Effects of Stray Capacitance to Ground in Three Electrode Monopolar Needle Bioimpedance measurements

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Abstract—Positive phase angle is documented and analyzed in a three electrode monopolar needle measurement. Inductance equivalent behavior of the stray capacitance to ground is described as error source in a non-inductive sample measurement.

I. INTRODUCTION

During development of new bioimpedance based applications (e.g. as described in Kalvøy [1]), we have had unexplained detections of positive phase angle in some of our measurements. These have been both for in-vitro laboratory setups and in clinical in-vivo experiments. Some of this behavior has been explained for 4-electrode setups by Grimnes and Martinsen [7]), but positive phase angle have also occurred in our monopolar 3-electrode Solartron® 1260/1294 setups. This has typically been at frequencies between 100 kHz and 1 MHz. The magnitude has been higher than expected from the inductive properties of tissue and it seems not to be fully explained by Grimnes and Martinsen, nor have we been able to avoid the positive phase by different optimizations of our 3-electrode setup. However, Aliau-Bonet and Pallas-Areny[4] addressed stray capacitance to ground as a contributor to apparent inductive behavior in 4-electrode impedance measurements. A manipulation of their 4-electrode equations showed that similar phenomenon may also occur in other setups, and in our hospital environment we have a lot of electronic equipment and large conductive surfaces representing possible stray capacitances between a human body surface and ground.

From this we postulate that stray capacitance can partly explain the positive phase angle in our 3-electrode Solartron® 1260/1294 measurement setup. In this paper we have tested this hypothesis by evaluating the theory of Aliau-Bonet and Pallas-Areny on an equivalent circuit modified for 3-electrode setups. Laboratory measurements were also performed to confirm the results from the theoretical analysis. The results have been used to propose strategies to avoid or minimize possible errors.

II. MATERIALS & METHODS

A. Three electrodes bioimpedance measurement

A large piece of bacon was used as sample. The type of biomaterial used is not critical for this study, and bacon has earlier been suggested as a convenient in vitro model for animal or human tissue [2]. A three electrode measurement was implemented by a 1294 impedance interface connected to a 1260 frequency response analyzer (Solartron Analytical [3]). The active measurement electrode (I_{in} in Fig 1) was a non-insulated stainless steel needle cannula (18G × 50 mm, Microlance 3, BD New Jersey, US) inserted 1 cm into a fatty part of the sample. The V_{inL} and V_{inH} electrodes were common ECG-electrodes (Blue sensor Q-00-A Ambu Medicotest, DK) placed on the skin of the sample. Signal ground of the transimpedance amplifier that measures current in the 1294 is "0 V floating" [3]. This electric potential reference node is not directly connected to ground (earth) potential but it is at the same potential. The sample under test was placed at a height h with respect to the equipment (Fig. 1). The metal enclosure of the 1260 analyzer was earth grounded hence the height (h) between the sample and the metal enclosure determined the stray capacitance between the sample and ground, which will increase for decreasing heights. Our aim is to reduce the effect of stray capacitances to ground in three electrode impedance measurements.

Fig. 1 is the equivalent circuit of the proposed setup, which includes the measurement functions of the 1294 interface and the sample with the positions of the electrodes. The voltage follower between the Solartron 1260 enclosure in Fig. 1 and signal ground describes the fact that signal ground is at earth-ground potential but not directly tied to it. If the stray capacitance between the sample and ground (C_g in Fig. 1) is not negligible then current I_g through C_g will not be zero. I_g will not reach the current measurement electrode (I_{in}) hence the impedance will be $Z = V_{in}/I_{L}$, and since $I_L = I_H - I_g$ (the amplifiers are assumed to be ideal), Z will be larger than that when $I_g = 0$ (ideal measurement) [3,4].

To minimize the effects of the stray capacitance to ground in the volume of the sample between low potential electrode (V_{inL}) and measurement current electrode (I_{in}) (Fig. 1), we place V_{inL} and I_{in} electrodes next to each other (5 cm apart compared to the distance between V_{inH} and V_{inL} electrodes, 19 cm apart. Since I_{in} is at ground potential, the density of electric field lines (displacement current) between the sample and the metal enclosure of the 1260 analyzer (ground plane) will be higher on the side at higher potential [6] (volume of the sample next to V_{inH} electrode). Therefore, C_g is mainly due to the volume of the sample between the two potential electrodes (V_{inH} and V_{inL} in Fig. 1).

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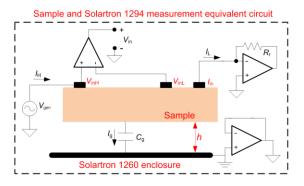


Figure 1. Equivalent circuit for the measurement setup. V_{inH} , V_{inL} and I_{in} are electrodes (red color).

B. Equivalent circuit

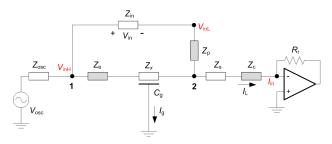


Figure 2. Circuit model where the stray capacitance from the sample to ground is a distributed element.

The equivalent circuit used as an electrical model for the measurement setup is shown in Fig. 2, which includes the equivalent discrete circuit component for each of the electrodes and the input impedance of the voltage amplifier used to measure the actual drop in voltage across the sample. C_g is shown as a distributed capacitance. Impedances with white color are volume impedances (conductors) and impedances with gray color are interface impedances (electrode impedances). Z_e is the impedance of the electrode where a sinusoidal voltage is applied to the sample and voltage is measured (V_{inH} , high potential measurement). Z_x is the impedance of the sample and Z_s is the segmental impedance between low potential measurement electrode (V_{inL} , Z_p) and current measurement electrode (I_{in}). Z_{in} is the input impedance of the voltage amplifier.

In order to include the stray capacitance from the sample to ground in the lumped-parameter circuit model, we use the coefficient α , which value is between 0 and 1 [4].

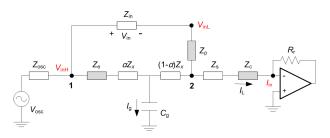


Figure 3. Circuit model where the stray capacitance from the sample to ground is a lumped element at an undetermined position.

III. RESULTS

A. Equivalent circuit analysis

To obtain the expression of the impedance measured $(V_{\rm in}/I_{\rm L})$ we have analyzed the circuit in Fig. 3. The detailed analysis is in the Appendix. The impedance measured is

$$Z_{m} = \frac{V_{m}}{L_{r}} = \frac{Z_{m}}{Z_{m} + Z_{r} + Z_{12}} \left\{ Z_{s} \left[1 + \frac{(Z_{s} + Z_{s})}{Z_{s}} \right] + Z_{s} \left[1 + (1 - \alpha) \frac{Z_{s}}{Z_{s}} + \alpha \frac{(Z_{s} + Z_{s})}{Z_{s}} + \alpha (1 - \alpha) \frac{Z_{s}}{Z_{s}} \right] \right\}$$
(1)

If Z_{in} is very large, we can approximate

$$Z_{m} \approx Z_{e} \left[1 + \frac{(Z_{s} + Z_{c})}{Z_{s}} \right] + Z_{x} \left[1 + (1 - \alpha) \frac{Z_{e}}{Z_{s}} + \alpha \frac{(Z_{s} + Z_{c})}{Z_{s}} + \alpha (1 - \alpha) \frac{Z_{x}}{Z_{s}} \right]$$
(1a)

where
$$Z_g = (j \omega C_g)^{-1}$$
 and Z_{12} is

$$Z_{12} = Z_e + Z_x \left[1 + (1 - \alpha) \frac{Z_e}{Z_g} + \alpha (1 - \alpha) \frac{Z_x}{Z_g} \right]$$
⁽²⁾

The first term in the expression (1), is the voltage loading effect due to the fact that the input impedance of the voltage amplifier is not ideal (infinite). This effect depends on C_{g} , which is included in Z_{12} , equation (2). This effect can be neglected as it is relevant at high frequency, above, say, 1 MHz [4], and the measurement frequency range of the 1294 is up to 0.75-1 MHz [3]. Then, the expression of the measured impedance is the equation (1a), which also depends on C_g . If $C_g = 0$, then Z_g is infinite and the measured impedance is $Z_m = Z_e + Z_x$, ideal result, But $C_g \neq 0$ and the actual Z_m will be larger than $Z_e + Z_x$ because both Z_e and Z_x are multiplied by a factor larger than 1 (1 plus an error term, expressions inside the square brackets in (1b)). Therefore, $C_{\rm g}$ affects both impedances Z_e and Z_x . The term that affects Z_e depends on the segmental impedance Z_s , the impedance Z_c of the current measurement electrode and the stray impedance to ground Z_{g} . The terms that affect Z_{x} depend on α , the impedance Z_e of the injecting electrode, the impedance Z_e of the current measurement electrode, the segmental impedance Z_s , the stray impedance to ground Z_g and itself (Z_x , non-linear effect [4]). The effect of C_g on the measured impedance Z_m will depend on the kind of the impedances involved in the expression. We can generalize the terms in (1a) as

$$Z_{k}\left[1+\sum_{i}c_{i}\frac{Z_{i}}{Z_{g}}\right]=Z_{k}\left[1+j\omega C_{g}\sum_{i}c_{i}Z_{i}\right]$$
(3)

 Z_k can be Z_e or Z_x , Z_i can be Z_e , Z_c , Z_s and Z_x , and c_i can be 1, α , $(1 - \alpha)$ and $\alpha(1 - \alpha)$. The coefficient c_i is a real number and its effect is only an attenuation of the error term. If $Z_i = R_i$ is resistive, the error term $Z_i/Z_g = j\omega R_i C_g$, this is an inductive effect, the impedance (magnitude and phase shift) increases when the frequency increases, and affect the impedance from 100 kHz or even lower frequencies [4]. If $Z_i = (j\omega C_i)^{-1}$ is capacitive, the error term $Z_i/Z_g = C_g/C_i$, this is a frequencyindependent error and affects the impedance in the overall measurement range [4]. When the ratio $C_g/C_i << 1$, there is not effect in the measured impedance [5].

If
$$Z_i$$
 has this form $Z_i = R_i + \frac{R}{1 + j\omega RC_i}$ (4)

Then the expression of the error term will be

$$j\omega Z_i C_g = j\omega C_g \left(R_i + \frac{R}{1 + \left[\omega R C_i\right]^2} \right) + \frac{\left[\omega R C_i\right]^2}{1 + \left[\omega R C_i\right]^2} \left(\frac{C_g}{C_i} \right)$$
(5)

The first term would be like an "inductive" effect and the second term would be like a "frequency-independent error". But, in both cases, the dependence on the frequency is more complex. If the Z_k has a form similar to Z_i , then the equivalent circuit of the measured impedance could contain parallel resonant RLC circuits [5].

At high frequencies (100 kHz-1 MHz) the impedances are

$$Z_{x} = R_{x} + \frac{R_{xx}}{1 + j\omega R_{xx}C_{x}} \bigg|_{\omega R_{xx}C_{x}>>1} \approx R_{x}$$
(6)

$$Z_{s} = R_{s} + \frac{R_{ss}}{1 + j\omega R_{ss}C_{s}} \bigg|_{\omega R_{ss}C_{s}>1} \approx R_{s}$$
(7)

$$Z_{e} = R_{e} + \frac{R_{ee}}{1 + j\omega R_{ee}C_{e}} \bigg|_{\omega R_{ee}C_{e}>1} \approx R_{e}$$
(8)

$$Z_{c} = R_{c} + \frac{R_{cc}}{1 + j\omega R_{cc} C_{c}} \bigg|_{\omega R_{cc} C_{c} > 1} \approx R_{c}$$
⁽⁹⁾

When 100 kHz $>> (2\pi R_{ii}C_i)^{-1}$, where *i* can be x, s, e and c, then equation (1a) becomes

$$Z_{m} \approx R_{e} \left[1 + j\omega C_{g} \left(R_{s} + R_{e} \right) \right] + R_{x} \left[1 + j\omega C_{g} \left\{ \left(1 - \alpha \right) R_{e} + \alpha \left(R_{s} + R_{e} \right) + \alpha \left(1 - \alpha \right) R_{x} \right\} \right]$$

$$= R_{e} + R_{x} + j\omega C_{g} \left[R_{e} \left(R_{s} + R_{e} \right) + R_{x} \left\{ \left(1 - \alpha \right) R_{e} + \alpha \left(R_{s} + R_{e} \right) + \alpha \left(1 - \alpha \right) R_{x} \right\} \right]$$

$$= R_{e} + R_{x} + j\omega L_{eq}$$

$$L_{eq} = C_{g} \left[R_{e} \left(R_{s} + R_{e} \right) + R_{x} \left\{ \left(1 - \alpha \right) R_{e} + \alpha \left(R_{s} + R_{e} \right) + \alpha \left(1 - \alpha \right) R_{x} \right\} \right]$$
(10)

Equation (10) corresponds to an equivalent circuit of the measured impedance like that in Fig. 5.

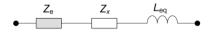
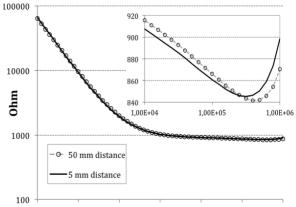


Figure 4. Equivalent circuit model of the measured impedance.



1,00E+00 1,00E+01 1,00E+02 1,00E+03 1,00E+04 1,00E+05 1,00E+06

Figure 5 Dubble logarithmic plot of measured impedance modulus as function of frequency. Inset shows details from the highest frequencies on a stretched linear y-axis from 840 to 920 ohms.

B. In-vitro measurements

The measured impedance modulus (Fig. 5) and phase angle (Fig. 6) show a significant effect of electrode impedance for frequencies up to 1-10 kHz. This low frequency phase shift is related to the relatively small electrode area of the needle electrode [1,7]. No significant effects caused by the change on the $C_{\rm g}$ value are expected at low frequency.

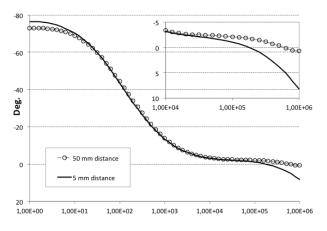


Figure 6 Measured phase angle as function of frequency (logarithmic xaxis). Inset shows details from the highest frequencies on a stretched y-axis from -5 to 10 degrees (reversed direction).

The effects of C_g are visible at high frequency, between 100 kHz and 1 MHz in the modulus of impedance, where the modulus increases when the value of C_g increases. The effects on the phase shift of impedance are more visible, between 10 kHz and 1 MHz, where the phase shift increases when the value of C_g increases. The difference, between phase shift at highest value of C_g and phase shift at lowest value of C_g , increases with the frequency, inductive effect.

The modulus of impedance of the sample between 10 kHz and 1 MHz seems unaffected of electrode impedance, and is in accordance with previous publicized measurements in fat [1] except for the inductor-like increase above 200 kHz. If we model the almost flat level as a resistor, then Z_k will be a resistance. Z_i is also a resistance (in the range from 10 kHz to 1 MHz) because no frequency dependent error is displayed in the measurements, then the ratio $C_e/C_i \ll 1$.

IV. DISCUSSIONS

A significant positive phase angle was found at the high end of the frequency spectrum measured in the sample for h = 5 mm (inset in Fig. 6.). A large reduction of the positive phase angle was obtained by changing to h = 50 mm and keep all other factors unchanged. The analyses of the proposed equivalent circuit resulted in a theoretical equivalent inductance (L_{eq}) that represented the analytical link between the stray capacitance to ground and this measured positive phase phenomenon. Stray capacitance to ground is not easily shielded from a patient or a clinician with a shielding plate or similar (Figure 3-15. Guarding technique (1) Agilent "Handbook"[9]). Hence, other strategies must be found.

Aliau-Bonet and Pallas-Areny [4] shows that the effect of stray capacitance can be reduced by minimize the distance between the current carrying electrode and the pick-up electrode. Gersing [10] has the same conclusion and states that "the more the lengths of the possible lines of current differ, the more positive are the phase values". However, other considerations can lead to the opposite conclusion. Shiffman [11] have described adverse effects due to close distance between the current-carrying and the pick-up electrodes in measurement of body segments where homogenous current distribution through the whole segment is crucial for reproducible results. But this problem will vanish for truly monopolar needle measurements setups since the spatial sensitivity zone is highly focused on the needle tip [12]. The role of highly conductive surface shunt paths e.g. associated with excessively moist skin that is addressed by Grimnes and Martinsen [7] can still be a problem in a clinical setting. We suggests that 3-electrode needle measurements is done with the skin electrodes attached on a dry surface some centimeters apart.

A phase shift between 5 and 50 mm measurement is seen for the lowest frequencies in Fig. 6. This is not in accordance with the equations presented above, but previous studies on stainless steel needle electrodes show that some temporal drift in the electrode polarization properties can be expected [8]. However, this sub kilohertz-range drift will not preclude the results based on the frequencies above this range.

We did some simple test moving the sample about half a meter from the Solartron equipment and introducing stray capacitance by letting the needle operator hold his naked fingers on the needle during the measurement. The resultant phase angle was negative for the complete frequency spectra without operator contact, but during contact between the operator and the needle a positive phase angle occurred for the highest frequencies quite similar to what was found at h = 50 mm without contact (Fig 7). Further test with operators using typical clinical rubber gloves should be done to decide if continuous measurements during the needle insertion reliable, or recommendations for the clinicians to remove their hands and step away from the patient before each measurement should be give to avoid this error source.

V. CONCLUSION

Our bioimpedance measurements show that the hypothesized positive phase angle, caused by capacitive coupling to ground, is a possible source of error in a Solartron monopolar 3-electrode measurement setup. Analysis of the proposed stray capacitance equivalent circuit furthermore shows that this behavior is consistent with general circuit theory.

APPENDIX

To find $Z_m = V_{in}/I_L$, expression (1) we can analyze the circuit of Fig. A1 (from Fig. 4), where $Z_1 = Z_e + \alpha Z_x$, $Z_2 = (1 - \alpha)Z_x$ and $Z_3 = Z_s + Z_c$. The current and voltage equations of the circuit (Fig. A1) are

$$I_1 = I_g + I_2$$
 (A.1)

$$I_{\rm L} = I_{\rm in} + I_2 \tag{A.2}$$

$$V_{12} = I_{in} \left(Z_{in} + Z_{p} \right)$$
 (A.3)

$$V_{12} = I_1 Z_1 + I_2 Z_2$$
 (A.4)

$$I_{g}Z_{g} = I_{2}Z_{2} + I_{L}Z_{3} \rightarrow I_{g} = I_{2}\frac{Z_{2}}{Z_{g}} + I_{L}\frac{Z_{3}}{Z_{g}}$$
 (A.5)

From (A.5), (A.1) and (A.4) we obtain

$$V_{12} = (I_g + I_2)Z_1 + I_2Z_2 = \left(I_2\frac{Z_2}{Z_g} + I_L\frac{Z_3}{Z_g} + I_2\right)Z_1 + I_2Z_2$$
(A.6)

Using (A.2)

$$V_{12} = I_2 \left(Z_1 + Z_2 + \frac{Z_1 Z_2}{Z_g} \right) + I_L \frac{Z_1 Z_3}{Z_g} = \left(I_L - I_{1n} \right) \left(Z_1 + Z_2 + \frac{Z_1 Z_2}{Z_g} \right) + I_L \frac{Z_1 Z_3}{Z_g}$$
(A.7)
$$V_{12} + I_R \left(Z_1 + Z_2 + \frac{Z_1 Z_2}{Z_g} \right) = I_L \left(Z_1 + Z_2 + \frac{Z_1 Z_2}{Z_g} + \frac{Z_1 Z_3}{Z_g} \right)$$
(A.8)

$$Z_{12} = Z_1 + Z_2 + \frac{Z_1 Z_2}{Z_g}$$
(A.9)

Using (A.3) and $I_{in} = V_{in}/Z_{in}$

$$\frac{V_{in}}{Z_{in}} \left(Z_{in} + Z_{p} + Z_{12} \right) = I_{L} \left(Z_{1} + Z_{2} + \frac{Z_{1}Z_{2}}{Z_{g}} + \frac{Z_{1}Z_{3}}{Z_{g}} \right)$$
(A.10)

$$Z_{\rm m} = \frac{V_{\rm in}}{I_{\rm L}} = \frac{Z_{\rm in}}{Z_{\rm in} + Z_{\rm p} + Z_{\rm 12}} \left(Z_{\rm 1} + Z_{\rm 2} + \frac{Z_{\rm 1}Z_{\rm 2}}{Z_{\rm g}} + \frac{Z_{\rm 1}Z_{\rm 3}}{Z_{\rm g}} \right)$$
(A.11)

Replacing the expressions of Z_1 , Z_2 i Z_3 in (A.11) we get the expression (1).

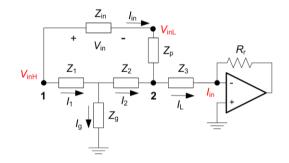


Figure A.1. Equivalent circuit

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