LINEAR CONTROL OF THE YAW AND RUDDER LIMITATIONS
FOR CORMORAN AUV

Julián González114, Ivan Masmitjà113, Spartacus Gomáriz115

Abstract
This work presents a detailed situation about the linear control design for the yaw in the Cormoran autonomous underwater vehicle (auv). The development includes the physical limitations of the rudder that involve more constraints for the control. The whole system is simulated in simulink and three different controls (P, PD, PID) are compared.

Keywords—auv; cormoran; linear control; rudder limitations

I. INTRODUCTION
The Cormoran is a low cost oceanic observation vehicle, which combines the characteristics of the ASVs and AUVs because its principle of motion [1]. This principle is based on the navigation at the surface level, where the vehicle has to follow a predefined path in the mission. The path is defined by a series of waypoints, in which the vehicles stops, dives and emerge vertically in order to obtain a profile of a water column.
This task leads to the need of a control system for the yaw which be fast and stable, but at the same time that take into account the physical constraints of the rudder, like saturation and reaction time. This work addresses this control using different linear controls (P, PD and PID) and comparing them with a root locus analysis that includes these constraints.

II. DYNAMIC MODEL
The dynamic model has been derived from the Fossen equations [2], and it was simplified to 3 degrees of freedom: surge (x), sway (y) and yaw (r).
This model includes two terms that influences the turns, which are \( Y_{uf} \delta_r \) and \( N_{uf} \delta_r \), where \( \delta_r \) represents the action of the rudder, and its action is limited in the range \( +/-20^\circ \).

III. LINEARIZATION
In order to design a control system of the yaw it is necessary to obtain a linearization of the dynamic model. This linearization assumes that the surge velocity (u) is bigger compared with the other sway (v) and yaw (r) velocities that are smaller and taken zero. The resulting transfer function of the yaw (y) respect the rudder (\( \delta_r \)) has the form: \( G(s) = \frac{-b}{s(s+a)} \), where \( a \) and \( b \) depends in the velocity of linearization \( u_0 \).

IV. LINEAR CONTROL DESIGN
The transfer function \( G(s) \) implies that while the gain loop is bigger, the control will be faster and exact in a step response. However, the gain loop affects directly the action of the rudder, which has a significant constraint. For this reason, in the control design is taken as definition that the gain loop cannot be bigger than the maximum rudder angle, i.e. 0.35 radians in order to not saturate the step response.
Figure 1 shows a root locus for a PD-control in where the gain loop has been limited and the zero is the varying variable (the final paper will extend to the other controls).

V. RESULTS AND CONCLUSIONS
The results show that due the rudder constraints the system has its own time responses depending of the forward velocity. For this reason, the margin for action of the linear control design is limited. As future work will be studied this design regarding different step sizes in order to have more margin with the gain loop.

REFERENCES

Fig. 1. Root locus for PD-control design