The PgaFrame -
A frame for parallel genetic algorithms

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PgaFrame

A frame for parallel genetic algorithms

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Overview

This page documents the PgaFrame - a frame for parallel genetic algorithms. The PgaFrame offers to non-expert users the possibility to solve optimization problems via genetic algorithms on parallel computers. This frame has appeared as the natural fusion of two different projects: PgaPack and Frames. The PgaFrame combines the major features of these projects: it integrates the capabilities to specify genetic algorithms offered by the PgaPack library and the support of Frames to the easy and portable programming of parallel machines. In this way, a complex framework to develop genetic algorithms is achieved.

With PgaFrame a genetic algorithm can be considered as an extensible skeleton. Thus, the user only has to provide his problem dependent parameters to adapt it to his needs. This specification task is done through an easy-to-learn interface and an easy-to-use graphical user interface that do not require any knowledge on parallel programming: only some radio buttons must be selected, some entries filled and a few sequential functions in ANSI C written. The core of the genetic algorithm and its parallelization are completely transparent to the user. As a consequence, executing a genetic algorithm on a parallel system with the PgaFrame is as easy as filling a form. Moreover, due to the portability of the PgaPack library and the Frames tools, it can run efficiently on almost any parallel or sequential computer.

Introduction

Genetic algorithms

Genetic algorithms (GAs) are adaptative methods which may be used to solve search and optimisation problems. They are based on the genetic process of biological organisms. Over
many generations, natural populations evolve according to the principles of natural selection and "survival of the fittest", first clearly stated by Charles Darwin in *The Origin of Species*. By mimicking this process, GAs are able to "evolve" solutions to real world problems, if they have been suitably encoded. The basic principles of GAs were first laid down rigorously by Holland.

Genetic algorithms simulate those processes in natural populations that are essential to evolution. They work with a population of "individuals", each representing a possible solution to a given problem. Each individual is assigned a "fitness score" according to how good a solution to the problem is. The highly fit individuals are given opportunities to "reproduce", by "cross breeding" with other individuals of the population. This produces new individuals as "offspring", which share some features taken from each parent. The least fit individuals of the population are less likely to get selected for reproduction, and so "die out". The process is then repeated with the new generation.

Genetic algorithms have been used in numerical function optimisation, image processing, combinatorial optimisation, design, machine learning and much more areas.

### The PgaPack library

**PgaPack** is a general-purpose, data-structure-neutral, parallel genetic algorithm library being developed at Argonne National Laboratory. Its key features on which we are interested are:

- Runs on uniprocessors, parallel computers, and workstation networks.
- Binary-, integer-, real-, and character-valued native data types.
- Parameterized population replacement.
- Multiple choices for selection, crossover, and mutation operators.
- Easy integration of hill-climbing heuristics.
- Easy-to-use interface for novice and application users.
- Fully extensible to support custom operators and new data types.

**PGAPack** is written in ANSI C and uses the **MPI** message passing interface and thus should run on most uniprocessors, parallel computers, and workstation networks. It was developed by [David Levine](https://www.ornl.gov) of the **Mathematics and Computer Science Division** at [Argonne National Laboratory](https://www.anl.gov). [See the PgaPack Copyright notice](https://www.anl.gov/pack)

### Frames

**Frames** provide support for the programming of distributed-memory machines via a library of basic algorithms, data structures and so-called programming frames (or frameworks). The latter are skeletons with problem dependent parameters to be provided by the users. Frames focuses on re-usability and portability as well as on small and easy-to-learn interfaces. Thus, non-expert users will be provided with tools to program and exploit parallel machines efficiently. All these frames will be especially valuable and relevant to industrial cooperators.

The main features of Frames are:

- Re-Usability
- Portability
- State-of-the-art techniques
- Efficiency
- Easy-to-learn
• Easy-to-use graphical interfaces.

Frames are constructed for different target machines and common programming environments (like PVM or MPI). The focus, however, is on distributed-memory machines. Frames will be adapted optimally to the target systems, contain efficient state-of-the-art programming techniques, and therefore increase the acceptance of parallel computing.

The Frames model is depicted in the next picture. In this model, each generated target executable is built from three specifications, an abstract level specification, an instance level specification and an implementation level specification.

Frames is a work-package of the AlCom-IT project. It is described in the paper Programming Frames for the Efficient use of Parallel Systems (1997) written by Thomas Römke from the Paderborn Center for Parallel Computing and Jordi Petit i Silvestre from the Departament de Llenguatges i Sistemes Informàtics (UPC).

The PGA Frame

The PFA frame is a modular frame (or framework, or toolbox) for genetic algorithms on distributed memory systems. The idea of programming frames augments the PgaPack library with graphical editors for specifying genetic parameters that customize the generic algorithm to the user needs. Crossover and mutation operators, selection policies, termination criteria and much other parameters can be set with this graphical tool. The parallelization is based on MPI which guarantees a portable code. Thanks to Frames, customizing or extending a genetic algorithm is very easy.

Following the Frames approach, the PgaFrame is made up of three different specifications. The first specification, also called the abstract specification, is used to define the parameters of the problem. These are the parameters that latter must be filled by the user in the second specification, also called the instance specification. A new instance for a genetic algorithm can be generated by simply changing this instance specification. In the third specification (implementation specification), the implementors of the PgaFrame have coded (using
PgaPack) the implementation of the generic genetic algorithm. The result of merging this
generic code with the instance filled by the user consists in a set of programs and a makefile.

The elements of the PgaFrame (called PGA) are:

- An abstract specification
- A graphical tool to let user specify instances
- Examples of instance specifications (TSP)
- An implementation specification
- The PgaPack library.

The abstract level

Let us now describe the abstract level of the PGA frame. The main task in this level is to
define the properties of the generic genetic algorithm. The declaration of these parameters is
done using the abstract specification language defined in Frames, which is simply a list of
standard ANSI C type definitions with some enhancements.

We remark that all the parameters are strongly sequential and portable: they do not contain
parallel constructs nor aspects of any target machine. This will ensure that they can be reused
over different systems. Along with the declaration of the parameters, the abstract specification
manages their documentation, which is presented in the User Documentation page in HTML
format.

The PGA frame contains a lot of parameters. However, only four of them are not optional; the
rest contain default values that do not need to be changed except for extra customization. The
parameters are structured in the following set of families:

Fundamental parameters:
Contains the information about the type of the chromosomes, the direction in which to
improve the evaluation function, the evaluation function itself and preprocessing and
postprocessing functions, which can be used to input and output data.

Population replacement:
Allows to select how many individuals will be keep in each iteration, how many will
reproduce, how they will replace the old ones, etc. In particular, the PGA frame supports
generational replament GAs (GRGA), steady-state GAs (SSGA), elitist selection....

Stopping criteria:
Three predefined stopping rules are offered, the user can parametrize them or write his
own stopping rule.

Initialization:
Specifies how to create the new individuals. Predefined operators exist, but user with
spetial needs can write their own initialization functions.

Selection:
Usual selection techniques can be parametrized.

Crossover:
Four popular operators can be selected and parametrized. If they are not enough, the user
can provide his own crossover operator.
Mutation:
Again, popular operators can be selected and parametrized. If they are not enough, the user can provide his own mutation operator.

Fitness:
In order to avoid premature convergence, fitness can be adapted.

Restart:
If requested, a new generation can be created periodically by filling the population with mutations of the best current string.

Report options:
Many kind of statistics (on-line and off-line) can be gathered.

Miscellaneous functions:
Includes random number seeding, user-defined printing of strings, and version information.

This is the abstract specification:

```c
ABSTRACT FRAME PGA;

DECLARATION

/* Enumeration types */
TYPE Boolean = enum (False, True);
TYPE DataTypeEnum = enum (Binary, Integer, Real, Character);
TYPE OptDirectionEnum = enum (Maximize, Minimize);
TYPE ReplacementTypeEnum = enum (ReplaceBest, ReplaceRandom, ReplaceRandomNoRep);
TYPE MutationCrossoverEnum = enum (MutationCrossoverOR, MutationCrossoverAND);
TYPE CrossoverTypeEnum = enum (CrossoverOnePt, CrossoverTwoPt, CrossoverUniform, CrossoverUser);
TYPE FitnessMappingTypeEnum = enum (FitnessRaw, FitnessRanking, FitnessFinal);  
TYPE MinimizationFitnessTypeEnum = enum (FitnessMinCmax, FitnessMinReciprocal);
TYPE SelectionTypeEnum = enum (SelectionProportional, SelectionSUS, SelectionTournament, SelectionProBPinTournament);
TYPE InitializationTypeEnum = enum (InitZero, InitBinRandom, InitCharLower, InitCharUpper, 
                                  InitCharMixed, InitPermutation, InitRange, InitPercent, InitUser);
TYPE MutationTtypeEnum = enum (MutationConstant, MutationRange, MutationUniform, 
                                MutationGaussian, MutationPermutation, MutationUser);

/* Out types (private) */
OUT TYPE PGAContext;
OUT TYPE FILE;

/* Pointer equivalent types */
TYPE PGAContextPtr = PGAContext*;
TYPE FILEPtr = FILE*;
TYPE charPtrPtr = char**;

/* Fundamental parameters */
CONSTANT DataTypeEnum DataType;
CONSTANT OptDirectionEnum Direction;
FUNCTION double Evaluate (PGAContextPtr ctx, int p, int pop);
FUNCTION int Preprocess (int argo, charPtrPtr argv);
OPTIONAL PROCEDURE Postprocess (int argo, charPtrPtr argv, PGAContextPtr ctx);
OPTIONAL STATEMENT UserCode ()

/* Population replacement */
OPTIONAL CONSTANT int PopulationSize = "100";
OPTIONAL CONSTANT int ReplacementValue = "10";
OPTIONAL CONSTANT ReplacementTypeEnum replacementType = "ReplaceBest";
OPTIONAL CONSTANT MutationCrossoverEnum MutationCrossover = "MutationCrossoverOR";
OPTIONAL CONSTANT Boolean AllowDuplicates = "False";
OPTIONAL FUNCTION int DuplicateChecking (PGAContextPtr ctx, int p1, int pop1, int p2, int pop2);

/* Stopping criteria */
OPTIONAL CONSTANT Boolean UserDefinedStopRule = "False";
OPTIONAL CONSTANT Boolean StopMaxIter = "True";
OPTIONAL CONSTANT Boolean StopNoChange = "False";
```
The instance level

In the second level (instance level) of the Frames approach, the user is asked to bind values to the abstract parameters. This part is therefore the inter-changeable part of the PGA frame. The generic genetic algorithm is converted in this level in a purpose specific genetic algorithm by simply instancying the abstract parameters. The values binded to the parameters are expected to be given in ANSI C and without parallel constructs. This is why the user is not supposed to have knowledge in parallel programming.

The user can specify his/her instance in three different ways:

- Using the textual instance specification language defined in Frames, which is simply a list of assignments of values to the abstract parameters.
• Using a graphical user interface we have designed adhoc for the PGA frame (called xpga).

• Using the Frames Instantiator Tool (FIT), ie the graphical user interface automatically generated by the Frames tools from the abstract specification.

Specifying the instance level textually is teddious, boring and error-prone, so we claim that, in general, users should use one of the two graphical interfaces available.

The xpga GUI has been expressly implemented to work with the PGA frame. Due to this knowledge, it is very practical, because it integrates the set of parameter families in different windows that can be displayed independently. It has been implemented using the Tcl/Tk programming language and thus it can be executed on almost any machine running Unix, Windows 95 or Macintosh.

The Frames Instantiator Tool is a generic tool to instantiate any frame, and thus, can work with the PGA frame. With this graphical tool, the user can easily access the Frames Repositories, input the values for the abstract parameters, display their corresponding documentation, and launch the compilation process. Since this tool is written in the Java programming language, it can be ran within a WWW browser such as Netscape. Of course, the FIT does not look so nice as the xpga because the GUI is generated automatically, but it brings some advantages as generality, portability and uniformity.

Last but not least, in the second level, the inscc tool of the Frames system carries out a type checking of the given instance against the abstract definition in order to verify that all the assignments are legal.

The implementation level

The implementation level contains the sources of the generic genetic algorithm and the rules on how to modify these sources to get an implementation that complies with the given values in the instance level. The PgaPack library is also provided in this level. The impcc tool of Frames processes all this information in order to create a directory with the new generated sources and a makefile. The user is then ready to compile them and execute them in his/her favourite computer, provided that an MPI implementation is available (for example, MPICH).

Internally, the PgaPack library uses a master/slave strategy in order to execute concurrently the genetic operators. This is sound, because most of the time used by the program is expended in computing the evaluation function for different strings. As there is any dependence with these calculations, their parallel executions brings high speedups.

An example: solving the TSP with the PgaFrame

As a simple demonstrator for the PGA frame, let us make a quick specification to approximate the Traveling Salesman Problem (TSP). The emphasis in this section is pedagogic, to show how to use the PgaFrame. It is not by any means a work of research about solving the TSP with genetic algorithms.

In the TSP, a salesman must visit n cities. Modeling the problem as a complete graph with n vertices, we can say that the salesman wishes to make a tour visiting each city exactly once
and finishing at the city he starts from. There is a cost \( M(i,j) \) to travel from city \( i \) to city \( j \), and the salesman wishes to make the tour whose total cost is minimum, where the total cost is the sum of the individual costs along the edges of the tour. Since this is an NP-complete problem, we will not try to find the minimum tour but one tour close to the minimum. And we will do that using genetic algorithms.

**Encoding and the genetic operators**

In our genetic algorithm, a possible tour will be encoded in chromosomes whose alleles will be integers and will represent a permutation of 0 to \( n-1 \) (a tour of the cities using C language). The evaluation function will be the length of the tour. We will initialize chromosomes at random with permutations, make mutations as flips permutations and use the PMX crossover operator. As global variables we will have the integer \( n \) and the matrix \( M \) of inter-city disances. In the preprocessing phase, we will read the matrix of distances between cities and in the postprocess we will output the best tour found so far. Of course, we want to minimize the evaluation function.

The evaluation of a tour simply consists in adding the lengths between the cities that make it up. This is done in the `Evaluate` function. Here the `PGAGetIntegerAllele` function is used to read a determined allele of a chromosome.

The pre-process consists on filling the \( n \) and \( M \) variables with the information provided through a file, whose name will be the first argument (\( argv[1] \)). In the post-process function, we will suppose that a file named \( argv[2] \) will hold the 2D coordinates of the cities, will order them according to the best tour found and will save them in a file named \( argv[3] \). We remark that the genetic algorithm we will build will not be restricted to two dimensional TSP problems. We output the solution in this way only because with 2D instances the tours can be easily drawn with tools such as gnuplot.

Let us now explain the mutation operator of user function `Mutation`. Given a chromosome, this function flips a coin according to the mutation probability \( m_r \). If the mutation is accepted, two alleles chosen at random in the interval \( 0 \ldots n-1 \) are exchanged.

The crossover function we will apply is the so-called PMX operator. This operator applied to two tours \( A \) and \( B \) does the following: A position \( i \) is chosen uniformly at random from \( 0 \ldots n-1 \), designating a transposition \( T=(A[j],B[j]) \). This transposition is applied to yield two children \( AT \) and \( BT \). This is the basic operation. The full-blown crossover operator in fact picks two positions \( j \leq k \) uniformly at random and performs the above operation on positions \( j \) to \( k \). As an example, consider two tours represented by the chromosomes \( A=(1 \ 4 \ 3 \ 2 \ 0 \ 5 \ 7 \ 6) \) and \( B=(6 \ 7 \ 5 \ 0 \ 3 \ 1 \ 4 \ 2) \). Applying the previous operator to position 3, we obtain \( A'=(1 \ 4 \ 3 \ 0 \ 2 \ 5 \ 7 \ 6) \) and \( B'=(6 \ 7 \ 5 \ 2 \ 3 \ 1 \ 4 \ 0) \).

The rest of the instance we show in the next subsection contains the implementation of the functions we have just described.

**Textual instance**

We can give as instance the following file (TSP.ins):

```c
FRAME TSP IS PGA (MP1)
CONSTANT DataType = Integer;
CONSTANT Direction = Minimize;
FUNCTION Evaluate = double Evaluate (PGAContextPtr ctx, int p, int pop)
```
int i, a, b;
    double s = 0;
    for (i = 0; i < n; i++) {
        a = PGAGetIntegerAllele(ctx, p_pop, i);
        b = PGAGetIntegerAllele(ctx, p_pop, (i + 1) % n);
        s += M[a][b];
    }
    return s;
}

FUNCTION Preprocess = int Preprocess (int argc, char* argv) {
    int i, j;
    FILE *f;
    f = fopen(argv[1], "r");
    fscanf(f, "%d\n", &n);
    for (i = 0; i < n; i++)
        for (j = 0; j < n; j++)
            fscanf(f, "%lf \n", &M[i][j]);
    fclose(f);
    return n;
}

PROCEDURE Postprocess = Postprocess (int argc, char* argv, PGAContextPtr ctx) {
    int x, y;
    FILE *f;
    p = PGAGetBestIndex(ctx, PGA_OLDPOP);
    for (i = 0; i < n; i++)
        fscanf(f, "%lf \n", &x[i]);
    for (i = 0; i < n; i++)
        fscanf(f, "%lf \n", &y[i]);
    fclose(f);
    for (i = 0; i < n; i++)
        j = PGAGetIntegerAllele(x[i], y[i], P_OLDPOP, 1);
    for (i = 0; i < n; i++)
        fprintf(f, "%d %d\n", x[i], y[i]);
    fclose(f);
}

STATEMENT UserCode = {
    int n;    /* Size of the problem */
    double M[200][200];    /* Distances between cities */
};

/* Population replacement */
CONSTANT PopulationSize = 1000;
CONSTANT ReplacementValue = 900;

/* Initialization (integer) */
CONSTANT InitializationType = InitPermutation;

/* Crossover */
PROCEDURE Crossover = Crossover (PGAContextPtr ctx, int p1, int p2,
    int p_pop, int cl, int c2, int c_pop) {
    int i, j, k, l, t1, t2;
    j = PGARandomInterval(ctx, 0, n - 1);
    k = PGARandomInterval(ctx, 0, n - 1);
    if (k > j) {
        i = j;
        j = k;
    }
    PGACopyIndividual(ctx, p_pop, cl, c_pop);
    PGACopyIndividual(ctx, p2, p_pop, c2, c_pop);
    for (i = j; i < k; i++)
        t1 = PGAGetIntegerAllele(ctx, c2, c_pop, i);
    for (i = 0; i < c2; i++)
        PGASetIntegerAllele(ctx, c2, c_pop, i, t1);
    for (i = 0; i < c1; i++)
        PGASetIntegerAllele(ctx, c1, c_pop, i, t2);
    for (i = 0; i < c1; i++)
        PGASetIntegerAllele(ctx, c1, c_pop, i, t2);
    for (i = 0; i < n; i++)
        PGASetIntegerAllele(ctx, c1, c_pop, i, t2);
    for (i = 0; i < n; i++)
        PGASetIntegerAllele(ctx, c1, c_pop, i, t2);
    for (i = 0; i < n; i++)
        PGASetIntegerAllele(ctx, c1, c_pop, i, t2);
}

CONSTANT CrossoverType = CrossoverUser;

/* Mutation (integer) */
CONSTANT MutationProb = 0.05;
CONSTANT MutationType = MutationUser;
FUNCTION Mutation = int Mutation (PGAContextPtr ctx, int p, int pop pop, double s) {
    int m = 0, i, j, a, s2;
    if (PGARandomFlip(ctx, m)) {
        i = PGARandomInterval(ctx, 0, n - 1);
        j = PGARandomInterval(ctx, 0, n - 1);
    }
Using the GUIs for specifying the instance

Instead of writing this file, a user could have used the xpgra tool that generates it automatically. The user task would then be limited to fill the entries of the GUI. For instance, the general parameters and the population strategy have been specified in these windows:

Another alternative would have been used the Frames Instantiator Tool. The look of this tool is as follows:
The results

We ran the previous genetic algorithm on the input given by the following map (100 cities):
The best tour we found is shown in the next figure. The tour does not look quite optimal, but is nevertheless a "good" solution. It must be remarked that, even if this inputs instance satisfies the triangle inequality, the genetic program we have developed does not use this information.

More information about the TSP and genetic algorithms can be found, for example, in [8].

Future work

This is the first version of the PgaFrame. It is also the second complex frame that has been developed following the Frames approach and its tools. As such, it is still a current working project and new enhancements are planned. Some of them are the following:

- User-defined datatypes.
- Creation of a new function parameter Set Up in order to modify the instance given at compile time at running time. For example, in this way it would be possible to adapt the size of the population respect to the input.
- Support to hybridization.
- Explicit usage of the main loop, ie over the steps performed in a single iteration of the GA.
- More convenient support for input/output. As soon as this will be included in Frames, the PGA will support it.

Summary

Lots of people involved in the algorithmic community (or in other fields where optimization methods are needed) are willing to apply genetic algorithms to their problems. However, they cannot invest a large effort to develop a truly efficient, parallel and portable program that
could satisfy their needs. Thanks to the PgaFrame, experts from these fields but not in parallel programming nor in evolutionary algorithms can easily specify a genetic program and run it on the most powerful parallel computers.

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More information

Information about the PgaFrame will be keep on-line at http://wwwlsi.upc.es/~jpetit/PgaFrame and at http://wwwlsi.upc.es/~alcom-it/frames/FRAMESRepository/PGA.

Jordi Petit i Silvestre is reachable by electronic mail as jpetit@lsi.upc.es.

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