ will guarantee robust stability.

The robustness of the proposed RC has been compared with the one obtained with plug-in design. Figure 9 shows the frequency response of both systems from i_l to v_o . It can be observed that, although plug-in approach obtains better robustness at some frequencies it has a high peak of 18.39 (its infinity norm) around 813 Hz, while the proposed RC design achieves a flatter frequency response around those frequencies. Therefore, the robust RC system proposed in this work provides an important improvement compared with this classical structure in terms of robust stability. It is important to note that the frequency response of $G_{vl}(z)$ is also interpreted as the system output impedance. Therefore, the proposed H_∞ design provides a lower H_∞ norm of the output impedance. Also, it can be seen from Figure 9, that at harmonic frequencies the output impedance of both system has very small values, being lower the values for the proposed H_∞ design.

4) *Hints for LC filter design:* The values of L_f and C in the output LC filter affects the obtained H_∞ norm. Figure 10 show how the values of the filter inductor and capacitor influence the minimum norm $\|G_{vl}(z)\|_\infty$ obtained. For that purpose, weight functions $W_l(z)$, $W_u(z)$, and $W_e(z)$ are set to 1. It can be observed that the larger the value of C the greater the robust stability margin. The value of the inductor affects only

Fig. 10. H_∞ norm of $G_{vi}(z)$ as a function of L_f and C .

moderately for higher capacitance, but a smaller inductance yields larger robustness. This fact can be taken into account during the design of the LC filter in order to obtain better robustness margin in the VSI system.

This selection guideline base on system robustness corresponds with the idea of having a small inductor L_f in order to obtain smaller losses in the LC filter. However, decreasing the inductance reduces the high frequency attenuation. As a result, it is needed to use a larger capacitance C in order to maintain the same relation $1/\sqrt{L_f C}$, and thus the same high frequency attenuation.

B. Experimental setup

The experimental setup is composed of a power inverter, which is an IGBT power stage by Semikron, and a set of linear and non-linear loads. The controller runs in the rapid control prototyping system XPCTarget, developed by Matlab. This platform incorporates a PWM generation card and an analog to digital interface. Current and voltage sensors are also included. The dc bus is created using a three phase rectifier bridge which takes the power from an autotransformer. Figure 11 shows the experimental platform.

C. Performance

To verify the performance of the proposed design, the single phase VSI is connected to different loads: a set of linear loads consisting of a fixed resistor branch of 8.5Ω in series with different inductors varying for 10 mH to 34 mH and a nonlinear load configured as a full-bridge diode rectifier with capacitor ($680 \mu\text{F}$) that feeds a resistive branch of 13Ω .

1) *Plug-in RC*: Based on the set-up defined previously in this section, the plug-in RC was implemented in the VSI. A linear load with a lag PF of 0.69 and the non-linear one were used. Figure 12 shows the resulting waveforms. A THD of 1.2% and 1.3% were obtained for nonlinear and linear loads, respectively. Figure 13 shows the transient response of the plug-in RC. In this case a resistive load and nonlinear load are arranged in parallel and connected to the VSI. The transient response occurs due to the connection of the linear load.

Fig. 11. Experimental platform.

Although the voltage amplitude does not suffer grater changes, it can be noticed a transient of 6 cycles in the waveform. Although the performance of the plug-in RC is acceptable, it can be noticed that its behavior is affected by the dynamics changes caused by the connected loads.

2) *H_∞ design*: In order to validate the proposed H_∞ design of the RC, the VSI is connected with linear and nonlinear loads. Figure 14 shows the obtained THD and waveforms for a linear load with PF=0.69 and the nonlinear load connected at the output of the VSI. As it can be seen, the performance is remarkable with very low THD and good voltage waveform even in case of nonlinear loads were current includes high harmonic content and small reactive power (see also the results in Table I).

Table I summarizes the results for various loads in terms of PF, active and reactive power and the obtained performance in THD. From Table I and Figure 14, it is observed that very low THD is preserved against different loads. Comparing these results with the ones obtained for the plug-in RC and shown

Fig. 12. System performance for plug-in RC with nonlinear (50 V/div, 20 A/div) (Top) and linear (50 V/div, 10 A/div) (Bottom) loads.

Fig. 13. Load change response for plug-in RC: connection of a linear load in parallel with fixed nonlinear load (50 V/div, 20 A/div).

TABLE I
LOAD CHARACTERISTICS AND OBTAINED PERFORMANCE.

PF	P [W]	Q [VAR]	Voltage THD	Current THD	Voltage [Vrms]	load type
≈ 1	910	0	0.2	0.6	110.4	linear
≈ 1	470	10	0.2	1.0	110.4	linear
0.86	630	350	0.3	15.5	110.4	linear
0.62	390	390	0.2	19.3	110.4	linear
0.5	190	300	0.2	20.5	110.4	linear
0.57	380	140	0.3	79.3	110.4	non-linear
0.84	860	140	0.3	51.5	110.7	nl // l

in Figure 12, it can be observed a substantial improvement in performance.

The system response against load changes is also analyzed. The system load is the parallel combination of linear and nonlinear loads as the one used in Figure 14. Figure 15, shows the system transient response resulting from connecting and disconnecting the linear load (the nonlinear load is always present). It can be observed that the system recovers the voltage amplitude in 1 cycle while the waveform recovery can take from 2 to 4 cycles.

These results are better compared with [19] that uses a multiplicative plant uncertainty, where THD=0.73 % for resistive loads and THD=1.52 % for nonlinear loads were

reported. Also, the transient is slightly improved since they report a convergence between 5 to 7 cycles. Additionally, compared to the robust continuous state-space design in [20], the performance obtained for nonlinear loads is considerably improved given that they reported a THD of 5.3 %. The work in [3] presents an adaptive approach with an experimental THD for non-linear loads of 1.52 %; however design and implementation are rather complex compared with the one proposed here.

Reference [18], shows an H_∞ design with RC for VSI. However, the main difference with the approach presented here is that the plant uncertainty was not considered, the proposed weighting functions are defined differently, and the error performance is not included. Furthermore, it is obtained a THD of 5.05 % and 1.1 % for non-linear and linear loads, respectively. In this way, the strategy proposed here outperforms those results.

Fig. 15. Load change response: linear load on-off in parallel with fixed nonlinear load (50 V/div, 20 A/div). Top: on, Bottom: off.

3) *Alternative scenario:* The experimental platform has a maximum current of 13 A. For that reason and in order to achieve more demanding scenarios for the control system, a lower output ac voltage of $V_{ac} = 40$ V_{peak} and dc bus voltage of $v_{dc} = 130$ V were also used. Furthermore, the loads were adjusted to draw currents with similar values as the ones obtained with the higher voltage scenario. This new setup represents more exigent conditions based on the fact that the THD is a relative measure of distortion, i.e. under the same current demand an inverter with lower output voltage will exhibit larger voltage distortion.

Figure 16 shows the system response for a non-linear in the case of conventional RC and proposed robust RC. It can be observed that the robust RC maintains its performance

Fig. 14. System performance for Robust RC with nonlinear (50 V/div, 20 A/div) (Top) and linear (50 V/div, 10 A/div) (Bottom) loads.

with low THD, while the conventional RC results much more affected under these operational conditions.

Fig. 16. System performance for conventional RC (50 V/div) (Top) and Robust RC (50 V/div) (Bottom). Non-linear load at 40 Vpeak.

TABLE II
LOAD CHARACTERISTICS AND OBTAINED PERFORMANCE.

PF	P [W]	Q [VAR]	Voltage THD	Current THD	Voltage [Vrms]	load type
≈ 1	127	3	0.6	0.9	28.94	linear
0.86	86	51	0.5	6.4	28.82	linear
0.62	39	47	0.6	6.9	28.82	linear
0.45	16	31	0.8	10.8	28.82	linear
0.74	113	69	0.5	49.4	28.94	non-linear
0.93	244	61	0.6	28.9	29.19	nl // 1

The results obtained in this new scenario are depicted in Table II. It can be shown that even under more demanding conditions, the proposed robust RC achieves remarkable performance.

Fig. 17. System performance for conventional PI control. Non-linear load (Top) and linear load with PF=0.68 lagging (Bottom).

4) *PI control case:* For comparison purposes, a PI controller is designed and experimentally validated (see Figure 18). The best performance was achieved using $k_p = 0.6$ and $k_i = 300$. As shown in Figure 17, the obtained THD was 3.9 % for a linear load with lagging $PF = 0.69$ and 7.2 %

Fig. 18. PI control structure.

for non-linear loads. This experiment shows that conventional controllers, as the PI control, are not able to achieve good enough harmonic compensation under different types of loads.

VI. CONCLUDING REMARKS

This work presents a repetitive control H_∞ design for VSI in a DG system application aimed at obtaining robust stability against load uncertainty/variations. As a result, the designed system can operate with different load characteristics preserving very high performance in terms of output voltage THD. Furthermore, the proposed design achieves better performance compared to conventional plug-in RC, allowing the improvement of the harmonic rejection and transient response.

As a difference with other robust RC used in VSI applications, the proposed scheme renders the unknown load as an unstructured uncertainty which helps to overcome this problem more directly. As a consequence of this treatment, solving the H_∞ minimization problem reduces the resonant peak response present in the output impedance of the VSI. In this way also possible resonances can be avoided.

The experimental validation also shows that the proposed H_∞ design allow us to obtain a robust control system with larger bandwidth in filter $H(z)$ and to shape the controller frequency response. The former affects positively the harmonic performance and the later help us to obtain better transient behavior and avoid high frequency amplifications. The performance shows low THD and good transient response. This performance is obtained using a single loop configuration, i.e. the output voltage as a feedback signal.

Finally, an insight is given about the values that can be used in the inverter LC filter for which we can obtain better robustness against load uncertainty. Therefore, in order to improve the robustness of the VSI, the idea of having large capacitance and small inductance can be taken into account during the LC filter design process.

ACKNOWLEDGMENTS

This work has been partially funded by the Spanish national project DOVELAR ref. RTI2018-096001-B-C32 (MCIU/AEI/FEDER, UE). This work is supported by the Spanish State Research Agency through the María de Maeztu Seal of Excellence to IRI (MDM-2016-0656). This work is partially funded by AGAUR of Generalitat de Catalunya through the Advanced Control Systems (SAC) group grant (2017 SGR 482). This work is partially funded by DIB Universidad Nacional de Colombia (Projects under Hermes codes 35664 and 41000).

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