Third-Order Intermodulation Distortion and Harmonic Generation in Mismatched Weakly Nonlinear Transmission Lines

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Abstract—This paper describes a procedure to obtain analytical expressions for the spurious signals generated in nonlinear transmission lines with impedance mismatch when they are subject to small-signals. Using these expressions one can rapidly extract the nonlinear parameters describing the nonlinear effects due to the conductor, $L(i)$ and $R(i)$, such as in superconductors, and/or the nonlinear parameters due to the dielectric, $C(v)$ and $G(v)$, such as in ferroelectrics. The resulting closed-form expressions have been validated by equivalent circuit simulations. Spurious signal measurements on several coplanar waveguide superconducting and ferroelectric transmission lines have been explained by the use of the resulting closed-form expressions.

Index Terms—Ferroelectrics, harmonic balance, intermodulation products, nonlinear measurements, nonlinearities, superconductors.

I. INTRODUCTION

BROADBAND response of materials to electromagnetic stimuli provides important information about their electronic and fundamental properties. This information may help to accelerate the development and incorporation of new electronic materials such as high-temperature superconductors (HTSs), ferroelectrics, and magneto-electric and/or multiferroics in general, into devices used for electronic applications [1]–[3]. For such characterization, we have used broadband coplanar waveguide (CPW) structures [2]. We have extracted the electrical parameters for the broadband frequency response of our CPW structures using accurate calibration techniques [4]–[6]; these electrical parameters may then be related to

the properties of the constituent materials. Recently, these techniques have been used to characterize fluids embedded in microchannel structures integrated with CPW test structures [7], [8]. While this broadband linear characterization is a necessary step toward the complete understanding of the electromagnetic response of these different materials, it does not always yield sufficient information to distinguish between different theoretical models, and therefore, may not provide a complete understanding of the material properties.

Additional information can be obtained for such materials from the third-order nonlinear response to electromagnetic stimuli [9]–[12] such as intermodulation distortion products or third-order harmonics. These types of spurious signals are often detectable at low signal levels, when there are no measurable effects on the fundamental response of the system (i.e., that occurring at the frequencies of the driving stimuli). For example, third-order intermodulation products are often measureable when no compression effects are seen in a two-port device, or when no de-tuning is observed in a resonator [13].

To obtain the nonlinear response of different materials we have developed a broadband two-tone high-dynamic-range measurement system to capture the spurious signals resulting from the nonlinear transmission lines [11], when they are fed with weak fundamental tones. Accurate circuit models that relate the measured spurious signals to the nonlinear circuit parameters are then essential to characterize the nonlinear properties of the materials using parameters that are independent of the specific test devices used in the measurements. Both commercial and custom simulation software have been used to adjust the relevant parameters in these equivalent circuit models so that their response fits the measured results [11]. In this study, we analyze these circuit models to obtain an analytical closed-form expression of the spurious signals generated in a mismatched nonlinear transmission line (MNLTL) as a function of the nonlinear distributed circuit parameters, which, in turn, may be linked to the nonlinear material properties [9], [11]. Note that these expressions are only valid in a small-signal regime, i.e., when no effects on the fundamental response are observed.

The circuit model for an MNLTL is described in Section II, and the analytical procedure to obtain closed-form expressions is presented in Section III and supported by the formulation of the Appendix. Due to the effect of mismatch, these expressions need to account for the presence of standing waves of the spurious signals on the transmission lines. The complexity of the
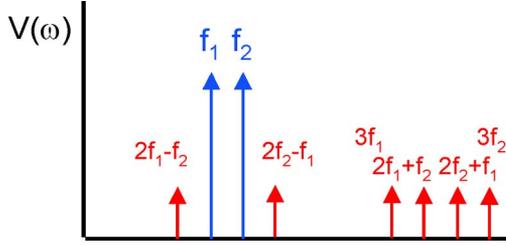
Fig. 1. Third-order nonlinear signals (at frequencies $2f_1 - f_2, 2f_2 - f_1, 3f_1, 2f_1 + f_2, 2f_2 + f_1$, and $3f_2$) generated by a two-tone incident signal with fundamentals f_1 and f_2.

Fig. 2. Equivalent-circuit model of an elemental segment of length dz of a nonlinear transmission line.

analysis requires verification of the resulting closed-form expression with simulated results. Section IV compares the spurious signals generated in an MNLTL using both the circuit simulation and the closed-form expressions. Finally, in Section V, we used the obtained closed-form expression to fit the spurious signals measured in an MNLTL [11].

II. NONLINEAR RESPONSE AND CIRCUIT MODEL FOR MNLTL

When a broadband nonlinear transmission line is fed with two weak tones, at frequencies f_1 and f_2, spurious signals appear at mixing products and harmonics of the two fundamental driving tones. Typically for third-order nonlinear products, we observe spurious signals at the intermodulation products at frequencies close to fundamental tones $2f_1 - f_2$ and $2f_2 - f_1$, the intermodulation products at high frequencies $2f_1 + f_2$ and $2f_2 + f_1$, as well as the third harmonics at frequencies $3f_1$ and $3f_2$ (see Fig. 1). Understanding the relationships between the different spurious signals generated by the nonlinear effects in the material (conductor or dielectric) is very important in order to find an accurate circuit model to describe their small-signal nonlinear response. Note that due to the distributed nature of the nonlinear effects, additional spurious signals would appear at other mixing frequencies. However, since we operate a small-signal regime, they may be usually neglected.

In the case of a unified description of the different spurious signals resulting from a perfectly matched nonlinear transmission line, one would expect a simple relationship between the spurious signals. In this case, due to the distributed nature of the nonlinear effects, the spurious signals show a characteristic linear dependence on the transmission line length. Closed-form expressions for this case were reported in [9] and [14].

However, when we characterize dielectric materials with high permittivity or *a priori* unknown permittivity, our CPW test structures usually result in mismatched transmission lines. In this case, the relationship between the spurious signals generated is not as straightforward and effects that one expects, such as length dependence due to the distributed origin of the nonlinear properties, might not be directly identified from the measured results.

A. Circuit Simulation

As we have done in our previous studies [9], [11], [14], we used a circuit simulator to extract the circuit parameters characterizing the nonlinear transmission line response. To accomplish this, we modeled the nonlinear transmission line by cascading
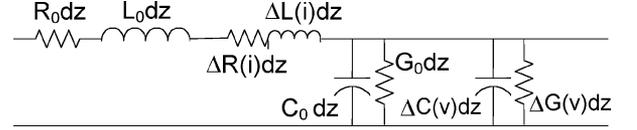
many nonlinear $RLCG$ elemental cells together, such as the one shown in Fig. 2. The circuit parameters R_0 and L_0 correspond to the resistance and inductance per unit length, respectively, and in a quasi-TEM transmission line may be related to the material properties of the conductor. G_0 and C_0 are the conductance and capacitance per unit length, respectively, and may also be linked to the dielectric properties. The nonlinear properties of the material (conductor or dielectric) may also be accounted for in the equivalent circuit of Fig. 2. To do that, we may use the characteristic $v - i$ curve and the characteristic $\phi - i$ curve (the flux being ϕ) to define the distributed resistance and inductance as a Taylor series expansion

$$v = R(i)i = R_0 i + \Delta R_1 i^2 + \Delta R_2 i^3 + \cdots \quad (1)$$
$$\phi = L(i)i = L_0 i + \Delta L_1 i^2 + \Delta L_2 i^3 + \cdots. \quad (2)$$

Similarly we use the characteristic $i - v$ curve and the characteristic $q - v$ curve (q being the charge) to define the distributed conductance and capacitance as a Taylor series expansion as

$$i = G(v)v = G_0 v + \Delta G_1 v^2 + \Delta G_2 v^3 + \cdots \quad (3)$$
$$q = C(v)v = C_0 v + \Delta C_1 v^2 + \Delta C_2 v^3 + \cdots. \quad (4)$$

The general nonlinear telegrapher's equations may be written as

$$\frac{\partial i}{\partial z} = -\frac{\partial q}{\partial t} - G(v)v$$
$$\frac{\partial v}{\partial z} = -\frac{\partial \phi}{\partial t} - R(i)i. \quad (5)$$

Therefore, the nonlinear effects of the conductors are defined by a nonlinear inductance and a nonlinear resistance ($\Delta L(i) = \Delta L_1 \cdot i + \Delta L_2 \cdot i^2 + \cdots$ and $\Delta R(i) = \Delta R_1 \cdot i + \Delta R_2 \cdot i^2 + \cdots$) that depend on the total current i flowing through the line, whereas the nonlinear effects due to the dielectric parts of the circuit are defined by a nonlinear capacitance and a nonlinear conductance ($\Delta C(v) = \Delta C_1 \cdot v + \Delta C_2 \cdot v^2 + \cdots$ and $\Delta G(v) = \Delta G_1 \cdot v + \Delta G_2 \cdot v^2 + \cdots$) that depend on the voltage v on the line. Note that this analogous approach is also used in [15] to obtain the second harmonic generated in a nonlinear transmission line. In [16], a similar small-signal approximation is used to assess the nonlinear effects in left-handed transmission lines.

While the analysis using circuit simulations gives very accurate results, this approach requires significant amounts of computing time. In [9], we state that one requires cascading approximately 200 elemental cells per wavelength to get accurate results. This rapidly ramps up to few thousand cells for long lines, which, in turn, results in the same amount of nonlinear ports to be solved with harmonic balance algorithms. Moreover, this approach gives no insight into how the relevant parameters interact

with each other to generate the measurable quantities. Therefore, iterative steps are required to extract the nonlinear terms from measurements of the spurious signals [11].

III. FORMULATION

This section uses the equivalent circuit of an elemental segment of a nonlinear transmission line (Fig. 2) to obtain closed-form expressions for the third-order intermodulation products—spurious signals appearing at frequencies $2f_1 - f_2$, $2f_2 - f_1$, $2f_1 + f_2$, and $2f_2 + f_1$—and third harmonics—spurious signals appearing at $3f_1$ and $3f_2$—occurring in an MNLTL. This procedure starts by applying the nonlinear telegraphers' equations, resulting from the set of equations (1)–(5)

$$\frac{\partial i}{\partial z} = -C_0 \frac{\partial v}{\partial t} - G_0 v - \frac{\partial i_{nl}}{\partial z} \tag{6}$$

$$\frac{\partial v}{\partial z} = -L_0 \frac{\partial i}{\partial t} - R_0 i - \frac{\partial v_{nl}}{\partial z} \tag{7}$$

where the terms $\partial v_{nl}/\partial z$ and $\partial i_{nl}/\partial z$ account for the nonlinear contributions due to the conductive and the dielectric parts, respectively. According to the equivalent circuit of Fig. 2, these terms can be written as

$$\frac{\partial v_{nl}}{\partial z} = \frac{\partial (\Delta L(i)i)}{\partial t} + \Delta R(i)i \tag{8}$$

$$\frac{\partial i_{nl}}{\partial z} = \frac{\partial (\Delta \mathrm{C}(v)v)}{\partial t} + \Delta G(v)v. \tag{9}$$

The propagation equation, for a given frequency component ω_i, resulting from the combination of (6) and (7), is

$$\frac{\partial^2 I_i(z)}{\partial z^2} = \gamma_i^2 I_i(z) + \frac{\gamma_i}{Z_{TLi}} \frac{\partial V_{nl,i}}{\partial z} - \frac{\partial^2 I_{nl,i}}{dz^2} \tag{10}$$

where γ_i and $Z_{TL,i}$ are, respectively, the propagation constant and characteristic impedance of the line at ω_i.

The voltage $(\partial v_{nl}/\partial z)$ and current $(\partial i_{nl}/\partial z)$ terms act as nonlinear generators at ω_i, and they may be obtained by using the Fourier transform as

$$\frac{dV_{nl,i}}{dz} = \mathcal{F}[\Delta R(i)i, \omega_i] + j\omega_i \mathcal{F}[\Delta L(i)i, \omega_i] \tag{11}$$

$$\frac{dI_{nl,i}}{dz} = \mathcal{F}[\Delta G(v)v, \omega_i] + j\omega_i \mathcal{F}[\Delta C(v)v, \omega_i] \tag{12}$$

where i and v are, respectively, the current and voltage at fundamental frequencies f_1 and f_2.

Now using the current and voltage distribution along the line of (32) and (33), derived in the Appendix, and assuming a quadratic nonlinear dependence as

$$\Delta R(i) = \Delta R_2 i^2 \text{ and } \Delta L(i) = \Delta L_2 i^2 \tag{13}$$

$$\Delta G(v) = \Delta G_2 v^2 \text{ and } \Delta C(i) = \Delta C_2 v^2 \tag{14}$$

where ΔR_2, ΔL_2, ΔG_2, and ΔC_2 set the strength of the nonlinear effects, we analytically obtain the nonlinear voltage (11) and current (12) generators at the frequency components where the spurious signals occur. Note also that the assumption of quadratic nonlinear effects is consistent with many experiments reported in the literature [9]–[14].

Assuming that the propagation equation (10) accepts a solution of the form

$$I_{\omega_i}(z) = A_i(z)e^{-\gamma_i z} + B_i(z)e^{\gamma_i z} \tag{15}$$

where $A_i(z)$ and $B_i(z)$ are, respectively, the forward and backward waveform along the transmission line at ω_i, we obtain the following equation:

$$\left(\frac{d^2 A_i(z)}{dz^2} - 2\gamma_i \frac{dA_i(z)}{dz}\right)e^{-\gamma_i z} + \left(\frac{d^2 B_i(z)}{dz^2} - 2\gamma_i \frac{dB_i(z)}{dz}\right)e^{-\gamma_i z}$$
$$= \frac{\gamma_i}{Z_{TLi}} \frac{dV_{nL,i}}{\partial z} - \frac{d^2 I_{nl,i}}{dz^2} \tag{16}$$

where $dV_{nl,i}/dz$ and $dI_{nl,i}/dz$ are the nonlinear sources at ω_i, detailed in the Appendix. The resulting $A_i(z)$ and $B_i(z)$ should moreover satisfy the boundary conditions at both ends of the transmission line $z = 0$ and $z = l$,

$$\frac{A_i(0)}{B_i(0)} = -\Gamma_{s_i} \tag{17}$$

$$\frac{B_i(l)}{A_i(l)} = -\Gamma_{l_i} e^{-2\gamma_i l} \tag{18}$$

where Γ_{s_i} and Γ_{l_i} are the reflection coefficients at the source $(z = 0)$ and at the load $(z = l)$ at ω_i.

To solve (16), we split the term on the right of (16) into its forward and backward components as

$$\frac{\gamma_i}{Z_{TLi}} \frac{dV_{nl,i}}{\partial z} - \frac{d^2 I_{nl,i}}{dz^2} = C_{Fi} e^{-\gamma_i z} + C_{Bi} e^{\gamma_i z} \tag{19}$$

where C_{Fi} and C_{Bi} represent the forward and backward components. Using (19), we can rewrite (16) as

$$\frac{d^2 A_i(z)}{dz^2} - 2\gamma_i \frac{dA_i(z)}{dz} - C_{Fi} = 0 \tag{20}$$

$$\frac{d^2 B_i(z)}{dz^2} - 2\gamma_i \frac{dB_i(z)}{dz} - C_{Bi} = 0. \tag{21}$$

Now we only need to solve the two ordinary differential equations (20) and (21), use the boundary conditions (17) and (18), and apply (15) to obtain the current distribution along the transmission line $I_i(z)$ at ω_i.

A. Intermodulation Product at $2\omega_1 - \omega_2$

This section uses the analytical procedure described above to obtain the current distribution along the line for the intermodulation product at $2\omega_1 - \omega_2$, $I_{2\omega_1 - \omega_2}(z)$. The forward $C_{F2\omega_1 - \omega_2}$ and backward $C_{B2\omega_1 - \omega_2}$ components are, respectively, detailed in (36) and (37).

The resulting $A_{2\omega_1 - \omega_2}(z)$ and $B_{2\omega_1 - \omega_2}(z)$ are

$$A_{2\omega_1 - \omega_2}(z) = \frac{-K_A}{2\gamma_{12}} + \frac{F_L e^{(\gamma_{12} + \gamma_2^*)z}}{\gamma_2^{2*} - \gamma_{12}^2}$$
$$+ \frac{D_L e^{(\gamma_{12} + \gamma_2^* - 2\gamma_1)z}}{(\gamma_2^* - 2\gamma_1)^2 - \gamma_{12}^2}$$
$$+ \frac{E_L e^{(\gamma_{12} - \gamma_2^* - 2\gamma_1)z}}{(-\gamma_2^* - 2\gamma_1)^2 - \gamma_{12}^2} \tag{22}$$

$$B_{2\omega_1-\omega_2}(z) = \frac{-K_B}{2\gamma_{12}} + \frac{A_L e^{-(\gamma_{12}+\gamma_2^*)z}}{\gamma_2^{*2} - \gamma_{12}^2}$$
$$+ \frac{B_L e^{-(\gamma_{12}+\gamma_2^*-2\gamma_1)z}}{(-\gamma_2^*+2\gamma_1)^2 - \gamma_{12}^2}$$
$$+ \frac{C_L e^{-(\gamma_{12}-\gamma_2^*-2\gamma_1)z}}{(\gamma_2^*+2\gamma_1)^2 - \gamma_{12}^2} \qquad (23)$$

where the constants K_A and K_B are found applying the boundary conditions (17) and (18). The constants A_L, B_L, C_L, D_L, E_L, and F_L are related to the nonlinear terms $\Delta_c = \Delta R_2 + j\omega_{12}\Delta L_2$ and $\Delta_d = \Delta G_2 + j\omega_{12}\Delta C_2$ and are detailed in (38). Note that, throughout this paper, subscripts $12, 1$, and 2 indicate the frequency components at $2\omega_1 - \omega_2$, ω_1, and ω_2, respectively.

The development for the intermodulation product at $2\omega_2 - \omega_1$ would read as (22) and (23) by only replacing the components at ω_1 by the ones at ω_2, and vice versa, and using the components at $2\omega_2 - \omega_1$ instead of at $2\omega_1 - \omega_2$ (this is using the subscript 21 instead of 12).

B. Intermodulation Product at $2\omega_1 + \omega_2$

For the intermodulation product at $2\omega_1 + \omega_2$, we use the forward $C_{F2\omega_1+\omega_2}$ and backward $C_{B2\omega_1+\omega_2}$ components (39) and (40), respectively. The resulting $A_{2\omega_1+\omega_2}(z)$ and $B_{2\omega_1+\omega_2}(z)$ are

$$A_{2\omega_1+\omega_2}(z) = \frac{-K_A}{2\gamma_{12+}} + \frac{D_H e^{(\gamma_{12+}-\gamma_2)z}}{\gamma_2^2 - \gamma_{12+}^2}$$
$$+ \frac{E_H e^{(\gamma_{12+}+\gamma_2-2\gamma_1)z}}{(\gamma_2-2\gamma_1)^2 - \gamma_{12+}^2}$$
$$+ \frac{F_H e^{(\gamma_{12+}-\gamma_2-2\gamma_1)z}}{(-\gamma_2-2\gamma_1)^2 - \gamma_{12+}^2} \qquad (24)$$

$$B_{2\omega_1+\omega_2}(z) = \frac{-K_B}{2\gamma_{12+}} + \frac{A_H e^{-(\gamma_{12+}-\gamma_2)z}}{\gamma_2^2 - \gamma_{12}^2}$$
$$+ \frac{B_H e^{-(\gamma_{12+}-\gamma_2-2\gamma_1)z}}{(\gamma_2-2\gamma_1)^2 - \gamma_{12+}^2}$$
$$+ \frac{C_H e^{-(\gamma_{12+}+\gamma_2-2\gamma_1)z}}{(-\gamma_2+2\gamma_1)^2 - \gamma_{12+}^2}. \qquad (25)$$

Now the subscript 12+ refers to the frequency components at $2\omega_1 + \omega_2$. The constants A_H, B_H, C_H, D_H, E_H, and F_H are detailed in (43).

Again the result would be easily expanded for the spurious signals occurring at $2\omega_2 + \omega_1$.

C. Harmonic Generation at $3\omega_1$

The forward and backward components of the current distribution along the line at $3\omega_1$ are found using the forward $C_{F3\omega_1}$ and backward $C_{B3\omega_1}$ components of (46) and (47), respectively. The resulting $A_{3\omega_1}(z)$ and $B_{3\omega_1}(z)$ are

$$A_{3\omega_1}(z) = \frac{-K_A}{2\gamma_3} + \frac{B_3 e^{(\gamma_3-\gamma_1)z}}{\gamma_1^2 - \gamma_3^2} + \frac{A_3 e^{(\gamma_3-3\gamma_1)z}}{(3\gamma_1)^2 - \gamma_3^2} \qquad (26)$$

$$B_{3\omega_1}(z) = \frac{-K_B}{2\gamma_3} + \frac{C_3 e^{(\gamma_1-\gamma_3)z}}{\gamma_1^2 - \gamma_3^2} + \frac{D_3 e^{(3\gamma_1-\gamma_3)z}}{(3\gamma_1)^2 - \gamma_3^2} \qquad (27)$$
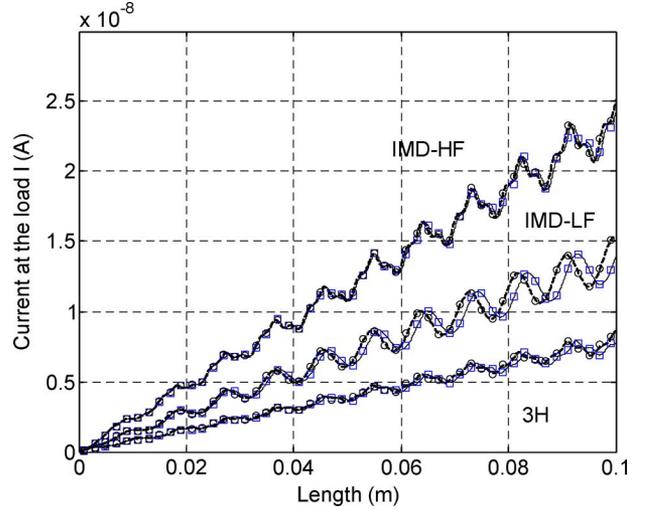

Fig. 3. Current at the end of the line for the spurious frequency components.

where the subscript 3 refers to the frequency components at $3\omega_1$. The constants A_3, B_3, C_3, and D_3 are detailed in (48). Note that these expressions would also be suitable for the third harmonic of ω_2.

In the case of perfectly matched transmission lines, $\Gamma_i = 0$, the above closed-form expression would read as reported in [14].

IV. VERIFICATION: CIRCUIT SIMULATIONS

This section checks the expressions developed above in (22)–(28) by comparing their results with the ones obtained from a circuit simulation of an MNLTL. The circuit simulation has been performed as outlined in Section II-A, and reported elsewhere [9], [11].

The linear distributed circuit parameters defining the simulated transmission line are $L_0 = 662.8$ nH/m, $C_0 = 490.2$ pF/m, $R_0 = 4\text{e}-3\ \Omega$/m, and $G_0 = 7.4\text{e}-6$ S/m (almost lossless dielectric). This results in a transmission line of 36.7-Ω characteristic impedance, which is then connected to a 50-Ω source and terminated with a 50-Ω load. For this simulation, we consider quadratic nonlinear effects coming from the conductor [see (13)], where $\Delta R_2 = 33.85\ \Omega/hbox{m}A^2$ and $\Delta L_2 = 1.07\text{e}-9$ H/mA^2. We then feed this line with two tones at $f_1 = 3$ GHz and $f_2 = 3.05$ GHz and evaluate the resulting spurious signals at $2\omega_1 - \omega_2$, $2\omega_2 - \omega_1$, $2\omega_1 + \omega_2$, $2\omega_2 + \omega_1$, $3\omega_1$, and $3\omega_2$ using the corresponding closed-form expressions and the simulated results.

Fig. 3 depicts the current at the end of the line $I(l)$ as a function of its length, l for all spurious signals occurring in the nonlinear transmission line. The labels on the figure IMD-HF, IMD-LF, and 3H refer to the intermodulation distortion at high frequency ($2\omega_1 + \omega_2$ and $2\omega_2 + \omega_1$), the intermodulation distortion at lower frequency ($2\omega_1 - \omega_2$ and $2\omega_2 - \omega_1$) and the third harmonics, respectively. The circles indicate the simulated results at the lower sideband of the spurious signals, i.e., $2\omega_1 - \omega_2$, $2\omega_1 + \omega_2$, and $3\omega_1$, whereas the squares indicate the simulated results at the upper sideband of the spurious signals, i.e., $2\omega_2 - \omega_1$, $2\omega_2 + \omega_1$, and $3\omega_2$. The solid and dashed lines
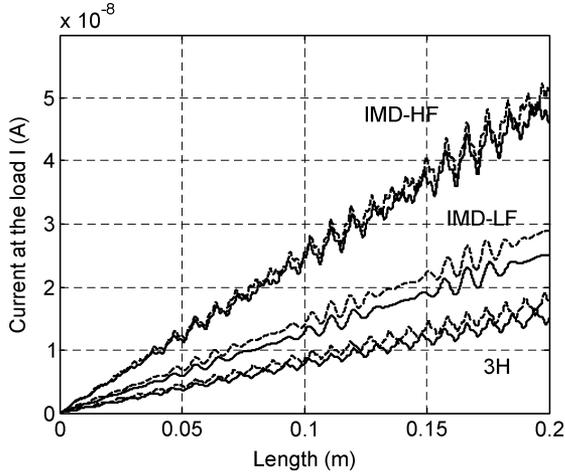
Fig. 4. Current at the end of the line for all spurious frequency components when the fundamental tones f_1 and f_2 are set to 3 and 3.5 GHz, respectively. Solid lines correspond to $2\omega_1 - \omega_2$, $2\omega_2 + \omega_1$, and $3\omega_2$, and dashed lines correspond to $2\omega_2 - \omega_1$, $2\omega_1 + \omega_2$, and $3\omega_1$.

Fig. 5. Measurements and analytical results of the spurious signals occurring in a set of ferroelectric nonlinear transmission lines.

correspond to the values evaluated by the use of the closed-form expressions, all agreeing very well with the simulated results.

The expected linear transmission line length dependence of the spurious signals can be used to confirm the distributed origin of the nonlinear effects and, therefore, rule out contributions from possible external nonlinear sources. Although the results in Fig. 3 show an increment of the spurious signals as a function of the length, they do not follow a linear dependence, as it occurs in a perfectly matched transmission line. The fluctuating length dependence, due to the mismatched effects, may give higher nonlinear effects in shorter lines. This makes it difficult to predict, from the raw data, the distributed origin of the nonlinearities without using simulations or the closed-form expressions developed here. Since the fluctuating behavior comes from the mismatched effects, it depends on the operating frequency and is, therefore, different for each spurious signal. This phenomenon, if not taken into account, may lead to misleading conclusions, such as asymmetries on the IMD (i.e., differences between the signal power at $2\omega_1 - \omega_2$ and $2\omega_2 - \omega_1$) due to memory effects [17].

Although not reported in this section, the closed-form expressions have also been verified when the nonlinear effects come only from the dielectric part and from both conductor and dielectric parts. We have also verified the obtained expressions for a several values of characteristic impedance ranging from 10 to 100 Ω and different frequencies.

As an example, to emphasize the effects of mismatch, this section also evaluates the length dependence of the spurious signals for lines longer than those of Fig. 3 (up to 0.2 m) fed with two input tones whose frequencies (f_1 and f_2) are 3 and 3.5 GHz, respectively, much farther apart than those of Fig. 3. Fig. 4 shows how the asymmetries between the spurious signals are more pronounced. Moreover, unlike in Fig. 3, the IMD-LF traces in Fig. 4 have fluctuations for only limited ranges of length.

From Figs. 3 and 4, we also see that small deviation in the length determination of the line may incur in a few decibel difference of the predicted spurious signal.
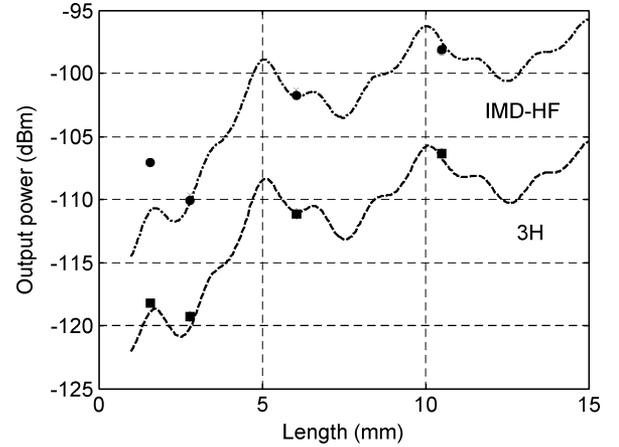
V. VERIFICATION: MEASUREMENTS

Simulations using the circuit model of Fig. 2 have been extensively used to analyze the distributed nonlinear effects in superconducting transmission line, confirming the expected length and frequency dependence [18]. Since in superconducting transmission lines the dielectric constants of the substrates are usually well known, one can build transmission lines with characteristic impedances matched to 50 Ω. For this case, we do not expect to observe any fluctuating effect due to the length of the line. The closed-form expressions developed here have also been used to explain such results.

However, this is not the case for substrates with large or nonlinear dielectric constants, such as ferroelectrics [2] or magnetoelectrics [3]. Fabrication of transmission lines incorporating these materials then results in a nonlinear mismatched transmission line.

This section applies the developed closed-form expressions to explain the nonlinear behavior occurring in CPW transmission lines incorporating an SrTiO$_3$ (STO) thin film of 400-nm thickness grown on a LaAlO$_3$ substrate with conductors defined by a 0.3-μm Au layer on top. Here we report the intercept point at 0-dBm input power of the spurious signals occurring in four CPW transmission lines, all with a 50-μm width of center conductor and 20-μm gap between the center conductor and ground planes. The four lines have different length: $L_1 = 1.58$ mm, $L_2 = 2.79$ mm, $L_3 = 6.06$ mm, and $L_4 = 10.52$ mm. Fig. 5 shows the measured intercept point at 0-dBm input power and outlines the length dependence predicted from the closed-form expression developed here. Circles and squares indicate the measured intercept points of the spurious signal at $2\omega_1 + \omega_2$ and $3\omega_1$, respectively. The input tones f_1 and f_2 were set to 6 and 6.1 GHz, respectively. Experiments performed to obtain measurements of the spurious signals are detailed in [11].

We then used the current at the end of the line, obtained from (22)–(28), to extract the power at the output port [19]. The output power generated at spurious frequencies depends on the propagation constant γ and characteristic impedance Z_{TL} of the line—obtained from a multiline thru-reflect line (TRL) calibration [4] as at each frequency point—and the nonlinear terms Δ_c and Δ_d, which are unknown. By equating the resulting output
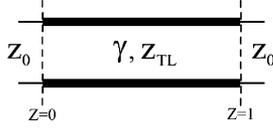
Fig. 6. Outline of a mismatched transmission line.

power expressions with the measured spurious signals, one can extract the nonlinear terms Δ_c and Δ_d. Note that, in this example, where all nonlinear effects are due to the dielectric part, the nonlinear effects from the conductor part are $\Delta_c = 0$. This same procedure has been used in previous studies [9], [11], but the extraction of the nonlinear terms was carried out by iterating circuit simulations to match measured and simulated spurious signals.

Fig. 5 reproduces the fitting of the experimental results reported in [11]. Dashed–dotted and dashed lines show the length dependence obtained from the closed-form expressions. Fig. 5 shows very good agreement between measurements and the length dependence obtained from the closed-form expressions.

VI. Conclusion

This study has developed general closed-form expressions to obtain the spurious signals resulting from a weakly nonlinear mismatched transmission line with quadratic nonlinear effects in both the conductor and dielectric parts of the circuit. The resulting closed-form expressions have been verified with circuit simulations. Assessment of the transmission line length dependence of the spurious signals reveals how the mismatch effect may mask the expected length dependence caused by distributed nonlinear effects. Without an accurate circuit model and extensive simulations, or without the use of the closed-form expressions developed here, nonlinear measurements may give misleading results due to the fluctuating length dependence and the asymmetry between spurious signals. Moreover, since the closed-form expressions show the interaction of the different sources of nonlinear effects, they offer the possibility of evaluating the nonlinear response and identifying the origin of the nonlinear effects in order to discern between different sources.

Appendix

Current and Voltage Distribution at Fundamental Frequencies

In a transmission line for which the characteristic impedance is neither matched to the impedance of the source, nor the load (see Fig. 6), the current and voltage distribution along the line of the fundamental signals is obtained from basic theory of circuit analysis [19].

We start by obtaining the forward current component at the input of the line ($z = 0$), I_{0i}^+, at ω_i (i for the fundamental components might by 1 or 2) as

$$I_{0i}^+ = I_{si} \frac{Z_0}{Z_{in,i} + Z_0} \frac{1}{1 - \Gamma_i}. \tag{28}$$

I_{si} indicates the current driven by the source and Γ_i is the reflection coefficient to the source and load both at ω_i. The input impedance $Z_{in,i}$ may be found as

$$Z_{in,i} = Z_{TLi} \frac{Z_0 + Z_{TLi} \tanh(\gamma_i l)}{Z_{TLi} + Z_0 \tanh(\gamma_i l)}. \tag{29}$$

The propagation constant γ_i and the characteristic impedance of the transmission line $Z_{TL,i}$, respectively, can be obtained from the linear distributed circuit parameters R_0, L_0, C_0, and G_0 of the line, as

$$\gamma_i = \sqrt{(R_0 + j\omega_i L_0)(G_0 + j\omega_i C_0)} \tag{30}$$

$$Z_{TL,i} = \sqrt{\frac{(R_0 + j\omega_i L_0)}{(G_0 + j\omega_i C_0)}}. \tag{31}$$

From the expressions above, i.e., (28)–(31), the current and voltage distribution along the line at fundamental frequency ω_i, being $i = 1$ or 2, are

$$I_i(z) = I_{01}^+[e^{-\gamma_i z} - \Gamma_i e^{\gamma_i z}] \tag{32}$$

$$V_i(z) = I_{01}^+ Z_{TLi}[e^{-\gamma_i z} + \Gamma_i e^{\gamma_i z}]. \tag{33}$$

Nonlinear Voltage and Nonlinear Current Generators

Assuming a quadratic nonlinear dependence of the distributed circuit parameters $\Delta R(i)$, $\Delta L(i)$, $\Delta C(v)$, and $\Delta G(v)$, as outlined in (13) and (14), we found the resulting nonlinear sources at the mixing products and harmonics of the fundamental components at ω_1 and ω_2 by applying (13) and (14) into (11) and (12), respectively. Although this Appendix only details the nonlinear voltage and current generators at $2f_1 - f_2$, $2\omega_1 + \omega_2$, and $3\omega_1$, their counterparts at $2\omega_2 - \omega_1$, $2\omega_2 + \omega_1$, and $3\omega_2$, respectively, could be directly derived.

The nonlinear voltage and the nonlinear current generators, respectively, at $2\omega_1 - \omega_2$ are

$$\frac{dV_{nl,2\omega_1-\omega_2}}{dz} = \frac{3}{4}I_{01}^{+2}I_{02}^{+\,*}\Delta_c$$
$$\times \Big[-2\Gamma_1 e^{-\gamma_2^* z} + \Gamma_1^2 2 e^{(2\gamma_1 - \gamma_2^*)z}$$
$$-\Gamma_1^2\Gamma_2^* e^{(2\gamma_1 + \gamma_2^*)z} - \Gamma_2^* e^{(-2\gamma_1 + \gamma_2^*)z}$$
$$+ e^{(-2\gamma_1 - \gamma_2^*)z} + 2\Gamma_1\Gamma_2^* e^{\gamma_2^* z} \Big] \tag{34}$$

$$\frac{dI_{nl,2\omega_1-\omega_2}}{dz} = \frac{3}{4}I_{01}^{+2}I_{02}^{+\,*}\Delta_d Z_{TL,1}^2 Z_{TL,2}^*$$
$$\times \Big[2\Gamma_1 e^{-\gamma_2^* z} + \Gamma_1^2 2 e^{(2\gamma_1 - \gamma_2^*)z}$$
$$+ \Gamma_1^2\Gamma_2^* e^{(2\gamma_1 + \gamma_2^*)z} + \Gamma_2^* e^{(-2\gamma_1 + \gamma_2^*)z}$$
$$+ e^{(-2\gamma_1 - \gamma_2^*)z} + 2\Gamma_1\Gamma_2^* e^{\gamma_2^* z} \Big] \tag{35}$$

where $\Delta_c = \Delta R_2 + j(2\omega_1 - \omega_2)\Delta L_2$ and $\Delta_d = \Delta G_2 + j(2\omega_1 - \omega_2)\Delta C_2$. Substituting (34) and (35) into (19), we may isolate the forward and backward components

$$C_{F,2\omega_1-\omega_2} = \left(D_L e^{(-2\gamma_1+\gamma_2^*)z} + E_L e^{(-2\gamma_1+\gamma_2^*)z} \right.$$
$$\left. + F_L e^{\gamma_2^* z}\right) e^{\gamma_{2\omega_1-\omega_2}z} \quad (36)$$

$$C_{B,2\omega_1-\omega_2} = \left(C_L e^{(2\gamma_1+\gamma_2^*)z} + B_L e^{(2\gamma_1-\gamma_2^*)z}\right.$$
$$\left. + A_L e^{-\gamma_2^* z}\right) e^{-\gamma_{2\omega_1-\omega_2}z} \quad (37)$$

where

$$A_L = 2\Gamma_1 \left(\frac{-\gamma_{12}}{Z_{TL,12}}k_c + k_d\gamma_2^*\right)$$

$$B_L = \Gamma_1^2 \left(\frac{\gamma_{12}}{Z_{TL,12}}k_c - k_d(2\gamma_1 - \gamma_2^*)\right)$$

$$C_L = \Gamma_1^2\Gamma_2^* \left(\frac{-\gamma_{12}}{Z_{TL,12}}k_c - k_d(2\gamma_1 + \gamma_2^*)\right)$$

$$D_L = \Gamma_2^* \left(\frac{-\gamma_{12}}{Z_{TL,12}}k_c - k_d(-2\gamma_1 + \gamma_2^*)\right)$$

$$E_L = \left(\frac{\gamma_{12}}{Z_{TL,12}}k_c - k_d(-2\gamma_1 - \gamma_2^*)\right)$$

$$F_L = 2\Gamma_1\Gamma_2^* \left(\frac{\gamma_{12}}{Z_{TL,12}}k_c - k_d\gamma_2^*\right) \quad (38)$$

with $k_c = (3/4)I_{01}^{+2}I_{02}^{+*}\Delta_c$ and $k_d = (3/4)I_{01}^{+2}I_{02}^{+*}Z_{TL,1}^2 Z_{TL,2}^*\Delta_d$.

By the used of analogous expressions to (34)–(38), the inter-modulation products at $2\omega_1 + \omega_2$ may be written as

$$\frac{dV_{nl,2\omega_1+\omega_2}}{dz} = \frac{3}{4}I_{01}^{+2}I_{02}^{+*}\Delta_c$$
$$\times \left[-2\Gamma_1 e^{-\gamma_2 z} + \Gamma_1^2 2 e^{(2\gamma_1-\gamma_2)z}\right.$$
$$-\Gamma_2\Gamma_1^2 e^{(2\gamma_1+\gamma_2)z} - \Gamma_2 e^{(-2\gamma_1+\gamma_2)z}$$
$$\left. + e^{(-2\gamma_1-\gamma_2)z} + 2\Gamma_1\Gamma_2 e^{\gamma_2 z}\right] \quad (39)$$

$$\frac{dI_{nl,2\omega_1+\omega_2}}{dz} = \frac{3}{4}I_{01}^{+2}I_{02}^{+*}\Delta_d Z_{TL,1}^2 Z_{TL,2}$$
$$\times \left[2\Gamma_1 e^{-\gamma_2 z} + \Gamma_1^2 2 e^{(2\gamma_1-\gamma_2)z}\right.$$
$$+\Gamma_1^2\Gamma_2 e^{(2\gamma_1+\gamma_2)z} + \Gamma_2 e^{(-2\gamma_1+\gamma_2)z}$$
$$\left. + e^{(-2\gamma_1-\gamma_2)z} + 2\Gamma_2\Gamma_1 e^{\gamma_2 z}\right] \quad (40)$$

where now $\Delta_c = \Delta R_2 + j(2\omega_1 + \omega_2)\Delta L_2$ and $\Delta_d = \Delta G_2 + j(2\omega_1 + \omega_2)\Delta C_2$. The forward and backward components are

$$C_{F,2\omega_1+\omega_2} = \left(E_H e^{(-2\gamma_1+\gamma_2)z} + F_H e^{(-2\gamma_1+\gamma_2)z}\right.$$
$$\left. + D_H e^{-\gamma_2 z}\right) e^{\gamma_{2\omega_1+\omega_2}z} \quad (41)$$

$$C_{B,2\omega_1+\omega_2} = \left(C_H e^{(2\gamma_1-\gamma_2)z} + B_H e^{(2\gamma_1+\gamma_2)z} +\right.$$
$$\left. A_H e^{\gamma_2 z}\right) e^{-\gamma_{2\omega_1+\omega_2}z} \quad (42)$$

where

$$A_H = 2\Gamma_1\Gamma_2 \left(\frac{\gamma_{12+}}{Z_{TL,12+}}k_c - k_d\gamma_2\right)$$

$$B_H = \Gamma_1^2\Gamma_2 \left(\frac{-\gamma_{12+}}{Z_{TL,12+}}k_c - k_d(2\gamma_1 + \gamma_2)\right)$$

$$C_H = \Gamma_1^2 \left(\frac{\gamma_{12+}}{Z_{TL,12+}}k_c - k_d(2\gamma_1 - \gamma_2)\right)$$

$$D_H = 2\Gamma_1 \left(\frac{-\gamma_{12+}}{Z_{TL,12+}}k_c + k_d\gamma_2\right)$$

$$E_H = \Gamma_2 \left(\frac{-\gamma_{12+}}{Z_{TL,12+}}k_c + k_d(-2\gamma_1 + \gamma_2)\right)$$

$$F_H = \left(\frac{\gamma_{12+}}{Z_{TL,12+}}k_c + k_d(2\gamma_1 + \gamma_2)\right) \quad (43)$$

with $k_c = (3/4)I_{01}^{+2}I_{02}^+\Delta_c$ and $k_d = -(3/4)I_{01}^{+2}/I_{02}^+ Z_{TL,1}^2 Z_{TL,2}\Delta_d$.

For the third harmonic at $3\omega_1$, the nonlinear voltage and current generators are

$$\frac{dV_{nl,3\omega_1}}{dz} = \frac{1}{4}I_{01}^{+2}I_{01}^{+*}\Delta_c \left[-3\Gamma_1 e^{-\gamma_1 z} - \Gamma_1^3 e^{3\gamma_1 z}\right.$$
$$\left. + 3\Gamma_1^2 e^{\gamma_1 z} + e^{-3\gamma_1 z}\right] \quad (44)$$

$$\frac{dV_{nl,3\omega_1}}{dz} = \frac{1}{4}I_{01}^{+2}I_{01}^{+*}\Delta_d Z_{TL,1}^3 \left[3\Gamma_1 e^{-\gamma_1 z} + \Gamma_1^3 e^{3\gamma_1 z}\right.$$
$$\left. + 3\Gamma_1^2 e^{\gamma_1 z} + e^{-3\gamma_1 z}\right] \quad (45)$$

where $\Delta_c = \Delta R_2 + j3\omega_1\Delta L_2$ and $\Delta_d = \Delta G_2 + j3\omega_1\Delta C_2$. The forward and backward components then result as follows:

$$C_{F,3\omega_1} = (A_3 e^{-3\gamma_1 z} + B_3 e^{-\gamma_1 z})e^{\gamma_{3\omega_1}z} \quad (46)$$

$$C_{B,3\omega_1} = (D_3 e^{3\gamma_1 z} + C_3 e^{\gamma_1 z})e^{-\gamma_{3\omega_1}z} \quad (47)$$

where

$$A_3 = \left(\frac{\gamma_3}{Z_{TL,3}}k_c + 3k_d\gamma_1\right)$$

$$B_3 = 3\Gamma_1 \left(\frac{\gamma_3}{Z_{TL,3}}k_c + k_d\gamma_1\right)$$

$$C_3 = 3\Gamma_1^3 \left(\frac{\gamma_3}{Z_{TL,3}}k_c - k_d\gamma_1\right)$$

$$D_3 = \Gamma_1^3 \left(\frac{\gamma_3}{Z_{TL,3}}k_c - 3k_d\gamma_1^3\right) \quad (48)$$

with $k_c = (1/4)I_{01}^{+2}I_{01}^{+*}\Delta_c$ and $k_d = (1/4)I_{01}^{+2}I_{01}^{+*}Z_{TL,1}^3\Delta_d$.

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