

Safety factor calibration for a new model of shear strength of reinforced concrete building beams and slabs

Jesús-Miguel Bairán¹, Joan R. Casas²

¹ Associate Professor, Department of Civil and Environmental Engineering. Universitat Politècnica de Catalunya – BarcelonaTECH, Barcelona (Spain). Email: jesus.miguel.bairan@upc.edu

² Professor, Department of Civil and Environmental Engineering. Universitat Politècnica de Catalunya – BarcelonaTECH, Barcelona (Spain). Email: joan.ramon.casas@upc.edu

ABSTRACT

When assessing existing structures, the availability of adequate safety factors, calibrated with the most accurate models, and for established target reliability indexes, is of critical importance in order to take the right decision regarding the maintenance/repair/strengthening interventions. In the case of shear resistance in reinforced concrete (RC) structures, when using the current design codes provisions for new constructions in assessment results that, in many cases, existing structures may be considered unsafe, implying large economic costs in strengthening or even dismantling. In this research, a proposal of safety factor relative to a recently developed model for shear strength, for elements with and without transversal reinforcement, based on a reliability-based calibration is presented. A formulation is proposed to determine the adequate strength factor for a selected target reliability index of the existing structure and desired remaining service life by means of a safety factor format, considering the load factors present in the Eurocodes. The calibration is carried out considering typical geometry and load ratios of building floors, as well as normal and high strength concrete. The derived safety factor is almost independent of the chosen remaining service life.

Keywords: safety factor; shear; reinforced concrete; assessment; reliability; building floors; beams, slabs

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28 1. INTRODUCTION

29 The design process of a new concrete structure, or assessment of an existing one, should verify
30 a limit-state condition of the form:

$$31 R_d \geq S_d \quad (1)$$

32 Being R_d and S_d the design values of the resistance and action-effects, respectively. The semi-
33 probabilistic approach is the most common methodology used in practical applications. In this
34 case, the action design value is computed by means of partial factors for loads, as e.g. Eq. (2) for
35 the case of persistent or transient load situations. Here, $S_{G,ki}$ and $S_{Q,kj}$ are the characteristic values
36 of the permanent action “ i ” and variable action “ j ”, γ_{Gi} and γ_{Qj} are the partial safety factors for
37 the permanent and variable actions. Variable load $j=1$ is the leading one, while the accompanying
38 loads ($j>1$) are affected by a combination factor Ψ_j , which is less or equal to 1.0.

$$39 S_d = \sum_{i=1}^n \gamma_{Gi} S_{G,ki} + \gamma_{Q1} S_{Q,k1} + \sum_{j>1}^n \gamma_{Qj} \Psi_j S_{Q,kj} \quad (2)$$

40 The design value of the resistance may be computed by means of partial safety factors applied
41 to materials characteristic values, usually concrete strength and steel yielding strength, as shown
42 in Eq. (3), where f_{ck} , f_{yk} , γ_C , γ_S are the characteristic compressive strength, yielding strength and
43 partial safety factors of concrete and steel. Alternatively, the design resistance can be obtained
44 by a strength reduction factor, as shown in Eq. (4). In this case, γ_R is a strength safety factor which
45 is applied in a global form to the resistance model, this is equivalent to the inverse of the strength
46 reduction factor (ϕ).

47 In general, partial load factors account for the possibilities of unfavourable deviation of the
48 load from its representative value, uncertainties in modelling of the load and of its effects.
49 Materials partial factors and strength reduction factor account for the possibility of unfavourable
50 deviation of the material property from the specified value, resisting model uncertainty, the
51 geometrical deviations not considered explicitly and, in some cases, the consequences of failure.

52 Equations (3) and (4) represent, respectively, the two currently most used approaches in which
53 safety factors are defined depending on the materials or the resisting mechanism involved, e.g.
54 shear and bending require different strength reduction factors.

$$55 R_d = R \left(\frac{f_{ck}}{\gamma_C}; \frac{f_{yk}}{\gamma_S} \right) \quad (3)$$

$$56 R_d = \frac{1}{\gamma_R} R(f_{ck}; f_{yk}) = \frac{1}{\gamma_R} R_k = \phi R_k \quad (4)$$

57 If the partial safety factors have been appropriately calibrated, the required level of safety is
 58 deemed satisfied through the verification of Eq. (1). Strength reduction factors shall be used
 59 together with the same set of load factors considered in their calibration, in order to approach the
 60 target reliability. For example, in the 2002 version of ACI-318 [1], the load factors were modified
 61 to adapt them to the ASCE/SEI-7 [2] general provisions for minimum design loads in order to
 62 simplify the design process of structures with components of different materials, that required a
 63 recalibration of the strength reduction factor for shear, see Table 1. However, the alternative set
 64 of load and strength factors in Annex C of ACI-318 is allowed, if they are used together.

65 In ACI-318 the strength reduction factor also considers the brittle or ductile nature of the
 66 failure mode. As in the former, the element is more sensitive to larger variation of concrete
 67 strength in tension and compression and consequences of failure may be higher, hence a more
 68 conservative value of the resistance, i.e. a lower fractile, is needed to achieve the needed
 69 reliability.

70 Table 1: Load and strength safety factors in ACI-318 and Eurocodes

	ACI-318-02 [1]		Eurocodes [3, 4]
	Main body	Annex C (prior 2002)	
Dead load factor	1.2	1.4	1.35
Live load factor	1.6	1.7	1.5
Shear strength reduction factor ($\phi = 1/\gamma_R$)	0.75	0.85	-
Concrete strength partial safety factor (γ_C)	-	-	1.5
Steel strength partial safety factor (γ_S)	-	-	1.15

71 On the other hand, Eurocodes 2 [3] and 1 [4] provide a set of partial safety factors for steel
 72 (γ_S) and concrete (γ_C) properties, together with a set of partial load factors. The code was
 73 calibrated for a yearly target reliability index of $\beta_1 = 4.7$, which is equivalent to a nominal
 74 probability of failure in 1 year of approximately 10^{-6} [5].

75 When dealing with the assessment and/or strengthening of an existing building, a question
 76 about the suitability of using the same partial safety factors of the design of new elements arises.
 77 In general, there is less uncertainty in the geometrical and material parameters and an increment
 78 of the safety level may require a much larger economic effort than to achieve the same increment
 79 in a new design. Additionally, the required remaining service life may be shorter than in new
 80 constructions.

81 Therefore, the definition of the target reliability level for assessing existing structures should
82 be based on risk of failure and cost optimization; including repair interventions, losses due to
83 malfunction, environmental and psychological effects. A framework for establishing the target
84 reliability corresponding to a remaining service life is available in some codes, as ISO 13822 [6],
85 ISO 2394 [7], and recommendations, such as fib [8]. Hence, economic optimization can be used
86 to derive target reliability values. However, human safety levels based on individual and societal
87 risk for ethical issues should also be considered in the process, as stated in Sýkora et al. [9],
88 Tanner and Hingorani [10], Steenbergen et al. [11]. As concluded in Steenbergen et al. [11], the
89 minimum levels related to human safety are often critical target reliabilities for existing structures.

90 After the target reliability index is defined, suitable and properly calibrated resistance models
91 are needed, including the statistical definition of the model error. The particular case of assessing
92 shear resistance in existing concrete elements has gained much attention recently, as the current
93 design provisions have raised doubts regarding the safety of constructed facilities, implying that
94 many structures are to be strengthened or dismantled. Furthermore, contrary to bending strength,
95 whose resisting theory is well consolidated, there are currently several shear strength theories,
96 based on different hypotheses and with different accuracy and complexity levels. In recent
97 investigations, experimental tests have been conducted in existing structures or elements that were
98 deemed unsafe according to current design provisions, e.g. Zwicky and Vögel [12], Bergström et
99 al. [13]. In some cases, shear performance observed by experimentation was much better than
100 the expected according to the provisions for new structures. The use of adequate non-linear
101 computational models accounting for non-linear shear behavior have also shown similar results,
102 Ferreira et al. [14, 15]. Hence, it can be expected certain cost reduction in strengthening of
103 structures or even no need of posting or substitution, after an advanced assessment of the existing
104 safety level.

105 However, adequate nonlinear models for shear assessment are not always available, or it is not
106 possible to systematically build a computational model for a large number of different structures
107 in a network and perform the probabilistic analyses. Therefore, simpler models that are adequate
108 for hand or spreadsheet calculations are useful in these cases. In addition, for practical and fast
109 assessment application in a semi-probabilistic format, the strength reduction factors should be
110 calibrated.

111 The objective of the present study is to propose adequate reliability-based design/assessment
112 equations with properly calibrated safety factors for reinforced concrete beams and slabs of
113 buildings, failing in shear, for a various target reliability indexes. The current method is restricted
114 to shear failure taking place in sections that have not yielded previously in bending or axial force.

115 The paper is organized in the following way. Section 2 presents a statistical analysis of selected
116 existing models for shear resistance in concrete members to define the most accurate and
117 statistically define the corresponding model error. By the use of this model and after the definition
118 of the sample set, Section 3 carries out the calibration process to define the safety factor, and the
119 analysis of the results and discussion is presented in Section 4. Finally, the main conclusions are
120 drawn in Section 5.

121 2. SHEAR RESISTANCE MODEL

122 For an appropriate calibration of safety factors, the first step is to derive accurate design
123 equations for the shear strength capacity of reinforced concrete beams, based on the available
124 theoretical models, jointly with the statistical characterization of the random variable of the
125 “model error”. This random variable represents the ratio of the actual response to the model
126 prediction and is characterized by a statistical distribution, its mean value (or bias ratio) and
127 standard deviation (or coefficient of variation, CoV).

128 In this paper, a recently mechanical-based formulation for shear-flexure strength of reinforced
129 concrete beams, proposed in Mari et al. [16], is used. This model assumes a combination of the
130 four classical shear resisting mechanisms; namely, capacity of the uncracked compression chord
131 (V_c), capacity of the diagonally cracked web (V_w) and the contribution of the transverse (V_s) and
132 longitudinal reinforcements (V_l). The model provides a set of mechanistic derived closed-form
133 equations for each action, here summarized in Table 2.

134 2.1. DESCRIPTION

135 The main aspects of the model can be explained based on Fig. 1; here, the shear stress
136 distributions in a reinforced concrete beam are analyzed for the free-body equilibrium of the
137 segment of the beam between the cross-sections 1 and 2 (Fig. 1a), at the initiation of an inclined
138 crack in the tensile side and its tip, respectively. As discussed in Marí et al. [16] and Bairán and
139 Marí [17, 18], the distribution of shear stresses depends on the crack pattern and bond between
140 concrete and reinforcement. Fig. 1b shows the shear stress distribution for an almost vertical
141 crack and perfect bond between reinforcement and concrete, the stresses are almost constant in
142 the tensile cracked portion and corresponds to the so-called *beam-action*. Although acceptable in
143 wide range of load stages, these hypotheses do not hold up to failure and thus shear stress
144 distribution varies.

145 In the ideal situation of zero bond of the longitudinal reinforcement, its tensile force is constant
146 between the two sections and the stress distribution is as in Fig. 1c, with a variation of the lever
147 arm. This leads to a pure *arch-action* in which shear stresses are resisted only in the compression

148 chord. Although completely loss of bond is not likely if ribbed reinforcement with adequate
149 development length is used, bond deterioration takes place as shear damage propagates. Recently,
150 Carmona and Ruiz [19] studied the role of bond deterioration on shear resistance on the basis of
151 fracture mechanics and Yang [20] related the formation of the longitudinal crack at the level of
152 tensile reinforcement with the on-set of shear failure. Therefore, it is plausible to accept that bond
153 will develop imperfect during the evolution of shear resisting actions.

154 In the cracked portion of the beam, shear stresses can be resisted by aggregate interlock,
155 residual tensile stresses and inclined compression stress field. However, after crack opening
156 increases, it is considered that the residual tensile stresses concentrate in the portion close to the
157 neutral axis, where crack width is still moderate, and in the uncracked compression chord; while
158 in the region with larger crack width, mainly the inclined compression strut acts. In this situation,
159 the distribution of shear stresses is depicted in Fig. 1d. The variation of tensile force is less than
160 for perfect beam-action and a combination of normal and shear stresses exist in the uncracked
161 compression chord. This is an intermediate situation between the perfect *beam-action* (Fig. 1b)
162 and the perfect *arch-action* (Fig. 1c). The compression stresses in the shear cracked portion of
163 the beam result from the longitudinal component of the inclined compression field.

164 The model was developed for elements that fail in shear before yielding of the longitudinal
165 reinforcement, so longitudinal reinforcement is elastic and the normal stresses in the compression
166 zone is considered to follow a linear distribution. The main hypothesis of the model is that, as
167 shear cracking opens and evolves, the distribution of shear stresses in the critical region varies
168 from one similar to Fig. 1b to that of Fig. 1d, making the magnitude of shear stresses in the
169 compression head to increase. The details on the derivation of the model equations can be found
170 in [16]; however, in the following, a global description of the process is presented.

171 Firstly, the shear contribution of the cracked web (v_w) is estimated from the residual tensile
172 strength according to the concrete's tensile fracture energy and the maximum crack width; which
173 is computed from the tensile strain in the longitudinal bar and by approximating the crack spacing
174 by the element's depth. The tensile force resulting from the integration of the previous stresses
175 is taken orthogonal to the crack's inclination and its vertical component is the shear contribution
176 of the web.

177 On the other hand, in the presence of transversal reinforcement, its contribution to shear
178 strength is the summation of all tensile ties crossed by the inclined crack (v_s). Also, if transversal
179 reinforcement exists; the contribution of longitudinal reinforcement (dowel action) is taken into
180 account (v_l). In order to compute the previous components, the inclination of the shear crack is

181 needed. In the shear critical region, the crack inclination is estimated after Eq. (5). In this
182 equation, x/d is the ratio of the neutral axis with linear stress distribution and the effective depth.

$$183 \quad \cot \theta = \frac{0.85}{1 - \frac{x}{d}} \quad (5)$$

184 The shear force that must be resisted by the compression zone is computed from equilibrium
185 by subtracting the three previous components (V_w , V_l , V_s) from the applied shear force, Eq. (6).

$$186 \quad V_c = V_{Ed} - V_w - V_l - V_s \quad (6)$$

187 To determine the shear capacity of the compression chord, the normal and shear forces are
188 distributed according to an elastic hypothesis. In the presence of closed hoops as transversal
189 reinforcement, the confining stresses in in the compression chord is accounted for. Further, the
190 tension and compression principal stresses can be computed along the compression chord.

191 Shear failure is assumed to occur when the most critical point in the compression chord reaches
192 its maximum capacity defined by the failure surface proposed by Kupfer et al. [21], see Fig. 2;
193 otherwise, the element resists the applied load. In Fig. 2, it is represented the elastic limit observed
194 in [21], where the Elastic Modulus and Poisson coefficient of concrete starts to vary from the
195 initial one. The volumetric expansion is the situation prior to failure where concrete lateral
196 expansion starts. It can be observed that in the compression-tension region, the volumetric
197 expansion and strength envelope practically coincide. Therefore, in the model, the linear
198 distribution of compression stresses is considered in the compression chord. Moreover, the
199 capacity of this resistance mechanism depends on both compression and tension strengths.

200 In order to find the maximum shear strength, an iteration is needed in which the applied load (V_{Ed})
201 is increased until a point in Kupfer's failure surface is found. This process is rather tedious for
202 practical purposes, so a parametric study was carried out that showed that the solution to the
203 compression head contribution could be approximated by a linear relationship (Fig. 3), resulting
204 in Eq. (7).

205 The linearized model is summarized in Table 2, where all terms have been normalized by $f_{ct}bd$.
206 Note that here, the tensile strength is the reference parameter, in contrast to other formulations
207 that are based on compression strength. The additional symbols in the equations of Table 2 are
208 defined in Eqs. (11) to (15).

209 The factor ζ represents the size effect of the shear capacity of the compression chord, which
210 was taken similar to the proposal of [22], which was based on experimental observation on beams
211 without shear reinforcement, Eq. 11. The term " a " is the shear span, given by Eq. (12). It should

212 be noticed that, in this model, a is computed on the basis of the maximum absolute bending
 213 moment and shear forces in the region of the beam under consideration up to the point of zero
 214 moment. Fig. 4 shows how to compute the shear span in the different regions of a beam.

215 For rectangular sections, x/d can be computed from Eq. (13), with α_e being the ratio of elastic
 216 modules of steel to concrete, Eq. (14). G_f is the fracture energy in Mode I of tension. In case it
 217 cannot be measured experimentally, Eq. (15) was proposed in [16] as a modification of the
 218 equation of Model Code [23] to account for the effect of the aggregate size (d_{max}).

219 Table 2. Summary of simplified equations derived for the different shear contributing actions

Compression chord	$v_c = \frac{V_c}{f_{ct}bd} = \zeta \left[(0.88 + 0.70v_s) \frac{x}{d} + 0.02 \right] \quad (7)$
Cracked concrete web	$v_w = \frac{V_w}{f_{ct}bd} = 167 \frac{f_{ct}}{E_c} \left(1 + \frac{2E_c G_f}{f_{ct}^2 d} \right) \quad (8)$
Longitudinal reinforcement	$v_s > 0 \rightarrow v_l = \frac{V_l}{f_{ct}bd} = 0.25 \frac{x}{d} - 0.05 \quad (9a)$
	$v_s = 0 \rightarrow v_l = 0 \quad (9b)$
Transversal reinforcement	$v_s = \frac{V_s}{f_{ct}bd} = 0.85 \rho_w \frac{f_{yw}}{f_{ct}} \quad (10)$

220 $\zeta = 1.2 - 0.2a \geq 0.65 \quad (11)$

221 $a = \frac{|M_{max, shear span}|}{|V_{max, shear span}|} \quad (12)$

222 $\frac{x}{d} = \alpha_e \rho \left(-1 + \sqrt{1 + \frac{2}{\alpha_e \rho}} \right) \quad (13)$

223 $\alpha_e = \frac{E_s}{E_c} \quad (14)$

224 $G_f = 0.028 f_{cm}^{0.18} d_{max}^{0.32} \quad (15)$

225 This model accounts for the failure mode of tension failure produced by shear forces. Two
 226 additional failure modes should be verified for the sake of completeness of the shear assessment.
 227 First, the failure of the diagonal compression stresses in the cracked web, which can be computed
 228 after Eq. (16) [3], by considering the inclination of the compression field from Eq. (5). Second,
 229 the capacity of the longitudinal reinforcement to resist the tensile force produced by the bending
 230 and axial force together with the increment produced by shear given in Eq. (17).

231 $V_{Rd,max} = \alpha_{cw} b_w z V_1 f_{cd} \frac{1}{\cot \theta + \tan \theta} \quad (16)$

$$\Delta F_t = (V_{Ed} - 0.5V_s) \cot \theta \quad (17)$$

233

234 2.2. MODEL ERROR

235 The model error was estimated by comparing the prediction against experimental databases
 236 collected in [24], [25] and [26], for elements with and without transversal reinforcement, as
 237 presented in [16]. The database included the reported average values of compression strength and
 238 yielding strength of the reinforcements. The concrete tensile strength was estimated from
 239 compression strength using [3], see Table 5. The model error was also compared against those
 240 of Eurocode 2 [3], ACI-318 [1] and Model Code 2010 [23]. The error characteristics of these
 241 models correspond well with those recently found in [27]. As can be seen in Table 3, the above
 242 model shows better performance in terms of average and CoV of the model error for both
 243 situations, which makes it a good option for an assessment model.

244 Table 3. Statistical characterization of the error of different shear resisting models

V_{test}/V_{pred}	892 beams without transversal reinforcement				239 beams with transversal reinforcement			
	EC-2	ACI 318-08	MC10 Lev II	Model. [16]	EC-2	ACI 318-08	MC10 Lev III	Model [16]
Average	1.07	1.28	1.20	1.04	1.72	1.25	1.21	1.02
Standard Deviation	0.226	0.346	0.223	0.179	0.638	0.262	0.225	0.169
CoV	0.211	0.271	0.186	0.173	0.371	0.210	0.186	0.166

245

246 3. SAFETY FACTOR CALIBRATION

247 The design equation (18) is selected, with a safety factor γ_R . $V_{R,k}$ is the shear strength
 248 computed according to Section 2, using the characteristic material properties for concrete tensile
 249 strength, Eq. (19).

$$250 \frac{1}{\gamma_R} V_{R,k} \geq \sum_i \gamma_{G,i} V_{G,ki} + \gamma_{Q,1} V_{Q,k1} + \sum_{j>1} \gamma_{Q,j} \Psi_j V_{Q,kj} \quad (18)$$

$$251 V_{R,k} = (v_c + v_w + v_l + v_s) f_{ct,k} b d \quad (19)$$

252 $V_{G,ki}$ is the shear force produced by the characteristic value of the dead load i , and $\gamma_{G,i}$ is the
 253 partial safety factor of the dead load i . $V_{Q,ki}$ is the shear force due to the characteristic value of
 254 the leading service load and $V_{Q,kj}$ is the shear force due to the accompanying load acting in
 255 combination with the leading one. $\gamma_{Q,j}$ is the partial safety factor for load j and Ψ_j the combination

256 factor for the accompanying load. In this study, the Eurocode partial factors for actions of Table
 257 1 were used. The characteristic design loads and characteristic material properties were selected
 258 according to Eurocode 1 and 2 [4, 3].

259 The next step is to specify the range of possible structures/elements where the obtained safety
 260 factors will be of application.

261 3.1. BUILDING FLOOR DESIGN SET

262 In order to determine the geometric characteristic and applied loads, a reference design set of
 263 typical floors was created, considering different values of beam length (l) and distance between
 264 adjacent beams (s). The combination of values for geometry and material strength in the design
 265 set are described in Table 4, producing 108 design cases. Here, h and b are the depth and width
 266 of the rectangular beam (see Fig. 5).

267 Table 4. Range of variables in the design set

Variable	Values	N° cases
l (m)	4, 8, 12	3
s (m)	3, 6, 9	3
l/h (-)	10, 15, 20	3
b/h (-)	0.5	1
f_{ck} (MPa)	25, 50, 70, 90	4
Total N° cases considered:		108

268 As described in Section 2.1, in this model, the size effect of V_c depends on the shear span (a).
 269 Without losing generality, all elements are considered as simply supported. In this case, a can be
 270 computed as shown in Fig. 5; hence, a is uniformly distributed between 1 m and 3 m.

271 It should be noticed that the shear span ratio (a/d) is known to affect the shear resistance
 272 through both moment-shear interaction and size effect [22]. As shown in [16], if the shear failure
 273 takes place without yielding of the longitudinal reinforcement, the most critical section in shear
 274 results to be the one in the tip of the crack closest to the point of zero bending. Therefore, the
 275 effect of accompanying bending moment interaction was conservatively accounted for by
 276 assuming it as the cracking moment.

277 On the other hand, the number of tests with distributed loads is scant with respect to those with
 278 point loads. However, it has been observed that the elements with distributed loads tend to have
 279 higher resistance than the equivalent specimen with point loads, [28], [29], among others. The
 280 effect of distributed loads in the current model was discussed in [30]. It was observed that the

281 critical shear crack tend to occur closer to the zero-moment section and, on the other, the
282 maximum reaction can be estimated by adding the resultant of the distributed load from the tip of
283 inclined crack to the support.

284 The resulting distribution of live to dead load ratio (L/D) is shown in Fig. 6. L/D in the set
285 ranges between 0.29 and 0.80, with a mean value of 0.60. It should be noticed that the difference
286 with respect to the range considered in Ellingwood et al [31] (0.25 to 1.5) is justified because
287 Ellingwood et al considered the wider range of live loads in the Building Code (including stage
288 floors), while here the calibration is made for office and residential use. When considering office
289 loads in [31], the range of L/D ratio is consistent with the here used.

290 To avoid bending failure in the representative set of beams the longitudinal reinforcement was
291 over-designed in bending by a factor of 1.5. The shear reinforcement ratio ($\rho_w f_{yd}$) that would
292 result from the application of current Eurocode provisions in this design set ranges between 0 and
293 8.8 MPa, with an average value of 1.17 MPa. 90% of the specimens in the set would require ρ_w
294 $f_{yd} \leq 3$ MPa, and the lower 60% of the set will require $\rho_w f_{yd} \leq 1$ MPa, which makes it consistent
295 with the usual reinforcement ratio used in this kind of structures.

296 **3.2 CALIBRATION**

297 The shear resistance safety factor (γ_R) in Eq. (18) is calibrated based on the selection of a
298 uniform reliability index (the target value) for the design set; as applied by several authors, e.g.
299 Melchers [32], Madsen et al. [33], Casas [34], Casas and Chambi [35], Trentin and Casas [36],
300 among others. Accordingly, when using the design equation (18), it should yield almost uniform
301 reliability indexes close to the target value (β^*).

302 In general, the shear resistance for the trial value of γ_R is first computed assuming $v_s=0$; if the
303 resistance is bigger than the design shear force, then no shear reinforcement is needed. Otherwise,
304 shear reinforcement is designed. Afterwards, the reliability index of each designed case is
305 computed by means of FORM (*First-Order Reliability Method*) analysis, with the limit state
306 function defined in Eq. (20). Here, V_R is the random variable representing the shear resistance
307 computed as function of the random variables of Table 5, as shown in Eq. (21).

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313 Table 5. Basic random variables in the resistance term (V_R)

Variable	Description	Statistical model	μ	CoV	Ref.
δ	Model error	Log-normal	$\rho_w=0$: 1.04 $\rho_w>0$: 1.02	0.173 0.166	Table 3
f_c	Concrete compression strength	Log-normal	$f_{ck}+8\text{MPa}$	0.05 – 0.147	[3, 37]
f_{ct}	Concrete tensile strength	Log-normal	$f_{ctm} = 0.3f_{ck}^{\frac{2}{3}}$ for $f_{ck} \leq 50 \text{ MPa}$ $f_{ctm} = 2.12 \ln\left(1 + \frac{f_{cm}}{10}\right)$ for $f_{ck} > 50 \text{ MPa}$	0.182	[3, 37]
f_y	Reinforcement yielding stress	Log-normal	550 MPa	0.055	[37]
Δb	Geometrical error in section's width	Normal	$0.003b \leq 3\text{mm}$	$\frac{4 + 0.006b \leq 10\text{mm}}{\mu_b}$	[37]
Δd	Geometrical error in section's effective depth	Normal	10 mm	1	[37]

314
$$G = V_R - V_E \quad (20)$$

315
$$V_R = \delta \cdot V_{R,mod}(f_c, f_{ct}, f_y, b + \Delta b, d + \Delta d, A_s, A'_s) \quad (21)$$

316 A random variable (δ) is considered in Eq. (21) to take into account the model error.
317 According to the recommendations of JCSS [37], δ is set as Log-Normal; its parameters were
318 selected according to the results of Table 3. The parameters of δ are defined in Table 5 for
319 elements without shear reinforcement ($\rho_w=0$) and with shear reinforcement ($\rho_w>0$).

320 V_E is the shear force in the critical section, which is a function of the load random variables of
321 Table 6. These variables may be considered as uncorrelated because they are due to independent
322 actions (self-weight, permanent load, live-load, etc.). The nominal value for the self-weight load
323 is calculated based on the dimensions of the elements and the density of reinforced concrete.

324 Following the recommendations in [37], the live load model is taken, as a Gamma distribution
325 for the sustained load, with mean and standard deviation μ_q and σ_q , respectively. Variations in
326 time of the sustained load is further taken into account by assuming that the time between load
327 changes is exponentially distributed. Therefore, the probability function for the maximum
328 sustained load is given by Eq. (22).

329

330 Table 6. Basic random variables in the action term (V_E)

Variable	Description	Statistical model	μ	CoV	λ	T	Ref.
g_0	Element weight	Lognormal	$24 \frac{kN}{m^3}$	0.04	-	-	[37]
g_1	Surface dead load	Lognormal	$0.45 \frac{kN}{m^2}$	0.04	-	-	[37]
q	Live load (kN/m ²)	Eq. (22)	$0.5 \frac{kN}{m^2}$	1.342	$\frac{1}{5} year^{-1}$	Service life	[37]

331
$$F_{q,max}(x) = \exp \left[-\lambda T \left[1 - F_q(x) \right] \right] \quad (22)$$

332 Where $F_q(x)$ is the probability function of the sustained load, T is the reference exposition time
 333 and λ is the occurrence rate of sustained load changes. Thus, λT is the mean of the number of
 334 occupancy changes [37].

335 The parameters of the live load are defined in [36] depending on the user category. For this
 336 study, the values corresponding to sustained loads in office buildings have been selected, as they
 337 are representative of a large number of existing buildings.

338 Finally, γ_R is optimized through a least squares minimization of the average error between the
 339 reliability index (β) and the target reliability (β^*), in the design set:

340
$$e^2 = \frac{1}{n} \sum_{j=1}^n (\beta_j - \beta^*)^2 \quad (23)$$

341 The selection of the proper target reliability index (β^*) for structural assessment of existing
 342 structures is currently a subject of active research, Luechinguer and Fisher [38], Steenbergen et
 343 al. [11], Sýkora et al. [9]. As mentioned before, economic optimization can be used to derive
 344 target reliability values; however, human safety levels based on individual and societal risk should
 345 also be considered. As concluded in Steenbergen et al. [11], the minimum levels related to human
 346 safety are often critical target reliabilities for existing structures. Based on an analysis of the
 347 consequences to persons in more than 100 buildings collapses presented by Tanner and Hingorani
 348 [10], Steenbergen et al. [11], these authors recommended a yearly target value of 4.2 (reference
 349 period $T_{ref} = 1$ year) for existing buildings, with a collapsed area, larger than 500 m² and in the
 350 consequence class CC2 according to EN 1990 [5].

351 Although the value of $\beta_1^* = 4.7$, for $T_{ref} = 1$ year, is the one mostly accepted in new
 352 constructions; here, a range of possible target reliability indexes have been considered based on
 353 the recommendations of JCCS [37], depending on the cost of safety measures and consequences
 354 of failure (see Table 7). In this way, the sensitivity of the results to this target value can be also
 355 analysed. The reliability index for service life (T) different than 1 year can be computed by

356 considering the probability of T successive non-failure years, and a rate of load changes λ . The
 357 reliability index is obtained as shown in Eq. (24).

358 Table 7. Recommended target yearly reliability indexes, β_I^* (adapted from JCCS [37])

Relative cost of safety measure	Consequences of failure		
	Minor	Moderate	Large
Large (A)	$\beta_I^* = 3.1$ ($P_{f,1} \approx 10^{-3}$)	$\beta_I^* = 3.3$ ($P_{f,1} \approx 5 \cdot 10^{-4}$)	$\beta_I^* = 3.7$ ($P_{f,1} \approx 10^{-4}$)
Normal (B)	$\beta_I^* = 3.7$ ($P_{f,1} \approx 10^{-4}$)	$\beta_I^* = 4.2$ ($P_{f,1} \approx 10^{-5}$)	$\beta_I^* = 4.4$ ($P_{f,1} \approx 5 \cdot 10^{-6}$)
Small (C)	$\beta_I^* = 4.2$ ($P_{f,1} \approx 10^{-5}$)	$\beta_I^* = 4.4$ ($P_{f,1} \approx 5 \cdot 10^{-6}$)	$\beta_I^* = 4.7$ ($P_{f,1} \approx 10^{-6}$)

359
$$\Phi(\beta(T)) = \Phi(\beta_1)^{\lambda T} \quad (24)$$

360 Similarly, the service life (remaining) of an assessed existing structure, or that of the designed
 361 strengthening may be different from that of a new construction. It may also be selected in terms
 362 of the planned future assessments and maintenance. Therefore, in this study the safety factor will
 363 be calibrated considering a range of different required service lives after the assessment. In this
 364 sense, the resulting factor will be useful for optimizing the possible combination of interventions.

365

366 4. RESULTS AND DISCUSSION

367 Figure 7 shows the least-square minimization for the case of one year exposition target
 368 reliability index of $\beta_I^*=4.2$, corresponding to the recommendations of Steenbergen et al. [11] for
 369 existing structures, and an expected remaining time in service of $T=20$ years. This is equivalent
 370 to a target reliability of 3.46 during the whole exposition period. By varying the shear safety
 371 factor used in design according to the resistance model of Section 2.1, the square of the difference
 372 between the calculated reliability index and the target one is minimized for a value of $\gamma_R=1.124$.

373 Similarly, the optimization of γ_R is carried out for the series of β_I^* of 3.3, 3.7, 4.2, 4.4 and 4.7,
 374 covering the range of recommended values for relative cost of safety measure for moderate and
 375 large consequences of failure. In addition, service life (T) is varied in the series of 5, 10, 20 and
 376 50 years, for a total of 20 combinations. The shape of the resulting least-square optimization
 377 curves is similar to that in Fig. 7. Fig. 8 compares the target reliability index (β_I^*) for the different
 378 service life and the average reliability index ($\beta_{I,average}$) in the design set after optimization of the

379 safety factor, for all the cases considered. It can be noticed that the correlation is good, with an
380 average difference between the target and the average reliability index of 0.88%.

381 The optimized safety factors (γ_R) for each combination of β_I^* and T are shown in solid lines in
382 Fig. 9. It can be observed that the effect of varying the service life is minor. This can be explained
383 after analysing the influence of T in both the load and required reliability index. As shown in Eq.
384 (23), larger exposition time implies a larger magnitude of the observed load with a given
385 probability of not been exceeded. On the other hand, the target reliability index for a period range
386 larger than one year, given by Eq. (24), reduces with time. Hence, the two effects compensate.
387 The optimized values of γ_R can be approximated by Eq. (25). This approximation is represented
388 in Fig. 9 as dotted lines.

$$389 \quad \gamma_R = 0.237\beta_1^{1.09} \quad (25)$$

390 As can be observed, the range of values for the optimized safety factor is smaller than usually
391 required for current shear resisting models and design codes. In particular, for target reliabilities
392 of 4.4 and 4.7, comparable to new constructions, the shear safety factor varies between 1.17 and
393 1.28 for a service life of 50 years.

394 On the other hand, in assessing existing structures, smaller target reliability indexes can be
395 justified, on the range of 3.3 and 3.7, based on larger cost of safety measure, as seen in Table 7.
396 In these cases, γ_R can even take values between 0.83 and 1.0. However, these values are to be
397 applied to the strength computed with the characteristic values of the material properties.

398 Fig. 10 shows the evolution of the reliability index with several design parameters, computed
399 for each element of the design, for the case case $\beta_I^*=4.2$ and service life $T=20$ years. The shear
400 safety factor obtained from Eq. (25) is $\gamma_R= 1.124$ and the target and average reliability indexes
401 are shown in dashed red and green lines, respectively. The approximation of the average
402 reliability to the target value is good, although some scatter is observed.

403 Fig. 10a shows the variation of the computed reliability as function of the live to dead load
404 ratio (L/D). Most cases are distributed between 4.4 and 4.1, with a mean value close to the target
405 value. However, two points show larger values of reliability, between 4.4 and 4.5 for L/D equal
406 to 0.3. The influence of L/D seems to stabilize after $L/D=0.6$.

407 On the other hand, Fig. 10b, shows the same distribution when the effective ratio of transverse
408 reinforcement varies. Reliability indexes are bigger in the region of zero or small transverse
409 reinforcement ratio. Moreover, the two peak values identified in Fig. 10a lie within this region.
410 This is explained as the elements not requiring transverse reinforcement, may resist larger shear

411 force than the strictly demanded. For moderate and large shear reinforcement ratios, scatter of
 412 the computed reliability tends to a stable value of 4.15, only 2% smaller than the target value.
 413 The smallest observed index is 4.1, only 2.4% less than the target value.

414 Figs. 10c and 10d show the influence of the concrete strength and the effective depth. Besides
 415 the cases explained above, the scatter is reasonably independent of the concrete class. As for the
 416 effective depth, it seems to be a slight tendency to increase the reliability index for larger sections.
 417 However, the latter is correlated with the smaller transverse shear ratio in these points, as can be
 418 observed in Fig. 11b. Nevertheless, it should be highlighted that the model reliability index does
 419 not decrease for large size specimens, at least up to 1.2 m depth.

420 Fig. 11 shows the CoV of the computed reliability index of all cases, as computed during the
 421 calibration. It is evidenced that the scatter of the calibration increases for lower β_l , while it
 422 reaches an almost uniform value between 0.01 and 0.02 for $\beta_l > 4$.

423 Alternatively, one may select a safety factor calibration that achieves a desired confidence
 424 level of the minimum reliability. In this case, the value of β_l to be used in Eq. (26) may be
 425 increased to a value larger than the target, $\beta_{1,d} \geq \beta_1^*$. $\beta_{1,d}$ is defined so that it is guaranteed that
 426 90% of the cases will show individual reliability indexes larger than a certain threshold of the
 427 target reliability index: $\beta_{1,individual} \geq c \beta_1^*$. Here, c is the fraction of the minimum reliability
 428 with respect to the target to be guaranteed. This is in agreement with Annex E of [7] if one
 429 considers that the value that guarantees a safe value 90% of the time is in line with the engineering
 430 judgement and tradition.

431 $\beta_{1,d}$ can be computed by multiplying the target reliability index (β_1^*) by a modification factor
 432 (f), as in Eq. (26). The proposed value for factor f is given in Eq. (27).

$$433 \quad \beta_{1,d} = f \beta_1^* \quad (26)$$

$$434 \quad f = \frac{\beta_{1,d}}{\beta_1^*} = 0.67 + 0.77c - 0.08\beta_1^* \geq 1 \quad (27)$$

435 In order to demonstrate the use of this approach in practice, consider the case of $\beta_l^* = 3.3$, for
 436 a service life of 20 years. As observed in Table 7, this is equivalent to a moderate consequence
 437 of failure and large cost of safety measure. The safety factor for this mean reliability is, $\gamma_R =$
 438 0.862. The reliability indexes for the individuals of the design set assessed with this safety factor
 439 are shown in Fig. 12a. The average reliability resulted as $\beta_{1,mean} = 3.416$, which is larger than the
 440 target value. However, the smallest individual reliability index in the set is $\beta_{1,min} = 3.050$, which

441 is 7.6% smaller than the target. Moreover, 34% of the set shows a computed reliability smaller
442 than the intended one

443 Consider that it is desired to guarantee, with a 90% confidence, that the minimum reliability
444 is larger than 0.85 of the target value, then Eq. (27) is used to obtain the modification factor as:
445 $f = 0.67 + 0.77 \times 0.85 - 0.08 \times 3.3 = 1.06$. Therefore, the intended reliability index is
446 $\beta_{1,d} = f \beta_1^* = 1.06 \times 3.3 = 3.50$. Further, the optimized shear safety factor will be computed
447 from Eq. 26, as: $\gamma_R = 0.23 \times 3.50^{1.09} = 0.928$.

448 The distribution of reliability indexes in the calibration with the latter safety factor ($\gamma_R =$
449 0.928) is shown in Fig. 12b. The mean computed reliability index in this case is 3.60 and the
450 minimum value in the set is $3.34 > \beta_1^* = 3.3$. Hence, in this set there is no element with smaller
451 reliability index than the target value ($\beta_1^* = 3.3$).

452 In order to show the effect of the model in design and assessment, the required shear
453 reinforcement ratio in the design set according to the calibrated method, for yearly target
454 reliabilities 4.7, 4.2 and 3.7, are compared against the current Eurocode and ACI-318 provisions.
455 Note that the comparison with the ACI-318 is not direct, as the load factors are different from the
456 ones used here for calibration. Moreover, the quantiles of the specified concrete strength also
457 differ, so the relationship $f_c \approx 1.05 f_{ck}$ was used.

458 Figure 13 shows the distribution of reinforcement ratio. When considering the target reliability
459 of new design ($\beta_1^* = 4.7$), the calibrated method prescribes, in average, higher reinforcement ratios
460 than the Eurocode and ACI-318. Although, the percentage of elements falling in the region of
461 small reinforcement ratios ($\rho_w f_{yd} = 0 - 0.25$ MPa) is similar to the Eurocode when considering
462 $\beta_1^* = 4.7$. However, in assessment, when lower reliability index can be justified, the percentage of
463 elements with zero to small reinforcement ratio increases to almost 27% of the set, although it is
464 still smaller than the share obtained for ACI-318 in this section. The average ratio for the three
465 target reliabilities considered are 1.91 MPa, 1.36 MPa and 0.89 MPa, while the average ratios in
466 the design set for the Eurocode and ACI-318 are 1.17 MPa and 1.29 MPa, respectively. In all
467 cases, the maximum required reinforcement ratio was smaller than the needed in the Eurocode.

468 Further, the predicted strength for fixed reinforcement ratio and different target reliability
469 index are compared to the code formulations in Table 8. The relative strength prediction increases
470 as the target reliability is smaller. The percentage of elements predicted with larger strength than
471 the code increases to 40% and to 80% in the case of Eurocode for β_1^* equal to 4.2 and 3.7,
472 respectively and from 60% to 77% in the case of ACI.

473 Finally, it should be taken into account that shear failure is, in general, brittle. In many design
 474 situations, when high ductility is required for correct performance, e.g. seismic situations, brittle
 475 failure modes can be prevented by applying “capacity design” approaches or over-strength factors
 476 in order to provide a larger safety margin to shear failure than bending. These approaches are
 477 also applicable with the present formulation. However, an advantage of the formulation is
 478 obtained from the fact that safety factors have been posed in terms of target reliability indexes.
 479 Hence, it allows for a reliability-based design in which, for example, a higher target reliability
 480 index can be attributed to shear failure than bending.

481 Although the model was derived from a mechanistic approach, the model error variable was
 482 calibrated with laboratory experimental data; and this data could not account for all realistic load
 483 conditions, such as those involving loads of long duration or repeated cyclic loading. However,
 484 this is a limitation of all shear design models used in practice today and present in the current
 485 design codes, as all them have been calibrated using laboratory experimental data as well. When
 486 more experimental data become available for other load situations, such as long-term or cyclic
 487 loads, the safety factor calibration may be updated accordingly.

488 Table 8. Representative values of the ratio of design shear strength of the calibrated model and
 489 the design strength of Eurocode and ACI-318 for different target reliability

$V_{Rd,model} / V_{Rd,Code}$	$\beta^*_1=4.7$		$\beta^*_1=4.2$		$\beta^*_1=3.7$	
	EC-2	ACI-318	EC-2	ACI-318	EC-2	ACI-318
Maximum	1.23	3.50	1.65	3.58	2.01	3.66
Minimum	0.45	0.41	0.61	0.44	0.81	0.47
Average	0.75	1.00	0.97	1.15	1.26	1.38
CoV	0.26	0.46	0.25	0.40	0.22	0.37
% $V_{Rd,model} > V_{Rd,Code}$	13.0%	35.2%	39.8%	62.0%	81.4%	76.9%

490

491 5. CONCLUSIONS

492 A safety factor for the shear assessment of existing beams and slabs in existing buildings with
 493 reinforced concrete structures was calibrated. This was carried out using the shear resistance
 494 model published in [16], that is based on a multi-action principle and considers rational
 495 quantification of four simultaneous shear resisting mechanisms. The model was found to give the
 496 best approximation to a large database of shear tests, compared to modern design codes. In its

497 present form, the model was developed for shear failure before yielding of longitudinal
498 reinforcement.

499 This study has looked into different target values of safety as well as several remaining service
500 life of the building under assessment. A wide range of reinforced concrete elements, with
501 geometry and load conditions typical of building constructions was considered in the calibration
502 of optimal safety factors for shear assessment. The covered sample included elements with and
503 without shear reinforcement; therefore, the calibration is also suitable for both beams and slabs
504 with live to dead load ratio (L/D) up to 0.8. The calibration is also adequate for normal and higher
505 strength concrete, up to 90 MPa.

506 The safety factor proposed should only be used for the failure mode related to tension in the
507 web and the compression chord capacity. It was not calibrated for crushing of concrete in thin
508 webs.

509 It was found that the effect of the remaining service life (T) on the value of the optimized
510 safety factor for shear strength can be neglected, compared to the effect of yearly target reliability
511 index.

512 An analytical expression (Eq. 25) is proposed to compute the optimal safety factor for the
513 considered model based on the adopted target reliability. The equation provides a very good
514 fitting of the average reliability of the design set.

515 Adopting, for example, a yearly target reliability of 4.2, , suggested in [11] as appropriate for
516 the assessment of existing structures, the corresponding safety factor obtained for the shear
517 resisting model is 1.13, both for elements with and without transversal reinforcement. Other
518 values of the safety factor can be derived using Eq. (25), if different target reliabilities are decided.

519 The shear resistance safety factor values of Eq. (25) are those that minimize the quadratic error
520 between the reliability index of the investigated set and the target reliability value. The scatter of
521 the observed reliability index ranged between CoV 2% and 9%, being larger for the smaller target
522 reliability indexes. Hence, a fraction of the set may show less individual reliability indexes than
523 the target. Therefore, a modification factor of the target reliability was proposed in Eq. (27), in
524 order to guarantee a minimum individual reliability index with a confidence of 90%. For $\beta^*_1=4.2$,
525 the application of this modification factor will modify the safety factor from 1.13 to 1.17 when
526 considering the average reliability index or the guaranteed one.

527 The proposed shear safety factors have to be used jointly with the design equation as defined
528 in Eq. (18) and the shear strength model as defined in Section 2. These safety factors are

529 applicable to cases similar to those in the range of the sample analysed, which comprises a wide
530 range of RC elements used in buildings. However, the proposed calibration methodology is
531 general and may be applied to other shear strength models and other building floor systems. This
532 approach will allow for quick and a more accurate assessment of existing reinforced concrete
533 buildings to shear, and therefore, for lower costs of repair and strengthening, resulting on a more
534 efficient allocation of limited resources, based on explicit target reliability indexes.

535 As shown in the paper, the model uncertainty is a strongly influent variable on the results
536 derived from a calibration process. Therefore, the safety factors should be always considered to
537 be valid for the particular case of the model used to obtain the design values of the variables.
538 When deriving the parameters of the random variable model error, it is also of crucial
539 importance to use, from the available experimental database, only those tests that correspond to
540 the failure modes of interest. Failing to do that will derive on unreliable values of the safety
541 factors.

542 It should be noticed that, although the model is derived from a mechanistic approach, the
543 model error variable was calibrated with laboratory experimental data; and this data could not
544 account for realistic load conditions that involve loads of long duration or repeated cyclic loading.
545 However, this is a limitation of all shear design models used in practice today and present in the
546 current design codes, as all them have been calibrated using laboratory experimental data as well.

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642 commission.
- 643

644

645 **FIGURE CAPTIONS**

646 Figure 1. Basis of the distribution of shear stresses in shear capacity model

647 Figure 2. Stress envelopes, adapted from Kupfer et al. [21]

648 Figure 3. Parametric analysis for solution of compression chord shear capacity and comparison
649 against linearized model (Eq. 7, in dashed lines)

650 Figure 4. Example of calculation of shear spans in the regions of a general beam

651 Figure 5. Static scheme of the elements in the design set, definition of the shear span length (a)
652 and cross-section dimensions

653 Figure 6. Distribution of live to dead load ratio (L/D) in design set

654 Figure 7. Square error minimization for target $\beta_l^* = 4.2$ and service life $T = 20$ years

655 Figure 8. Correlation between average β corresponding to optimized γ_R and target values $\beta^*(T)$
656 for different combinations of annual target values β_l^* and service life periods (T) ranging from
657 5 to 50 years

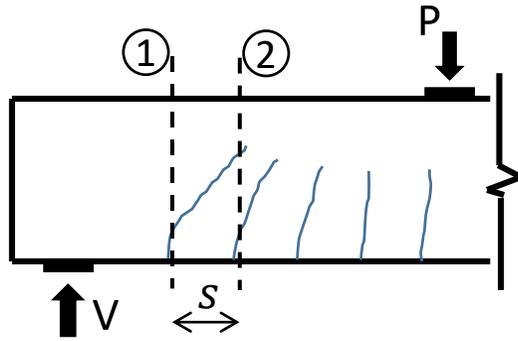
658 Figure 9. Safety factor for different target β_l^* and service life. Eq. (26) shown in dashed lines

659 Figure 10. Distribution of β_l for $\gamma_{Rf} = 1.124$, target $\beta_l^* = 4.2$ and service life $T = 20$ years with
660 varying different design parameters

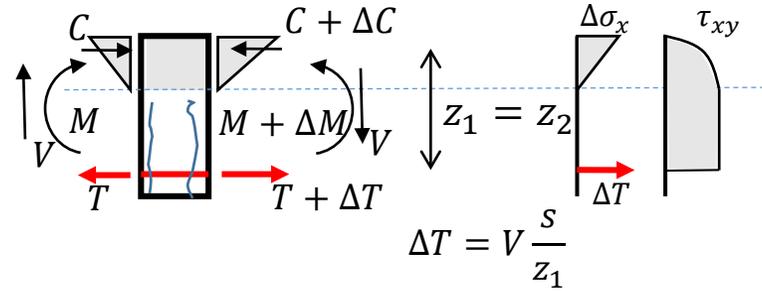
661 Figure 11. Variation of CoV of β_l as function of mean value in the design set

662 Figure 12. Distribution of β_l in the design set. a) $\gamma_R = 0.862$, for a mean target $\beta_l^* = 3.3$, b) $\gamma_R =$
663 0.928 , for a target $\beta_{l,d} = 3.5$

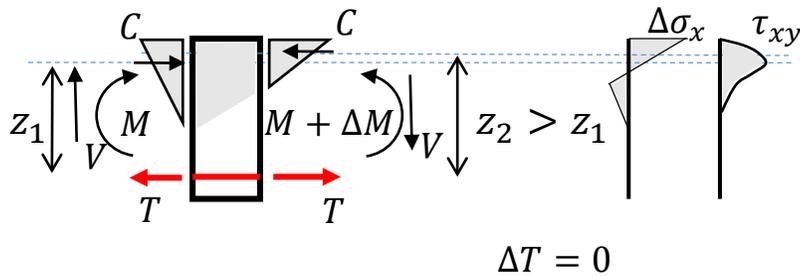
664 Fig. 13 Distribution of the shear reinforcement ratio designed for different β_l^* , Eurocode and ACI-
665 318



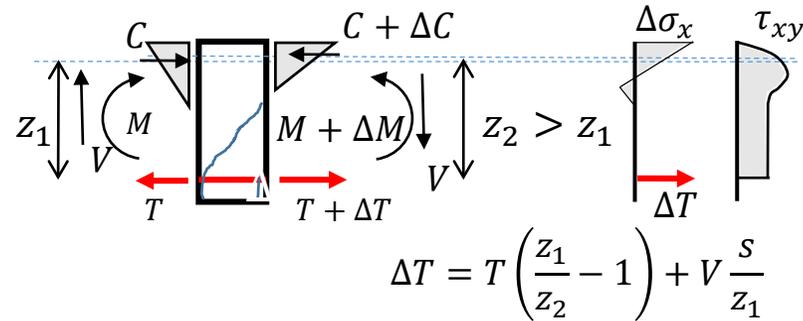
a) Free body cut limited by cross-sections 1 and 2



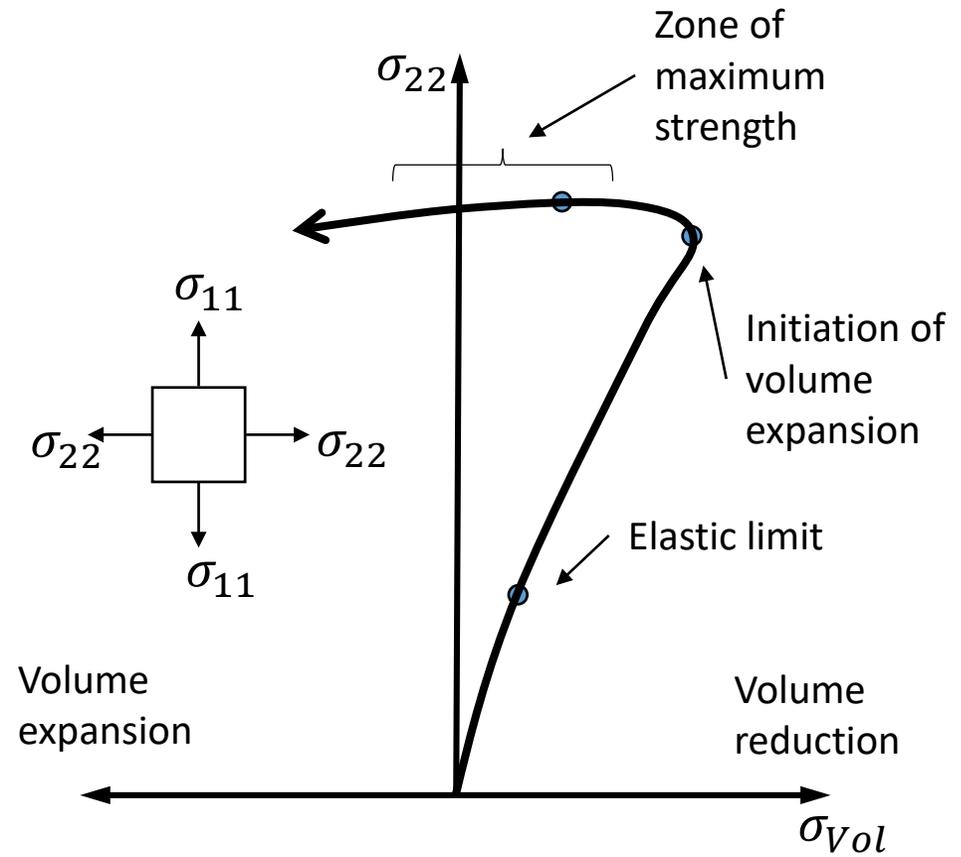
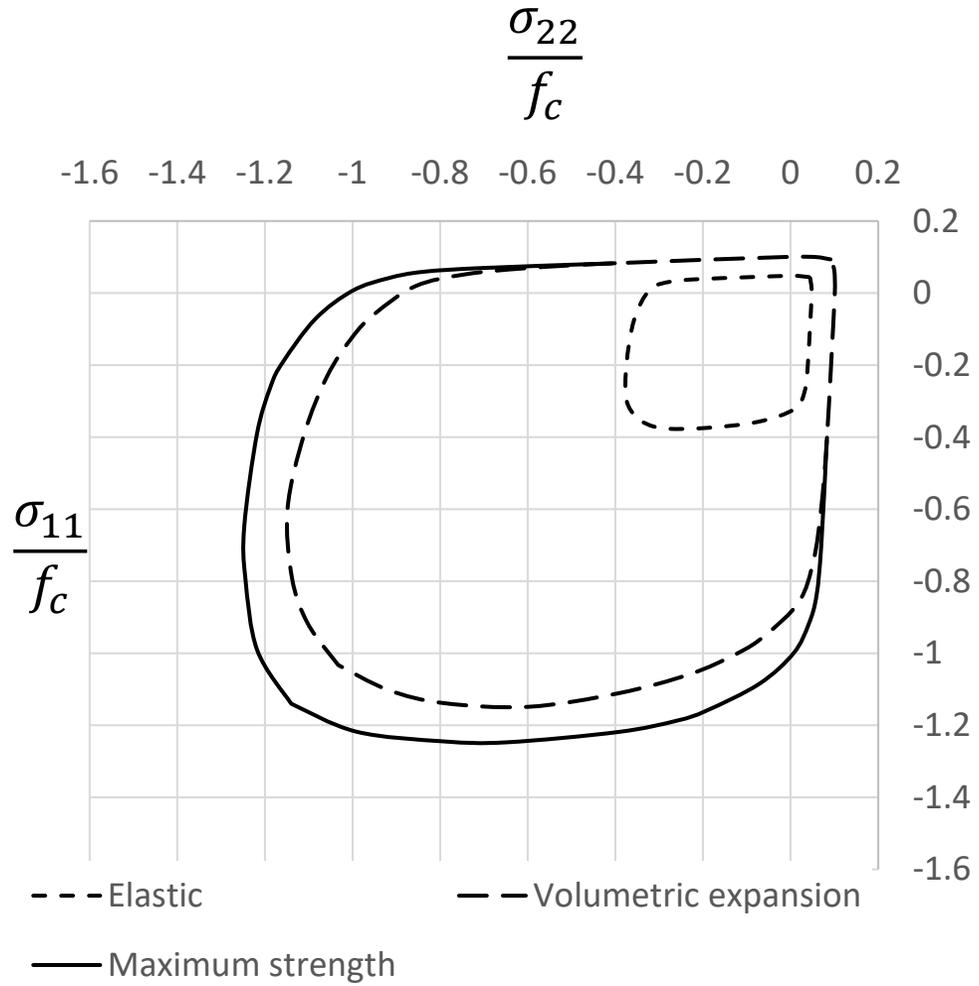
b) Free body equilibrium and stress distribution for perfect beam-action

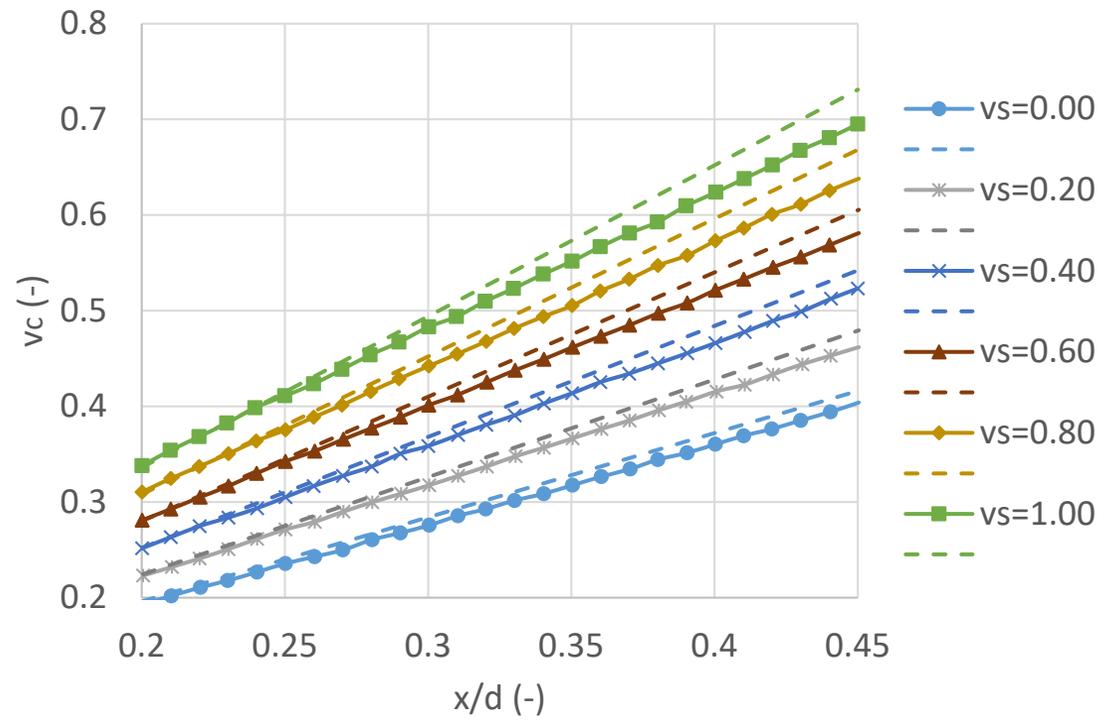


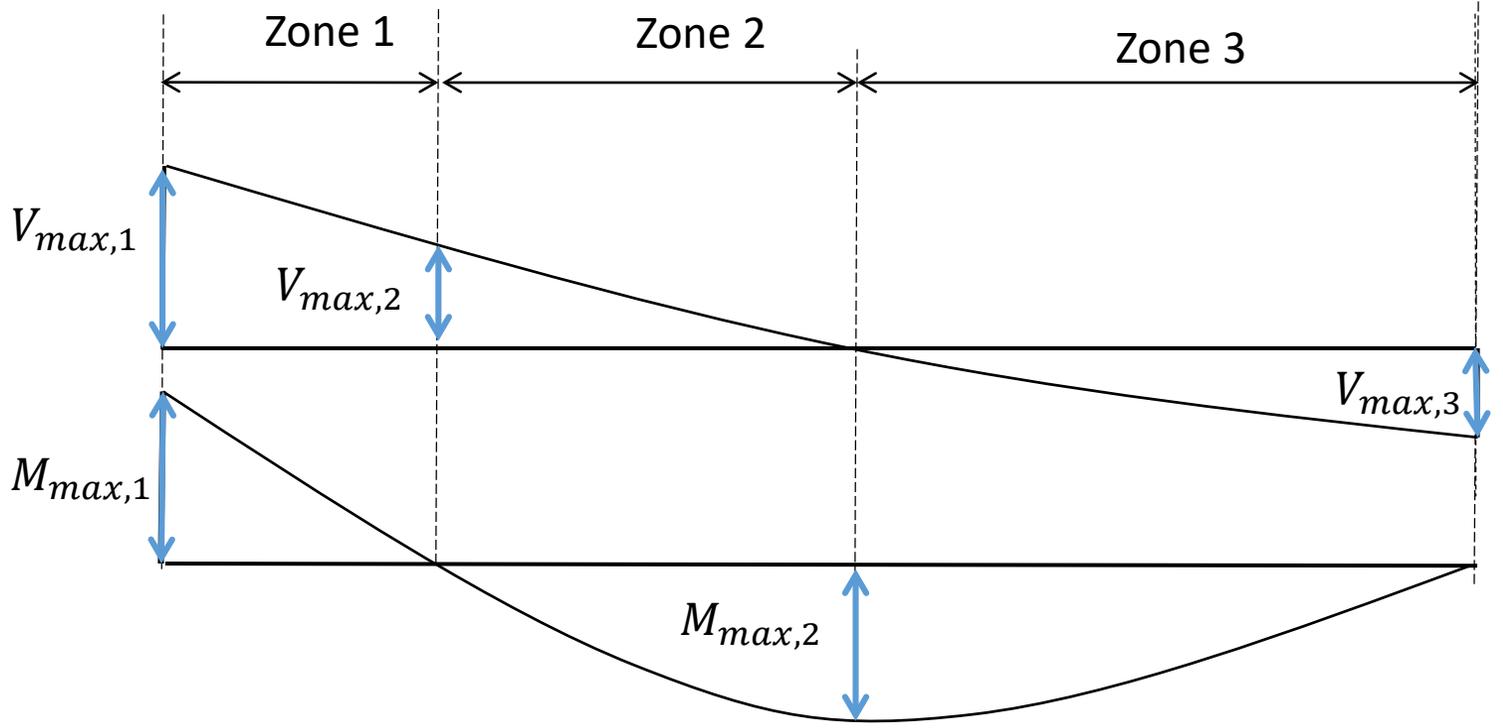
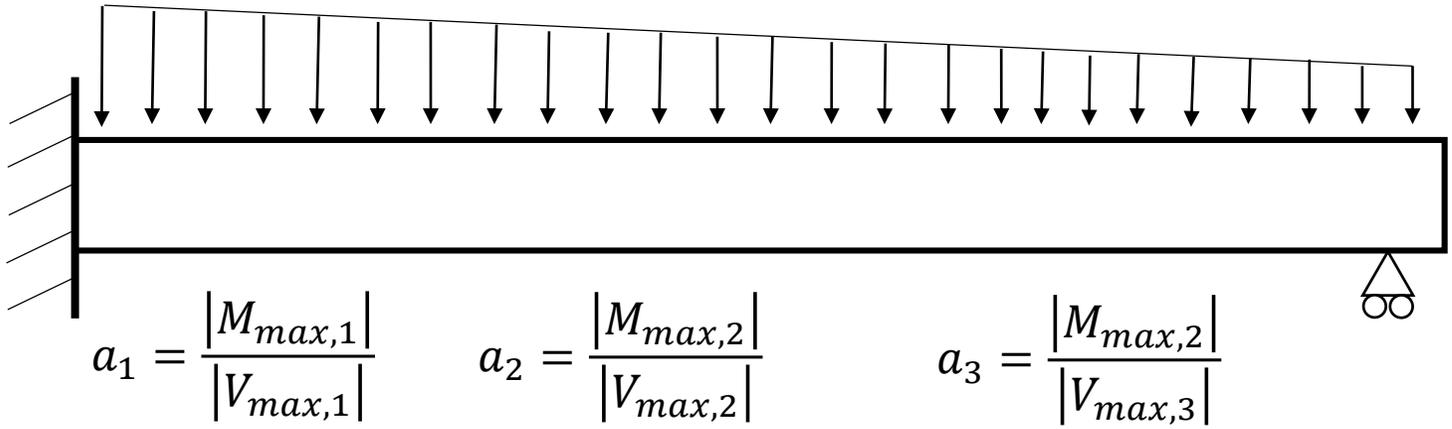
c) Free body equilibrium and stress distribution for perfect arch-action

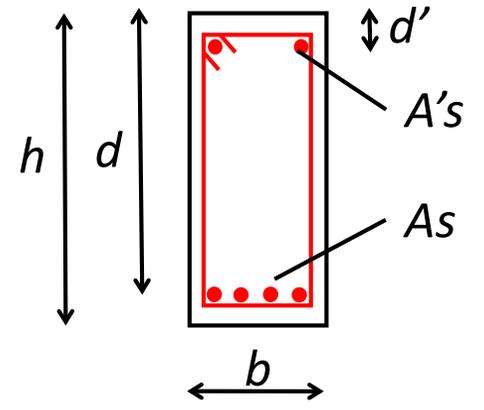
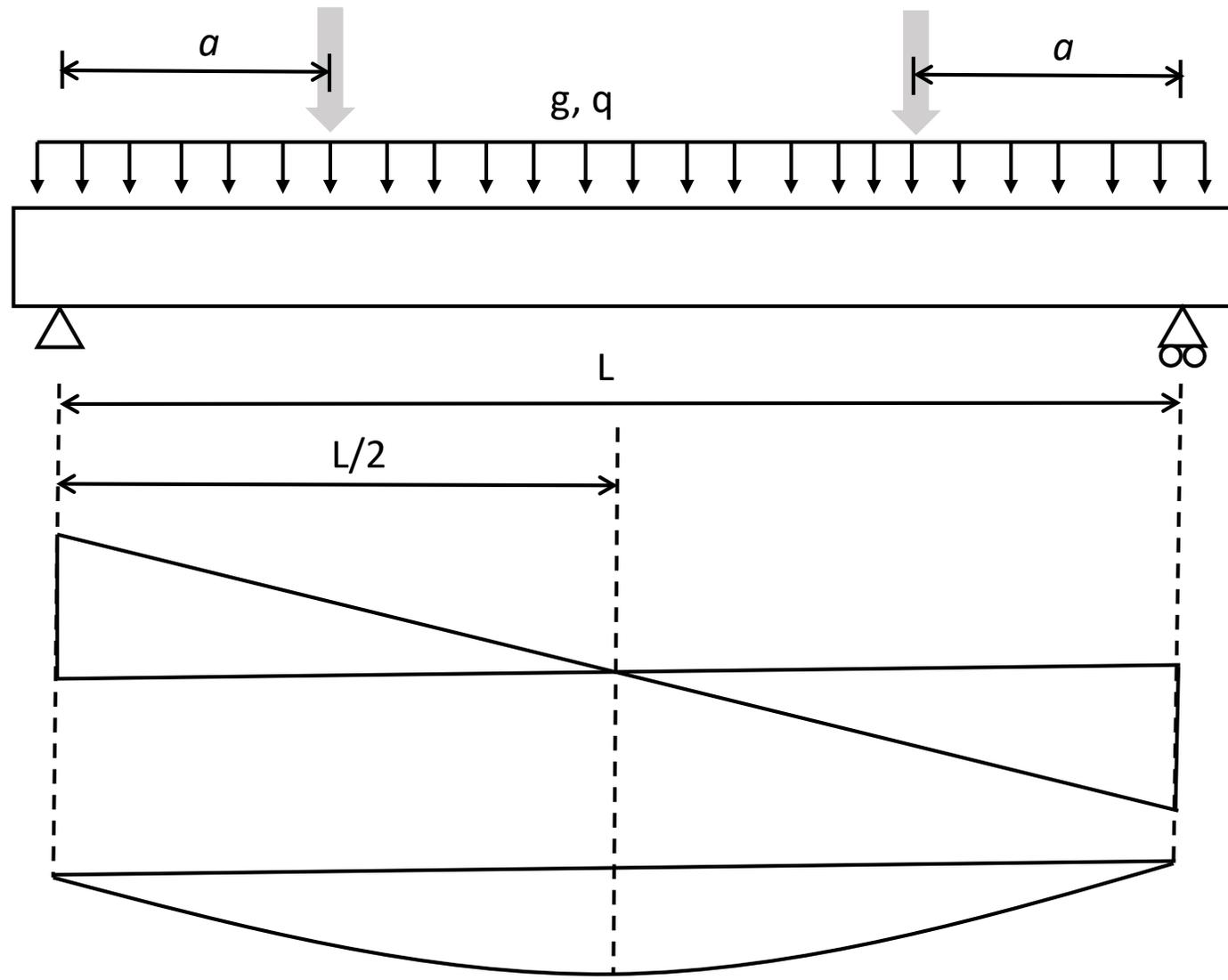


d) Free body equilibrium and stress distribution for combined beam-arch action

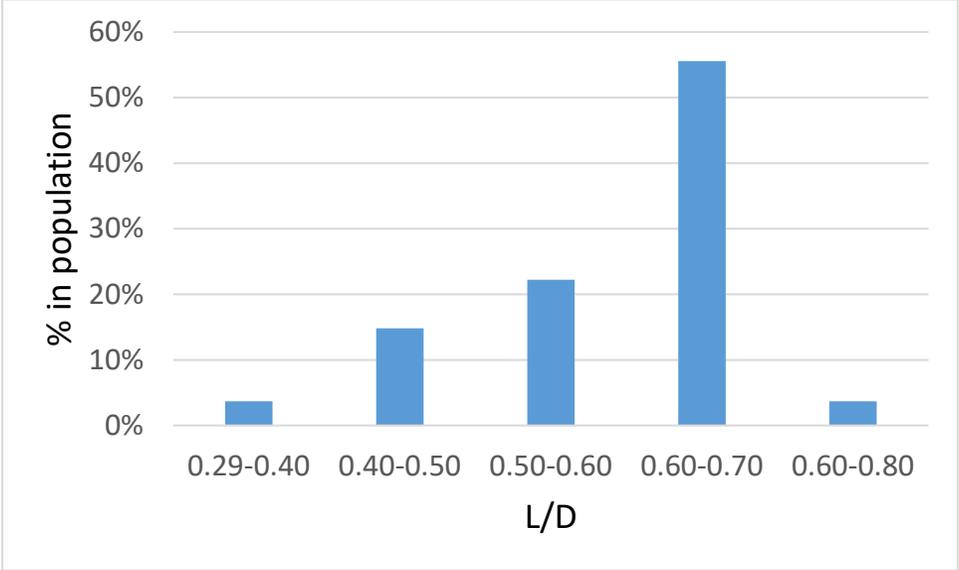


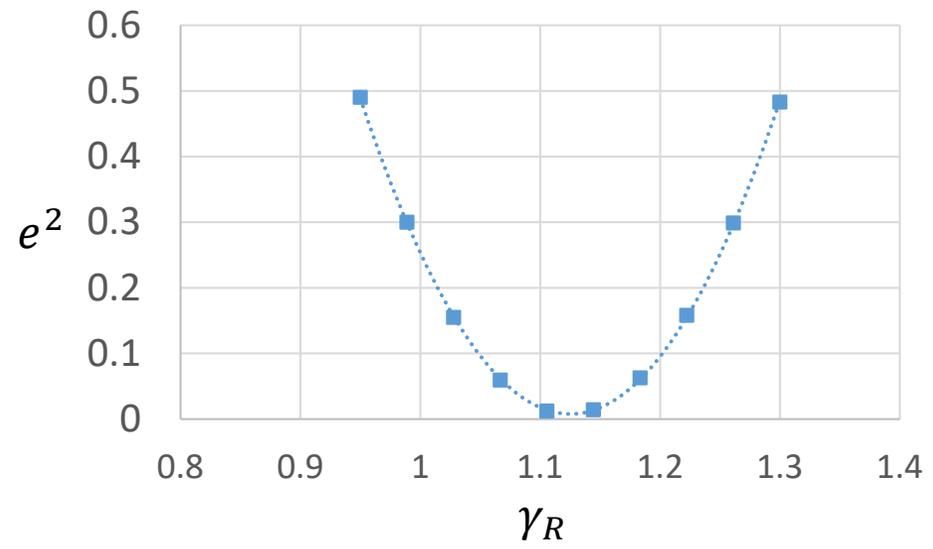


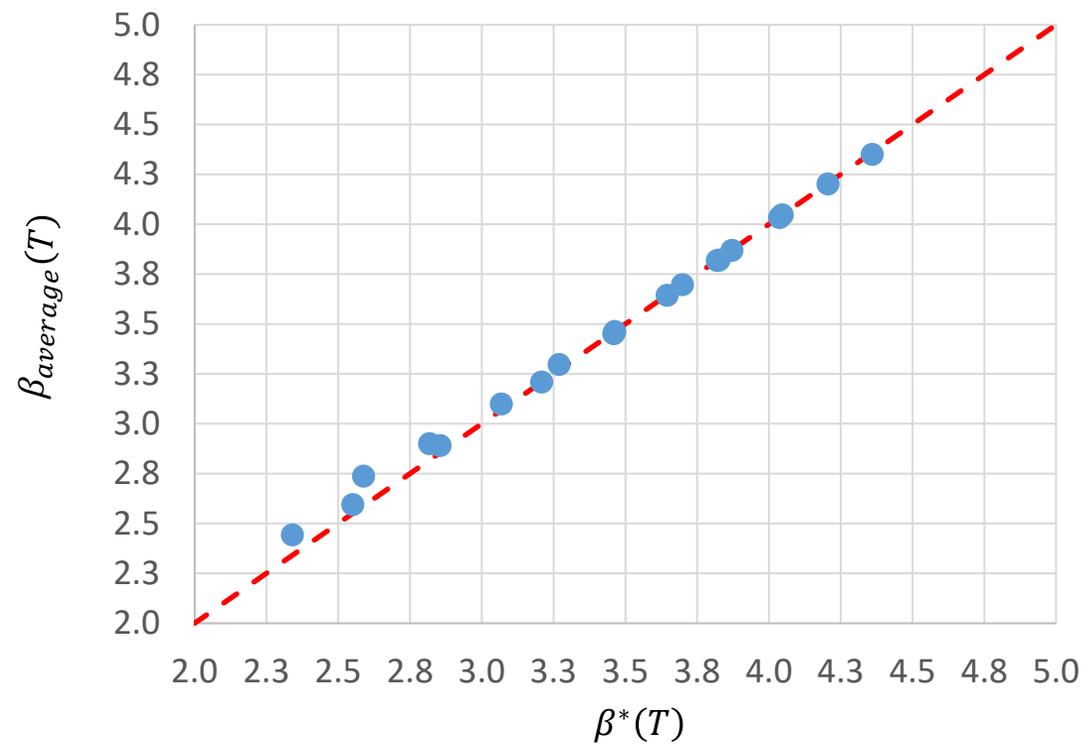


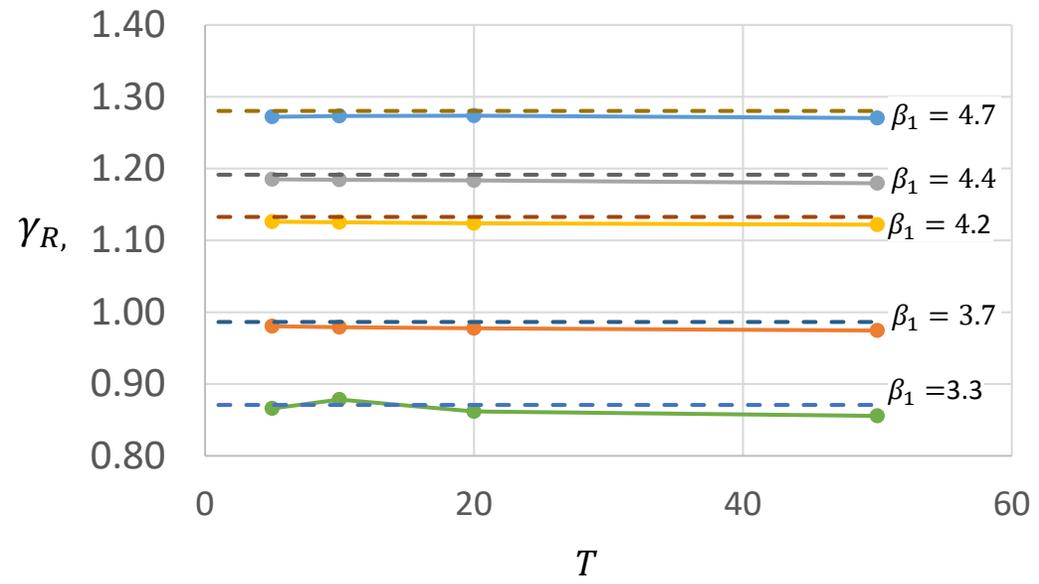


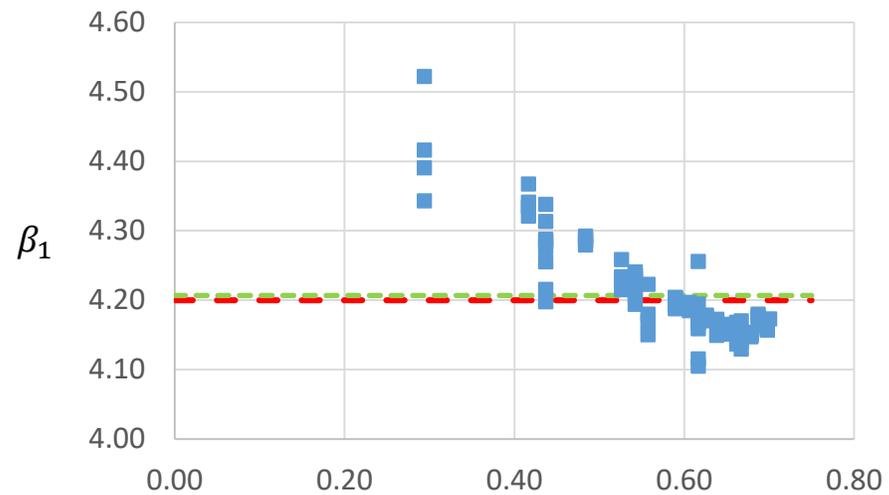
$$a = \frac{M_{max, shear span}}{V_{max, shear span}} = \frac{L}{4}$$



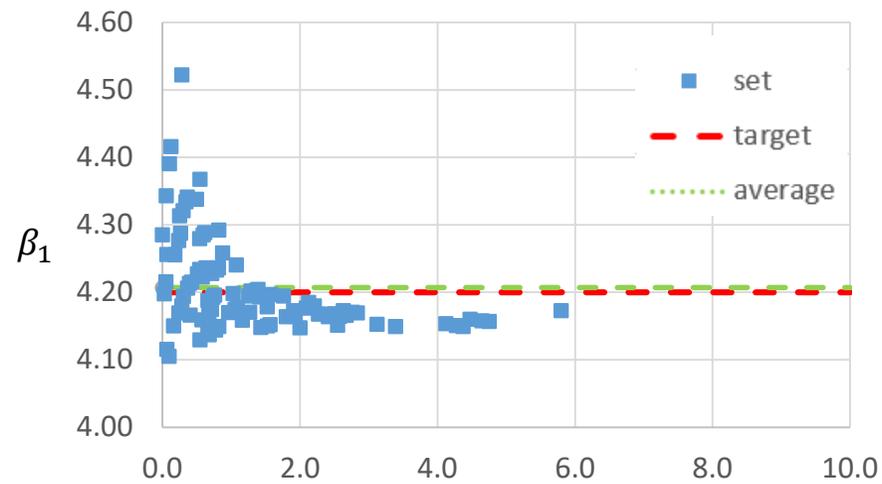




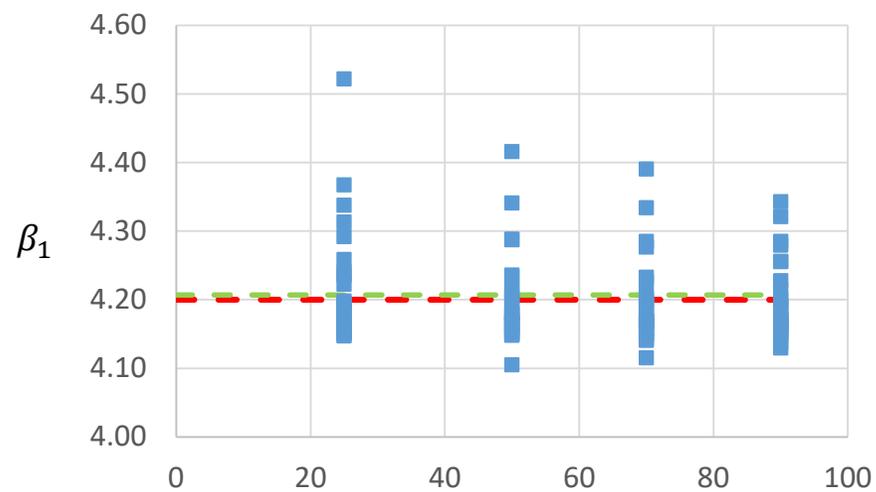




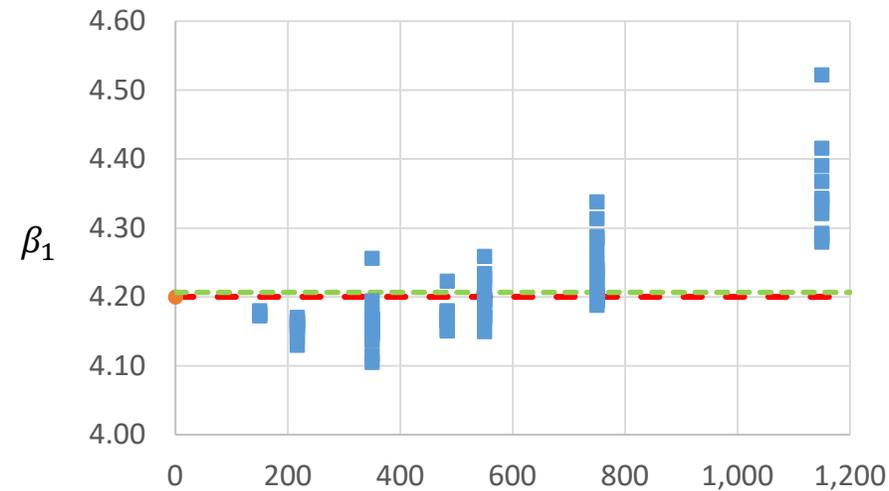
a) $\frac{L}{D}$



b) $\rho_w f_y$ [MPa]



c) f_{ck} [MPa]



d) d [mm]

