Comparing MapReduce and Pipeline implementations for Counting Triangles

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A common method to define a parallel solution for a computational problem consists in finding a way to use the Divide & Conquer paradigm in order to have processors acting on its own data and scheduled in a parallel fashion. MapReduce is a programming model that follows this paradigm, and allows for the definition of efficient solutions by both decomposing a problem into steps on subsets of the input data and combining the results of each step to produce final results. Albeit used for the implementation of a wide variety of computational problems, MapReduce performance can be negatively affected whenever the replication factor grows or the size of the input is larger than the resources available at each processor. In this paper we show an alternative approach to implement the Divide & Conquer paradigm, named dynamic pipeline. The main features of pipeline are illustrated on a parallel implementation of the well-known problem of counting triangles in a graph. This problem is especially interesting either when the input graph does not fit in memory or is dynamically generated. To evaluate the properties of pipeline, a dynamic pipeline of processes and an ad-hoc version of MapReduce are implemented in the language Go, exploiting its ability to deal with channels and spawned processes. An empirical evaluation is conducted on graphs of different topologies, sizes, and densities. Observed results suggest that pipeline allows for the implementation of an efficient solution of the problem of counting triangles in a graph, particularly, in dense and large graphs, drastically reducing the execution time with respect to the MapReduce implementation.

1 Introduction

The Divide & Conquer paradigm [2] is an algorithm design schema that enables to solve large and complex computational problems in three stages: i) Divide: an instance of the problem is partitioned into subproblems; ii) Conquer: the subproblems are solved independently; iii) Combine: the solutions of the subproblems are combined to produce the final results. The Divide & Conquer paradigm is well-known for giving good complexity results. MapReduce [15] is an implementation schema/programming

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paradigm of the Divide & Conquer paradigm, extensively used in the implementation of complex problems. The divide stage is done by establishing an equivalence relation on the set of values which are the images of an input set transformed by a mapping processes, such that in the Conquer stage reducers can act on disjoint sets, i.e., each reducer acts on a different equivalence class. Finally, other processes collect the partial results produced by the reducers to generate the solution in the combine stage.

Frameworks that implement the MapReduce schema have had great success and are mostly addressed to run on distributed architectures. Parallelism is a mean for speeding up solutions for computational programs with large amounts of data in memory and that have, in general, a regular behavior. The MapReduce scheme utilizes the Valiant’s Bulk Synchronous Parallel (BSP) model of computation [21], and it is defined in terms of a pipe of three steps: Map, Shuffle, and Reduce. Map transforms a domain, where the equivalence relation can be established. Shuffle divides the collection into sub-collections where the reducers can act independently; the communication between processes in the pipe is done via distributed files which act as shared memory for the processors. Some problems require the composition of several MapReduce processes. The number of composed processes is called the number of passes the solution requires. MapReduce implementations require that users provide at least the code for the Map and for Reduce processes, as well as determine the number of processors assigned to the solution.

Hadoop [22] is a framework that provides programing file system and operating system abstractions for distributing data and processing; it enables the evaluation and testing the goodness of a MapReduce solution for a problem, as well as facilities the recovery from runtime errors.

The success of the MapReduce schema for solving problems having massive input data has been extensively reported in the literature [14], however, it is also known the MapReduce approach is not suitable for solving problems that require the existence of a shared global state at execution time and solutions that require several passes. In this work, we tackle limitations of the MapReduce programing schema, and present an alternative computing approach of the Divide & Conquer paradigm for solving problems with massive input data. This implementation is based on a dynamic pipeline of processes via an asynchronous model of computation, synchronized by channels. To be concrete, we consider the problem of triangle counting and present both, an implementation of counting triangles based on two rounds of the MapReduce schema [20], and the pipeline implementation following the approach proposed by Aráoz and Zoltan [1]. In particular, we use Go [8] as programming language. We empirically evaluate the performance of pipeline and MapReduce on a large variety of graphs of different size and density. The observed results in this preliminary study suggest that the benefits of pipelining in the implementation of the problem of triangle counting on dense graphs and with a large number of edges, where the savings in execution time can be of up to two orders of magnitude.

In summary in this paper, we make the following contributions:

- A comparison of the MapReduce and dynamic pipeline programing schemas in the resolution of the problem of counting triangles.
- Implementations in the Go language of two algorithms that follow the MapReduce and dynamic pipeline programing schemas to solve the problem of counting triangles. These algorithms exploit the main properties of Go, i.e., channels and spawned processes, and correspond to implementations of the dynamic pipeline and MapReduce programing schemas under the same conditions.
- An empirical evaluation of the MapReduce and dynamic pipeline based algorithms in a variety of graphs of different density, topology, and size, to demonstrate the performance of both algorithms.

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1 Some implementations combine the shuffle step with the Map step
2 We consider this problem interesting since it is useful to compute the clustering coefficient which is a measure of interest in social networks.
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This paper is a revised and extended version of a short paper that was presented at AMW2016[17] and it is organized as follows. In the next section we describe the implementations of the problem of triangle counting in both MapReduce and pipelining using the Go language. In Section 3, results of the experimental evaluation are reported and discussed. Finally, we present the concluding remarks and future work in Section 4.

2 The Problem of Counting Triangles

2.1 Preliminaries

Counting triangles is a building block for determining the connectivity of a community around a node, representing a relevant problem in the context of social network analysis. Specifically, given the size of existing social networks, efficiency needs to be ensured, and existing approaches have been exploited the benefits of parallel computation in MapReduce [5, 16, 20], as well as approximate solutions to the problem [4, 12, 18]. We tackle an exact solution to the problem, and present two algorithms that exploit the properties of MapReduce and pipeline in the Go programming language. To be concrete, we present Go implementations for the algorithm proposed by Suri et al. [20] and for the algorithm proposed by Araóz et al. [1], for counting triangles in a graph represented as a sequence of unordered edges. As a precondition, the problem of counting triangles receives undirected simple graphs, i.e., no multiple edges are admitted; to ensure this requirement multiple edges are filtered in a pre-processing stage.

Go [8] is a programming language that facilitates efficient implementations of parallel programs, and naturally supports concurrency as well as processes for automatic memory management and garbage collection. Go additionally provides a mechanism of channels to enable the implementation of both pipeline and MapReduce. Moreover, Go makes available goroutines, which are needed not only for dynamically spawning processes, but for describing processes that resume their work when stop being blocked. All these features are fundamental and crucial for the selection of Go as the programming language for the problem of counting triangles on pipeline and MapReduce. In Figures 1 and 2, we illustrate the structure of the two-round MapReduce solution and the pipeline approach for the studied problem, respectively. Both implementations are explained in next subsections.

2.2 A MapReduce Solution

Suri and Vassilvitskii [20] present a composition of two MapReduce algorithms for solving the triangle counting problem. In the first MapReduce application, the input is a set of edges of an undirected graph, and the output is a set of 2-length paths having a given responsible node. Each 2-length path with its responsible node is represented by a triple (path-triple). The second application of MapReduce receives the path-triples generated by the previous application of MapReduce and the edge-triples, i.e., the edges present in the input graph with an empty middle element. For each triple, the pair of its end nodes is used as its key. If a path-triple and an edge-triple are in the same cluster, the number of triangles is equal to the cluster size minus one. Otherwise, the number of triangles in the cluster is zero. Adding the number of triangles in each cluster gives the total number of triangles in the graph. It is common that the number of reducers coincides with the number of available processors. So the behavior is not smooth in the number of processors.

MapReduce Implementation: Figure 1 shows the phases of our implementation of Suri and Vassilvitskii’s MapReduce algorithm [20]. The program receives as an input a file which is partitioned into as
2.3 A Pipeline Solution

The pipeline solution is the composition of a sequence of filters specialized to the vertices of the input graph, and each one works on a set of values not consumed by the previous filter. Each filter has three inputs and three outputs for receiving/sending messages to their neighbors. The first filter receives the complete set of edges, using the third input. Each filter specializing itself with the first incoming edge, using the first node of the edge as responsible node and add the other to an adjacent list. Afterwards, each
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Figure 2: Pipeline Solution for Triangle Counting. Rectangles represent filters and ovals correspond to vertices

filter treats the incoming edges, keeping those incident to its responsible node and sending the others to its neighbor. Filters are created dynamically, as new values not consumed by already created filters arrive. As each filter consumes at least one value, no more than $|V| - 1$ filters can be created\(^3\). The number of filters is equal to the number of classes generated by the relations on the original set\(^4\). Whenever there are no more edges in the third input, the filter will count the number of edges in the second input having both endpoints in the adjacency list of the filter responsible node. After all edges in the second input are processed, each filter has the number of triangles, having the responsible node as one of its nodes. The first input/output of each filters is used to collect the total number of triangles present in the graph. The proof of correctness of this pipeline algorithm can be found in [1].

Pipeline Implementation: Figure 2 shows the topology of our implementation of the pipeline of the algorithm proposed by Aráoz and Zoltan [1]. In particular, this topology is the composition of a sequence of filters specialized to vertices of the input graph, and each one works on a set of values that are not consumed by the previous filter. The first filter receives the complete set of edges on the third input. Each new filter specializes itself with the first incoming edge, using the first node of the edge as responsible node and add the other one to an adjacent list. Afterwards, each filter treats the incoming edges, keeping those nodes belonging to edges incident to its responsible node and sending the others to their neighbor.

Whenever all the edges are being processed, each filter has the nodes of the received edges incident to its responsible node. The number of filters is equal to the number of classes generated by the relation on the original set. In the implementation, filters are processes/goroutines that communicate via unbuffered channels and each process is specialized by a responsible node. Further, goroutines have three input channels and three output channels. Processes use lists to keep nodes adjacent to the responsible one. In each filter, every incoming edge in the second input is checked if it is incident to two nodes adjacent to the corresponding responsible one. If so, the number of triangles found is increased by one. When there are no more edges, each filter has the total number of triangles in the graph that includes its responsible node. The first channel will carry the number of triangles found by each goroutines. A final process adds up the partial results.

3 Experiments

In this section, we present the experimental results of MapReduce and Pipeline implementations for the problem of counting triangles. The goal of the experiment is to analyze the impact of graph proper-

\(^3\)It is an upper bound because the graph does not have isolated nodes

\(^4\)The partition relation is created during the execution.
ties on time and space complexity of both implementations. We study the following research questions:

**RQ1)** Is the Pipeline based implementation able to overcome the performance of MapReduce implementation independently of the input graph characteristics?; **RQ2)** Are density, topology, and size of the input graph equally affecting Pipeline and MapReduce implementations; **RQ3)** Is the number of cores equally affecting Pipeline and MapReduce implementations?. The experimental configuration to evaluate these research questions is as follows:

<table>
<thead>
<tr>
<th>Graph</th>
<th># Vertices</th>
<th># Arcs</th>
<th>Density</th>
<th>File size</th>
</tr>
</thead>
<tbody>
<tr>
<td>DSJC.1</td>
<td>1,000</td>
<td>99,258</td>
<td>0.10</td>
<td>1.1MB</td>
</tr>
<tr>
<td>DSJC.5</td>
<td>1,000</td>
<td>499,652</td>
<td>0.50</td>
<td>5.2MB</td>
</tr>
<tr>
<td>DSJC.9</td>
<td>1,000</td>
<td>898,898</td>
<td>0.90</td>
<td>9.3MB</td>
</tr>
<tr>
<td>Fixed-number-arcs-0.1(FNA.1)</td>
<td>10,000</td>
<td>10,000,000</td>
<td>0.10</td>
<td>140MB</td>
</tr>
<tr>
<td>Fixed-number-arcs-0.5 (FNA.5)</td>
<td>4,472</td>
<td>10,000,000</td>
<td>0.50</td>
<td>138MB</td>
</tr>
<tr>
<td>Fixed-number-arcs-0.9 (FNA.9)</td>
<td>3,333</td>
<td>10,000,000</td>
<td>0.90</td>
<td>136MB</td>
</tr>
<tr>
<td>USA-road-d.NY (NY)</td>
<td>264,346</td>
<td>730,100</td>
<td>1.04E-5</td>
<td>13MB</td>
</tr>
<tr>
<td>Facebook-SNAP(107)</td>
<td>1,911</td>
<td>53,498</td>
<td>1.47E-2</td>
<td>0.524MB</td>
</tr>
</tbody>
</table>

Table 1: Benchmark of Graphs

Graphs of different sizes and densities. Density is defined as \( \frac{\text{#Arcs}}{\text{#Vertices} \times (\text{#Vertices} - 1)} \)

**Datasets:** We compare these two implementations using graphs of different topologies, densities, and sizes. These graphs are part of the 9th DIMACS Implementation Challenge - Shortest Paths\[6\]: DSJC.1, DSJC.5, and DSJC.9 are graphs with the same number of nodes and different densities, while in Fixed-number-arcs-0.1(FNA.1), Fixed-number-arcs-0.5(FNA.5), and Fixed-number-arcs-0.9(FNA.9), the number of nodes is changed to affect the graph density. USA-road-d.NY and Facebook-SNAP(107)\[13\] are real-world graphs that correspond to the New York City road network and a Facebook subgraph, respectively. Table 1 describes these graphs in terms of number of vertices, arcs, graph density, and file size.

**Metrics:** As evaluation metrics, we consider the execution time (ET) and Virtual-memory (VM). ET represents the elapsed time (in seconds) between the submission of a job and completion of the job including the generation of the final results. VM represents the virtual memory consumed by the batch job measured in GB. Both ET and VM are reported by the qsub command when a batch job is submitted to the machine \[7\].

**Implementation:** Programs are run on a node of the cluster of the RDLab-UPC\[5\] having two processors Intel(R) Xeon(R) CPU X5675 of 3066 MHz with six cores each one. The configuration used in the experiments for submitting jobs is up to 12 cores and 40GB of RAM. Programs are implemented in Go 1.6 \[9\]. The same job is executed 10 times and the average is reported, given enough shared memory and a timeout of five hours.

**Discussion** Graphs with different sizes and densities (0.10, 0.50, and 0.90) are evaluated to study our research questions **RQ1** and **RQ2**. Graphs with high density can be considered as the worst case for both program schemes. Plots in Figures \[3\] and \[4\] report on execution time (ET in log10-scale secs) and virtual memory (VM in GB) for each of the schemas. Jobs that time out at five hours are reported using red bars. Jobs for the pipeline program in the different graphs are finished in less than 3 hours, while

[https://rdlab.cs.upc.edu/](https://rdlab.cs.upc.edu/)
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Figure 3: **Execution Time.** For graphs of different size and density, performance of the Pipeline and MapReduce implementations is reported in terms of execution time (ET in log10-scale secs). Jobs that time out at five hours are reported using light grey bars.

Figure 4: **Virtual Memory.** For graphs of different size and density, performance of the Pipeline and MapReduce implementations is reported in terms of virtual memory (VM in GB). Jobs that time out at five hours are reported using light grey bars.

three jobs of the MapReduce implementations do not produce any response in five hours, i.e., these three jobs time out and are reported in light grey bars in Figures 3 and 4. The results suggest that the pipeline implementation exhibits the best results in response time and virtual memory consumption for graphs as the ones in DSJC.1, DSJC.5, DSJC.9, FNA.1, FNA.5, and FNA.9. Particularly, in the highly dense graphs, i.e., DSJC.9 and FNA.9, pipeline drastically reduces execution time with respect to MapReduce. Similar performance is observed in the real-world subgraph of Facebook (Facebook-SNAP(107)), where pipeline execution time overcomes MapReduce by three orders of magnitude. Finally, the graph NY that represents the road network of NY city, is highly sparse and the pipeline implementation generates a large number of processes that the Go scheduler is not able to deal with.

Our benchmark of graphs is also used to evaluate our research question **RQ3.** Plots in Figures 5 and 6 report on execution time (ET secs) for each of the schemas when the number of cores is eight or twelve. Jobs that time out at five hours are reported using light grey bars. For the graphs DSJC.1, DSJC.5, DSJC.9, and 107, jobs of the pipeline implementation requires less than 18 secs. to be completed and produce the response. Similarly, in graphs DSJC.9, (Facebook-SNAP(107)) and NY, jobs of the MapReduce
Figure 5: **Impact of the Number of Cores in Pipeline.** For graphs of different size and density, the impact of the number of cores in execution time (ET secs.) of the pipeline implementation is reported. For graphs DSJC.1, DSJC.5, DSJC.9, and 107 execution time is less than 18 secs.

Figure 6: **Impact of the Number of Cores in MapReduce.** For graphs of different size and density, the impact of the number of cores in execution time (ET secs.) of the MapReduce implementation is reported. Jobs that time out at five hours are reported using grey bars. Graphs DSJC.9, (Facebook-SNAP(107)) and NY, jobs of the MapReduce implementations produce the responses in less than 29 secs.

Implementations produce the responses in less than 29 secs. As the results reported in Figures 3 and 4, jobs for the MapReduce implementation time out at five hours for large graphs: FNA.1, FNA.5, and FNA.9. This negative performance of MapReduce is caused by the replication factor of the problem of counting triangles, i.e., the size of the set of 2-length paths (output in the first phase of MapReduce) is extremely large, $O(n^2)$ where $n$ is the number of graph vertices and these graphs have up to 10,000 vertices. These results corroborate our statement that the pipeline programming schema is a promising model for implementing complex problem and provides an adaptive solution to the characteristics of the input dataset. Furthermore, pipeline is competitive with MapReduce and does not require any previous knowledge of the input dataset.
4 Conclusions and Future Work

We presented an alternative approach, named dynamic pipeline, that follows the Divide & Conquer paradigm, and relies on a dynamic pipeline of processes via an asynchronous model of computation for process communication. Users of the pipeline approach need to provide a sequential code or filters, and require no understanding of standard concurrency mechanisms, e.g., threads and fine-grain concurrency control, which are aspects known to be difficult to deal with in order to obtain race condition free code in a parallel solution. Contrary to MapReduce, where implementations differ depending on the architectures, implementations based on the pipeline approach can make transparent to users the implementation of channels. The channel abstraction could have several concrete implementations that use shared memory, TCP pipes, or files temporarily persisted in a file system, e.g., as the ones provided by the Dryad distributed technologies[19]. This abstraction can allow for the deployment of the same program in a single machine with several cores, or a net of computing units.

The well-known problem of triangle counting is utilized to illustrate the features of the pipeline approach as well as the differences with the MapReduce programming schema. Both programs were implemented in multi-processor nodes. The proposed implementations provide exact solutions for counting triangles by exploiting the main characteristics of the Go programming language, i.e., the evaluation model, a scheduler able to cope with dynamic scheduling, and the notion of channels to enable the communication between processes. The performance of both implementations was empirically evaluated in artificial and real graphs with different sizes and densities. The observed results show a superiority in execution time for the pipeline schema even in dense graphs. The only case where MapReduce exhibits a better performance corresponds to a graph where a large number of nodes have an approximate degree of 2, and this particular configuration results in a program that negatively affects the Go scheduler. The results also suggest that the number of processors has a greater positive impact on the pipeline schema than in MapReduce. Based on these results, we can conclude that the pipeline approach is highly scalable, and is able to exhibit performance gains on large problem instances with thousands of tasks, seeming to be most promising when a large number of processors work on shared memory, e.g., in architectures as the one implemented in The Machine from Hewlett Packard Labs[6]. In the future, we plan to continue the evaluation of the behavior of the pipeline approach in other complex computational problems, and create a programming framework. Further, other algorithms for counting triangles in graph will be implemented and included in our evaluation study, e.g., algorithms by Hu et. al [10][11]. However, it is important to highlight that because these algorithms require different representations of a graph, e.g., adjacent lists, and are not implemented as MapReduce, they will require a pre-processing phase and will not be able to be used in graphs dynamically generated. In consequence, the experimental evaluation will have to be redefined in order to conduct a fair comparison of the studied approaches.

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References


