Cooperative Energy Management for a Cluster of Households Prosumers

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Abstract — The increment of electrical and electronic appliances for improving the lifestyle of residential consumers has led to a larger demand of energy. In order to supply their energy requirements, the consumers have changed the paradigm by integrating renewable energy sources to their power grid. Therefore, consumers become prosumers in which they internally generate and consume energy looking for an autonomous operation. This paper proposes an energy management system for coordinating the operation of distributed household prosumers. It was found that better performance is achieved when cooperative operation with other prosumers in a neighborhood environment is achieved. Simulation and experimental results validate the proposed strategy by comparing the performance of islanded prosumers with the operation in cooperative mode.


I. INTRODUCTION

The modern living style involves increments in the acquisition of electrical and electronics appliances to make our daily life easier and more comfortable. The appliances vary from white goods, such as refrigerators, washing machines or kitchen stoves, to small entertainment and information appliances such as video game consoles, tablets, phones, TV sets, etc. This is a generalized phenomenon in home areas that implies increments in global energy consumption [1]. It is forecasted that by 2030 the world energy demand will be doubled and similarly the carbon dioxide emission due to conventional power generation systems will increase by 75% [2]. In that case, the capability and reliability of the conventional energy generation and transmission system as well as its environmental impact will be seriously compromised [3]. In light of the growing concern about ensuring the energy supply, without increasing the greenhouse gas emission, the integration of renewable energy sources (RES) has been recently promoted for household consumers as can be seen in Fig. 1. [2]

This new trend in the integration of RESs means a change in the paradigm for energy consumers, which is motivated not only by personal environmental commitment but also for economic reasons. From the point of view of the Distribution System Operator, the increasing penetration of RES, implies additional technical challenges in regulation, support and control of the traditional power grid [4], [5]. The cost associated to the new technological requirements, is mainly passed to the end-consumers by means of surcharges in the electricity [5]. This fact, together with less attractive tariffs for selling the renewable energy generation to the main grid, and also taking into account more efficient energy consumption of new appliances, have changed the preferences of the household energy consumers. Household consumers want to be as much independent as possible from the main grid and promoting self-energy consumption, which in turn is reflected in reductions on the energy bill [6]. Even considering the initial investment associated with the installation of RES, household consumers are still willing to deploy RESs even under low internal rate of return [7].

Within this new scenario, there is a change in the paradigm of typical household consumers in which they have become household prosumers, since they not only consume but also produce their own energy based on local resources and requirements. Due to the unpredictable nature of the RESs and for increasing the local consumption rate of RESs, generation prosumers have to integrate Energy Storage Systems (ESS) within their small-scale power systems [8]. ESSs based on batteries are the most commonly used for household applications, because batteries offer a good commitment

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between energy density, life cycling and cost [4], [9]. In that case, a household prosumer can be seen as a small-scale microgrid where the operation of distributed units (RESs, ESSs and appliances) can be coordinated for ensuring a reliable operation of the local power grid [10].

For an optimal operation of each prosumer, it is required an energy management system (EMS) which ensures the power balance of the local power system and optimizes the power consumption and generation at home [11]. To be more clear, the EMS schedules the operation of the distributed energy resources (DERs) by considering load requirements, while ensuring proper ESSs performance, and maximizing the use of renewable energy resources [12].

To achieve an independent operation of the main grid, the prosumer can operate in islanded mode. However, due to the uncertain generation of the RESs, sometimes it is not possible to meet the required demand relying only on local DERs, or store the surplus of energy when the ESSs are fully charged [13]. Because of that, prosumers sometimes have to disconnect their load, or waste some available energy from the RESs in order to avoid excessive discharge and overcharge of the ESSs. Nevertheless, a better performance can be achieved when an external power system can help with some energy support the prosumer. At this sense, a prosumer can cooperate with others neighbor prosumers, in order to reach a better global performance and increase the reliability of the cooperative cluster of residential microgrids [14]. A cluster of household prosumers can be seen as a neighborhood as is shown in Fig. 2.

In this paper, a central EMS is proposed for ensuring an optimal operation of a cluster of islanded residential prosumers operating in islanded mode. The proposed strategy, considers cooperative operations between prosumers such as power sharing and storage energy balance. Nevertheless, the optimization problems consider restrictions for fair disconnection of the loads, by taking into account unequal generation and consumption profiles of each prosumer. The performance of islanded prosumers is compared with the performance of the cooperative cluster of prosumers. Experimental results are used in order to evaluate the proposed strategy. This paper is an extended version of the conference paper [18], which includes a detailed description of the optimization problem and extends the evaluation of the performance of clusters of household prosumers under different scenarios.

II. HOUSEHOLD PROSUMERS

A. Islanded prosumers

The paradigm for private owners is to achieve autonomous power supply and consumption based on their own installed energy resources, and become independent form the utility grid [6]. Islanded operation requires maximizing the generation from RESs while ensuring safe operational conditions for the stored energy in ESSs, which in turn will be reflected in longer lifespan for their installation. In light of the above, an EMS can schedule optimally the operation of the distributed resources within a small-scale microgrid by forecasting the resource availability and scheduling the power generation [3], [19], [20].

A typical configuration of a household prosumer based on renewable energy can be seen in Fig. 1. The residential power grid is composed by renewable energy generation units, energy storage systems and household appliances which can be seen as an aggregated load. A simplified electrical scheme can be seen in Fig. 3. The renewable sources can be photovoltaic (PV) generators, small wind turbine (WT)
generators or combinations of both. Also, ESS are required for smooth the variability of RESs, they are commonly based on batteries arrays and also battery based electric vehicles have been recently used [8], [21].

Commonly, ESSs are the responsible of ensuring the power balance in the islanded power grid by regulating the voltage and frequency in the common bus. Because of that, ESS will operate in voltage control mode (VCM) [22], [23]. Meanwhile, RESs will operates as power sources and their power reference \( P^* \) will be determined by the minimum value between the scheduled power \( P_g \) from the EMS and the power defined by an algorithm of maximum power point tracking (MPPT), \( P_{MPPT} \) [19].

The cycle life of batteries decreases with deep discharge, and overcharge may cause high degradation of batteries. Because of that, it is important to constrain the state of charge (SoC) of a battery within a safe window (normally 20 to 90\%) [4]. From the point of view of the residential owner, this is an important issue to take into account, since the installation cost and replacement cost of batteries represent a big percentage of the total cost of the installed local energy system [24]. Therefore, for ensuring the power balance of the local power system and properly constrains the SoC of the batteries, sometimes it is necessary to shift the load or limit the RESs generation during periods of low and high generation, respectively. Consequently, the main objective of the power scheduling performed by the EMS is to ensure a reliable supply of the load as long as safe SoC window is warranted.

**B. Neighborhood of Household Prosumers**

Geographical aggregation of household prosumers can be considered as a neighborhood. As members of a community, independent household prosumers may cooperate between them in order to enhance the performance of their own installed power systems. Fig. 4 shows a scheme of a neighborhood of \( n \) household prosumers. Each prosumer is able to operate independently from their neighbors with its own local EMS. On top of that, a central EMS can coordinate the operation of the distributed prosumers in order to improve the behavior of the local power systems. This improvement can be reflected in more usage of the renewable resources and less disconnection of the loads. On top of that, additional collaborative behaviors such as shared regulation of the common bus and stored energy balance between distributed ESSs can be easily addressed by the central EMS. Each prosumer uses a full-duplex communication channel between their DERs with the local EMS. Also, another communication channel can be considered between local EMSs and the central EMS. In local area power system, wireless communication has been easily deployed with good performance for home and neighborhood area networks [25]–[27].

### III. Independent Prosumer Optimization Model

The problem for optimal coordination of DERs has been defined as a mixed integer linear programming (MILP) model that is composed by real variables, \( x \), and binary variables, \( z \), and can be written in general as,

\[
\begin{align*}
\min_{x,z} & \quad f(x,z) = a^T x + b^T z \\
\text{subject to.} & \quad G(x,z) = c \\
& \quad H(x,z) \leq d \\
& \quad x \in \mathbb{R}, z \in [0,1]
\end{align*}
\]

where, \( f(x,z) \) is the objective function, \( c \) and \( d \) are scalar vectors, and \( G(x,z), H(x,z) \) are linear combinations of the variables that define equalities and inequalities constraints. Along this section, the mathematical formulation of the optimization problem will be presented in detail.

The variables used in the model are presented in Table I, one binary variable \( z = z_{load}(t) \) and real variables \( x \) which are the others shown variables. Note that the variables are denoted in lower-case. The parameters used in the model are summarized in Table II.
The first term in (3) corresponds to the cost associated to disconnect the load, which is equal to 0 if the load is connected \( z_{load} = 1 \).

The second term is a penalization for not using the available power in the RESs, computed as the difference between the predicted available profile of energy and the power reference multiplied by the penalty cost of curtailment.

### B. Constraints

1) **Balance equation**: The demand must be supplied by the sources and the storage system.

\[
    p_g(t) \Delta t + p_{bat}(t) \Delta t = p_{load}(t) \Delta t \times z_{load}(t), \quad \forall t. 
\]

2) **Power Sources**: The power reference for the power source at each \( t \), \( p_g(t) \), must be less than or equal to the maximum power that can be provided for them \( P_{max}(t) \), at these \( t \).

\[
    0 \leq p_g(t) \leq P_{max}(t), \quad \forall t. 
\]

3) **Energy Storage System**: The SoC of a battery can be defined in terms of the power as,

\[
    SoC(t) = SoC(t - 1) - \varphi_{bat} \times [p_{bat}(t) \Delta t], \quad \forall t. 
\]

Note that, when \( p_{bat}(t) \) is positive, the battery provides energy to the load (it is being discharged) and when is negative, it absorbs energy from the sources (it is being charged). This variable must be limited,

\[
    P_{bat_{min}} \leq p_{bat}(t) \leq P_{bat_{max}}, \quad \forall i, t. 
\]

Additionally, the SOC at each \( t \) is bounded in the range,

\[
    SoC_{min} \leq SoC(t) \leq SoC_{max}, \quad \forall t. 
\]

### IV. Optimization model for Cluster of Prosumers

For the cluster of prosumers, the MILP model presented in the previous section is adapted. In this case, the index \( i = \{1, 2, ..., n\} \) is added to represent the \( i \)-th prosumer of a cluster of \( n \) household prosumers. Nevertheless, due to the variability of the primary energy resources under certain environmental conditions it is not possible to ensure a continuous supply of the load. Because of that, it is necessary to disconnect the load totally or partially. For partial disconnection of the load, the optimization problem penalizes more the prosumer with low ratio between local generation and consumption.

#### A. Objective Function

Here, the objective function minimizes disconnection of the load, for the households interconnected in the cluster, and maximizes the available generation as,
\[
\sum_{t=1}^{T} \sum_{i=1}^{n} p_{\text{load}}^{(i)}(t) \Delta t \cdot (1 - z^{(i)}_{\text{load}}(t)) \cdot C^{(i)}_{\text{load}}(t) \cdot \xi^{(i)} + \sum_{t=1}^{T} \sum_{i=1}^{n} [p^{(i)}_{\text{max}}(t) \Delta t - p^{(i)}(t) \Delta t] \cdot C^{(i)}_g(t)
\]

where the parameter \( \xi^{(i)} \) has been included in order to penalize the load disconnection, and it is defined as,

\[
\xi^{(i)} = \frac{\sum_{t=1}^{T} p^{(i)}_{\text{max}}(t)}{\left(\sum_{i=1}^{T} p^{(i)}_{L}(t)\right)}, \quad \forall i.
\]

The value of \( \xi^{(i)} \) will bigger for the prosumer with larger ratio between generation and consumption and the disconnection of its load will be highly penalized in the optimization model. On the contrary, for small values of \( \xi^{(i)} \), the load of that prosumer will be more likely to be disconnected when required. In this way, a fair criterion for load disconnection is provided within the optimization model.

**B. Constraints**

1) **Balance equation**: The energy balance should be fulfilled in the cluster of prosumers, and it can be written as,

\[
\sum_{i=1}^{n} p^{(i)}_g(t) \Delta t + \sum_{i=1}^{n} p^{(i)}_{\text{bat}}(t) \Delta t = \sum_{i=1}^{n} p^{(i)}_{\text{load}}(t) \Delta t + z^{(i)}_{\text{load}}(t), \quad \forall t.
\]

2) **Power Sources**: The scheduled generation reference can be generalized for the cluster of prosumers as,

\[
0 \leq p^{(i)}_g(t) \leq p^{(i)}_{\text{max}}(t), \quad \forall i, t.
\]

3) **Battery**: The SoC can be rewritten as,

\[
SoC^{(i)}(t) = SoC^{(i)}(t-1) - \varphi_{\text{bat}} \cdot \left[p^{(i)}_{\text{bat}}(t) \Delta t\right], \quad \forall i, t.
\]

In the same way, the boundaries of the related variables can be written as,

\[
SoC_{\text{min}} \leq SoC^{(i)}(t) \leq SoC_{\text{max}}, \quad \forall i, t
\]

\[
P_{\text{bat}}_{\text{min}} \leq p^{(i)}_{\text{bat}}(t) \leq P_{\text{bat}}_{\text{max}}, \quad \forall i, t.
\]

Additionally, in order to enhance the performance of distributed ESSs, which are cooperating within the cluster of household prosumers, the operation of the cooperative power grid is complemented with energy storage balance between distributed ESSs [29]. The equalization of the SoC between ESSs brings additional advantages to the overall performance of them, such as reduction in the DoD and faster charge of all the distributed ESSs [30]. For considering the effect of SoC equalization between distributed ESSs within the optimization model, an additional condition is defined as,

\[
SoC^{(i)}(t) = SoC^{(j)}(t), \quad \forall i \neq j, t \geq 1.
\]

**V. SIMULATION RESULTS**

The EMS determines the load connection and power references for the local RES units based on a 24-h ahead optimal scheduling. The optimization problem is solved by using a commercial algebraic modeling language. The model is tested by using forecasted data of generation and consumption of for a day, with time slots of one hour (\( \Delta T = 1 \) h), as is shown in Fig. 5 for a typical winter day. To simplify the analysis, as case study is considered a neighborhood composed by \( n = 2 \) household prosumers one with PV generation (prosumer 1) and the other with WT generation (prosumer 2). Table III summarizes the values of the parameters used for case study.

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Fig. 5 shows the forecasted generation and load profiles for prosumer 1 (Fig. 5a) and prosumer 2 (Fig. 5b) respectively. Those data are used for the optimization program to schedule
the power generation and load connection in a daily basis.

Real time simulation is performed into a real time platform. The model downloaded to this platform is previously established as a simulation model which includes the RESs generation profiles for 24h, the local controllers of the power converters as well as a detailed model of valve-regulated lead-acid (VRLA) batteries [31]. On top of that, the references scheduled by the EMS are downloaded in a table and are read by the simulation model every time slot of the scheduling. Furthermore, to perform the real simulation of one day, the data were time-scaled i.e. one hour corresponds to one minute of simulation, so that the whole simulation spends 1440 s. instead of 1440 min [32].

Fig. 6 shows the generation profiles, load consumption profiles and the SoC for prosumer 1 (Fig. 6a) and 2 (Fig. 6b) respectively. In this figure, it is possible to see that for the prosumer 1 the load has to be shedding for 12 hours one at the beginning of the day and 11 hours more after 14 hours. Meanwhile, in the case of the prosumer 2 the power generation at the WT is curtailed for 4 hours in order to limit the SoC to 90 %.

On the other hand, Fig. 7 shows the PV (prosumer 1) and WT (prosumer 2) generation profiles, the load profiles for both prosumers and the SoC when prosumers are cooperating between them. In this case, the SoC is equalized between prosumer 1 and 2. In addition, it is possible to see that WT generation is not curtailed and the load of prosumer 1 is only disconnected during two hours. The load of prosumer 1 is penalized with more disconnection since this prosumer has small ration between generation and consumption ($\xi$ in equation (10)). Nevertheless, the overall operation of both prosumers is improved and the use of RESs generation is maximized thanks to the cooperative operation between them.

VI. EXPERIMENTAL RESULTS

The proposed strategy has been tested experimentally in the in the Microgrid Research Laboratory of Aalborg University. The experimental setup is integrated by fourth inverters fed by a stiff dc source as is shown in Fig. 8. Each of the inverters is connected to a LCL filter which, in turn, is connected to the common bus of each local power grid. In this case constant loads are considered for both prosumers each one with a nominal value of 345W.

Fig. 9 shows the foretasted generation profiles for prosumer 1 and 2 (Fig. 5a) and (Fig. 5b) respectively for a spring day.
order to achieve independence from the main grid while increasing the reliability and usage of the local power system.

**REFERENCES**


Fig. 10. Experimental generation, consumption and SoC profiles for (a) prosumer 1 and (b) prosumer 2

Fig. 11. Experimental results with central scheduling

Fig. 10 shows the experimental results obtained for independent operation of prosumer 1 and 2 respectively. Here, it is possible to see that the generation for prosumer 1 is curtailed for 2 hours in order to avoid overcharge of the ESS. Meanwhile, the load of prosumer 2 is disconnected for 4 hour. On the contrary, Fig. 11 shows the performance of the household prosumers operating in a cooperative way and controlled by the central EMS. In this case the generation from RESs is maximized and the disconnection of the loads is completely avoided. Additionally, SoC equalization between ESSs and proper operation levels for the SoC is achieved.

**VII. CONCLUSION**

The proposed central EMS enhances the performance of the cluster of household prosumers compared to independent operation of them. This improvement can be reflected in better loads profile connections and mayor usage of the renewable resources. On top of that, collaborative behaviors such a power sharing and stored energy balance between distributed ESSs can be easily addressed by the central EMS. This strategy ensures the global balance of the system, while maximizing the use of distributed generators. Cooperative operation between household prosumers is a feasible option in


**BIographies**

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