Abstract—This paper presents the kinematic design of a single degree-of-freedom exoskeleton mechanism: a planar eight-bar mechanism for finger curling. The mechanism is part of a finger-thumb robotic device for hand therapy that will allow users to practice key pinch grip and finger-thumb opposition, allowing discrete control inputs for playing notes on a musical gaming interface. This approach uses the mechanism to generate the desired grasping trajectory rather than actuating the joints of the fingers and thumb independently. In addition, the mechanism is confined to the back of the hand, so as to allow sensory input into the palm of the hand, minimal size and apparent inertia, and the possibility of placing multiple mechanisms side-by-side to allow control of individual fingers.

I. INTRODUCTION

Over the past several decades, robotic devices have emerged as a promising tool for both administering and investigating rehabilitation after stroke. For an introduction to this research topic, see [1], [2]. There are two often referenced advantages when developing robotic devices for administering therapy: automating the repetitive and strenuous aspects of physical therapy and delivering it in a highly repeatable manner. As a scientific investigation tool, robotic devices offer a second set of advantages: the ability to quantify recovery progress with a wide variety of performance metrics (strength, range-of-motion, etc.) and to test and compare therapy paradigms.

A wide variety of assistive control strategies have been developed (see review: [3]) including robots that rigidly follow fixed paths, robots that assist only if patient performance failure is detected, and soft robots that form a model of the patient’s weakness. Implementations of these control strategies have produced a large body of clinical evidence that suggests that exercise with robotic therapy device can benefit, albeit modestly, stroke patients (see reviews [4], [5], [6]). However, it is still unclear what factors directly promote recovery. It is therefore crucial to more clearly identify the recovery mechanisms present in robotic therapy and how these mechanisms may be optimized to increase recovery gains.

Two key factors that are thought to influence motor recovery during physical therapy are the intensity of motor output (subject voluntary participation) and the intensity of movement-correlated sensory information (from movement completion). In a robotic therapy device, these two factors may be in conflict. If the robot completes therapy movements independent of patient output, then motor output may be reduced, but if the subject cannot complete the movement without assistance, then the correlated sensory information is limited. To address this problem we previously developed an assist-as-needed control algorithm [7] that allows the effort of the patient to be modulated while maintaining the kinematics of movement performance within close bounds to a specified desired movement. This allows neuromuscular motor control output and afference to be independently controlled. One limitation with the previous implementation of this algorithm [7] was that the relative low bandwidth of its control limited the ability of the device to provide inertial assistance during therapy movements. In addition, we only applied the algorithm to arm movement, while some studies indicate that focusing on forearm/wrist [8] or hand training may produce large benefits for some patients [9]. For this reason a more specialized, focused study of the assist-as-needed controller for hand movement is desired.

The hand is also a particularly interesting target for studying assist-as-needed control as it is one of the most sensitive organs of the body; thus if sensory information matters, it should be used more for hand recovery. Focusing on the hand also allows the development of a relatively small, safe home-training device which will facilitate a rigorous test of the effects of increased motor output on motor outcomes with robotic training. We are therefore developing a device to test the assist-as-needed controller on the rehabilitation of the hand.

Previous robotic hand rehabilitation devices can be classified into two general categories: glove designs and exoskeleton designs (for example see [10], [11]). The exoskeleton design is typically the approach that least interferes with different sensory feedback and allows the most precise control and thus was chosen for the proposed hand rehabilitation study. In addition, in order to meet the needs of the proposed study, the robotic device should meet several specific design goals. Ideally, the device should: 1) be highly backdrivable, 2) be force and compliance controllable, 3) have a high controllable bandwidth, 4) allow unobstructed tactile feedback, and 5) have...
a low apparent inertia. These characteristics will allow the assistance-as-needed algorithm described above to be robustly and safely implement for the hand, and it will allow home-based delivery of training for greater intensity, allowing us to rigorously answer our questions about the role of motor output and afference in recovery.

A further consideration is the types of movements the device should assist, and the training environment for those movements. For the device described here, we are focusing on a musical training paradigm to assist in learning functional grips. Learning to play music is challenging, interesting, and rewarding, and allows for more compact interfaces than visual-gaming approaches. Further, auditory input is known to facilitate motor output [12]. The device described here will assist the user in learning to play music by opposing the thumb with the fingers, producing notes on a scale while also practicing functionally relevant gripping movements. We have pilot tested this approach with a passive glove and individuals with a stroke have found it motivating and challenging [13].

To meet the design needs of the robotic device, we have chosen to develop lightweight single-degree-of-freedom mechanisms for following the trajectories of the fingers and thumb during the desired movements. This paper presents the methodology for the kinematic design of a single degree-of-freedom exoskeleton mechanism for finger curling motion. The mechanism is a planar eight-bar with two end-effectors; one for controlling both the angle and position of the proximal phalanx and a second to control the position only of the middle phalanx. When combined with the future thumb mechanism, the mechanisms will produce a single robotic device for hand rehabilitation that is capable of assisting in grasping tasks. This approach is unique in that the mechanism will be actuated with a linear actuator so that the design of the mechanism will generate the grasping motion, rather than actuating the joints of the fingers independently. In addition, the mechanism is confined to the back of the hand, so as to minimize sensory feedback interference, to allow the mechanism to be manufactured with minimal size, and to allow multiple copies to be placed side-by-side if desired to control individual fingers. This, combined with the intended location of the linear actuators (back of the wrist/arm) will allow the device to be constructed with low apparent inertia to the intended subjects so that we may maximally exploit the high bandwidth and force controllable ability of the linear actuator.

II. FINGER MECHANISM DESIGN

A. Design objectives

The design objectives for the finger mechanism are summarized below:

1) Single degree-of-freedom planar mechanism.
   The goal is to curl the finger(s) in a natural motion using a single actuator and a planar mechanism. This has the advantage that the actuator may be located behind the hand and/or wrist, connected to the base of the device. This reduces the apparent inertia of the mechanism. The limiting of the finger to natural positions is another advantage, as it provides inherent safety.

2) Exoskeleton Mechanism Offset Design
   The goal is for the mechanism, including joint axes, to be located behind the hand and fingers during the full range of motion. This will allow the mechanism to be constructed out of light material, as all rotating joints can be designed with balanced side loading. Also, a similar mechanism could be used to actuate each finger independently, if desired.

3) Exoskeleton to Finger Interface
   The goal is to attach the mechanism to the finger(s) at the proximal and middle phalanx, leaving the distal phalanx free for sensory feedback during rehabilitation exercises. In order to assure the correct alignment between the finger and mechanism during motion, the mechanism will control both angle and orientation of the proximal phalanx and the position of the middle phalanx. Position-only control of the middle phalanx will be achieved by locating a revolute joint between the mechanism and the middle phalanx.

B. Finger Data

Finger trajectory data from both proximal and middle phalanges were synthesized for the initial design from hand closing/opening motion. The data assumes the metacarpal is fixed along the x-axis and that the proximal and middle phalanges rotate about two revolute joints (the metacarpophalangeal and proximal interphalangeal joints). The curling model assumes that both relative angles are the same, with a curling motion from 0 to 80 degrees. Fifteen points along this path were collected, as shown in Figure 1 below.

![Fig. 1. Desired motion for the finger](image-url)
proved successful. The solution presented here is an eight-

This led to the consideration o

it was determined that the planar six-bar does not have

numerous attempts at synthesizing Watt type six-bar chains,

Configurations of six-bar chains are presented in [15]. After

six-bar mechanisms with revolute joints were considered.

may be designed with two output links. As a starting point,

phalanx. To achieve this goal, two output links are required.

desired output of the mechanism design is two end-effectors;

reach all of the trajectory configur

ations; using a squared error

as those generated from a desired trajectory. In this case the

formulations, using a squared error

must be satisfied. The inner loop constraint equation has the

The other two loop equations can be defined in a similar

fashion. The loop constraint equations for both the mid-

dle and outer loops can be defined by the joint chains

GWHP. This vector equation has the detailed form

G + d_1 \{c\theta / s\theta\} + d_2 \{c(\alpha + \phi) / s(\alpha + \phi)\} + m \{c(\psi + \alpha_2 + \delta) / s(\psi + \alpha_2 + \delta)\} = P, \quad (1)

where c and s stand for cosine and sine, respectively.

The other two path equations for the proximal phalanx
are the joint chains \(G_1 W_1 WHP\) and \(G_1 W_2 H_2 HP\). These

equations are similar to Equation 1 above. In a similar

fashion, three path equations for the middle phalanx position

are defined by the joint chains \(GWHY M, G_1 W_2 H_2 Y' M\),

and \(G_1 W_2 Y_2 Y_1 Y' M\). In addition to the above output path
equations described above, three loop constraint equations
must be satisfied. The inner loop constraint equation has the form

\[
G + d_1 \begin{pmatrix} c\theta \\ s\theta \end{pmatrix} + d_2 \begin{pmatrix} c(\alpha + \phi) \\ s(\alpha + \phi) \end{pmatrix} + m \begin{pmatrix} c(\psi + \alpha_2 + \delta) \\ s(\psi + \alpha_2 + \delta) \end{pmatrix} = P, \quad (2)
\]

There are numerous possibilities of planar topologies that
may be designed with two output links. As a starting point,
six-bar mechanisms with revolute joints were considered.

Configurations of six-bar chains are presented in [15]. After
numerous attempts at synthesizing Watt type six-bar chains,

it was determined that the planar six-bar does not have the
necessary solution span to produce the desired motions.

This led to the consideration of eight-bar mechanisms, which
proved successful. The solution presented here is an eight-
bar planar mechanism with all revolute joints (Chain 1 from
[16]). A diagram of the mechanism is given in Figure 2
above. The output is the position \((P)\) and angle \((\mu_P)\) of the
proximal phalanx and the position \((M)\) of the middle phalanx.

The mechanism consists of 10 revolute joints \((G, G_1, \text{which}
\text{are fixed, and \(W, W_1, W_2, H, H_2, Y, Y_1, \text{and \(Y_2,\\text{seven configuration angles \((\theta, \theta_1, \phi, \phi_1, \phi_2, \psi, \text{and \(\psi_1,\) seven structural angles \((\alpha, \alpha_2, \delta, \delta_2, \gamma, \gamma_2, \text{and \(\mu,\) 13 link lengths \((d_1 \text{ to \(d_{11}, \(m, \text{and \(m_2, \text{and two base positions \((G_x, G_y, G_{1x}, \text{and \(G_{1y}\)\). Because only one of the configuration angles is independent (in this
application, we have chosen \(\theta\), the 18 design equations have
25 unknowns for each desired configuration of the outputs
(position and angle of the proximal phalanx and position of the
middle phalanx). For a direct solution, this requires 8
desired configurations. For our application, however, we have
chosen to specify a series of configurations along the desired
curling motion exceeding the minimum eight, so that the
design problem becomes an optimization problem; determine
the structure variables and a set of \(n\) configuration angles
\((\theta_1 \text{ through \(\theta_n))\) that most accurately reach the \(n\) desired
configurations.

E. Optimization Constraints

There are numerous constraints that must be included in the
optimization in order to achieve the desired results. Several
constraints can be implemented with simple upper and lower

Fig. 2. Eight-bar mechanism diagram for the finger curling mechanism
bounds. For example, the location of the base points \( G \) and \( G_1 \) were constrained within the following ranges: \(-8 < G_x < 6\), \(-6 < G_y < -1.2\), \(-8 < G_{1x} < 6\), \(-6 < G_{1y} < -1.2\). These limits on the location of the base points keeps them located off of the back of the hand and at a reasonable distance from the desired configuration points.

The structure lengths were also constrained with upper and lower bounds, \( A < d_1 - d_{11}, m, m_2 < 4 \). The lower bound keeps the joints a manufacturable distance and the upper bound keeps the link lengths small so that the synthesized mechanism is compact. Using the law of cosines, constraints were also applied to the remaining six distances between joints that are not directly controlled by the structural length variables, such as the distance between joints \( H \) and \( W_1 \). The structural angles, however, were not constrained, as doing so unnecessarily limits the search space during optimization. These angles may be trimmed after optimization as needed.

It was also necessary to constrain the mechanism design so that the location of any two joints during the desired motion do not interfere. For example, depending on the structural variables, it may be possible for joints \( W_1 \) and \( H_2 \) to collide for some relative angle \( \theta_1 - \phi_1 \). To complete this set of constraints, the distances between all joints that might collide must be calculated at each configuration of the mechanism. These distances are constrained to be between 0.4 and 8 inches in order to keep the mechanism both manufacturable and compact.

A final set of constraints, while not simple to implement, are required to generate the desired mechanism. Specifically, it is necessary to constrain the location of the joints to behind the finger for all desired configurations. This cannot be achieved with upper and lower bounds, because the allowable position of the joints depends on the configuration of the desired finger configuration. To implement these constraints, three vectors are defined at each configuration of the finger, one starting at the base \((y_b)\), one at the desired proximal phalanx position \((y_p)\), and one at the desired middle phalanx position \((y_m)\). The vectors are perpendicular to the surface of the base, proximal phalanx, and middle phalanx for each angle, and pointing away from the hand, as shown in Figure 3. An additional set of three vectors \((u_b, u_p, u_m)\) are created for each arbitrary joint \( J \). These vectors start at the same respective points as \( y_b \), \( y_p \), and \( y_m \), but they all point to the current location of the joint.

As it can be seen in Figure 3, the arbitrary joint located at \( J \) is safely clear of the undesirable joint area, as defined by the current location of finger. The maximum of the three dot products between the corresponding \( y \) and \( u \) vectors gives the distance of the joints away from the hand at the current configuration. As long as this value is positive, the joint position is safely located behind the hand. Therefore, the maximum of the three dot products is constrained at each configuration to be between 0.1 and 6 inches. This constraint keeps each joint location behind the hand during all desired output configurations.

III. Results

Using the design equations and the constraints described in the previous section, an eight-bar mechanism candidate suitable for our intended robotic device was achieved. The solution was found using a constrained nonlinear optimizer (fmincon function in Matlab). The optimization process included randomly generated initial conditions. A visual check was used to screen solutions from each attempt at optimization. Those with a promising structure were further optimized by both exploring initial conditions near the solution and by allowing more iterations and setting tighter stopping conditions for the optimization. The structural variables of the selected solution are given in Figure 4 below.

**Figure 3. Vectors for constraining joint location for the 8-bar linkage**

**Figure 4. Resulting eight-bar linkage parameters**

Figure 5 shows the selected solution and a few configura-
tions during the curling motion.

Fig. 5. Resulting eight-bar linkage

IV. CONCLUSIONS

The results presented for the finger mechanism are at the prototype stage. Although these initial results look promising, further work is necessary to determine the validity of the proposed mechanism.

The solution finger mechanism meets many of the criteria previously identified. It is confined to the back of the hand and it successfully produces the desired angles and positions of the proximal phalanx and the desired positions of the middle phalanx during the specified motion. There is, however, a trade-off in terms of mechanism complexity. The proposed solution has seven links which will require complex shapes in order to clear each other. In addition, the mechanism has 11 revolute joints which must be implemented with both low friction and minimum backlash less the mechanism become unwieldy and unstable to control. We believe this can be achieved, in part, due to the stabilizing nature of the inherent parallel linkages in the designed mechanism. This does, however, require precise machining to ensure parallelism between all rotation axes.

The next step for the mechanism optimization is to identify a small subset of structural variables, that when modified in a known fashion, will produce a mechanism which tracks a different desired set of trajectories. It will be important to choose the variable subset as to avoid the disassembly of the mechanism joints. In a fashion similar to [14], this will allow the mechanism to be re-configured to varying finger sizes without rebuilding the entire mechanism.

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REFERENCES


